



# C O M P A S

```
    if key in mesh.vertices():
        if key in fixed:
            continue

        p = key_xyz[key]
        nbrs = mesh.vertex_neighbours(key, ordered=True)
        c = center_of_mass_polygon([[key_xyz[nbr] for nb
```

Visualisation

Geometry

Cross Product

OABB using PCA

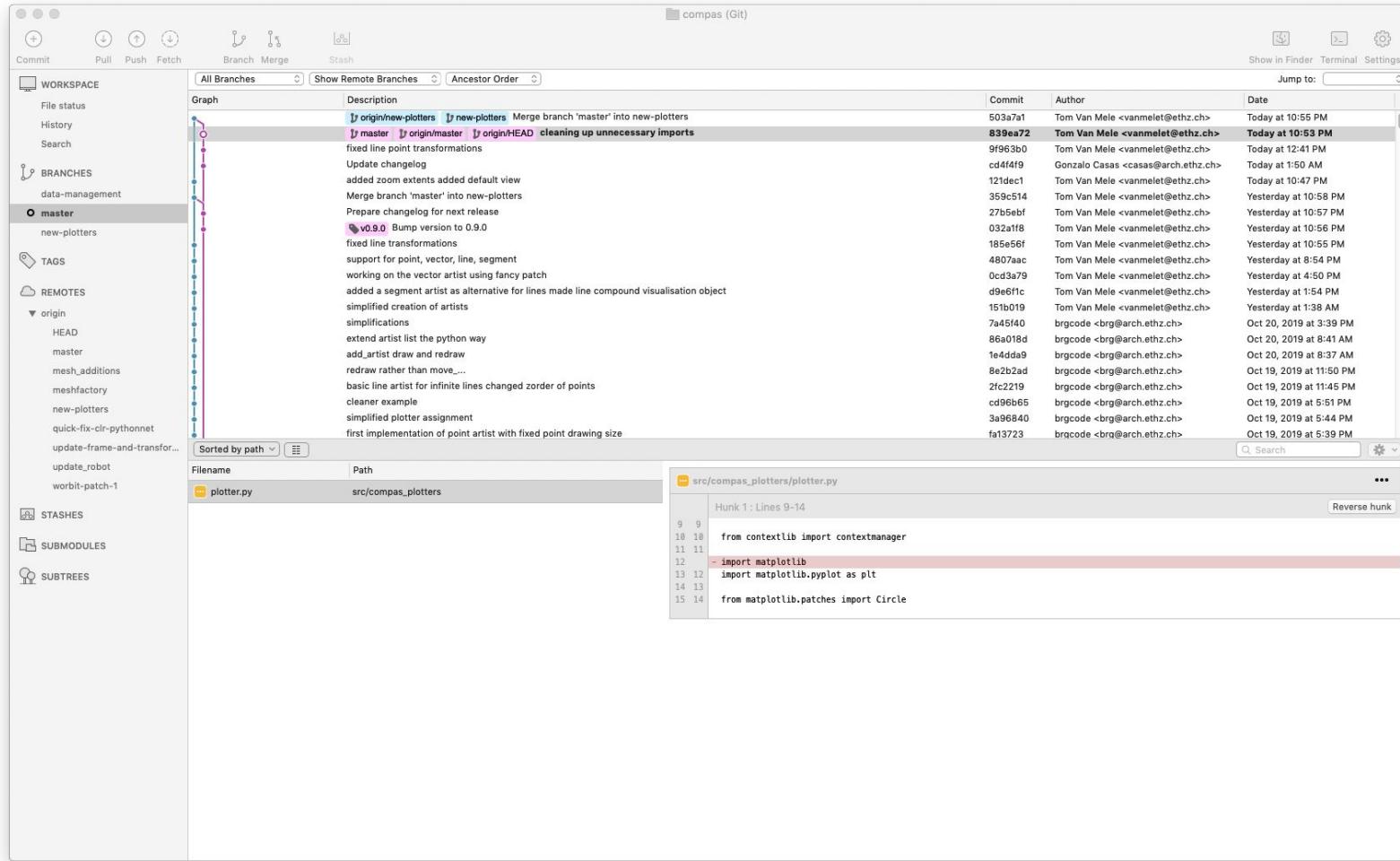
Data Structures

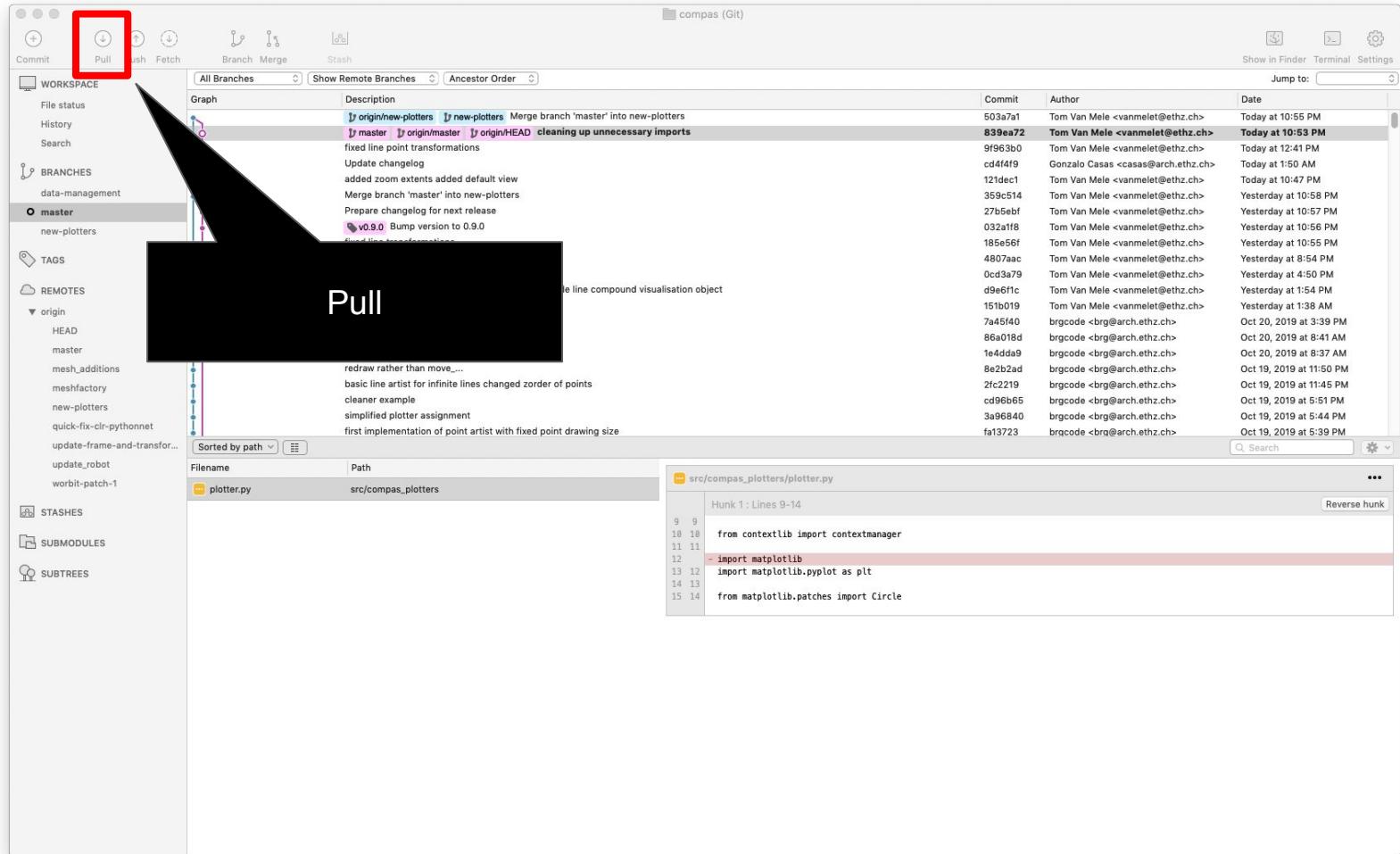
Network

Mesh

(VolMesh)

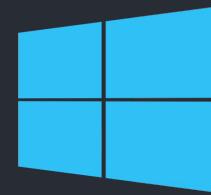
Update COMPAS repo





ita19 vs ita19-dev

⌘ + SPACE



Terminal

Anaconda Prompt







```
>>> import compas
```

```
>>>
```

```
>>> import compas  
>>> compas.__version__  
'0.8.1'  
>>>
```

```
>>> import compas  
>>> compas.__version__  
'0.8.1'  
>>>
```

```
>>> import compas  
>>> compas.__version__  
'0.8.1'  
>>> exit()
```







```
>>> import compas
```

```
>>>
```

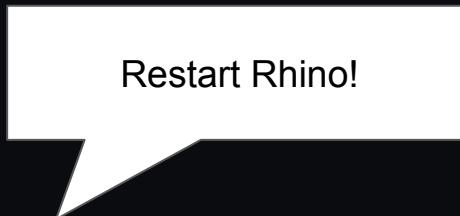
```
>>> import compas  
>>> compas.__version__  
'0.9.0'  
>>>
```

```
>>> import compas  
>>> compas.__version__  
'0.9.0'  
>>>
```

```
>>> import compas  
>>> compas.__version__  
'0.9.0'  
>>> exit()
```

# Update Rhino





Restart Rhino!

```
python -m compas_rhino.install -v 6.0 -p compas compas_rhino compas_ghpython
```

Update ITA19 repo

IT19 (Git)

Commit Pull Fetch Branch Merge Stash

Show in Finder Terminal Settings

Jump to:

All Branches Show Remote Branches Ancestor Order

WORKSPACE

File status

- History
- Search

BRANCHES

- dev
- master
- Week3

TAGS

REMOTES

- origin
- dev
- HEAD
- mas\_week
- master
- Week3

STASHES

SUBMODULES

SUBTREES

Pull

Description Commit Author Date

Description	Commit	Author	Date
if master if origin/master if origin/HEAD almost there :)	3f8da83	Tom Van Mele <vannmelet@ethz.ch>	Today at 11:41 AM
placeholders for first weeks	d6b3cb4	Tom Van Mele <vannmelet@ethz.ch>	Today at 1:29 AM
Merge branch 'Week3'	4f3c2ab	Tom Van Mele <vannmelet@ethz.ch>	Today at 1:27 AM
if origin/Week3 if Week3 cleaning up	e48246a	Tom Van Mele <vannmelet@ethz.ch>	Today at 1:26 AM
moved stuff around	20e907c	Tom Van Mele <vannmelet@ethz.ch>	Yesterday at 8:45 PM
slide images	83d437d	Tom Van Mele <vannmelet@ethz.ch>	Yesterday at 3:00 PM
selected assignments	d65be5c	Tom Van Mele <vannmelet@ethz.ch>	Yesterday at 12:37 PM
adding a text box	8d877e2	brgcode <brg@arch.ethz.ch>	Yesterday at 7:56 AM
adding a text box	45ee12a	Tom Van Mele <vannmelet@ethz.ch>	Oct 21, 2019 at 11:01 PM
adding a text box	1ec6212	Tom Van Mele <vannmelet@ethz.ch>	Oct 21, 2019 at 4:50 PM
Update Path planning.ipynb	6982847	Tom Van Mele <vannmelet@ethz.ch>	Oct 21, 2019 at 1:37 AM
Update notebooks after session	50ba6df	Tom Van Mele <vannmelet@ethz.ch>	Oct 19, 2019 at 8:06 AM
update	8fb2f9d	brgcode <brg@arch.ethz.ch>	Oct 16, 2019 at 5:17 PM
Merge branch 'mas_week'	e34b5a9	Tom Van Mele <vannmelet@ethz.ch>	Oct 15, 2019 at 11:38 PM
if origin/mas_week update	e1cc6b3	Gonzalo Casas <casaas@arch.ethz.ch>	Yesterday at 6:58 PM
	447874	Gonzalo Casas <casaas@arch.ethz.ch>	Yesterday at 6:29 PM
	124a9a6	Romana Rust <rurst@rch.ethz.ch>	Yesterday at 6:07 PM
	5f0f6e1	Gonzalo Casas <casaas@arch.ethz.ch>	Yesterday at 6:10 PM
	cc440ff	Romana Rust <rurst@rch.ethz.ch>	Yesterday at 11:48 AM
	8491fff	Romana Rust <rurst@rch.ethz.ch>	Oct 21, 2019 at 12:15 PM
	00938c3	Romana Rust <rurst@arch.ethz.ch>	Oct 21, 2019 at 12:12 PM

modules/module2/crossproduct\_1a.py

Hunk 1 : Lines 1-13

```
from compas.geometry import cross_vectors
from compas.geometry import length_vector
from compas.geometry import angle_vectors
```

1 1
2 2
3 3
4 4
5 5
6 6
7 7
8 8
9 9
10 10
11 11
12 12
13 13

print(length\_vector(uxv))
u\_uxv = angle\_vectors(u, u\_xv)
v\_uxv = angle\_vectors(v, uxv)
+
print(u\_uxv)
print(v\_uxv)

VS Code

 Welcome ×

## Start

- [New file](#)
- [Open folder...](#)
- [Add workspace folder...](#)

## Recent

No recent folders

## Help

- [Printable keyboard cheatsheet](#)
- [Introductory videos](#)
- [Tips and Tricks](#)
- [Product documentation](#)
- [GitHub repository](#)
- [Stack Overflow](#)
- [Join our Newsletter](#)

Show welcome page on startup

## Customize

## Tools and languages

Install support for [JavaScript](#), [TypeScript](#), [Python](#), [PHP](#), [Azure](#) and [more](#)

## Settings and keybindings

Install the settings and keyboard shortcuts of [Vim](#), [Sublime](#), [Atom](#) and others

## Color theme

Make the editor and your code look the way you love

## Learn

## Find and run all commands

Rapidly access and search commands from the Command Palette (⌃⌘P)

## Interface overview

Get a visual overlay highlighting the major components of the UI

## Interactive playground

Try essential editor features out in a short walkthrough

Welcome

The image shows the 'Welcome' screen of the Visual Studio Code (VS Code) application. On the left, there's a vertical sidebar with icons for file operations (New file, Open folder, Add local repository), recent files (Recent), help resources (Help), and settings (Settings). The main area is divided into several sections:

- Start**: Contains options to 'New file', 'Open folder...', and 'Add local repository...'. The 'Open folder...' option is highlighted with a red rectangle.
- Customize**: Includes sections for 'Tools and languages' (support for JavaScript, TypeScript, Python, PHP, Azure, Docker, etc.), 'Settings and keybindings' (Vim, Sublime, Atom), and 'Color theme' (make the editor look like your favorite editor).
- Recent**: Shows that there are no recent folders.
- Help**: Provides links to a keyboard cheatsheet, introductory videos, tips and tricks, product documentation, GitHub repository, Stack Overflow, and a newsletter sign-up.
- Learn**: Offers tutorials on 'Find and run all commands' (using the Command Palette), 'Interface overview' (UI components), and an 'Interactive playground' (try features in a walkthrough).
- Settings**: Shows a checkbox for 'Show welcome page on startup' which is checked.

At the bottom right, there are status icons for battery, signal, and notifications.

The screenshot shows the VS Code interface with the 'Welcome' tab selected in the top navigation bar. The left sidebar displays the file tree under the 'EXPLORER' tab, showing a workspace named 'ITA19' containing files like '.vscode', 'modules', 'slides', '.gitignore', 'LICENSE', 'README.md', and 'setup.cfg'. The main content area features the 'Welcome' screen with sections for 'Start', 'Recent', 'Help', and 'Customize'.

**Welcome**

Start

- New file
- Open folder...
- Add workspace folder...

Recent

No recent folders

Help

- [Printable keyboard cheatsheet](#)
- [Introductory videos](#)
- [Tips and Tricks](#)
- [Product documentation](#)
- [GitHub repository](#)
- [Stack Overflow](#)
- [Join our Newsletter](#)

Show welcome page on startup

Customize

Tools and languages

Install support for [JavaScript](#), [TypeScript](#), [Python](#), [PHP](#), [Azure](#), Docker and more

Settings and keybindings

Install the settings and keyboard shortcuts of [Vim](#), [Sublime](#), [Atom](#) and others

Color theme

Make the editor and your code look the way you love

Learn

Find and run all commands

Rapidly access and search commands from the Command Palette (⌃⌘P)

Interface overview

Get a visual overlay highlighting the major components of the UI

Interactive playground

Try essential editor features out in a short walkthrough

OUTLINE

master 0 ↓ 13↑ 0 △ 0

The screenshot shows the Visual Studio Code (VS Code) interface with a dark theme. The Explorer sidebar on the left lists project files and folders:

- OPEN EDITORS: crossproduct\_0a.py
- ITA19
  - .vscode
  - modules
    - module0
    - module1
    - module2
      - crossproduct\_0a.py
      - crossproduct\_0b.py
      - crossproduct\_1a.py
      - crossproduct\_1b.py
      - datastructures\_0.py
      - plotters\_0.py
      - plotters\_1.py
      - plotters\_2.py
    - module6
    - module8
    - module9
    - slides
  - .gitignore
  - LICENSE
  - README.md
  - setup.cfg

The main editor area displays the content of `crossproduct_0a.py`:

```
1  from compas.geometry import cross_vectors
2
3  u = [1.0, 0.0, 0.0]
4  v = [0.0, 1.0, 0.0]
5
6  uxv = cross_vectors(u, v)
7
8  print(uxv)
9
```

The status bar at the bottom provides information about the workspace and terminal:

master 0 13↑ Python 3.6.7 64-bit ('ita19': conda) 0 △ 0 Ln 1, Col 1 Spaces: 4 UTF-8 LF Python ☺ 🔍

The screenshot shows the Visual Studio Code interface with the following details:

- EXPLORER** sidebar:
  - OPEN EDITORS: `crossproduct_0a.py`
  - IT19 folder:
    - .vscode
    - modules:
      - module0
      - module1
      - module2:
        - `crossproduct_0a.py` (highlighted)
        - `crossproduct_0b.py`
        - `crossproduct_1a.py`
        - `crossproduct_1b.py`
        - `datastructures_0.py`
        - `plotters_0.py`
        - `plotters_1.py`
        - `plotters_2.py`
      - module6
      - module8
      - module9
      - slides
    - `.gitignore`
    - `LICENSE`
    - `README.md`
    - `setup.cfg`
  - CODE** tab: `crossproduct_0a.py`

```
1  from compas.geometry import cross_vectors
2
3  u = [1.0, 0.0, 0.0]
4  v = [0.0, 1.0, 0.0]
5
6  uxv = cross_vectors(u, v)
7
8  print(uxv)
9
```
  - STATUS BAR**:
    - master
    - Python 3.6.7 64-bit ('IT19': conda) (highlighted with a red box)
    - 0 △ 0
    - Ln 1, Col 1   Spaces: 4   UTF-8   LF   Python   😊   📰

The screenshot shows the Visual Studio Code (VS Code) interface with a dark theme. The left sidebar contains icons for Explorer, Search, Problems, and others. The Explorer view shows a project structure for 'ITA19' with files like 'crossproduct\_0a.py', 'crossproduct\_0b.py', etc., under 'module2'. The main editor area displays a Python script named 'crossproduct\_0a.py' with the following code:

```
1  from compas.geometry import cross_vectors
2
3  u = [1.0, 0.0, 0.0]
4  v = [0.0, 1.0, 0.0]
5
6  uxv = cross_vectors(u, v)
7
8  print(uxv)
9
```

The status bar at the bottom shows the current workspace ('master'), the Python interpreter ('Python 3.6.7 64-bit ('ita19-dev': conda)'), and other system information like line and column numbers, spaces, and encoding.

The screenshot shows the Visual Studio Code (VS Code) interface with a dark theme. The Explorer sidebar on the left lists the project structure, including modules, files, and configuration files like .vscode/settings.json and setup.cfg. Two code editors are open at the top: crossproduct\_0a.py and crossproduct\_0b.py. The active editor, crossproduct\_0b.py, contains Python code for calculating the cross product of two vectors:

```
1  from compas.geometry import Vector
2
3  u = Vector(1.0, 0.0, 0.0)
4  v = Vector(0.0, 1.0, 0.0)
5
6  uxv = u.cross(v)
7
8  print(uxv)
9
```

The status bar at the bottom provides information about the repository (master), Python version (Python 3.6.7 64-bit ('ita19-dev': conda)), and other settings (Spaces: 4, LF, Python).

The image shows a screenshot of the Visual Studio Code (VS Code) interface. On the left is the Explorer sidebar, which lists several project components: GROUP 1 (crossproduct\_0a.py), GROUP 2 (crossproduct\_0b.py), ITA19 (.vscode, settings.json, modules, module0, module1, module2, crossproduct\_0a.py, crossproduct\_0b.py, crossproduct\_1a.py, crossproduct\_1b.py, datastructures\_0.py, plotters\_0.py, plotters\_1.py, plotters\_2.py, module6, module8, module9, slides, .gitignore, LICENSE, README.md). The main area contains two code editors side-by-side.

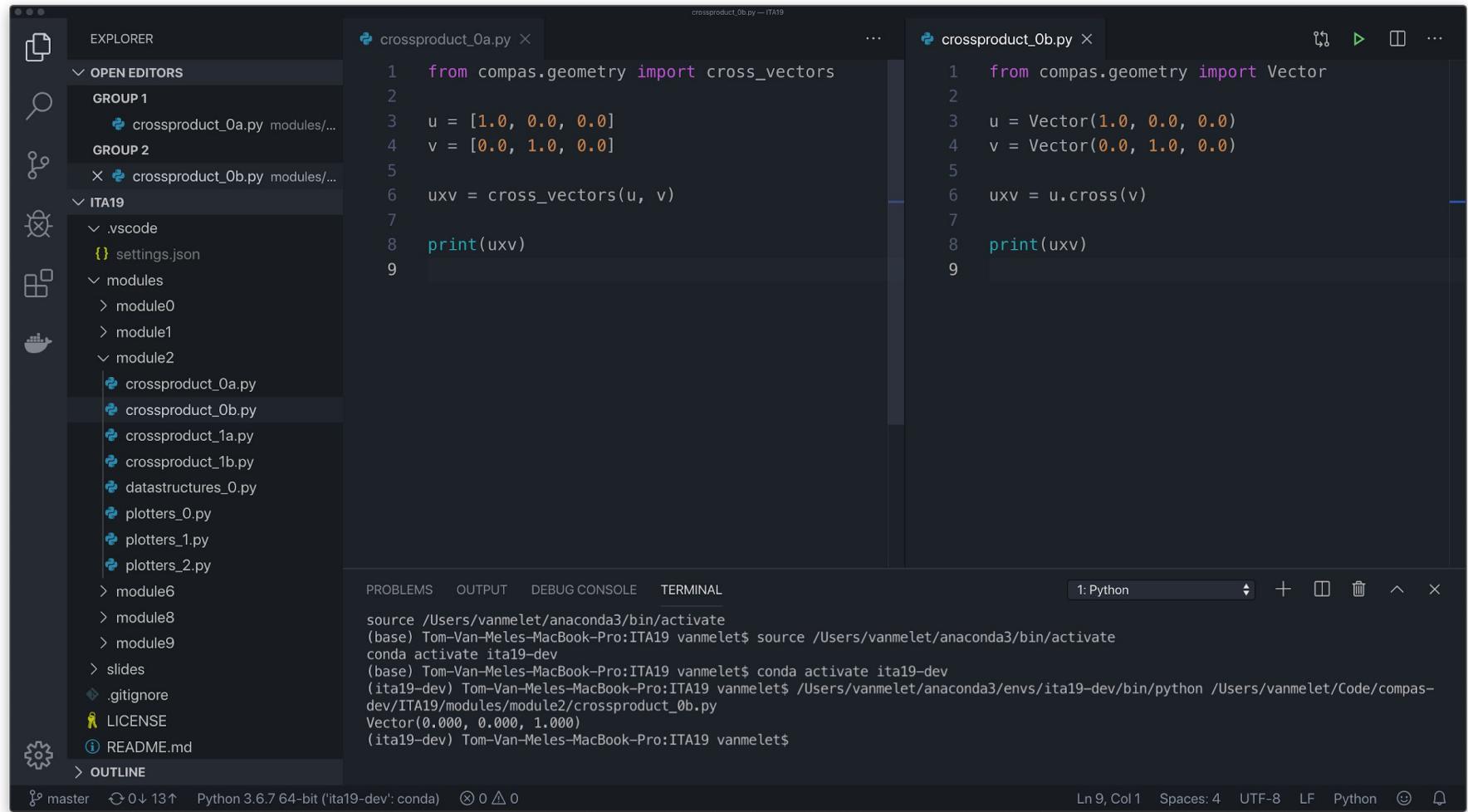
**Left Editor (crossproduct\_0a.py):**

```
1  from compas.geometry import cross_vectors
2
3  u = [1.0, 0.0, 0.0]
4  v = [0.0, 1.0, 0.0]
5
6  uxv = cross_vectors(u, v)
7
8  print(uxv)
9
```

**Right Editor (crossproduct\_0b.py):**

```
1  from compas.geometry import Vector
2
3  u = Vector(1.0, 0.0, 0.0)
4  v = Vector(0.0, 1.0, 0.0)
5
6  uxv = u.cross(v)
7
8  print(uxv)
9
```

At the bottom, the status bar displays: master, Python 3.6.7 64-bit ('ita19-dev': conda), 0 △ 0, Ln 9, Col 1, Spaces: 4, UTF-8, LF, Python, and a set of small icons.



EXPLORER

OPEN EDITORS

GROUP 1

- crossproduct\_0a.py

GROUP 2

- crossproduct\_0b.py

IT19

- .vscode
- settings.json
- modules
  - module0
  - module1
  - module2
    - crossproduct\_0a.py
    - crossproduct\_0b.py
    - crossproduct\_1a.py
    - crossproduct\_1b.py
    - datastructures\_0.py
    - plotters\_0.py
    - plotters\_1.py
    - plotters\_2.py
  - module6
  - module8
  - module9

slides

.gitignore

LICENSE

README.md

> OUTLINE

crossproduct\_0a.py ×

```
1   from compas.geometry import cross_vectors
2
3   u = [1.0, 0.0, 0.0]
4   v = [0.0, 1.0, 0.0]
5
6   uxv = cross_vectors(u, v)
7
8   print(uxv)
9
```

crossproduct\_0b.py ×

```
1   from compas.geometry import Vector
2
3   u = Vector(1.0, 0.0, 0.0)
4   v = Vector(0.0, 1.0, 0.0)
5
6   uxv = u.cross(v)
7
8   print(uxv)
9
```

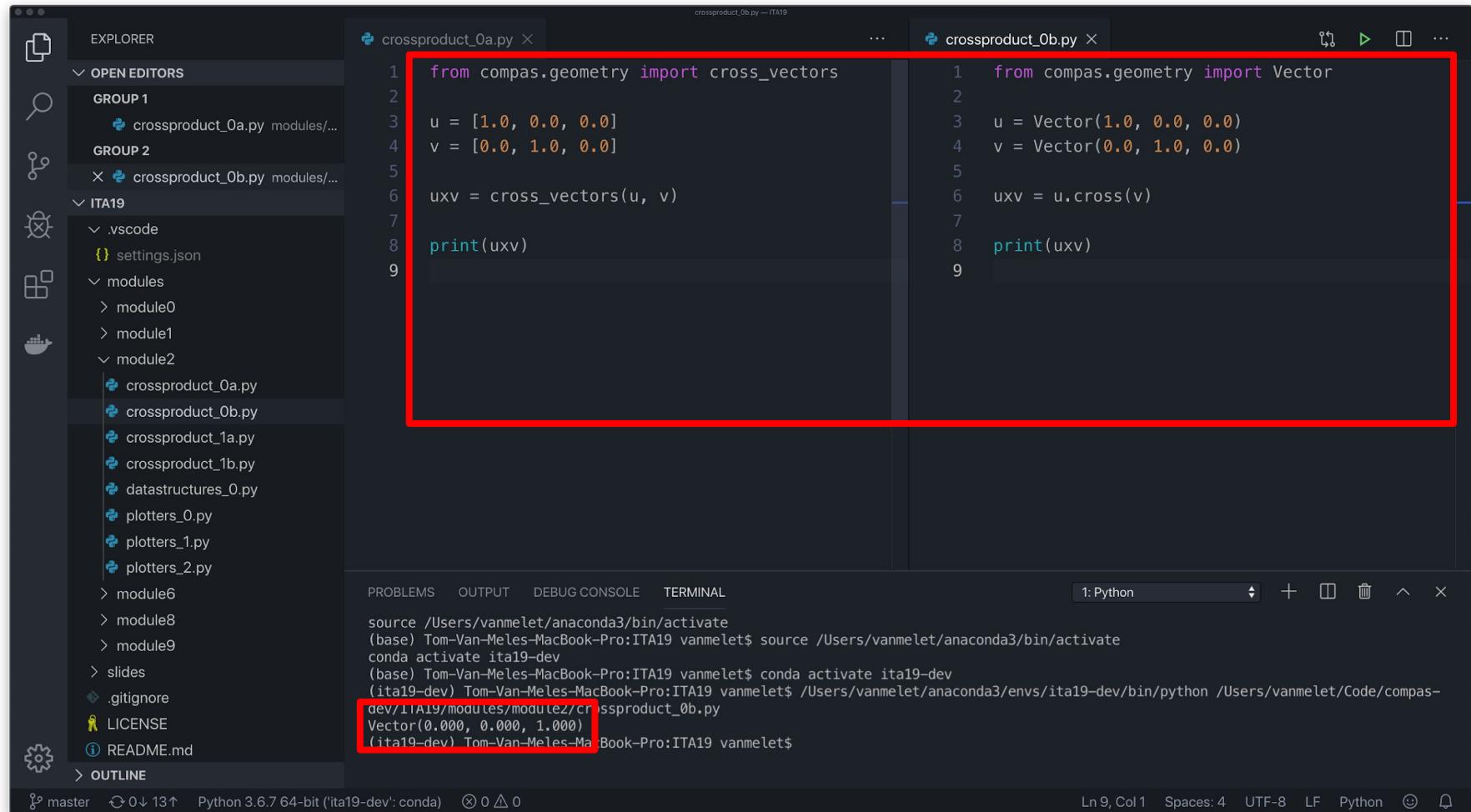
PROBLEMS OUTPUT DEBUG CONSOLE TERMINAL

1: Python

```
source /Users/vanmelet/anaconda3/bin/activate
(base) Tom-Van-Meles-MacBook-Pro:IT19 vanmelet$ source /Users/vanmelet/anaconda3/bin/activate
conda activate ita19-dev
(base) Tom-Van-Meles-MacBook-Pro:IT19 vanmelet$ conda activate ita19-dev
(ita19-dev) Tom-Van-Meles-MacBook-Pro:IT19 vanmelet$ /Users/vanmelet/anaconda3/envs/ita19-dev/bin/python /Users/vanmelet/Code/compas-dev/IT19/modules/module2/crossproduct_0b.py
Vector(0.000, 0.000, 1.000)
(ita19-dev) Tom-Van-Meles-MacBook-Pro:IT19 vanmelet$
```

master 0 13 Python 3.6.7 64-bit ('ita19-dev': conda) 0 0 △ 0

Ln 9, Col 1 Spaces: 4 UTF-8 LF Python ☺ 🔍



The screenshot shows a Visual Studio Code (VS Code) interface with the following details:

- EXPLORER** sidebar:
  - OPEN EDITORS**:
    - GROUP 1**: `crossproduct_0a.py`
    - GROUP 2**: `crossproduct_0b.py`
  - ITA19**:
    - .vscode**: `settings.json`
    - modules**:
      - `module0`
      - `module1`
      - module2**:
        - `crossproduct_0a.py`
        - `crossproduct_0b.py`
        - `crossproduct_1a.py`
        - `crossproduct_1b.py`
        - `datastructures_0.py`
        - `plotters_0.py`
        - `plotters_1.py`
        - `plotters_2.py`
      - `module6`
      - `module8`
      - `module9`
    - `slides`
    - `.gitignore`
    - `LICENSE`
    - `README.md`
  - CROSS PRODUCT FILES**: Two code editors side-by-side, both titled `crossproduct_0a.py` and `crossproduct_0b.py`. Both files contain the following Python code:

```
1  from compas.geometry import cross_vectors
2
3  u = [1.0, 0.0, 0.0]
4  v = [0.0, 1.0, 0.0]
5
6  uxv = cross_vectors(u, v)
7
8  print(uxv)
9
```

A red box highlights the entire content of both code editors.
  - TERMINAL**: Shows the output of running the code:

```
source /Users/vanmelet/anaconda3/bin/activate
(base) Tom-Van-Meles-MacBook-Pro:ITA19 vanmelet$ source /Users/vanmelet/anaconda3/bin/activate
conda activate ita19-dev
(base) Tom-Van-Meles-MacBook-Pro:ITA19 vanmelet$ conda activate ita19-dev
(ita19-dev) Tom-Van-Meles-MacBook-Pro:ITA19 vanmelet$ /Users/vanmelet/anaconda3/envs/ita19-dev/bin/python /Users/vanmelet/Code/compas-dev/ITA19/modules/module2/crossproduct_0b.py
Vector(0.000, 0.000, 1.000)
(ita19-dev) Tom-Van-Meles-MacBook-Pro:ITA19 vanmelet$
```

A red box highlights the output line `Vector(0.000, 0.000, 1.000)`.
  - STATUS BAR**: Shows the current branch (`master`), the number of changes (`0`), the Python version (`Python 3.6.7 64-bit ('ita19-dev': conda)`), and other system information.

```
from compas.geometry import cross_vectors
```

```
u = [1.0, 0.0, 0.0]
```

```
v = [0.0, 1.0, 0.0]
```

```
uxv = cross_vectors(u, v)
```

```
print(uxv)
```

```
[0.0, 0.0, 1.0]
```

```
from compas.geometry import Vector
```

```
u = Vector(1.0, 0.0, 0.0)
```

```
v = Vector(0.0, 1.0, 0.0)
```

```
uxv = u.cross(v)
```

```
print(uxv)
```

```
Vector(0.000, 0.000, 1.000)
```

# Visualisation

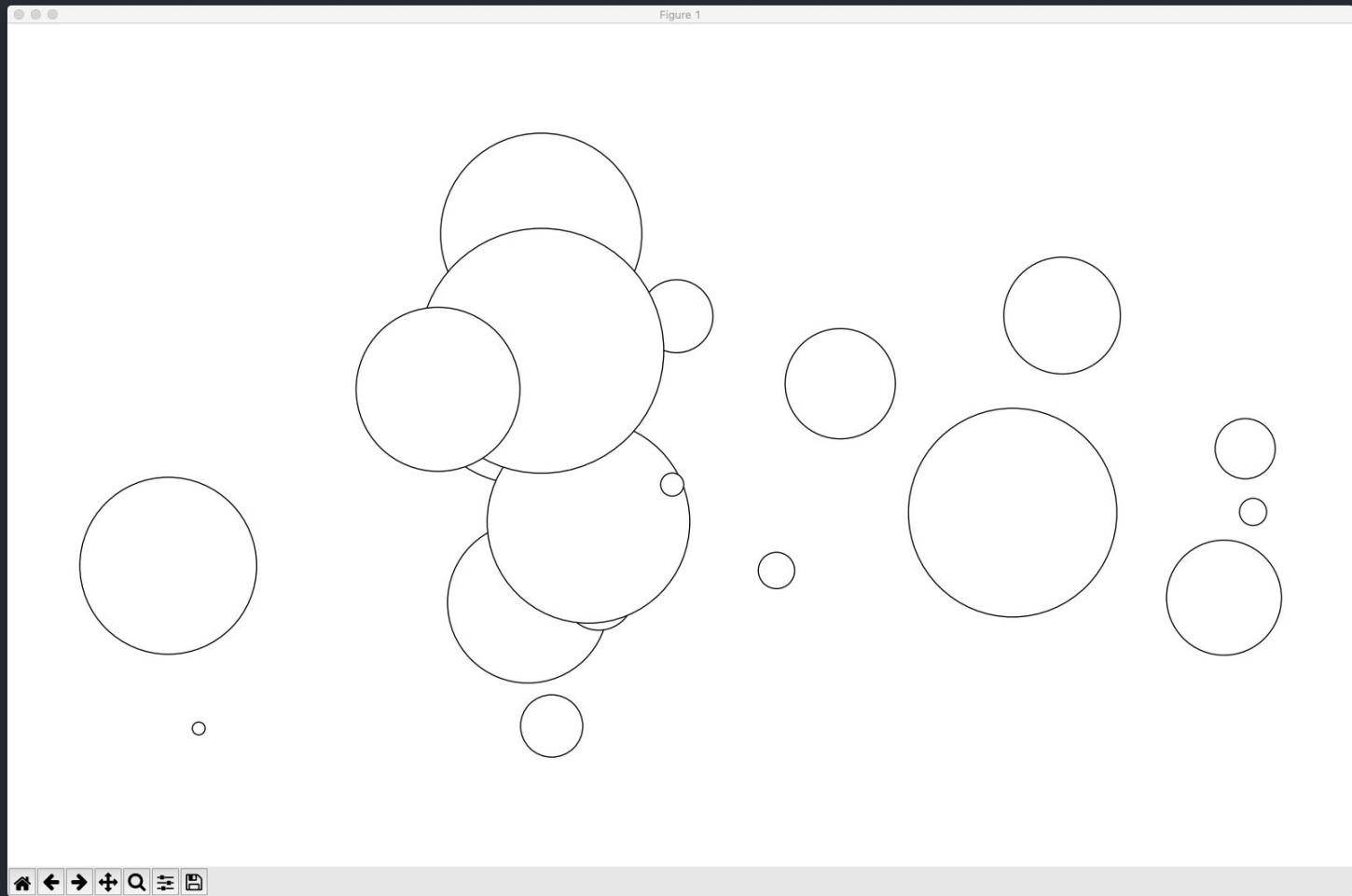
```
from compas.geometry import pointcloud_xy
from compas_plotters import Plotter

cloud = pointcloud_xy(20, xbounds=(0, 10), ybounds=(0, 5))

points = []
for xyz in cloud:
    points.append({'pos': xyz, 'radius': 0.1})

plotter = Plotter(figsize=(16, 10))
plotter.draw_points(points)
plotter.show()
```





```
from ... import ...
from compas.geometry import pointcloud_xy
from compas_plotters import Plotter

cloud = pointcloud_xy(20, (0, 10), (0, 5))

points = []
for xyz in cloud:
    points.append({'pos': xyz, 'radius': ...})

plotter = Plotter(figsize=(8, 5))
plotter.draw_points(points)
plotter.show()
```

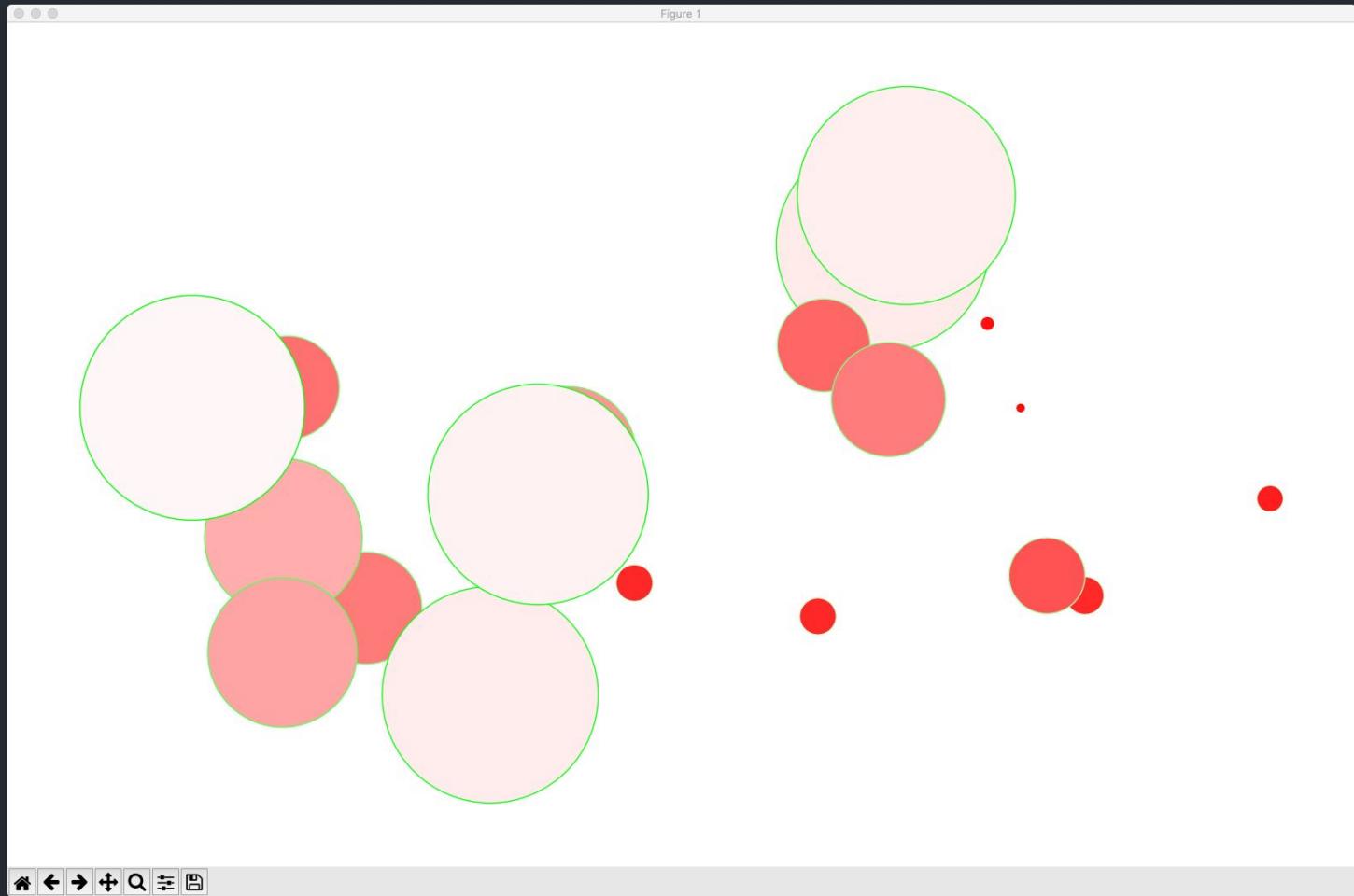
```
from ... import ...
from compas.geometry import pointcloud_xy
from compas_plotters import Plotter

cloud = pointcloud_xy(20, (0, 10), (0, 5))

points = []
for xyz in cloud:
    points.append({'pos': xyz, 'radius': ...})

plotter = Plotter(figsize=(8, 5))
plotter.draw_points(points)
plotter.show()
```

```
from random import random  
from compas.geometry import pointcloud_xy  
from compas_plotters import Plotter  
  
cloud = pointcloud_xy(20, (0, 10), (0, 5))  
  
points = []  
for xyz in cloud:  
    points.append({'pos': xyz, 'radius': random()})  
  
plotter = Plotter(figsize=(8, 5))  
plotter.draw_points(points)  
plotter.show()
```



```
from random import random
from compas.geometry import pointcloud_xy
from compas_plotters import Plotter
from compas.utilities import i_to_green
from compas.utilities import ...
```

```
cloud = pointcloud_xy(20, (0, 10), (0, 5))
```

```
points = []
for xyz in cloud:
    n = ...
    points.append({
        'pos': xyz,
        'radius': ...,
        'edgecolor': ...,
        'facecolor': ...})
```

```
plotter = Plotter(figsize=(8, 5))
plotter.draw_points(points)
plotter.show()
```

```
from random import random
from compas.geometry import pointcloud_xy
from compas_plotters import Plotter
from compas.utilities import i_to_green
from compas.utilities import i_to_red

cloud = pointcloud_xy(20, (0, 10), (0, 5))

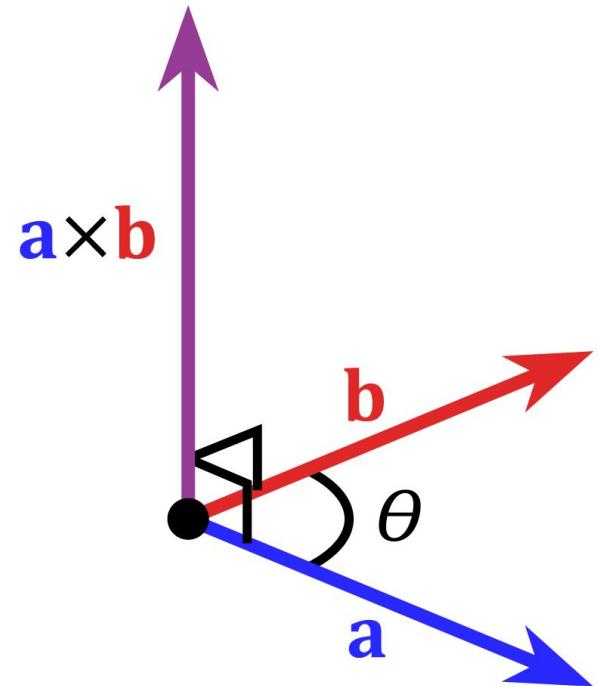
points = []
for xyz in cloud:
    n = random()
    points.append({
        'pos': xyz,
        'radius': n,
        'edgecolor': i_to_green(n),
        'facecolor': i_to_red(1 - n)})

plotter = Plotter(figsize=(8, 5))
plotter.draw_points(points)
plotter.show()
```

## Part 1: Geometry

Cross Product

```
from compas.geometry import area_polygon
from compas.geometry import centroid_polygon
from compas.geometry import centroid_polyhedron
from compas.geometry import circle_from_points
from compas.geometry import convex_hull
from compas.geometry import decompose_matrix
from compas.geometry import distance_point_line
from compas.geometry import distance_line_line
from compas.geometry import intersection_line_line
from compas.geometry import intersection_line_triangle
from compas.geometry import intersection_plane_plane
from compas.geometry import is_coplanar
from compas.geometry import is_point_in_triangle
from compas.geometry import local_to_world_coords
from compas.geometry import matrix_from_basis_vectors
from compas.geometry import normal_polygon
from compas.geometry import normal_triangle
from compas.geometry import offset_line
from compas.geometry import orient_points
from compas.geometry import orthonormalize_axes
from compas.geometry import plane_from_points
from compas.geometry import reflect_line_triangle
from compas.geometry import volume_polyhedron
from compas.geometry import world_to_local_coords
...  
...
```







```
from compas.geometry import cross_vectors  
  
u = [1.0, 0.0, 0.0]  
v = [0.0, 1.0, 0.0]  
  
uxv = cross_vectors(u, v)  
  
print(uxv)
```

```
from compas.geometry import Vector  
  
u = Vector(1.0, 0.0, 0.0)  
v = Vector(0.0, 1.0, 0.0)  
  
uxv = u.cross(v)  
  
print(uxv)
```

```
from compas.geometry import cross_vectors          from compas.geometry import Vector  
  
u = [1.0, 0.0, 0.0]                                u = Vector(1.0, 0.0, 0.0)  
v = [0.0, 1.0, 0.0]                                v = Vector(0.0, 1.0, 0.0)  
  
uxv = cross_vectors(u, v)                          uxv = u.cross(v)  
  
print(uxv)                                         print(uxv)
```

```
from compas.geometry import cross_vectors
```

```
u = [1.0, 0.0, 0.0]
```

```
v = [0.0, 1.0, 0.0]
```

```
uxv = cross_vectors(u, v)
```

```
print(uxv)
```

```
from compas.geometry import Vector
```

```
u = Vector(1.0, 0.0, 0.0)
```

```
v = Vector(0.0, 1.0, 0.0)
```

```
uxv = u.cross(v)
```

```
print(uxv)
```

```
from compas.geometry import cross_vectors  
  
u = [1.0, 0.0, 0.0]  
v = [0.0, 1.0, 0.0]  
  
uxv = cross_vectors(u, v)  
  
print(uxv)
```

```
from compas.geometry import Vector  
  
u = Vector(1.0, 0.0, 0.0)  
v = Vector(0.0, 1.0, 0.0)  
  
uxv = u.cross(v)  
  
print(uxv)
```

[0.0, 0.0, 1.0]

Vector(0.000, 0.000, 1.000)

```
from compas.geometry import cross_vectors
from compas.geometry import angle_vectors
```

```
u = [1.0, 0.0, 0.0]
v = [0.0, 1.0, 0.0]
```

```
uxv = cross_vectors(u, v)
```

```
u_uxv = angle_vectors(u, uxv)
v_uxv = angle_vectors(v, uxv)
```

```
print(u_uxv)
print(v_uxv)
```

```
1.5707963267948966
1.5707963267948966
```

```
from compas.geometry import Vector
```

```
u = Vector(1.0, 0.0, 0.0)
v = Vector(0.0, 1.0, 0.0)
```

```
uxv = u.cross(v)
```

```
u_uxv = u.angle(uxv)
v_uxv = v.angle(uxv)
```

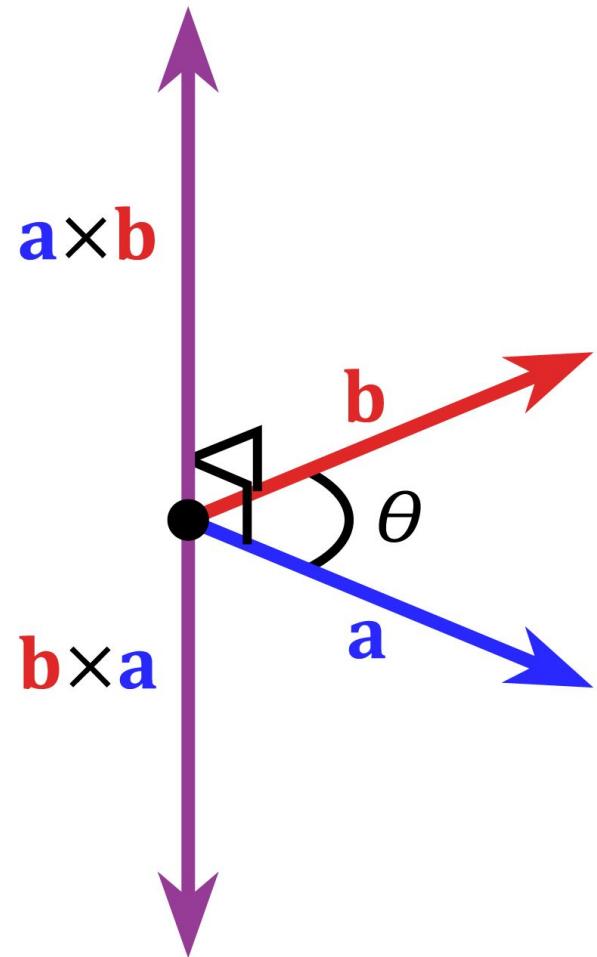
```
print(u_uxv)
print(v_uxv)
```

```
1.5707963267948966
1.5707963267948966
```

# Assignment

Given two vectors, use the cross product to create a set of three ortho**normal** vectors.

- orthonormal vectors are orthogonal and normalised!



```
from compas.geometry import cross_vectors  
  
u = [1.0, 0.0, 0.0]  
v = [0.0, 1.0, 0.0]  
  
uxv = cross_vectors(u, v)  
vxu = cross_vectors(v, u)  
  
print(uxv)  
print(vxu)
```

```
[0.0, 0.0, 1.0]  
[0.0, 0.0, -1.0]
```

```
from compas.geometry import Vector  
  
u = Vector(1.0, 0.0, 0.0)  
v = Vector(0.0, 1.0, 0.0)  
  
uxv = u.cross(v)  
vxu = v.cross(u)  
  
print(uxv)  
print(vxu)
```

```
Vector(0.000, 0.000, 1.000)  
Vector(0.000, 0.000, -1.000)
```

## Assignment (last week)

Write a function that determines if the rotation from one vector onto another is CCW or not.

```
from compas.geometry import cross_vectors
from compas.geometry import angle_vectors
```

```
u = [1.0, 0.0, 0.0]
v = [0.0, 1.0, 0.0]
```

```
print(angle_vectors(u, v))
print(angle_vectors(v, u))
```

```
1.5707963267948966
1.5707963267948966
```

```
from compas.geometry import Vector
```

```
u = Vector(1.0, 0.0, 0.0)
v = Vector(0.0, 1.0, 0.0)
```

```
print(u.angle(v))
print(v.angle(u))
```

```
1.5707963267948966
1.5707963267948966
```

```
from compas.geometry import cross_vectors  
  
u = [1.0, 0.0, 0.0]  
v = [0.0, 1.0, 0.0]  
  
print(cross_vectors(u, v)[2] > 0)  
print(cross_vectors(v, u)[2] > 0)
```

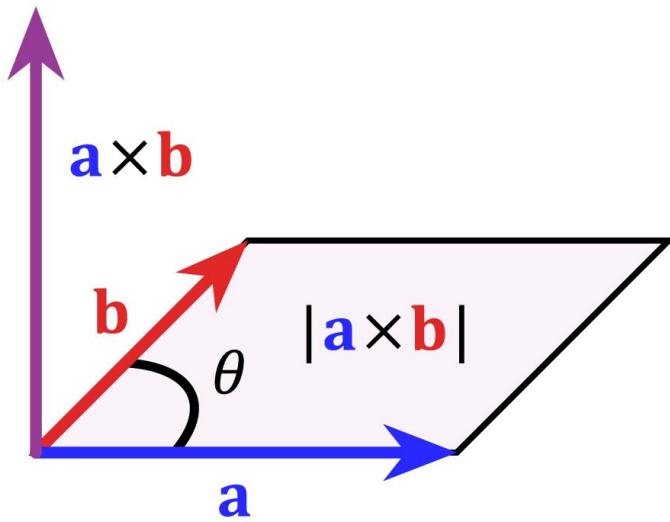
True  
False

```
from compas.geometry import Vector  
  
u = Vector(1.0, 0.0, 0.0)  
v = Vector(0.0, 1.0, 0.0)  
  
print(u.cross(v)[2] > 0)  
print(v.cross(u)[2] > 0)
```

True  
False

```
def is_ccw_xy(a, b, c, colinear=False):
    """Determine if c is on the left of ab when looking from a to b,
    and assuming that all points lie in the XY plane.
    """
    ab_x = b[0] - a[0]
    ab_y = b[1] - a[1]
    ac_x = c[0] - a[0]
    ac_y = c[1] - a[1]

    if colinear:
        return ab_x * ac_y - ab_y * ac_x >= 0
    return ab_x * ac_y - ab_y * ac_x > 0
```



```
from compas.geometry import cross_vectors
from compas.geometry import length_vector
```

```
u = [1.0, 0.0, 0.0]
v = [0.0, 1.0, 0.0]
```

```
uxv = cross_vectors(u, v)
```

```
print(length_vector(uxv))
```

1.0

```
from compas.geometry import Vector
```

```
u = Vector(1.0, 0.0, 0.0)
v = Vector(0.0, 1.0, 0.0)
```

```
uxv = u.cross(v)
```

```
print(uxv.length)
```

1.0

```
from compas.geometry import subtract_vectors
from compas.geometry import cross_vectors
from compas.geometry import length_vector
from compas.geometry import area_triangle

a = [0.0, 0.0, 0.0]
b = [1.0, 0.0, 0.0]
c = [0.0, 1.0, 0.0]

ab = subtract_vectors(b, a)
ac = subtract_vectors(c, a)

L = length_vector(cross_vectors(ab, ac))
A = area_triangle([a, b, c])

print(0.5 * L == A)
```

True

```
from compas.geometry import Vector
from compas.geometry import area_triangle

a = [0.0, 0.0, 0.0]
b = [1.0, 0.0, 0.0]
c = [0.0, 1.0, 0.0]

ab = Vector.from_start_end(a, b)
ac = Vector.from_start_end(a, c)

L = ab.cross(ac).length
A = area_triangle([a, b, c])

print(0.5 * L == A)
```

True

# Assignment

Use the cross product to compute the area of a convex, 2D polygon.

- decompose the polygon into triangles from the centroid
- use the cross product to compute the total area

```
from compas.geometry import area_polygon
from compas.geometry import centroid_polygon
from compas.geometry import centroid_polyhedron
from compas.geometry import circle_from_points
from compas.geometry import convex_hull
from compas.geometry import decompose_matrix
from compas.geometry import distance_point_line
from compas.geometry import distance_line_line
from compas.geometry import intersection_line_line
from compas.geometry import intersection_line_triangle
from compas.geometry import intersection_plane_plane
from compas.geometry import is_coplanar
from compas.geometry import is_point_in_triangle
from compas.geometry import local_to_world_coords
from compas.geometry import matrix_from_basis_vectors
from compas.geometry import normal_polygon
from compas.geometry import normal_triangle
from compas.geometry import offset_line
from compas.geometry import orient_points
from compas.geometry import orthonormalize_axes
from compas.geometry import plane_from_points
from compas.geometry import reflect_line_triangle
from compas.geometry import volume_polyhedron
from compas.geometry import world_to_local_coords
...  
...
```

Object Aligned Bounding Box using PCA

PCA of a dataset  
finds the directions  
along which the variation of the data  
is largest,  
i.e. the directions along which the data is most spread out.

```
from math import radians

import compas_rhino

from compas.geometry import pointcloud
from compas.geometry import bounding_box
from compas.geometry import Frame
from compas.geometry import Rotation
from compas.geometry import Transformation
from compas.geometry import transform_points

from compas.utilities import pairwise

# from compas.numerical import pca_numpy
from compas.rpc import Proxy

numerical = Proxy('compas.numerical')
```

```
# =====
# Helpers
# =====

def draw_cloud(cloud, color, layer):
    points = []
    for xyz in cloud:
        points.append({'pos': xyz, 'color': color})
    compas_rhino.draw_points(points, layer=layer, clear=True)

def draw_bbox(bbox, color, layer):
    lines = []
    for a, b in pairwise(bbox[:4] + bbox[:1]):
        lines.append({'start': a, 'end': b, 'color': color})
    for a, b in pairwise(bbox[4:] + bbox[4:5]):
        lines.append({'start': a, 'end': b, 'color': color})
    for a, b in zip(bbox[:4], bbox[4:]):
        lines.append({'start': a, 'end': b, 'color': color})
    compas_rhino.draw_lines(lines, layer=layer, clear=True)

def draw_frame(frame, layer):
    ...
```

```
# =====
# Algorithm
# =====

cloud1 = pointcloud(20, (0, 10), (0, 5), (0, 3))
bbox1 = bounding_box(cloud1)

Rz = Rotation.from_axis_and_angle([0.0, 0.0, 1.0], radians(30))
Ry = Rotation.from_axis_and_angle([0.0, 1.0, 0.0], radians(20))
Rx = Rotation.from_axis_and_angle([1.0, 0.0, 0.0], radians(40))

R = Rz * Ry * Rx

cloud2 = transform_points(cloud1, R)
bbox2 = transform_points(bbox1, R)

average, vectors, values = numerical.pca_numpy(cloud2)

origin = average[0]
xaxis = vectors[0]
yaxis = vectors[1]
zaxis = vectors[2]
...
```

```
# =====
# Visualisation
# =====

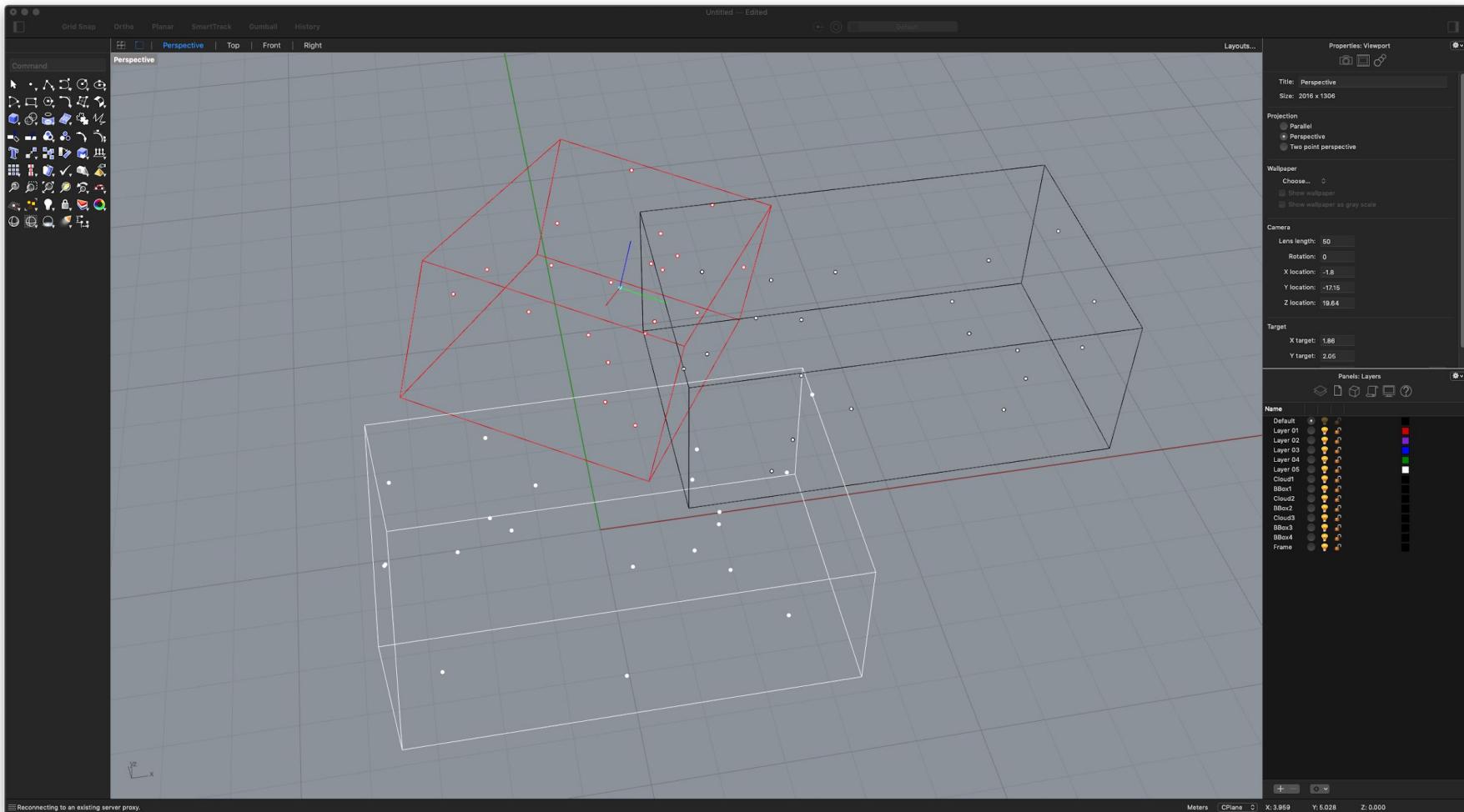
draw_cloud(cloud1, (0, 0, 0), "Cloud1")
draw_bbox(bbox1, (0, 0, 0), "BBox1")

draw_cloud(cloud2, (255, 0, 0), "Cloud2")

draw_cloud(cloud3, (255, 255, 255), "Cloud3")
draw_bbox(bbox3, (255, 255, 255), "BBox3")

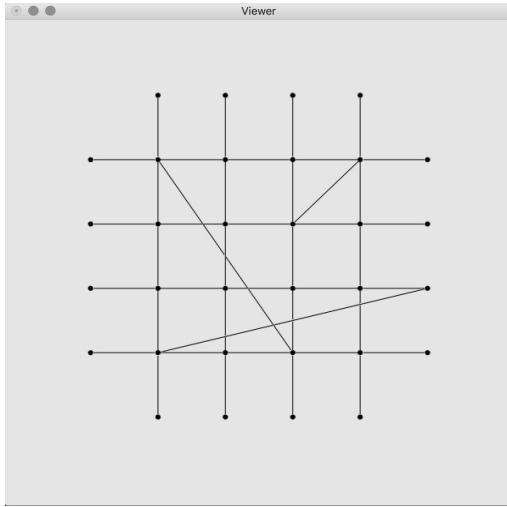
draw_bbox(bbox4, (255, 0, 0), "BBox4")

draw_frame(frame, "Frame")
```



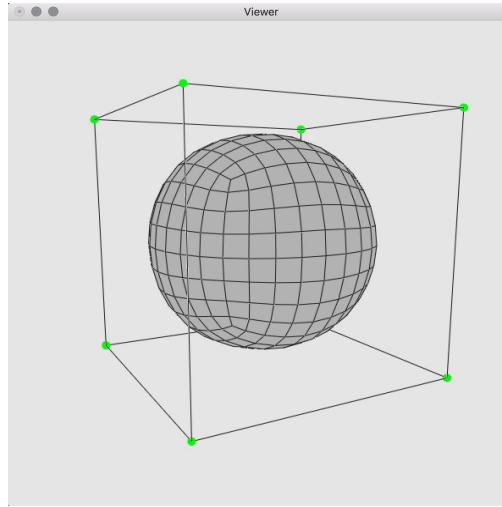
## Part 2: Data Structures

## Network



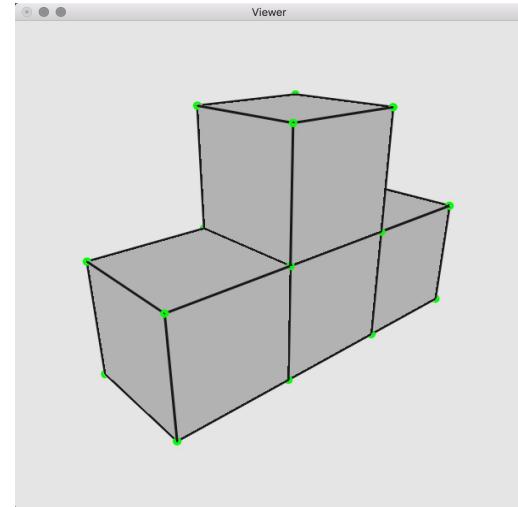
- General networks
- Edge graph

## Mesh

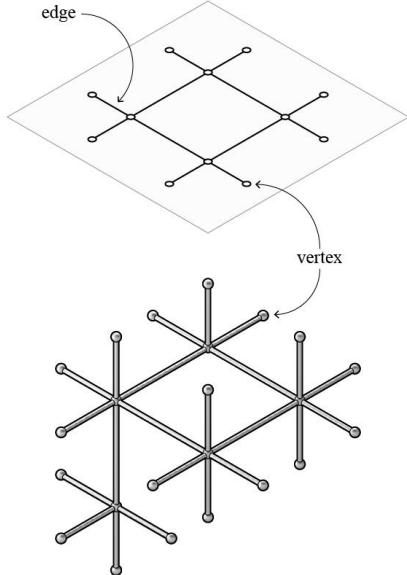


- Surface meshes
- Half-edge

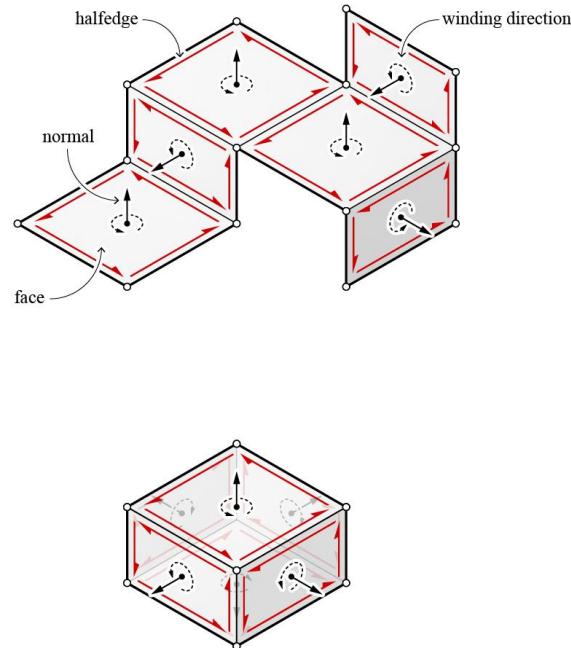
## VolMesh



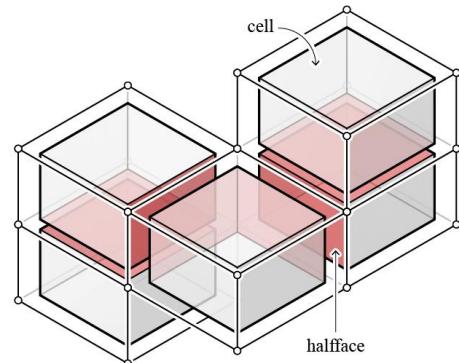
- Cellular meshes
- Half-plane



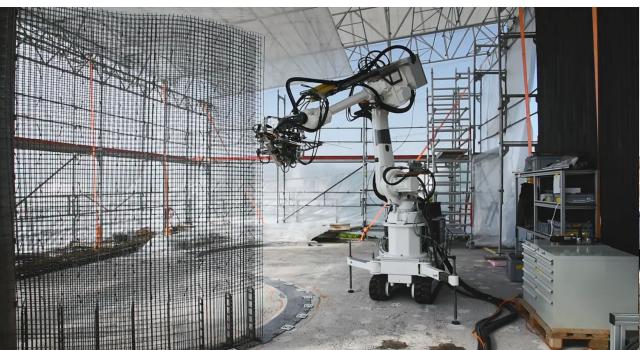
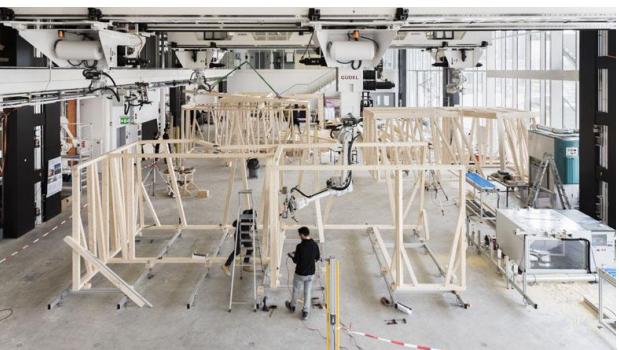
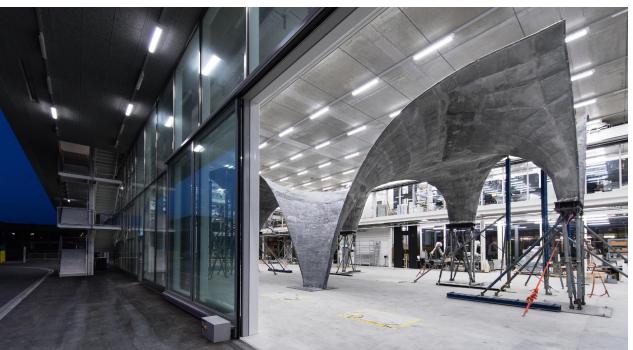
a network of vertices,  
with vertex connectivities defined by directed edges



a network of faces,  
with face connectivities defined by halfedge adjacencies



a network of cells,  
with cell connectivities defined by halfface adjacencies



# Constructors

```
import os
import compas
from compas.datastructures import Network

HERE = os.path.dirname(__file__)
DATA = os.path.join(HERE, 'data')
FILE = os.path.join(DATA, 'lines.obj')

network = Network.from_obj(FILE)

print(network.summary())
```

- name: Network
- vertices: 32
- edges: 43
- vertex degree: 1/5

```
import os
import compas
from compas.datastructures import Mesh

HERE = os.path.dirname(__file__)
DATA = os.path.join(HERE, 'data')
FILE = os.path.join(DATA, 'faces.obj')

mesh = Mesh.from_obj(FILE)

print(mesh.summary())
```

- name: Mesh
- vertices: 36
- edges: 60
- faces: 25
- vertex degree: 2/4
- face degree: 2/4

```
from compas.datastructures import Network  
  
network = Network.from_vertices_and_edges()  
  
network = Network.from_lines()  
  
network = Network.from_data()  
network = Network.from_json()  
  
network = Network.from_obj()
```

```
from compas.datastructures import Mesh  
  
mesh = Mesh.from_vertices_and_faces()  
  
mesh = Mesh.from_lines()  
  
mesh = Mesh.from_data()  
mesh = Mesh.from_json()  
  
mesh = Mesh.from_obj()  
mesh = Mesh.from_off()  
mesh = Mesh.from_stl()  
mesh = Mesh.from_ply()
```

# Visualisation

```
import os
import compas

from compas.datastructures import Mesh
from compas_plotters import MeshPlotter

HERE = os.path.dirname(__file__)
DATA = os.path.join(HERE, 'data')
FILE = os.path.join(DATA, 'faces.obj')

mesh = Mesh.from_obj(FILE)

plotter = MeshPlotter(mesh, figsize=(8, 5))

plotter.draw_vertices()
plotter.draw_edges()
plotter.draw_faces()

plotter.show()
```

```
import os
import compas

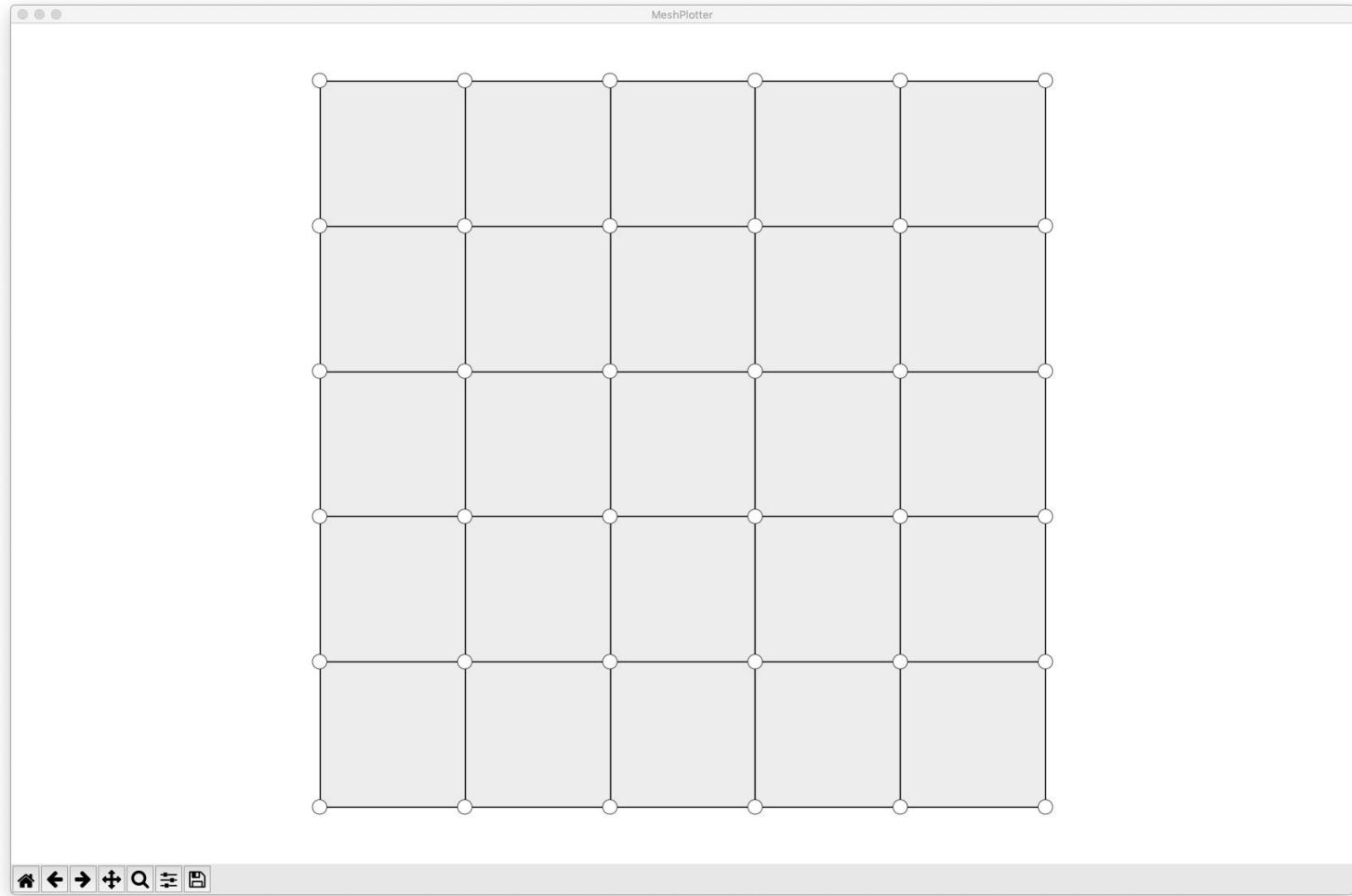
from compas.datastructures import Mesh
from compas_rhino.artists import MeshArtist

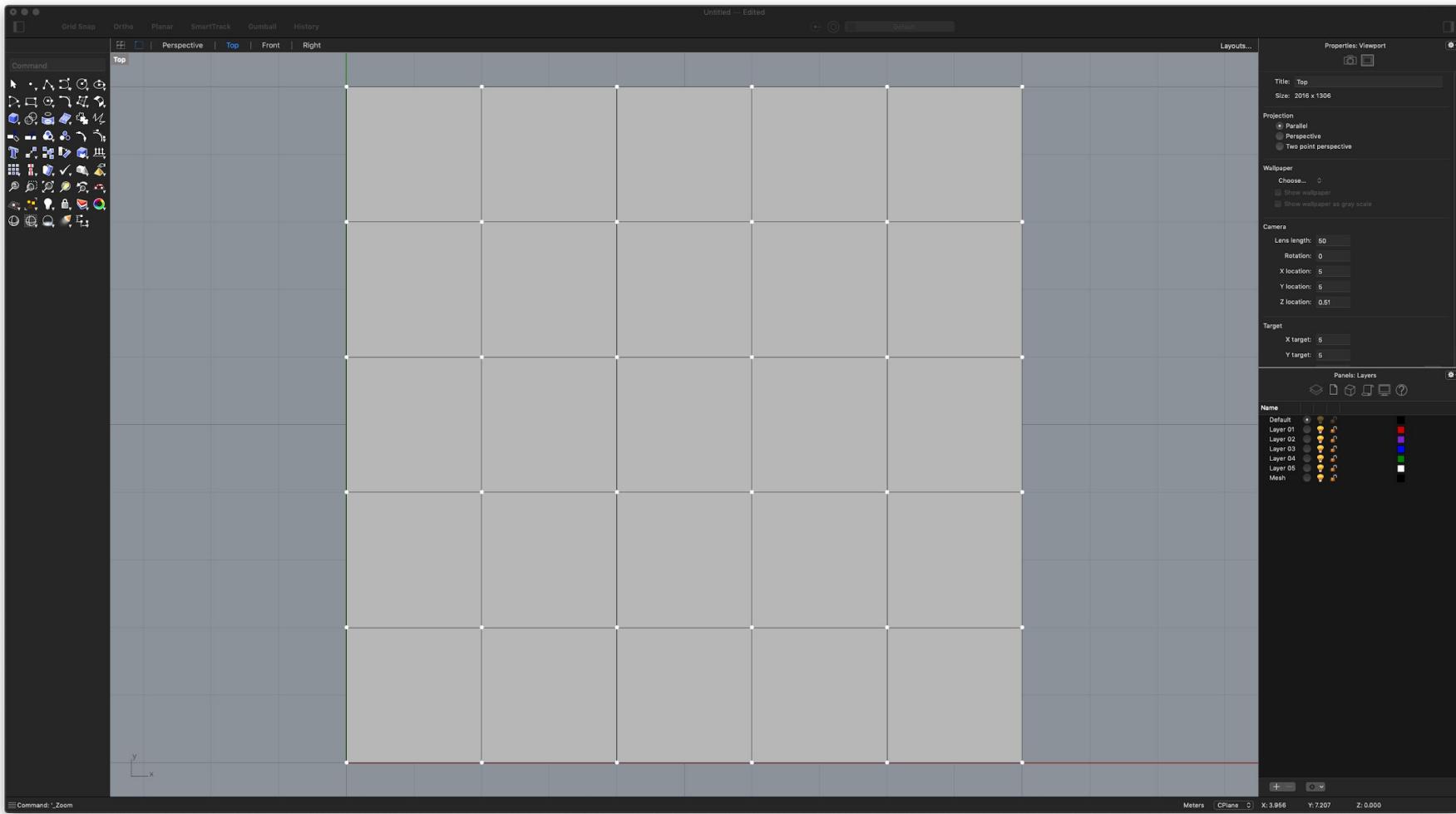
HERE = os.path.dirname(__file__)
DATA = os.path.join(HERE, 'data')
FILE = os.path.join(DATA, 'faces.obj')

mesh = Mesh.from_obj(FILE)

artist = MeshArtist(mesh, layer="Mesh")

artist.draw_vertices()
artist.draw_edges()
artist.draw_faces()
```





```
mesh = Mesh.from_obj(FILE)

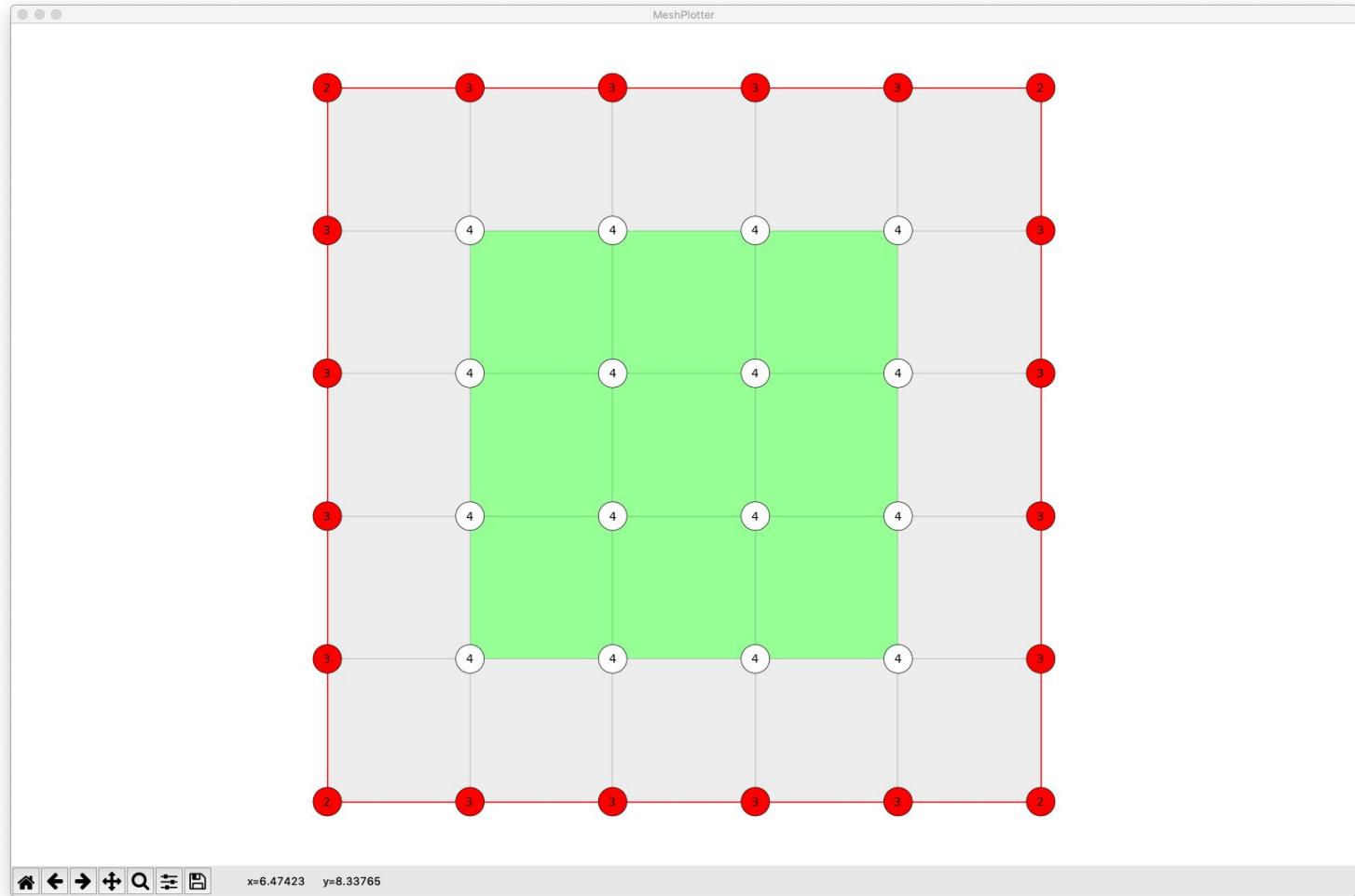
plotter = MeshPlotter(mesh, figsize=(16, 10))

plotter.draw_vertices(
    facecolor={key: (255, 0, 0) for key in mesh.vertices_on_boundary()},
    text={key: str(mesh.vertex_degree(key)) for key in mesh.vertices()},
    radius=0.2)

plotter.draw_edges(
    keys=list(mesh.edges_on_boundary()),
    color=(255, 0, 0))

plotter.draw_faces(
    facecolor={key: (150, 255, 150) for key in mesh.faces() if not mesh.is_face_on_boundary(key)}) 

plotter.show()
```



```
mesh = Mesh.from_obj(FILE)

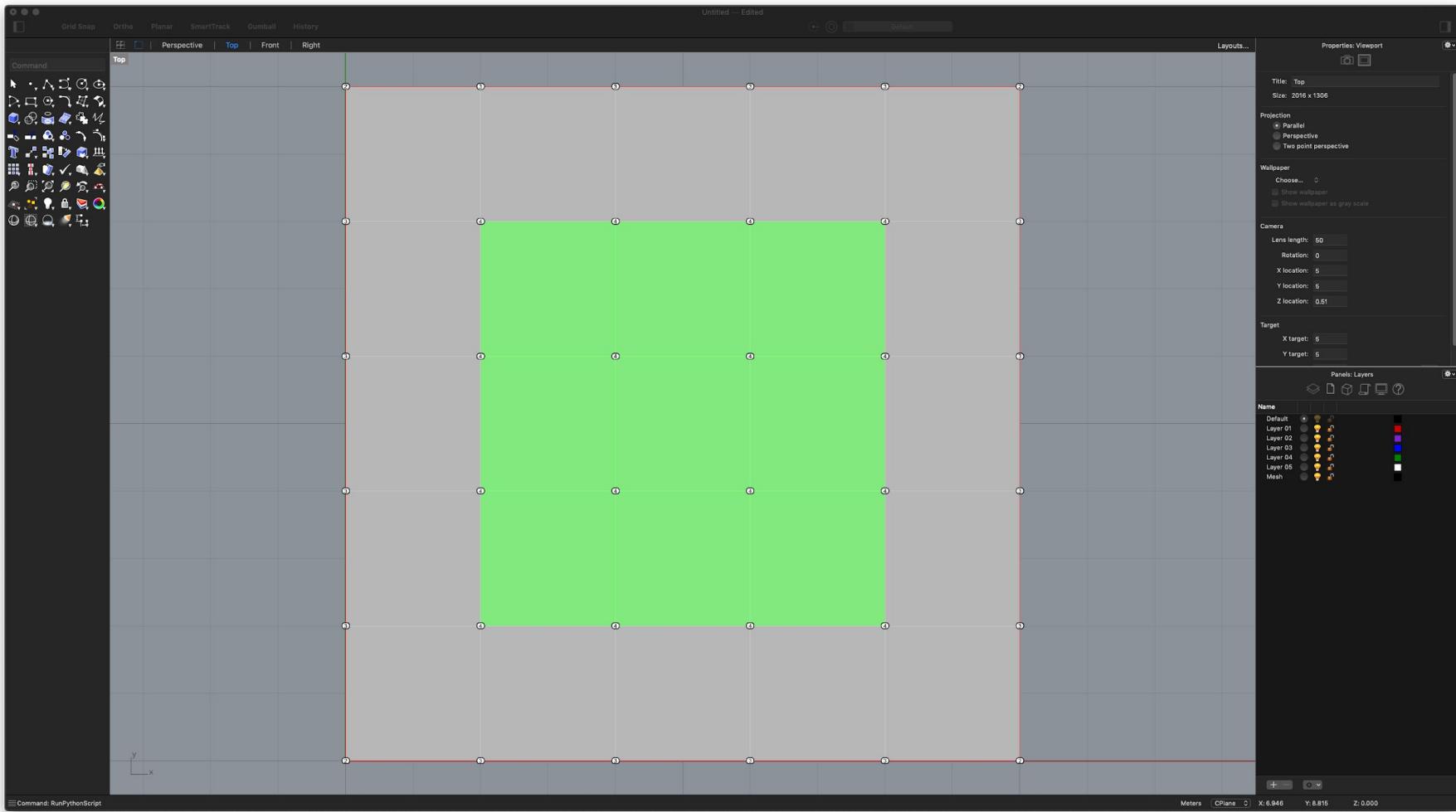
artist = MeshArtist(mesh, layer="Mesh")

artist.draw_vertices(
    color={key: (255, 0, 0) for key in mesh.vertices_on_boundary()})

artist.draw_vertexlabels(
    text={key: str(mesh.vertex_degree(key)) for key in mesh.vertices()})

artist.draw_edges(
    keys=list(mesh.edges_on_boundary()),
    color=(255, 0, 0))

artist.draw_faces(
    color={key: (150, 255, 150) for key in mesh.faces() if not mesh.is_face_on_boundary(key)})
```



Accessing the data

```
mesh = Mesh.from_obj(FILE)

print(mesh.vertices())
print(mesh.faces())
print(mesh.edges())
```

<generator object Mesh.vertices at ... >	0	0	(0, 1)
<generator object Mesh.faces at ... >	1	1	(0, 6)
<generator object Mesh.edges at ... >	2	2	(1, 7)
	...	...	...

```
mesh = Mesh.from_obj(FILE)

for key in mesh.vertices():
    print(key)

for key in mesh.faces():
    print(key)

for key in mesh.edges():
    print(key)
```

```
mesh = Mesh.from_obj(FILE)
print(list(mesh.vertices()))
print(list(mesh.faces()))
print(list(mesh.edges()))

mesh = Mesh.from_obj(FILE)
for key in mesh.vertices():
    print(key)
for key in mesh.faces():
    print(key)
for key in mesh.edges():
    print(key)

[0, 1, 2, ... ]
[0, 1, 2, ... ]
[(0, 1), (0, 6), (1, 7), ... ]
```

	0	0	(0, 1)
	1	1	(0, 6)
	2	2	(1, 7)
	...	...	...

## Attributes

```
mesh = Mesh.from_obj(FILE)

print(mesh.default_vertex_attributes)
print(mesh.default_face_attributes)
print(mesh.default_edge_attributes)
```

```
{'x': 0.0, 'y': 0.0, 'z': 0.0}
{}
{}
```

```
mesh = Mesh.from_obj(FILE)

for key, attr in mesh.vertices(data=True):
    print(key, attr)

for key, attr in mesh.faces(data=True):
    print(key, attr)

for u, v, attr in mesh.edges(data=True):
    print((u, v), attr)
```

```
0 {'x': 0.0, 'y': 0.0, 'z': 0.0}
1 {'x': 2.0, 'y': 0.0, 'z': 0.0}
2 {'x': 4.0, 'y': 0.0, 'z': 0.0}
...

```

```
mesh = Mesh.from_obj(FILE)

print(mesh.default_vertex_attributes)
print(mesh.default_face_attributes)
print(mesh.default_edge_attributes)
```

```
{'x': 0.0, 'y': 0.0, 'z': 0.0}
{}
{}
```

```
mesh = Mesh.from_obj(FILE)

for key, attr in mesh.vertices(data=True):
    print(key, attr)

for key, attr in mesh.faces(data=True):
    print(key, attr)

for u, v, attr in mesh.edges(data=True):
    print((u, v), attr)
```

```
0 {}
1 {}
2 {}
...
...
```

```
mesh = Mesh.from_obj(FILE)

print(mesh.default_vertex_attributes)
print(mesh.default_face_attributes)
print(mesh.default_edge_attributes)
```

```
{'x': 0.0, 'y': 0.0, 'z': 0.0}
{}
{}
```

```
mesh = Mesh.from_obj(FILE)

for key, attr in mesh.vertices(data=True):
    print(key, attr)

for key, attr in mesh.faces(data=True):
    print(key, attr)

for u, v, attr in mesh.edges(data=True):
    print((u, v), attr)
```

```
(0, 1) {}
(0, 6) {}
(1, 7) {}
...
...
```

```
mesh = Mesh.from_obj(FILE)

mesh.update_default_edge_attributes({
    'q': 1.0,
    'f': 0.0})

for u, v, attr in mesh.edges(data=True):
    print((u, v), attr)
```

```
(0, 1) {'q': 1.0, 'f': 0.0}
(0, 6) {'q': 1.0, 'f': 0.0}
(1, 7) {'q': 1.0, 'f': 0.0}
...
```

```
mesh = Mesh.from_obj(FILE)

print(mesh.get_vertex_attribute(0, 'x'))

print(mesh.get_vertex_attributes(0, 'xyz'))

print(mesh.get_vertices_attribute('x'))

print(mesh.get_vertices_attributes('xyz'))
```

0.0

[0.0, 0.0, 0.0]

[0.0, 2.0, 4.0, ... ]

[[0.0, 0.0, 0.0], [2.0, 0.0, 0.0], [4.0, 0.0, 0.0], ... ]

Topology vs Geometry

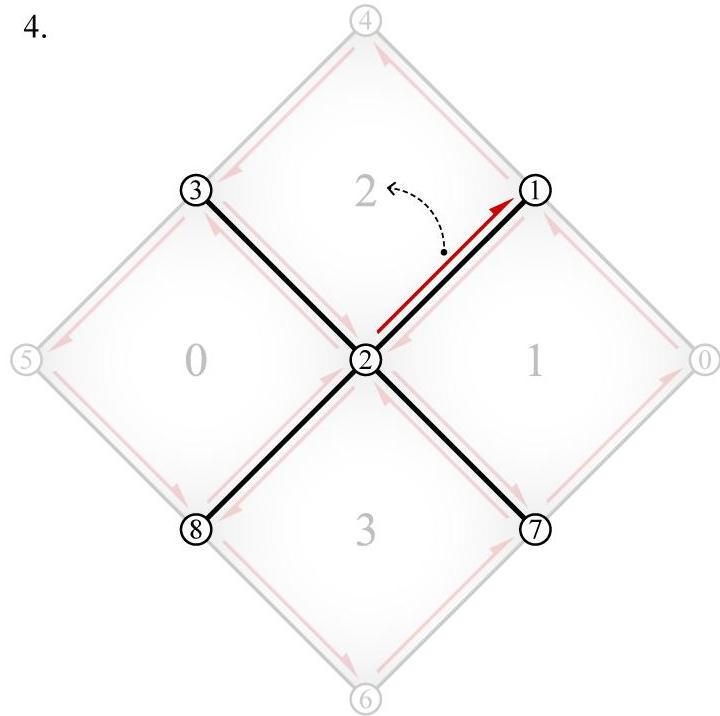
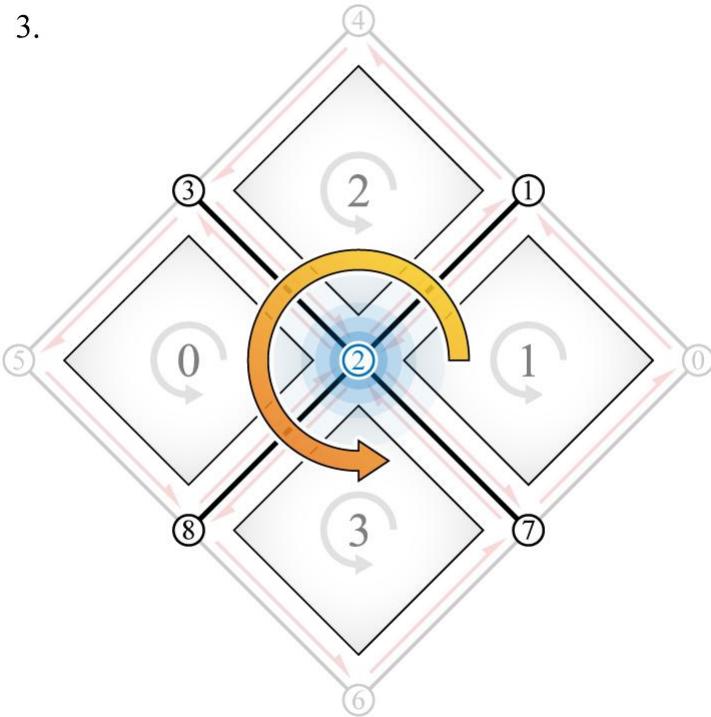
```
mesh = Mesh.from_obj(FILE)                         mesh = Mesh.from_obj(FILE)

for key in mesh.vertices():                      for key in mesh.vertices():
    print(mesh.vertex_coordinates(key))          print(mesh.vertex_neighbors(key))
    print(mesh.vertex_normal(key))                print(mesh.vertex_degree(key))
    print(mesh.vertex_area(key))                  print(mesh.vertex_neighborhood(key))
                                                print(mesh.vertex_faces(key))

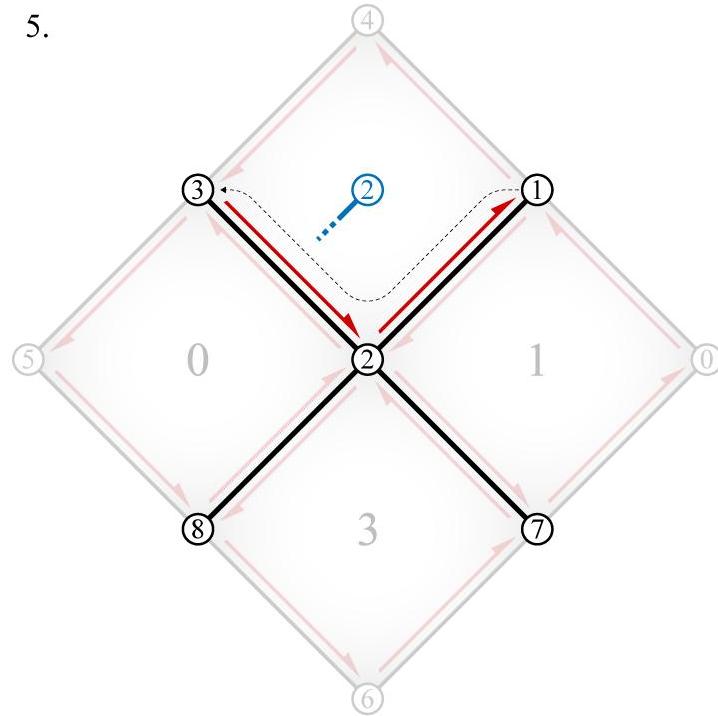
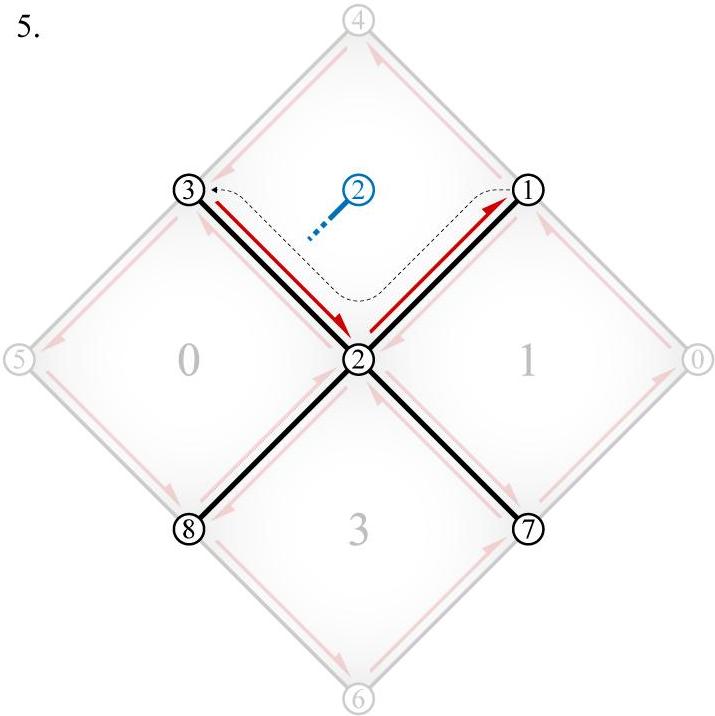
for fkey in mesh.faces():                        for fkey in mesh.faces():
    print(mesh.face_coordinates(fkey))          print(mesh.face_vertices(fkey))
    print(mesh.face_normal(fkey))                print(mesh.face_neighbors(fkey))
    print(mesh.face_area(fkey))                  print(mesh.face_halfedges(fkey))

                                                for key in mesh.face_vertices(fkey):
                                                    print(mesh.face_vertex_ancestor(fkey, key))
                                                    print(mesh.face_vertex_descendant(fkey, key))
```

## Mesh topology

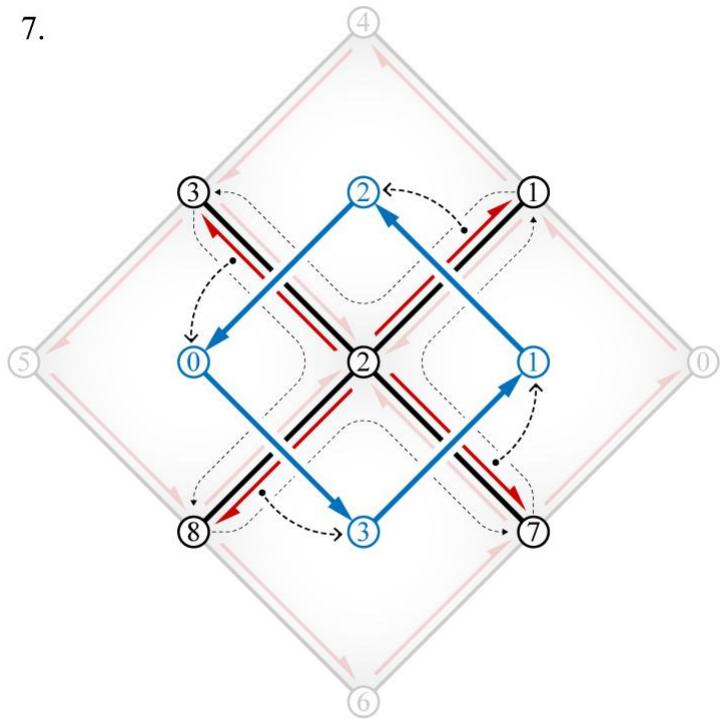


## Mesh topology

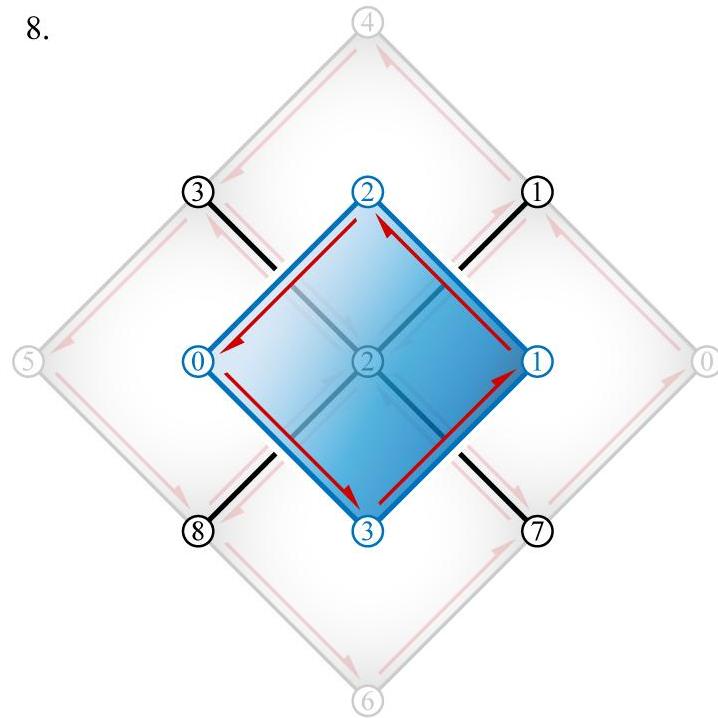


## Mesh topology

7.



8.



```
from compas.datastructures import Mesh
from compas.topology import breadth_first_ordering
from compas.utilities import i_to_red
from compas_plotters import MeshPlotter

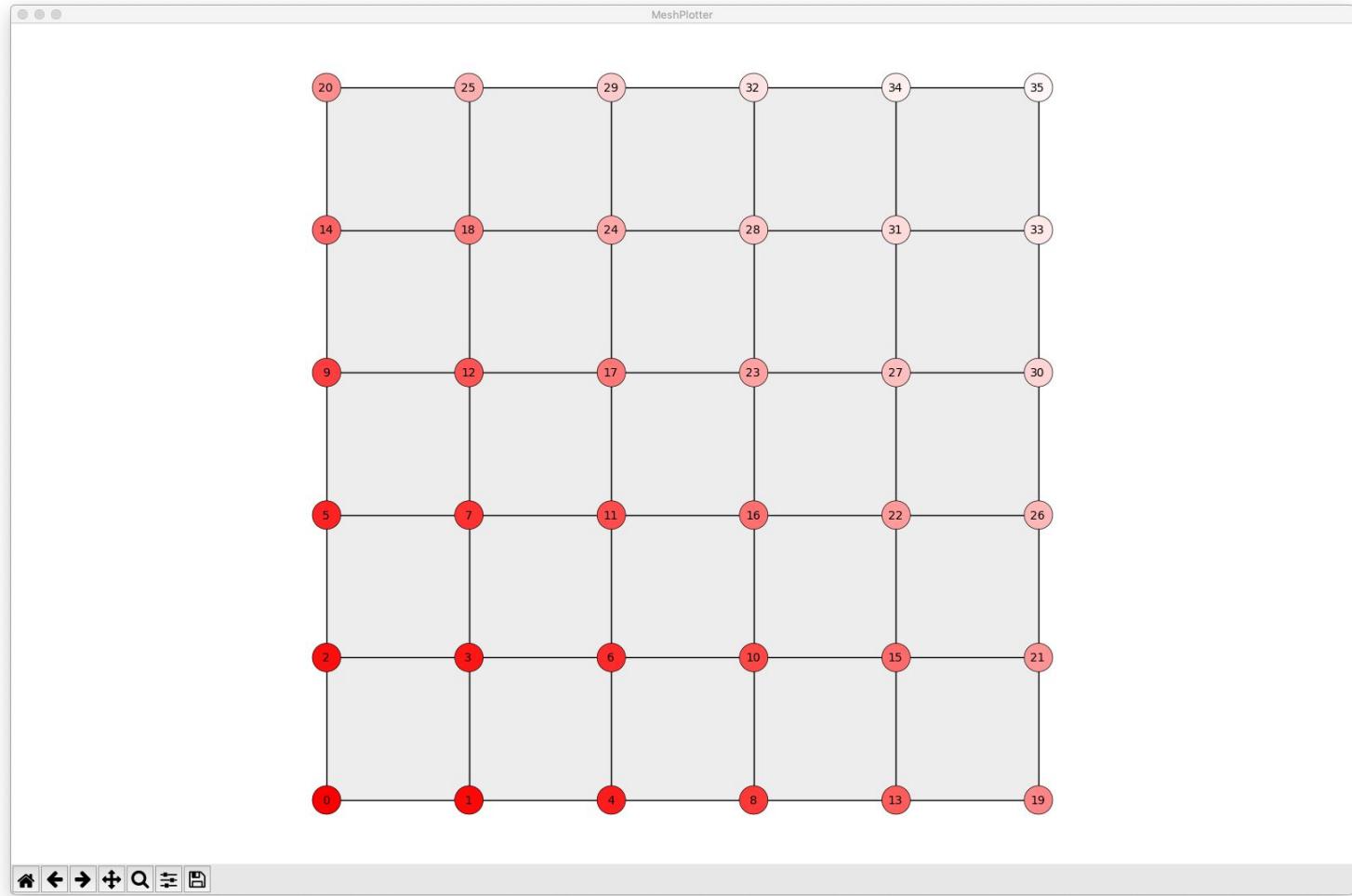
HERE = os.path.dirname(__file__)
DATA = os.path.join(HERE, 'data')
FILE = os.path.join(DATA, 'faces.obj')

mesh = Mesh.from_obj(FILE)

bfo = breadth_first_ordering(mesh.adjacency, 0)

print(bfo)
```

```
[0, 1, 6, 7, ..., 35]
```



```
from compas.datastructures import Mesh
from compas.topology import breadth_first_ordering
from compas.utilities import i_to_red
from compas_plotters import MeshPlotter

HERE = os.path.dirname(__file__)
DATA = os.path.join(HERE, 'data')
FILE = os.path.join(DATA, 'faces.obj')

mesh = Mesh.from_obj(FILE)

mesh.set_vertices_attributes('xyz', [0, 0, 0])

bfo = breadth_first_ordering(mesh.adjacency, 0)

print(bfo)
```

```
[0, 1, 6, 7, ..., 35]
```

```
from compas.datastructures import Mesh
from compas.topology import breadth_first_ordering
from compas.utilities import i_to_red
from compas_plotters import MeshPlotter

mesh = Mesh.from_obj(FILE)

bfo = breadth_first_ordering(mesh.adjacency, 0)

v = mesh.number_of_vertices()

plotter = MeshPlotter(mesh, figsize=(16, 10))

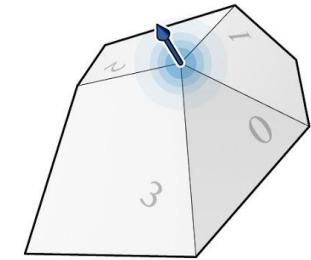
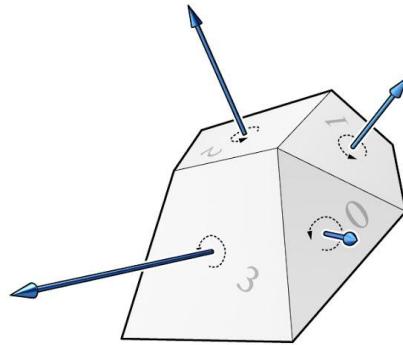
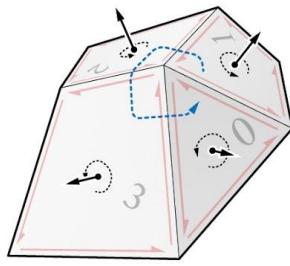
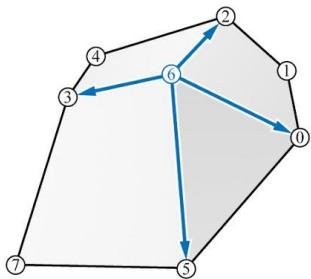
plotter.draw_vertices(
    text={key: index for index, key in enumerate(bfo)},
    radius=0.2,
    facecolor={key: i_to_red(1 - index / v) for index, key in enumerate(bfo)})

plotter.draw_edges()
plotter.draw_faces()

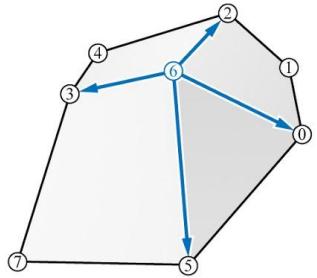
plotter.show()
```

# Applications

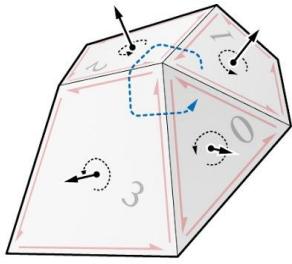
# Mesh vertex normal



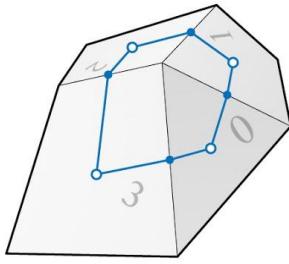
# Mesh vertex tributary area



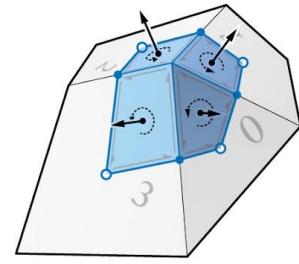
1. vertex neighbors



2. vertex faces

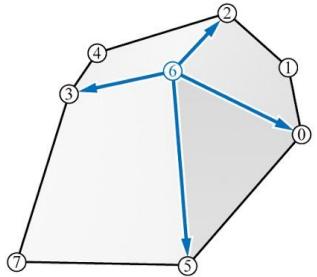


3. face centroids

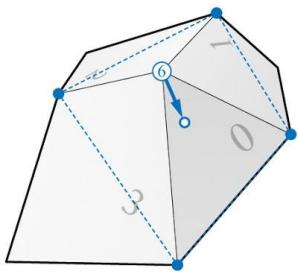


4. tributary area

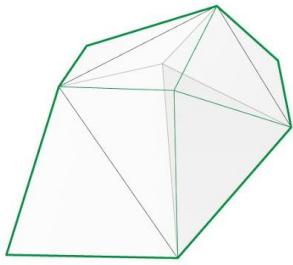
# Mesh centroidal smoothing



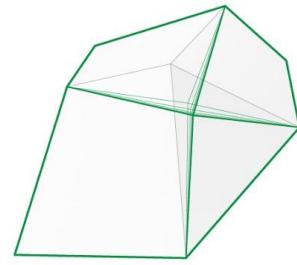
1. vertex neighbors



2. vertex neighbor centroid



3.  $k=1$



4.  $k=10$

# Assignments

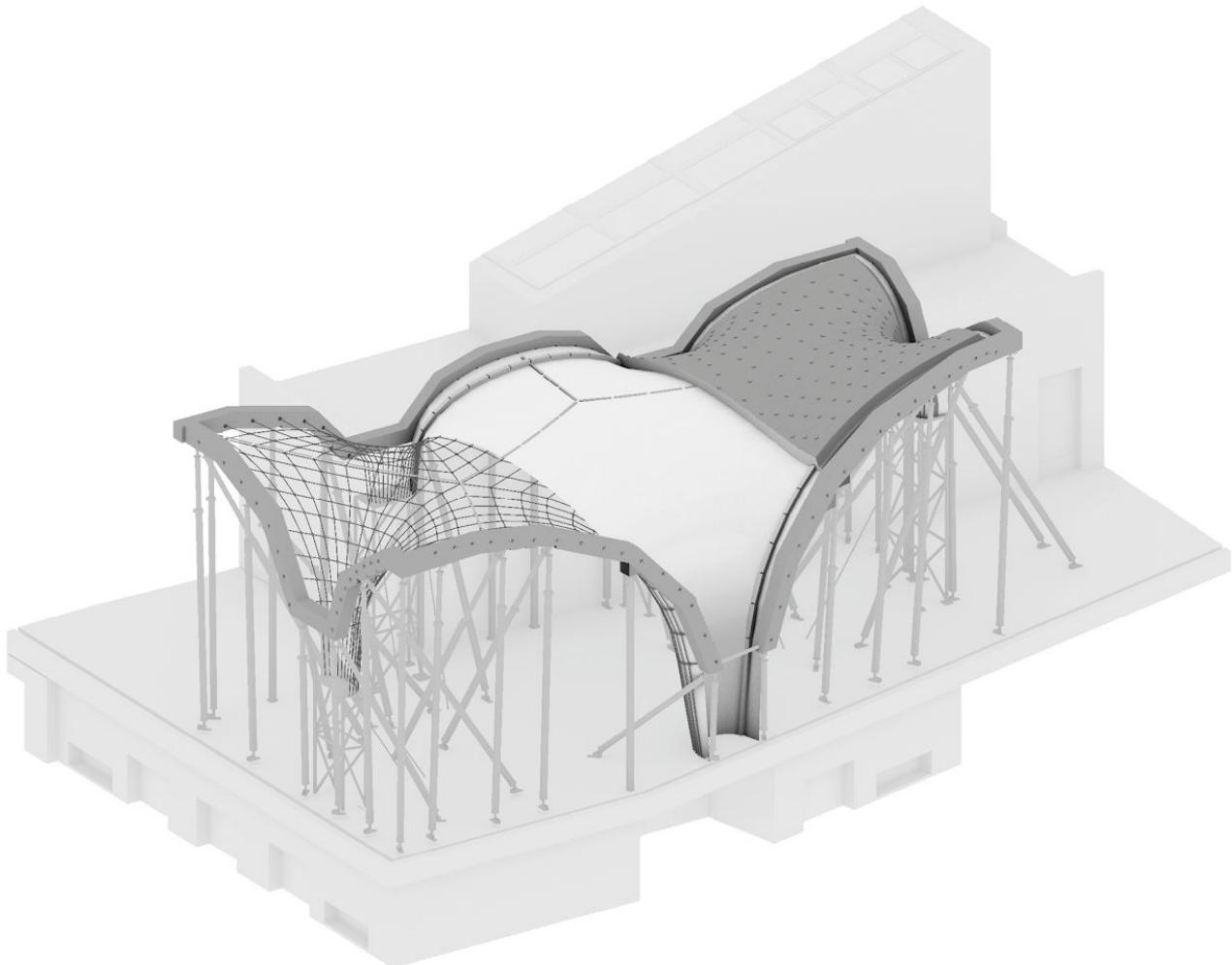
# Geometry

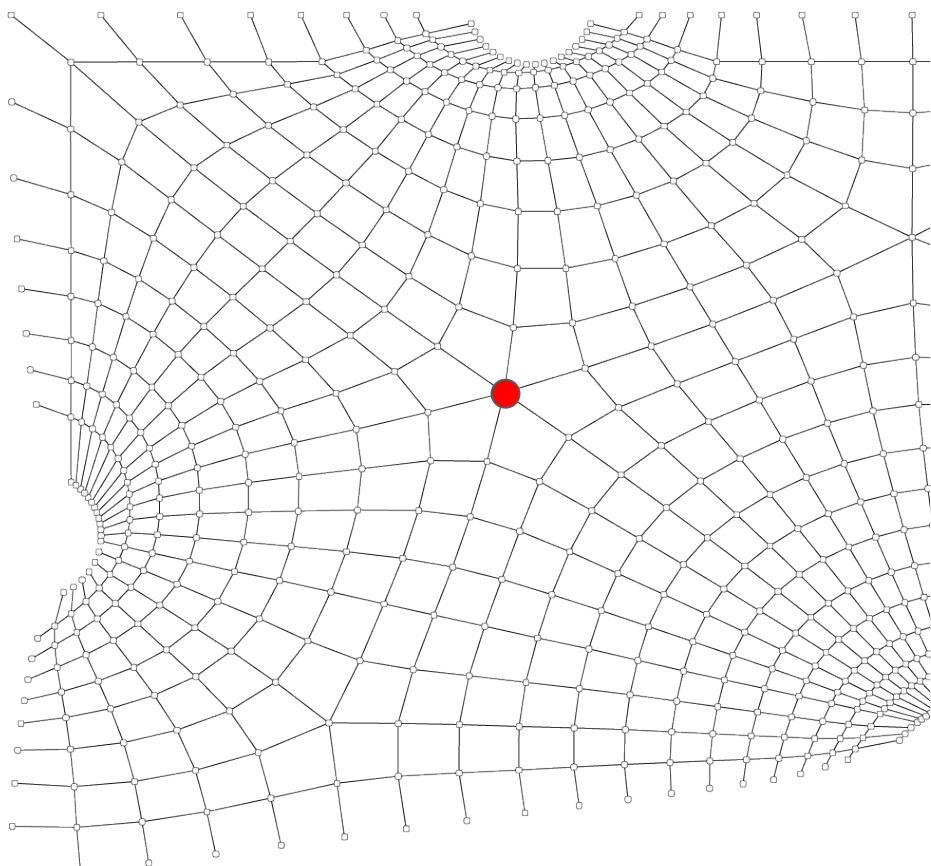
1. Given two vectors, use the cross product to create a set of three ortho**normal** vectors.
2. Use the cross product to compute the area of a convex, 2D polygon.
3. Define a function for computing the cross products of two arrays of vectors.
  - a. The input arrays have the same length (same number of vectors).
  - b. Prototype in pure Python (loop over the arrays).
  - c. Make Numpy equivalent without loops.

# Data Structures

1. Using **faces.obj**
  - a. Define a function for traversing the mesh from boundary to boundary in a “straight” line.
  - b. Visualise the result.

Next Week





```
cablenet.vertex[745] => {  
    'constraint_name': 'target',  
    'constraint_type': None,  
    'cx': 0.950,  
    'cy': 0.950,  
    'damping': 1,  
    'is_anchor': False,  
    'is_constrained': True,  
    'is_fixed': False,  
    'is_ridge': False,  
    'px': 0.000,  
    'py': 0.000,  
    'pz': 0.000,  
    'ring_type': 'XL',  
    'rx': 0.000,  
    'ry': 0.000,  
    'rz': 0.000,  
    'sag': 0.024,  
    'sw1': 0.672,  
    'sw2': 0.981,  
    'x': 6.405,  
    'y': 5.366,  
    'z': 5.653,
```

