# OHM'S LAW

V = IR

# **ELECTRICAL RESISTIVITY**

$$\rho = \frac{RA}{\ell} = \frac{VA}{I\ell}$$
units =  $(\Omega \cdot m)$ 

#### **ELECTRICAL CONDUCTIVITY**

ease with which a material generates an electric current

$$\sigma = \frac{1}{\rho}$$
units =  $(\Omega \cdot m)^{-1}$ 

# **CURRENT DENSITY**

$$J = \sigma \mathcal{E} \dots \mathcal{E} = \frac{V}{\ell}$$

#### **CONDUCTIVITIES**

Metals –  $10^7 \ (\Omega \cdot m)^{-1}$ Semi-conductors –  $10^{-6} \ to \ 10^4 \ (\Omega \cdot m)^{-1}$ Insulators –  $10^{-10} \ to \ 10^{-20} \ (\Omega \cdot m)^{-1}$ 

#### **CURRENT**

result of motion of charged particles responding to forces from externally applied electric field [+ moves with current direction, - moves opposite]

**ELECTRIC CONDUCTION:** flow of electron causing a current (within most solids) **IONIC CONDUCTION:** possible current produced from net motion of charged ions (diffusion of ions)

# BAND STRUCTURE = how electrons fill orbitals in an atom

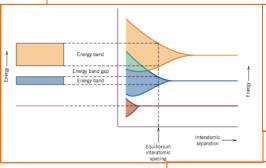
- electrons acted upon by the electrons & nuclei of adjacent atoms when in close proximity
  - may split into series of closely spaced electronic states (electron energy bands)
  - extent of splitting depends on separation
  - energy band gaps = the gaps between adjacent bands
- total # states in each band = total states from N atoms (s band = N states, p band = 3N states)

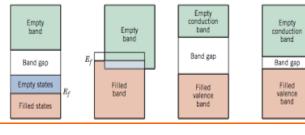
# FERMI ENERGY (E<sub>f</sub>)

energy of last filled state at 0K.

CONDUCTOR if bands partially full/overlap INSULATOR/ SEMICONDUCTOR

if valence bond full & conduction band empty





**FREE ELECTRON** participates in conduction process **HOLE (semiconductor/insulators)** electrons with energy LESS than E<sub>f</sub> and still participate in conduction

#### ELECTRON MOBILITY

- free electrons accelerate opposite field direction
- acceleration is counteracted by friction
  - friction from scattering e- from lattice impurities
  - impurity atoms, vacancies, thermal vibrations, dislocations, interstitial atoms
- scattering—e loses kinetic energy, motion changes direction, resistance to passage of current
- net motion opposite field
- drift velocity ( $V_d$ ) = average e-velocity opposite field

 $V_d = \mu_E E$  electron mobility (m<sup>2</sup>/Vs) x electric field

# - very high conductivity – many electrons excited into empty state above $E_{\rm f}$ RESISTIVITY depends on TEMPERATURE

CONDUCTION IN METALS

- electron excited to empty state about the Fermi energy (free electron)

• requires little energy because there are vacant states adjacent to highest-filled state at Fermi energy (provided by electric field)

as T increases, # of impurities increases, BUT ue decreases (dominates)

$$\rho_t = \rho_0 + aT$$

$$\frac{1}{\sigma} = \rho = \rho_0 + aT$$

a is the material constant for T > -200 °C

#### **RESISTIVITY depends on # OF IMPURITIES**

as T increases, # of impurities increases, BUT ue decreases (dominates)

 $\rho_i = Ac_i (1 - c_i)$ 

A is the constant

concentration is in terms of atomic fraction (%at / 100)

**Matthieson's Rule:**  $\rho_{total} = \rho_t + \rho_i + \rho_d$  (temp + impurities + deformation)

# RESISTIVITY depends on COLDWORKING Strengthening pure alloys (soft) by adding

Strengthening pure alloys (soft) by adding solutes/particles – not much effect on conductivity

# CONDUCTION IN SEMICONDUCTORS & INSULATORS

- electron must be thermally promoted across band gap into empty states at bottom of conduction band to become a free electron
- band gap energy ( $E_g$ ) ~ 1eV ... from non-electric source
- $E_g > 3eV$  = insurmountable gap = insulating material
- Eg increase = larger band gap & decreased electrical conductivity
- Semiconductors have a narrow band gap
- Insulators have a relatively wide band gap

#### N-TYPE EXTRINSIC SEMICONDUCTION

- e-loosely bound—weak attraction promotes conduction band
- e- binding energy = E requited to excite e- to state within conduction band (E<sub>D</sub>)
- each excitation donates an e- to the conduction band (donor)
- no corresponding hole created in valence bond
- Fermi level shifted up in band gap
- $E_D$  <<  $E_g$  , n >> p many donor  $e^{\scriptscriptstyle -}$  promoted at room T

$$\sigma = n|e|\mu_E$$

# INTRINSIC SEMICONDUCTIVITY

- narrow band gap (less than 2eV)
- At T = 0K, conductivity = 0
- At T > 0K heat helps e- jump over band gap (e—hole pair)
- Hole is created for every  $e^{\text{-}}$  excited to conduction band

#### INTRINSIC CONDUCTION

- Free electrons (n = # e<sup>-</sup> / m<sup>3</sup>)
- Holes ( $p = \# holes / m^3$ )
- $\sigma = n|e|\mu_E + p|e|\mu_h$
- since # holes = # free e- for intrinsic semi-conductors

$$\sigma = n |e| (\mu_E + \mu_h)$$

- electrons and holes move in response to electric field
- e/atom = e/volume x volume/atom

# P-TYPE EXTRINSIC SEMICONDUCTION

- Dopant atoms (each with a valence bond deficient in an e-)
- Hole for electron... new level above valence (acceptor state)
- Hole left in valence bond when e- fills acceptor state
- p >> n ...  $\sigma = n|e|\mu_E$
- Fermi level positioned within

# **CARRIER CONCENTRATION - TEMPERATURE DEPENDENCE** (semiconductors)

- Increased thermal energy allows e- to move to conduction band
  - Intrinsic carrier concentration increases
- Intrinsic excitations insignificant vs. extrinsic donor excitations until very high temperatures

# INTRINSIC SEMICONDUCTORS

$$n = n_0 e^{-\frac{E_g}{2kT}}$$

# $n = n_o e^{-\frac{E_g}{2kT}} \label{eq:norm}$ N-TYPE EXTRINSIC SEMICONDUCTORS

$$n = n_{D_o} e^{-\frac{E_L}{kT}}$$

# $n = n_{D_0} e^{-\frac{E_D}{kT}} \label{eq:n_D_0}$ P-TYPE EXTRINSIC SEMICONDUCTORS

$$p = n_{A_0} e^{-\frac{E_A}{kT}}$$

### COEFFICIENT OF THERMAL EXPANSION

- Materials expand/contract when heated and cooled

$$\frac{\Delta \ell}{\ell} = \alpha_{\ell} \, \Delta T \quad \text{OR} \quad \frac{\ell_f - \ell_o}{\ell_o} = \alpha_{\ell} \left( T_f - T_o \right) \quad (^{\circ}\text{C}^{-1})$$
- **Thermal expansion** = extent a material expands upon heating
- **Volume changes with T:**  $\frac{\Delta V}{V_o} = \alpha_V \, \Delta T$ 

- For materials with isotropic thermal expansion,  $\alpha_V = 3\alpha_\ell$
- Thermal expansion—increase in avg. distance between atoms
- Thermal expansion due to asymmetric curvature of potential energy trough NOT the increased vibrational amplitudes with T
  - → A symmetric potential energy curve = NO NET CHANGE in interatomic separation (NO THERMAL EXPANSION)
- Thermal stress = stresses induced in body due to T changes

$$\sigma = E\alpha_{\ell} \left( T_o - T_f \right)$$

## THERMAL CONDUCTIVITY (steady-state heat flow)

- Heat transported from high T to low T regions
- Thermal conductivity = ability to transport heat
- **Heat flux (q)** = rate heat energy transfer through given surface  $q\left(\frac{W}{m^2}\right) = -k\frac{dT}{dx} \qquad \frac{dT \ is \ T \ gradient \ through \ conducting \ medium}{k \ is \ thermal \ conductivity} \left(\frac{W}{mK}\right)$
- Heat is conducted by lattice vibration waves (phonons) and free electrons (usually just one predominates)
  - → Metals = free electrons
  - → Ceramic = phonons (vibrational)
  - → Polymers = vibrational/rotational

### STRESS-STRAIN BEHAVIOUR

- Hooke's law relation: stress & strain for elastic deformation
  - Tension  $\sigma = E \mathcal{E}$  (E is Young's elastic Modulus) Shear (G is Shear Modulus)
- Modulus of Elasticity (Young's), E = proportionality constant
  - → Ration stress: strain in elastic region (measures stiffness)
  - → Deformation completely elastic
- **Elastic Deformation** = when stress & strain are proportional
  - → Slope of line = E, independent of time
- → Nonpermanent (return original shape when load released)
- High Modulus of Elasticity (E) = stiff material
- Varies by 106 depends little on alloying/T in crystalline solid
- Apply tension (pull solid) atoms forced apart  $(r > r_0)$ 
  - → Net attractive force (reaction force apposed applied force)
- If forve vs. interatomic spacing in appox. straight line
  - $\rightarrow$  If slope = S then...F = -s (r-r<sub>0</sub>)

  - → To describe elastic behavior:  $\sigma = E \mathcal{E}$ →  $\sigma$  is stess  $\left(\frac{F}{\text{unit A}}\right)$ , E is modulus of elasticity,  $\mathcal{E}$  is strain
- response correlated by stress (normalized force) & strain

#### CARRIER DENSITY—CONDUCTIVITY

- Steeper T-dependence for intrinsic region (E<sub>g</sub>>> E<sub>A</sub>)
- Small saturation region
- Nearly constant conductivity near room temperature
- Conductivity SOMETIMES DECREASE with T in extrinsic regions
  - # of carriers in extrinsic region is constant
  - mobility decreases with temperature due to increased scattering from thermal fluctuations

#### **HEAT CAPACITY**

- Solids increase in temperature when heater (absorb energy)
- **Heat capacity** = ability to absorb heat from surroundings
- (C) energy to raise 1 mole of solid by 1 degree

$$C = \frac{dQ}{dt} \left( \frac{J}{mol \cdot K} \right)$$

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- **Specific heat capacity** = energy per unit mass per degree  $c = \left( \frac{J}{kg \cdot K} \right)$  ... energy content of material

- → Can be measured at constant volume (C<sub>V</sub>) or pressure (C<sub>P</sub>)
- Atoms constantly vibrate at high frequency and small amplitude
  - → Elastic/sound waves—short wavelength, high frequency, propagate at speed of sound
  - → Quantized energy—phonon = single quantum of vibrational energy
  - → Elastic waves responsible for thermal scattering
- Increasing K.E. of e- (only for free e- about E<sub>f</sub>)
- Heat Capacity depends on TEMPERATURE
  - $\rightarrow \theta_D$  = **Debye temperature** (usually less than room T)

  - → At low T ( $<\theta_D$ ) C<sub>V</sub>=AT<sup>3</sup> (T-dependent) → At high T ( $>\theta_D$ ) C<sub>V</sub>=3R ... 25 $\frac{J}{mol\cdot K}$  (T-independent)

#### MECHANICAL PROPERTIES OF METALS

- Solid moves if: a net force acts OR if forces & moments balance atoms are pushed close (compression) or apart (tension)
- External compressive force forces atoms closer (r < r<sub>0</sub>)
  - → Net repulsive force (solid exerts reaction force)
- Apply tension (pull solid) atoms forced apart (r > r<sub>0</sub>)
  - → Net attractive force (reaction force apposed applied force)
- If forve vs. interatomic spacing in appox. straight line
  - $\rightarrow$  If slope = S then... F = -s (r-r<sub>0</sub>)

  - → To describe elastic behavior:  $\sigma = E \mathcal{E}$ →  $\sigma$  is stess  $\left(\frac{F}{\text{unit A}}\right)$ , E is modulus of elasticity,  $\mathcal{E}$  is strain
- response correlated by stress (normalized force) & strain (normalized destruction)
- loads can be applied through...compression, tension, or shear

- stress (MPa): 
$$\sigma = \frac{F}{A_o} = \frac{instaneous load applied}{instaneous load applied} \left[ 1 MP_a = 10^6 \frac{N}{m^2} \right]$$
- strain:  $\sigma = \frac{\ell_i - \ell_o}{\ell_o} = \frac{\Delta gauge lenth (direction of applied force)}{original gauge lenth} NO UNITS$ 
- shear stress:  $\tau = \frac{F}{A_o} = \frac{instantaneous shear load}{original corss-sectional area}$ 
- shear strain ( $\gamma$ ): tangent of shear angle from applied shear load

- **strain**: 
$$\sigma = \frac{\ell_i - \ell_o}{\ell_o} = \frac{\Delta \text{ gauge lenth (direction of applied force)}}{\text{original gauge lenth}}$$
 NO UNITS