1 Preamble

- section name and its parents
- basic process header
- \bullet typed channel
- generic typed channels
- synchronisation channels
- various auxiliary declarations used

 ${\bf section} \ \ action_grammar_rules \ {\bf parents} \ \ circustime_toolkit$

```
channel d:\mathbb{N}
```

```
outside: \mathbb{N}
```

channel $c: \mathbb{N} \times \mathbb{N} \times \mathbb{N} \times \mathbb{N}$

process CircusTimeActionTests =**begin**

```
n1, n2 : \mathbb{N}
x?, y!, z? : \mathbb{N}
```

$$f: \mathbb{N} \to \mathbb{N} \times \mathbb{N}$$

$$S == [y : \mathbb{N}]$$

```
\begin{array}{l} letExpr == \mathbf{let} \ x == 1 \bullet x \\ muExpr1 == (\mu \ x : \mathbb{N} \bullet x) \\ muExpr2 == (\mu \ x : \mathbb{N} \mid true) \\ condExpr == \mathbf{if} \ true \ \mathbf{then} \ 1 \ \mathbf{else} \ 2 \\ bindExpr == \langle one == 1 \rangle \\ tupleExpr == (1, \{2\}, \mathbb{P}\{3\}) \end{array}
```

$A \mathrel{\widehat{=}} \mathbf{Skip}$

2 Example 1 — CIRCWAIT

Production rule:

CIRCWAIT:cw expression:e

- simple wait with expressions of various kinds and no following action
- expressions can come from within and outside the process
- expressions that look funny like partially applied on several type expressions like theta, mu, condition, bind and tuple expressions

```
Test0 = wait 10 + outside
Test1 \stackrel{\frown}{=} wait n1 + n2
Test2 \stackrel{\frown}{=} \mathbf{wait} f
Test3 \stackrel{\frown}{=} \mathbf{wait} \, \theta \, S
Test4 = \mathbf{wait}[x : \mathbb{N} \mid x > 10]
Test5 \stackrel{\frown}{=} \mathbf{wait} \ letExpr
Test6 \stackrel{\frown}{=} \mathbf{wait} \ muExpr1
Test7 \stackrel{\frown}{=} \mathbf{wait} \ muExpr2
Test8 \stackrel{\frown}{=} \mathbf{wait} \ condExpr
Test9 = wait bindExpr
Test10 = wait tupleExpr.1
Test11 \stackrel{\frown}{=} wait 1...10
Test12 \stackrel{\frown}{=} c \longrightarrow \mathbf{wait} \ outside
Test13 \stackrel{\frown}{=} wait outside; wait outside
Test14 \stackrel{\frown}{=} c \longrightarrow \mathbf{wait} \ outside \ ; \ c \longrightarrow \mathbf{wait} \ outside
Test15 \stackrel{\frown}{=} d!x \longrightarrow \mathbf{wait} \ x + outside
Test16 \stackrel{\frown}{=} \mathbf{vres} \ vart : \mathbb{N} \bullet \mathbf{wait} \ vart
Test17 \stackrel{\frown}{=} \mathbf{vres} \ vart : \mathbb{N} \bullet c \longrightarrow \mathbf{wait} \ vart + outside
```

The following examples presents with erroneous productions like

```
\t1 TestX1 \circdef \circwait 10 \then \Skip
\t1 TestX2 \circdef \circwait \lcirctime 10 \rcirctime
```

Production rule:

CIRCWAIT DECLWORD: dw COLON expression: e CIRCSPOT circusAction:ac

- complex wait patterns with ensuing actions
- complex wait patterns with duplicated names (i.e. already declared)
- the strokes are accepatable by the parser, but that must be avoided during type checking

```
Test18 = wait x : 10 + outside • Skip
Test19 = wait y : n1 + n2  • Skip
Test20 \stackrel{\frown}{=} \mathbf{wait} \ z : f \bullet \mathbf{Skip}
Test21 \stackrel{\frown}{=} \mathbf{wait} \ w : \theta \ S \bullet \mathbf{Skip}
Test22 = wait x? : S    Skip
Test23 = wait f: S \bullet Skip
Test24 \stackrel{\frown}{=} \mathbf{wait} \ m : letExpr \bullet \mathbf{Skip}
Test25 \stackrel{\frown}{=} \mathbf{wait} \ m : muExpr1 \bullet \mathbf{Skip}
Test26 \stackrel{\frown}{=} \mathbf{wait} \ m : muExpr2 \bullet \mathbf{Skip}
Test27 = wait m : condExpr • Skip
Test28 \stackrel{\frown}{=} \mathbf{wait} \ m : bindExpr \bullet \mathbf{Skip}
Test29 \stackrel{\frown}{=} \mathbf{wait} \ m : tupleExpr \bullet \mathbf{Skip}
Test30 = wait m: 1...20 • c \longrightarrow Skip
Test31 \mathrel{\widehat{=}} c \longrightarrow \mathbf{wait} \; m:1 \dots 20 \; \bullet \; c \longrightarrow \mathbf{Skip}
Test32 \stackrel{\frown}{=} \mathbf{wait} \ m:1...20 \bullet c \longrightarrow \mathbf{wait} \ outside
Test33 \stackrel{\frown}{=} d!u \longrightarrow \mathbf{wait} \ m:1...20 \bullet \mathbf{wait} \ outside + u
Test34 \stackrel{\frown}{=} \mathbf{wait} \ m: 1...20 \bullet \mathbf{Skip} \ ; \ \mathbf{wait} \ n: 1...20 \bullet \mathbf{Skip}
Test35 \stackrel{\frown}{=} \mathbf{vres} \ vart : \mathbb{N} \bullet \mathbf{wait} \ m : 1 \dots 20 \bullet \mathbf{Skip}
Test36 \stackrel{\frown}{=} \mathbf{vres} \ vart : \mathbb{N} \bullet \mathbf{wait} \ m : 1 \dots 20 \bullet c \longrightarrow \mathbf{wait} \ vart + outside
Test37 \stackrel{\frown}{=} \mathbf{wait} \ m: 1...20 \bullet \mathbf{wait} \ n: 1...20 \bullet \mathbf{Skip}
```

3 Example 2 — CIRCSTARTBY and CIRCENDBY

Production rule:

LCIRCTIME expression:e RCIRCTIME CIRCSTARTBY circusAction:ca circusAction:ca CIRCENDBY LCIRCTIME expression:e RCIRCTIME

- StartBy and EndBy operatrs with actions
- Expressions are acceptable by parser (similar to wait expression)

```
Test38 = \langle 10 + outside \rangle \triangleleft Skip
Test39 = \langle n1 + n2 \rangle \triangleleft \mathbf{Skip}
Test40 \stackrel{\frown}{=} \langle f \rangle \blacktriangleleft \mathbf{Skip}
Test41 \stackrel{\frown}{=} \langle \theta \, S \rangle \blacktriangleleft \mathbf{Skip}
Test42 = \langle x? \rangle \triangleleft \mathbf{Skip}
Test43 \cong \langle letExpr \rangle \blacktriangleleft \mathbf{Skip}
Test44 \stackrel{\frown}{=} \langle muExpr1 \rangle \blacktriangleleft \mathbf{Skip}
Test45 \stackrel{\frown}{=} \langle muExpr2 \rangle \blacktriangleleft \mathbf{Skip}
Test46 \stackrel{\frown}{=} \langle condExpr \rangle \blacktriangleleft \mathbf{Skip}
Test47 \stackrel{\frown}{=} \langle bindExpr \rangle \blacktriangleleft \mathbf{Skip}
Test48 \stackrel{\frown}{=} \langle tupleExpr.1 \rangle \blacktriangleleft \mathbf{Skip}
Test49 = \langle 1...20 \rangle \triangleleft \mathbf{Skip}
Test50 \stackrel{\frown}{=} \langle outside \rangle \blacktriangleleft c \longrightarrow \mathbf{Skip}
Test51 \stackrel{\frown}{=} c \longrightarrow \langle outside \rangle \blacktriangleleft \mathbf{Skip}
Test52 \stackrel{\frown}{=} c \longrightarrow \langle outside \rangle \blacktriangleleft d \longrightarrow \langle outside \rangle \blacktriangleleft \mathbf{Skip}
Test53 \stackrel{\frown}{=} d!u \longrightarrow \langle u \rangle \blacktriangleleft \mathbf{Skip}
Test54 \stackrel{\frown}{=} \mathbf{vres} \ vart : \mathbb{N} \bullet c \longrightarrow \langle vart \rangle \blacktriangleleft \mathbf{Skip}
Test55 \stackrel{\frown}{=} \mathbf{vres} \ vart : \mathbb{N} \bullet c \longrightarrow \langle vart + outside \rangle \blacktriangleleft \mathbf{Skip}
Test56 \stackrel{\frown}{=} A; \langle 10 + outside \rangle \blacktriangleleft \mathbf{Skip}
```

An erroneous example for the gievn production

\t1 TestX3 \circdef A \lcirctime 10 + outside \rcirctime \circstartby \Skip
\t1 TestX4 \circdef 10 \circstartby A

```
Test57 \stackrel{\frown}{=} A \triangleright \langle 10 + outside \rangle
Test58 \stackrel{\frown}{=} A \triangleright \langle n1 + n2 \rangle
Test59 \stackrel{\frown}{=} A \triangleright \langle f \rangle
Test60 \stackrel{\frown}{=} A \triangleright \langle \theta S \rangle
Test61 \stackrel{\frown}{=} A \triangleright \langle x? \rangle
Test62 \stackrel{\frown}{=} A \triangleright \langle 1 \dots 20 \rangle
Test63 \stackrel{\frown}{=} A \triangleright \langle letExpr \rangle
Test64 \stackrel{\frown}{=} A \blacktriangleright \langle muExpr \rangle
Test65 \stackrel{\frown}{=} A \blacktriangleright \langle muExpr1 \rangle
Test66 \stackrel{\frown}{=} A \triangleright \langle condExpr \rangle
Test67 \stackrel{\frown}{=} A \blacktriangleright \langle bindExpr \rangle
Test68 \stackrel{\frown}{=} A \triangleright \langle tupleExpr \rangle
Test69 \stackrel{\frown}{=} c \longrightarrow A \triangleright \langle outside \rangle
Test70 \stackrel{\frown}{=} d!u \longrightarrow A \triangleright \langle u \rangle
Test71 \stackrel{\frown}{=} \mathbf{vres} \ vart : \mathbb{N} \bullet c \longrightarrow A \blacktriangleright \langle vart \rangle
Test72 \stackrel{\frown}{=} \mathbf{vres} \ vart : \mathbb{N} \bullet c \longrightarrow A \blacktriangleright \langle vart + outside \rangle
Test73 \stackrel{\frown}{=} A \triangleright \langle outside \rangle ; A
```

An erroneous example for the gievn production

\t1 TestX5 \circdef A \circendby \lcirctime f \rcirctime \then A
\t1 TestX6 \circdef A \circendby 10

4 Example 3 — CIRCTIMEOUT

Production rule:

circusAction:al CIRCTIMEOUT LCIRCTIME expression:e RCIRCTIME circusAction:ar

- Timeout operator with actions
- Expressions are acceptable by parser (similar to previous expression patterns)

$$Test74 \stackrel{\widehat{=}}{=} A \stackrel{\langle 10+outside \rangle}{\triangleright} A$$

$$Test75 \stackrel{\widehat{=}}{=} c \longrightarrow A \stackrel{\langle outside \rangle}{\triangleright} A$$

$$Test76 \stackrel{\widehat{=}}{=} c \longrightarrow A \stackrel{\langle outside \rangle}{\triangleright} d \longrightarrow A$$

$$Test77 \stackrel{\widehat{=}}{=} A \stackrel{\langle f \rangle}{\triangleright} A; A$$

$$Test78 \stackrel{\widehat{=}}{=} c \longrightarrow A \stackrel{\langle f \rangle}{\triangleright} c \longrightarrow A; d \longrightarrow A$$

$$Test79 \stackrel{\widehat{=}}{=} d!u \longrightarrow A \stackrel{\langle u \rangle}{\triangleright} A$$

$$Test80 \stackrel{\widehat{=}}{=} \mathbf{vres} \ vart : \mathbb{N} \bullet c \longrightarrow A \stackrel{\langle vart \rangle}{\triangleright} A$$

$$Test81 \stackrel{\widehat{=}}{=} \mathbf{vres} \ vart : \mathbb{N} \bullet c \longrightarrow A \stackrel{\langle vart \rangle}{\triangleright} A$$

An erroneous example for the gievn production

\t1 TestX7 \circdef A \circtimeout 10 A

5 Example 4 — CIRCTIMEDINTERRUPT

Production rule:

circusAction CIRCTIMEDINTERRUPT LCIRCTIME expression RCIRCTIME circusAction

- Timedinterrupt operator with actions
- Expressions are acceptable by parser (similar to previous expression patterns)

$$\begin{split} Test82 & \triangleq A \triangle_{\langle 10+outside \rangle} A \\ Test83 & \triangleq c \longrightarrow A \triangle_{\langle outside \rangle} A \\ Test84 & \triangleq c \longrightarrow A \triangle_{\langle outside \rangle} d \longrightarrow A \\ Test85 & \triangleq A \triangle_{\langle f \rangle} A \; ; \; A \\ Test86 & \triangleq c \longrightarrow A \triangle_{\langle f \rangle} c \longrightarrow A \; ; \; d \longrightarrow A \\ Test87 & \triangleq d!u \longrightarrow A \triangle_{\langle u \rangle} A \\ Test88 & \triangleq \mathbf{vres} \ vart : \mathbb{N} \bullet c \longrightarrow A \triangle_{\langle vart \rangle} A \\ Test89 & \triangleq \mathbf{vres} \ vart : \mathbb{N} \bullet c \longrightarrow A \triangle_{\langle vart + outside \rangle} A \end{split}$$

An erroneous example for the gievn production

\t1 TestX8 \circdef A \circtimedinterrupt 10 A

6 Example 5 — timed prefix

Production rule:

communication PREFIXTHEN:pt LCIRCTIME expression RCIRCTIME circusAction

- Timed prefix with communication channel is uesed to express the complexity of timed communication using circus-time operators to test the smart scanner.
- Expressions are acceptable by parser (similar to previous expression patterns)

$$Test90 \stackrel{\frown}{=} c?x?y?z \longrightarrow \langle 10 + outside \rangle \mathbf{Skip}$$

$$Test91 \stackrel{\frown}{=} c?x!n1.n2 \longrightarrow \langle x? \rangle \mathbf{Skip}$$

$$Test92 \stackrel{\frown}{=} c!n1?x.n2 \longrightarrow \langle f \rangle \mathbf{Skip}$$

$$Test93 \stackrel{\frown}{=} c.n1!n2?x \longrightarrow \langle 20 \rangle d \longrightarrow \langle \theta | S \rangle \mathbf{Skip}$$

$$Test94 \stackrel{\frown}{=} d \longrightarrow \langle f \rangle e \longrightarrow \langle f \rangle \mathbf{Skip}$$

$$Test95 \stackrel{\frown}{=} c?i!(f|i) \longrightarrow \langle f \rangle \mathbf{Skip}$$

$$Test96 \stackrel{\frown}{=} c.(S.y)?z \longrightarrow \langle 20 \rangle \mathbf{Skip}$$

$$Test97 \stackrel{\frown}{=} c.(x?)!(y!)!(z?) \longrightarrow \langle 20 \rangle \langle skip \rangle$$

$$Test98 \stackrel{\frown}{=} c.(x?)!(y!)!(z?) \longrightarrow \langle 20 \rangle \langle skip \rangle$$

$$Test99 \stackrel{\frown}{=} c.(x?)!(y!)!(z?) \longrightarrow \langle 20 \rangle \langle skip \rangle$$

$$Test100 \stackrel{\frown}{=} c.(x?)!(y!)!(z?) \longrightarrow \langle 20 \rangle \langle skip \rangle$$

$$Test101 \stackrel{\frown}{=} c.(x?)!(y!)!(z?) \longrightarrow \langle 20 \rangle \langle skip \rangle$$

$$Test102 \stackrel{\frown}{=} c.(x?)!(y!)!(z?) \longrightarrow \langle 20 \rangle \langle skip \rangle$$

$$Test102 \stackrel{\frown}{=} c.(x?)!(y!)!(z?) \longrightarrow \langle 20 \rangle \langle skip \rangle$$

$$Test103 \stackrel{\frown}{=} c.(x?)!(y!)!(z?) \longrightarrow \langle 20 \rangle \langle skip \rangle$$

$$Test103 \stackrel{\frown}{=} c.(x?)!(y!)!(z?) \longrightarrow \langle 20 \rangle \langle skip \rangle$$

$$Test103 \stackrel{\frown}{=} c.(x?)!(y!)!(z?) \longrightarrow \langle 20 \rangle \langle skip \rangle$$

$$Test103 \stackrel{\frown}{=} c.(x?)!(y!)!(z?) \longrightarrow \langle 20 \rangle \langle skip \rangle$$

^{*} $S \in \mathbb{P}(\langle y == \mathbb{N} \rangle)$, hence $S.y \in \mathbb{N}$.

^{*} x?, y!, z? are decorated names; usually they appear in schemas. If this proves too complicated, perhaps having it separate as another file is a good away to divide-and-conquer.

Description

Action	Communication pattern
Test25	$\operatorname{In}(x,\mathbb{N}), \operatorname{In}(y,\mathbb{N}), \operatorname{In}(z,\mathbb{N})$
Test26	$In(x, \mathbb{N}), Out(n1), Dot(n2)$
Test27	$\operatorname{Out}(n1), \operatorname{In}(x, \mathbb{N}), \operatorname{Dot}(n2)$
Test28	$\operatorname{Dot}(n1)$, $\operatorname{Out}(n2)$, $\operatorname{In}(x,\mathbb{N})$, Synch
Test29	Synch, Synch, Synch
Test30	$\operatorname{In}(i,\mathbb{N}), \operatorname{Out}(\mathbb{N} \times \mathbb{N})$
Test31	$\operatorname{Dot}(S.y), \operatorname{In}(z, \mathbb{N} \times \mathbb{N})$
Test32	$\operatorname{Out}(x?), \operatorname{Out}(y!), \operatorname{Out}(z?)$

Timed comminication prefix with restricting expression.

$$Test104 \stackrel{\frown}{=} c?x: (x>1)!(fx) \longrightarrow \mathbf{Skip}$$

$$Test105 \stackrel{\frown}{=} c?x \longrightarrow c?z: (z>x.1).(f(x.2+x.3)) \longrightarrow \mathbf{Skip}$$

$$Test106 \stackrel{\frown}{=} c?x: (x>1).(f(x.2+x.3)) \longrightarrow \langle outside \rangle \mathbf{Skip}$$

$$Test107 \stackrel{\frown}{=} c?x: (x>1).(f(x.2+x.3)) \longrightarrow \langle outside \rangle c?z: (z>x.1).(f(x.2+x.3)) \longrightarrow \langle \mathbf{Skip}$$

$$Test108 \stackrel{\frown}{=} c?x: (x>1).(f(x.2+x.3)) \longrightarrow \langle outside \rangle c?z: (z>x.1).(f(x.2+x.3)) \longrightarrow \langle 20 \rangle \mathbf{Skip}$$

$$Test109 \stackrel{\frown}{=} c?x: (x>1).(f(x.2+x.3)) \longrightarrow \langle outside \rangle c?z: (z>x.1).(f(x.2+x.3)) \longrightarrow \langle 20 \rangle \langle outside \rangle c$$

$$Test110 \stackrel{\frown}{=} c?x: (x>1).(f(x.2+x.3)) \longrightarrow \langle outside \rangle c?z: (z>x.1).(f(x.2+x.3)) \longrightarrow \langle 20 \rangle \langle outside \rangle c$$

Description

Action	Communication pattern
Test33	$\operatorname{In}(x, \{v : \mathbb{N} \mid v > 1\}), \operatorname{Out}(\mathbb{N} \times \mathbb{N})$
Test34	$\operatorname{In}(x, \mathbb{N} \times \mathbb{N} \times \mathbb{N}); \operatorname{In}(z, \{v : \mathbb{N} \mid v > x.1\}), \operatorname{Out}(\mathbb{N} \times \mathbb{N})$

^{*} type on inputs are restricted according to given predicate.

Finally we have generic channels version with time

$$Test111 \stackrel{\frown}{=} g[\mathbb{N} \times \mathbb{N} \times \mathbb{N}]?x!n1.n2 \longrightarrow \langle 20 \rangle \mathbf{Skip}$$

 $Test112 \stackrel{\frown}{=} g.n1.(f n1) \longrightarrow \langle 20 \rangle \mathbf{Skip}$

7 Example 6 — AT timed prefix

Production rule:

communication ATTIME DECORWORD PREFIXTHEN circusAction communication ATTIME DECORWORD PREFIXTHEN LCIRCTIME expression RCIRCTIME circusAction

• Grammar for @ operator with actions

^{*} Test34 input on z is from "?z: (z > x.1)".

- Grammer for @ operator with expression and action
- Expressions are acceptable by parser (similar to previous expression patterns)
- Comminication channel can allow previous communication patterns and restricted inputs

```
Test113 \triangleq c?x?y?z@X \longrightarrow \langle 10 + outside \rangle \mathbf{Skip}
Test114 \triangleq c?x!n1.n2@Z \longrightarrow \langle x? \rangle \mathbf{Skip}
Test115 \triangleq c!n1?x.n2@Y \longrightarrow \langle f \rangle \mathbf{Skip}
Test116 \triangleq c.n1!n2?x@x? \longrightarrow \langle 20 \rangle d@f \longrightarrow \langle \theta S \rangle \mathbf{Skip}
Test117 \triangleq d \longrightarrow \langle f \rangle e \longrightarrow \langle f \rangle \mathbf{Skip}
Test118 \triangleq c?i!(fi)@W \longrightarrow \mathbf{Skip}
Test119 \triangleq c.(S.y)?z@K \longrightarrow \mathbf{Skip}
Test120 \triangleq c.(x?)!(y!)!(z?)@Q \longrightarrow \langle 20 \rangle \mathbf{Skip}
Test121 \triangleq c!n1?x.n2@Y \longrightarrow \langle f \rangle d \longrightarrow \mathbf{Skip}
Test122 \triangleq c!n1?x.n2@Y \longrightarrow \langle f \rangle d \longrightarrow \langle outside \rangle \mathbf{Skip}
Test122 \triangleq c!n1?x.n2@Y \longrightarrow \langle f \rangle d \longrightarrow \langle outside \rangle \langle 20 \rangle \blacktriangleleft \mathbf{Skip}
Test123 \triangleq c!n1?x.n2@Y \longrightarrow \langle f \rangle d \longrightarrow \langle outside \rangle \langle 20 \rangle \blacktriangleleft \mathbf{wait} \ 20
Test124 \triangleq c!n1?x.n2@Y \longrightarrow \langle f \rangle d \longrightarrow \langle outside \rangle \langle 20 \rangle \blacktriangleleft \mathbf{wait} \ t : \mathbb{N} \bullet d \longrightarrow \mathbf{Skip}
Test125 \triangleq c!n1?x.n2@Y \longrightarrow \langle f \rangle d \bigcirc \langle outside \rangle \langle 20 \rangle \blacktriangleleft \mathbf{wait} \ t : \mathbb{N} \bullet d \longrightarrow \mathbf{Skip}
```

8 (! Prolegomena) — basic process footer

It just terminates

• Skip

 \mathbf{end}