# Circus Grammar Explained — Channels

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#### Abstract

This article documents the various ways one can declare *Circus* channels and channel sets using LATEX markup. It also documents the open issues of the language related to these two syntactic categories.

## 1 Introduction

In this file, we explain the various aspect of *Circus* related to channel declarations. At each section relevant to the grammar, we include its corresponding CUP rule, as "Section name — grammarRule".

Circus productions must be included within the circus LATEX environment in order to be recognised by the parser. Therefore, to use Circus one needs to have the current version of the circus.sty LATEX style file.

Amongst other commands, it contains all *Circus* keywords, and some useful environments.

# 2 Circus channel paragraphs — channelPara

In *Circus* channels are global paragraphs at section level. Other global paragraphs are channel sets, processes, and all other Z paragraphs. Firstly, we need to create a new section containing the circus\_toolkit as a parent.

 ${\bf section} \ \ circus\_channels \ {\bf parents} \ \ circus\_toolkit$ 

begin{zsection}
 \SECTION\ circus\\_channels \parents\ circus\\_toolkit
end{zsection}

We include with each typeset text the corresponded LATEX code.

# 2.1 Common channels — channelDecl

Channels are declared in *Circus* to specify synchronisation points. Channel types are any Z expression, and they define the communication patterns to synchronise.

Untyped channels are also allowed. They represent synchronisation points with the given type Synch. Thus, declaring a untyped channel has the same effect as declaring the channel with type Synch, as defined in the circus\_toolkit.tex file.

Channels are declared within the circus IATEX environment, which are typeset as Z unboxed items like in the zed IATEX environment. As the Z standard, various unboxed *Circus* items can be declared within the same environment, as long as they are separated by a **NL** (new-line) token.

### 2.1.1 Typed channels

Let us define some typed channels,

```
channel a, b : \mathbb{N} begin{circus} \circchannel\ a, b: \natend{circus}\%
```

STROKES ARE NOT ALLOWED IN CHANNEL NAMES - it messes up communication patterns.

#### 2.1.2 Generic channels

Generic channels can also be declared, where generic formal parameters given are right after the **channel** keyword.

As before, names with decorations must have hard spaces before hitting a COMMA token, as shown above.

#### 2.1.3 Synchronisation channels

Synchronisation channels are defined without a type expression. The parser introduces a *Synch* **RefExpr** for it automatically, as it is necessary for translation to and from ZML. This name is defined as a given set in the circus\_toolkit.tex file.

```
channel c, d
channel z, w
begin{circus}
    \circchannel\ c, d \\
    \circchannel\ z, w
end{circus}%
```

This time, we left two declarations within the same Z box, but separated by a **NL** (new-line) token.

#### 2.2 Channels through schemas — channelFromDecl

Another way of declaring typed channels is through schema references. Let us define a schema named S with two channels a and b

```
S = a, b : \mathbb{N}
a > b \land b \neq 0
begin{schema}{S}
a, b: \nat
\where
a > b \land b \neq 0
end{schema}
```

With the **channelfrom** keyword, we can declare these channels as well.

```
channelfrom S
begin{circus}
  \circchannelfrom\ S
end{circus}%
```

These declarations include four channels of type  $\mathbb{N}$ , namely:  $a, b, a_1$ , and  $b_1$ . Another option is to have schemas with generic types.

```
T[X] = x, y : \mathbb{P}[X]
x \subseteq y
```

```
begin{schema}{T}[X]
    x, y: \power~X
\where
    x \subsetteq y
end{schema}
```

In this case, one can define the channels from the schema via either: (i) declaring the schema name with corresponding number of generic actuals; (ii) leaving the original generic formal parameters (possibly renaming them); (iii) letting the typechecker decide; or (iii) redefining the generic formal parameters of channel types in terms of a new pattern of formal parameters for the schema generic actuals.

```
\begin{array}{l} \textbf{channelfrom} \quad T[\mathbb{N}] \\ \textbf{channelfrom} \quad [Y] \quad T[Y] \\ \textbf{channelfrom} \quad T2 \\ \textbf{channelfrom} \quad [A,B] \quad T3[A\times B] \\ \\ \textbf{begin\{circus\}} \\ \quad \quad \\ \textbf{circchannelfrom} \quad T[\setminus \text{nat}] \quad \setminus \\ \quad \quad \\ \textbf{circchannelfrom} \quad [Y] \setminus \quad T1[Y] \quad \setminus \\ \quad \quad \\ \textbf{circchannelfrom} \quad T2 \quad \setminus \\ \quad \quad \\ \textbf{circchannelfrom} \quad [A,B] \setminus \quad T3[A \setminus \text{cross} \ B] \\ \textbf{end\{circus\}\%} \end{array}
```

It is the task of the typechecker to guarantee that either the instantiation or (re)definitions are type-correct. For each case we would have:

```
i channel x,y:\mathbb{P}\ \mathbb{N}
ii channel [Y]\ x1,y1:\mathbb{P}\ Y
iii channel x2,y2:\mathbb{P}\ X
iv channel [A,B]\ x3,y3:\mathbb{P}(A\times B)
```

Thus, **channelfrom** is just syntactic sugar for a corresponding **channel** declaration.

# 3 Circus channel set paragraphs — channelSetPara

Channel sets defines an expression to represent a particular set of channels. They are normally used as reference names for other *Circus* operators that have channel references as parts of their AST, such as the parallel and the hiding operators.

Channel sets are given as a name and a corresponding channel set expression.

```
channelset C == \emptyset
channelset C0 == \{ | \} 
channelset C1 == \{ a, b, c, d \}
channelset C2 == \{ |x, y, x1, y1| \}
channelset [A, B]C3 == \{|x2[A \times B], y2[A \to B], x1[A], y1[B]\}
channelset C4 == (C1 \cup C2 \cap C3) \setminus (C0 \cup C1 \cup C)
begin{circus}
    \circchannelset\ C == \emptyset \\
    \circchannelset\ CO == \lchanset \rchanset %\\
    \circchannelset\ C1 == \lchanset a, b, c, d \rchanset \\
    \circchannelset\ C2 == \lchanset x, y, x1, y1 \rchanset \\
    \circchannelset\ [A, B] C3 == \lchanset x2[A \cross B],
                                                  y2[A \setminus fun B], x_1[A],
                                                  y1[B] \rchanset \\
    \circchannelset\ C4 == (C1 \cup C2 \cap C3) \setminus
                               (CO \cup C1 \cup C)
end{circus}
```

The channel set expressions mostly used are: set union, intersection and difference expressions; set extension expressions; reference expressions; and application expressions

Considering **BasicChannelSetExpr** a special case of set extension (with special brackets), the channel set expressions are a subset of the whole Z expression tree. More precisely, table ?? shows which one of the available Z expression productions are valid channel set expressions. On the third column of the table table: "Y(N)" means the Z expression is (is not) valid; " $Y^*$ " means the Z expression is valid provided one changes the normal ( $\{\}$ ) brackets to the special ( $\{\}\}$ ) channel set brackets; "Y!" means an undecided inclination towards accepting; and "?" means yet unknown. At the moment, the parser implementation only filters set extension and comprehension, hence accepting all other Z expression productions.

[Including all Z restrictions] Add the other restrictions from table ??

[How are the type rules for channel set references?] That is, could channel set references have generic actuals, as in?

```
\begin{array}{l} \textbf{channel} \ [X]\,c,\,d:X\\ \textbf{channel} \ [Y]\,e,\,f:Y\\ \textbf{channelset} \ \ CS1 = \{\!\!\{\,c,\,d\,\}\!\!\}\\ \textbf{channelset} \ \ CS2 = \{\!\!\{\,e,f\,\}\!\!\}\\ \textbf{channelset} \ \ CS3 = CS1[\mathbb{N}] \cup CS2[\mathbb{P}\ \mathbb{Z}] \end{array}
```

This is a typechecking problem that shouldn't affect the parser, unless one wanted to restrict the generic instantiation as a parsing error, something that would require the use of **RefName** rather than **RefExpr**.

Even further, as occurred with channel declaration from schemas, where we could possibly have channels as well as the schema generics, shouldn't we allow this for channel sets as well (*i.e.*, shouldn't it has generic actions?

```
channelset [A, B]CS4 = CS1[\mathbb{N} \times A] \cup CS2[A \times B]
```

If this is a desired feature, the AST for ChannelSet do require modification to include the list of **DeclName** for the generic formals.

[decorated channel sets] Decorated channel sets are also valid in the parser at the moment, as it makes the production rules easier accepting strokes.

$$CS1_0 \Rightarrow \{ c_0, d_0 \}$$

This could be removed if needed, though. At the moment, I am assuming it as a typechecking rather than a parsing problem.

[Channel set expressions subtree — restrictions] To simplify the implementation of channel set expressions, we simply encapsulate a Z expression (**expression**) filtered "adequately" (*i.e.*, do not containing set extensions or comprehension) and include the production for **BasicChannelSet-Expr**.

From the expressive options to include Z applications, this is the simplest one. Nevertheless, as  ${\bf BasicChannelSetExpr}$  is not embedded into the Z expression subtree, one cannot mix it with normal Z expressions. The consequence is a fairly uncompromising (verboseness) restriction. For example, something like

```
channelset CS1 == \{\mid a, b \mid \}
channelset CS2 == \{\mid c \mid \}
channelset CS3 == CS1 \cup CS2
```

is valid because no Z expression is mixed with **BasicChannelSetExpr**, whereas something like

**channelset** 
$$CS3 == \{ |a, b| \} \cup \{ |c| \}$$

is not valid because such mix occurs.

One first (abandoned) alternative solution was to include the **Basic-ChannelSetExpr** production under a Z expression and use flags to say when to consider it or not. The consequences are neither elegant, nor desirable: clumsy code, difficulty in properly restricting the channel set expression tree properly, etc.

## 4 Conclusion

## 5 Future work

The ideal solution for channel set expressions would be to have their own expression subtree. This would be the neatest choice as it neither requires filtering on the Z expression subtree, nor imposes the restrictions on mixed expressions just mentioned above. Nevertheless, it is a quite hard choice as sorting the precedences and solving the conflicts of such subtree is very difficult (see the parser/tests/circus/cs\_expression.Parser.xml file for details).

Another task for the near future is to sort out the JAXB problem from **ChannelDecl**.

Description	Example	Valid CSE?
Conditional	if pred then expr else expr	Y
Universal quantification	$\forall decl \mid pred \bullet expr$	N
Existential quantification	$\exists decl \mid pred \bullet expr$	N
Unique existential quant.	$\exists_1 \ decl \mid pred \bullet expr$	N
Function construction	$\lambda \ decl \mid pred \bullet expr$	Y
Definite description	$\mu \ decl \mid pred \bullet expr$	Y
Substitution expression	$\mathbf{let} \ abbrv \bullet expr$	Y
Schema equivalence	$S \Leftrightarrow T$	N
Schema implication	$S \Rightarrow T$	N
Schema disjunction	$S \vee T$	N
Schema conjunction	$S \wedge T$	N
Schema negation	$\neg S$	N
Schema composition	$S \circ T$	N
Schema piping	$S \gg T$	N
Schema hiding	$S \setminus T$	N
Schema projection	$S \uparrow T$	N
Schema precondition	$\operatorname{\mathbf{pre}} S$	N
Powerset	$\mathbb{P}X$	?
Cartesian product	$X \times Y$	N
Prefix application (PRE)	$f_{-}$	?
Prefix application (L, ERE)	$a_b$	?
Prefix application (L, SRE)	I .	?
Postfix application (POST)	a, , b X *	?
Postfix application (ELP, ERP)	_a_b	?
Postfix application (ELP, SREP)	_a_,, b	?
Infix application (I)	_U_	Y
Infix application (EL, ERE)	$a_b$	?
Infix application (EL, SRE)	_a_,, b_	?
Nofix application (L, ER)	$a_b$	?
Nofix application (L, SR)	$\langle -,, \rangle$	Y
Set extension	$\{a,b\}$	Y*
Set comprehension	{ decl   pred }	?
Characteristic set comp.	$\{ decl \mid pred \bullet expr \}$	?
Tuple extension	(x,y,z)	N
Characteristic definite desc.	$(\mu \ decl \mid pred)$	?
Binding extension	$\langle x = 10, y = \{ \} \rangle$	N
Empty schema construction		N
Schema construction	[decl   pred] or [  pred]	N
Binding selection	$S.x \text{ or } \langle x == 10 \rangle.x$	Y!
Tuple selection	t.1  or  (x,y).1	Y!
Schema decoration	$S' \text{ or } S_1$	Y!
Binding construction	$\theta S$	Y!
Function appl with Sch Expr.	$f [decl \mid pred]$	?
Generic instantiation	$seq[\mathbb{N},\mathbb{Z}], \text{ or } (\_\to\_)[X,Y]$	Y
Schema renaming	S[x/y, a/b]	Y!
Number literal	10	N
Reference	Name:	Y

Table 1: Filtering the Z expression tree for channel sets