# 拡張アンサンブル法によるモンテカルロ計算 Extended Ensemble method for Monte Carlo Methods

理学研究科 物理学専攻 大久保 毅

### Contents

- Histogram method
- Multi Canonical Method
- Wang-Landau method
- Replica exchange method
- ALPS and Report

Back ground

### Extended ensemble = general ensemble

In conventional MC or MD simulation:

We try to estimate expectation values under "physically relevant" ensembles.

NVE, NVT, NPT, ...



Even if an ensemble is not directly connected to any physical systems, we can use is to enhance the efficiency of numerical calculation (MC, MD) for interested physical system.

### Large relaxation time in standard MC and MD

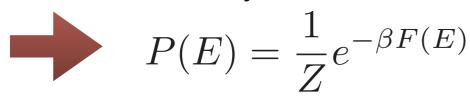
- Critical phenomena
  - $\tau \sim L^z$  with standard algorithm (critical slowing down)
  - z can be significantly reduced by using "global update"
- First order phase transition, Glass transition (structural glass, spin glass), protein folding,
  - $\tau \sim \exp(\Delta E/T)$  or  $\exp(\Delta E/|T-T_c|)$ ; Note  $\Delta E \propto L^d$ !
  - exponential can be reduce to polynomial by using extended ensemble methods

## Origin of exponentially long relaxation time

Partition function of the canonical ensemble

$$Z = \int d\Gamma e^{-\beta \mathcal{H}(\Gamma)} = \int dE \underline{\rho(E)} e^{-\beta E} = \int dE e^{-\frac{\beta F(E)}{\P}}$$
 Density of state

Probability distribution for energy

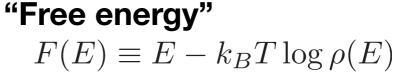


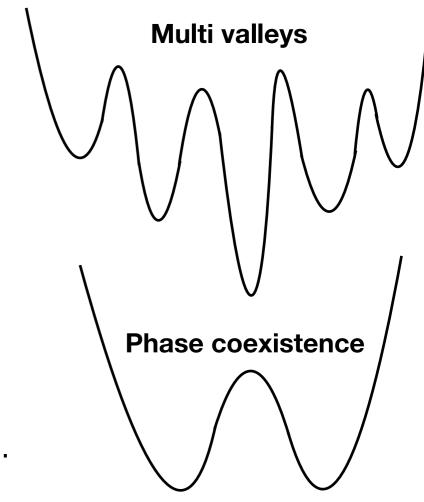
Note! Free energy is extensive:  $F(E) \propto N$ 

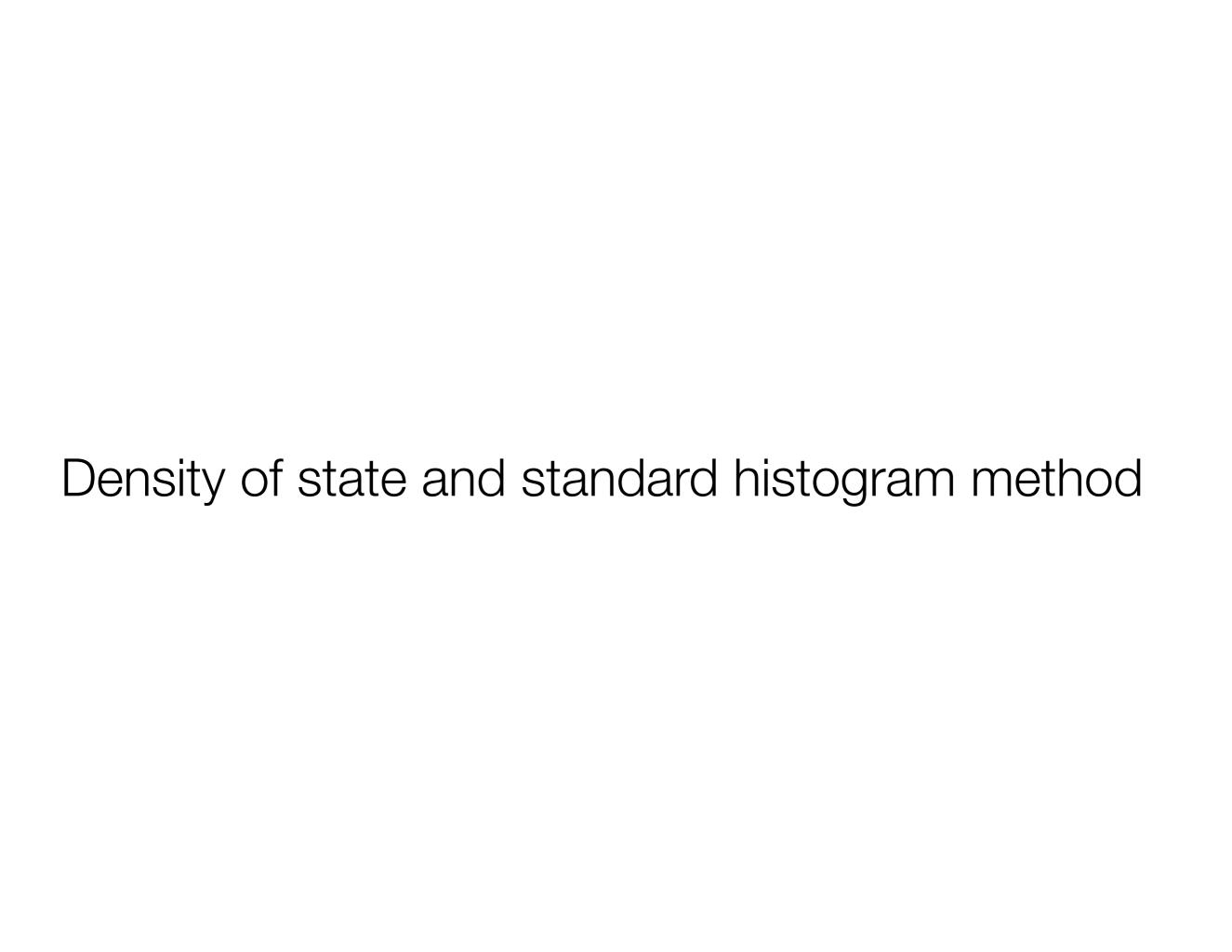
- "Transition probability" is proportional to the exponential of Free-energy difference:  $\exp(-\Delta F/T)$
- Usual algorithm of MC (and MD) changes the state (or the energy) gradually.



If there are local minima, the relaxation time could be exponentially large as the size is increased.







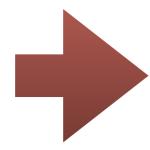
## Density of state

$$Z = \int d\Gamma e^{-\beta \mathcal{H}(\Gamma)} = \int dE \rho(E) e^{-\beta E} \qquad \int d\Gamma \quad \text{~O(N)-dimensional integral}$$
 
$$= \int dE \int dM \rho(E, M) e^{-\beta E} \qquad \int dE \quad \text{~1-dimensional}$$
 
$$\int dE \int dM \quad \text{~2-dimensional}$$

- If we know the exact  $\rho(E)(\text{or }\rho(E,M))$ , the calculation of partition function reduced to 1 or (a few) -dimensional integral.
- Even if we only know an approximate density of state,

$$\tilde{\rho}(E) \simeq \rho(E)$$

we can improve the sampling efficiency by using its information



- Histogram method
- Multi canonical method
- Wang-Landau method

### Energy Histogram

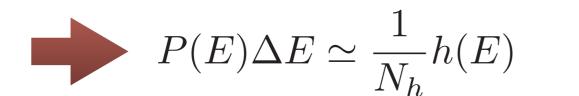
#### 3500 3000 2500 -1500 1000 500 4 -2 0 E

### Energy histogram:

In MC or MD calculations

 $h(E_i)$  :# or samples (snap shots) with energy in

$$E_i - \Delta E/2 \le E < E_i + \Delta E/2$$



Total # of samples 
$$N_h \equiv \sum h(E_i)$$

For e.g. NVT ensemble

$$P(E) = \frac{1}{Z(\beta)} \rho(E) e^{-\beta E} \qquad \qquad \rho(E) \simeq \frac{Z(\beta)}{N_h \Delta E} h(E) e^{\beta E}$$

We can calculate (approximate) density of state from usual MC or MD simulations!

## Histogram method (reweighting method)

### **Energy expectation value of different temperature**

$$\langle E \rangle_{\beta'} = \frac{\int dE \rho(E) E e^{-\beta' E}}{\int dE \rho(E) e^{-\beta' E}} \simeq \frac{\sum_{i} E_{i} h(E_{i}) e^{-(\beta' - \beta) E_{i}}}{\sum_{i} h(E_{i}) e^{-(\beta' - \beta) E_{i}}}$$

Any expectation values can also be calculated by the histogram method

$$\rho(E) \simeq \frac{Z(\beta)}{N_h \Delta E} h(E) e^{\beta E}$$

$$\langle O \rangle_{\beta'} \simeq \frac{\sum_{i} O(E_i) h(E_i) e^{-(\beta' - \beta)E_i}}{\sum_{i} h(E_i) e^{-(\beta' - \beta)E_i}}$$

#### Average at energy $E_i$

$$O(E_i) \equiv \sum_{E(\Gamma_j) \in E_i} O(\Gamma_j)$$

## Limitation of histogram method

Reweighted histogram becomes less accurate when T' is far from the original T.

"Tail" of the original histogram has only small # of snapshots→large noise

#### **Central limit theorem**

Width of energy distribution:  $\propto \sqrt{N}$ 

Average of energy:  $\propto N$ 

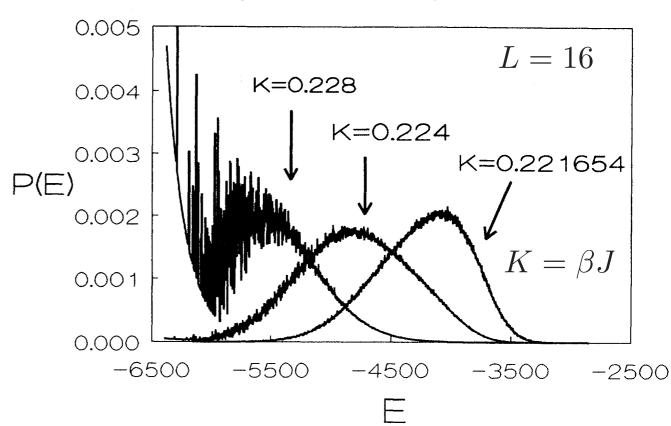
Distribution becomes narrower as N is increased!

Reliable temperature region for reweighting:

$$\Delta T \propto \frac{1}{\sqrt{N}}$$

# Energy distribution of 3d-Ising model

A. M. Ferrenberg and D. P. Landau, Phys. Rev. B 44, 5081 (1991)



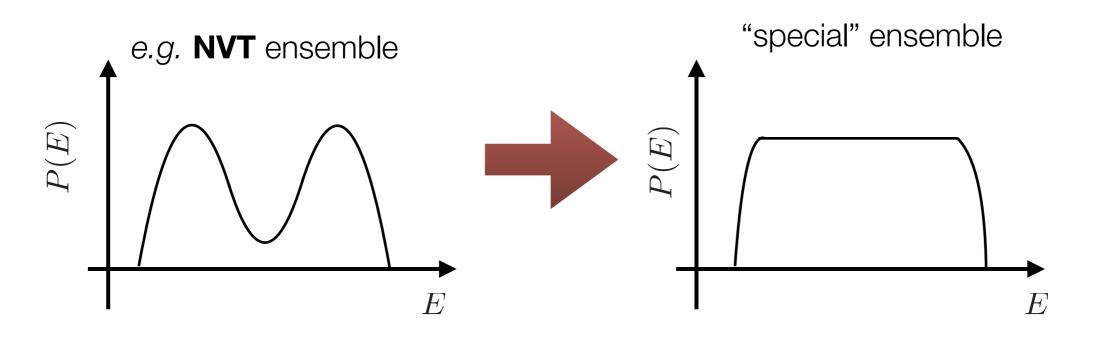
MC simulation at K=0.221654



Reweighting to K=0.224 and K=0.228

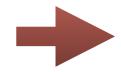
Multi Canonical methods

If we can prepare a special ensemble where the energy distribution is "flat", we can efficiently sample all relevant states.



$$P(E) \propto \rho(E)e^{-\beta E}$$

$$\tilde{P}(E) \propto \rho(E)e^{-S(E)} = \text{const.}$$



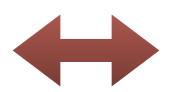
**Special ensemble is log of DOS!** 

$$S(E) = \log \rho(E)$$

## How to obtain the special ensemble?

#### Special ensemble is log of DOS!

$$S(E) = \log \rho(E)$$



#### DOS is unknown!

We can obtain f(E) approximately by iterative calculations.

### "Image" of an iterative algorithm

- 1. Run MC simulation on a temperature and calculate energy histogram  $h(E) \sim \rho(E)e^{-\beta E}$
- 2. Based on the energy histogram, extract approximate S(E)

$$S^0(E) = \beta E + \log h(E)$$

- 3. **Loop** *n* 
  - 1. Run MC simulation under  $S^{(n)}(E)$  and calculate histogram  $h^{(n)}(E)$
  - 2. Calculate next  $S^{(n+1)}(E)$  as

$$S^{(n+1)}(E) = S^{(n)}(E) + \log h^{(n)}(E)$$

### Detailed algorithm

B.A. Berg, Nucl. Phys. B (Proc. Suple.) **63**A-C, 982 (1998)

Suppose S(E) looks like:  $S(E) = \beta(E)E - \alpha(E)$ 

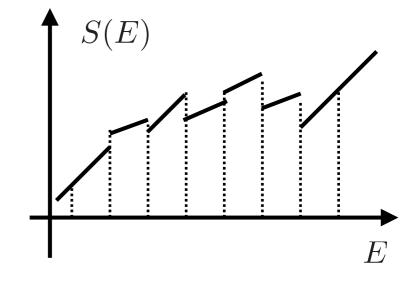
(Energy dependent temperature)



$$S(E) \simeq \beta_i E - \alpha_i$$
 for  $E_i - \Delta E/2 \le E \le E_i + \Delta E/2$ 

In a specific interval, we want to optimize  $\beta$  and  $\alpha$ , i.e. P(E) becomes flat.

By defining 
$$\beta_i \equiv \frac{S(E_{i+1}) - S(E_i)}{\Delta E}$$



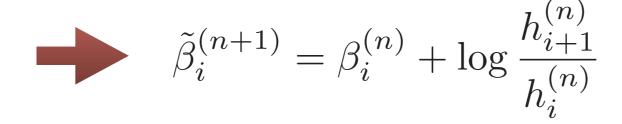
$$\alpha_{i-1} = \alpha_i + (\beta_{i-1} - \beta_i)E_i$$

We fix 
$$\alpha_{i_{max}} = 0$$

**Iteration** :how to determine next  $\beta$  and  $\alpha$ 

In order to make the histogram flat,

$$S^{(n+1)}(E) = S^{(n)}(E) + \log h^{(n)}(E)$$



This estimator could be suffered from large statistical error



Gradual change from the previous 
$$\beta$$
 
$$\beta_i^{(n+1)} = (1-c_i)\beta_i^{(n)} + c_i\tilde{\beta}_i^{(n+1)} \qquad \text{*For optimal $c_i$, see the reference}$$

 $\alpha$  is calculated from  $\beta$ 

$$\alpha_{i-1}^{(n+1)} = \alpha_i^{(n+1)} + (\beta_{i-1}^{(n+1)} - \beta_i^{(n+1)}) E_i$$

## Example of application

### *q*-state Potts model on the square lattice

$$\mathcal{H} = -J \sum_{\langle i,j \rangle} \delta_{S_i,S_j}$$

$$\mathcal{H} = -J \sum_{\langle i, j \rangle} \delta_{S_i, S_j} \qquad S_i = 0, 1, 2, \cdots, q - 1$$

#### Phase transition at

$$T_c/J = \frac{1}{\log(1+\sqrt{q})}$$

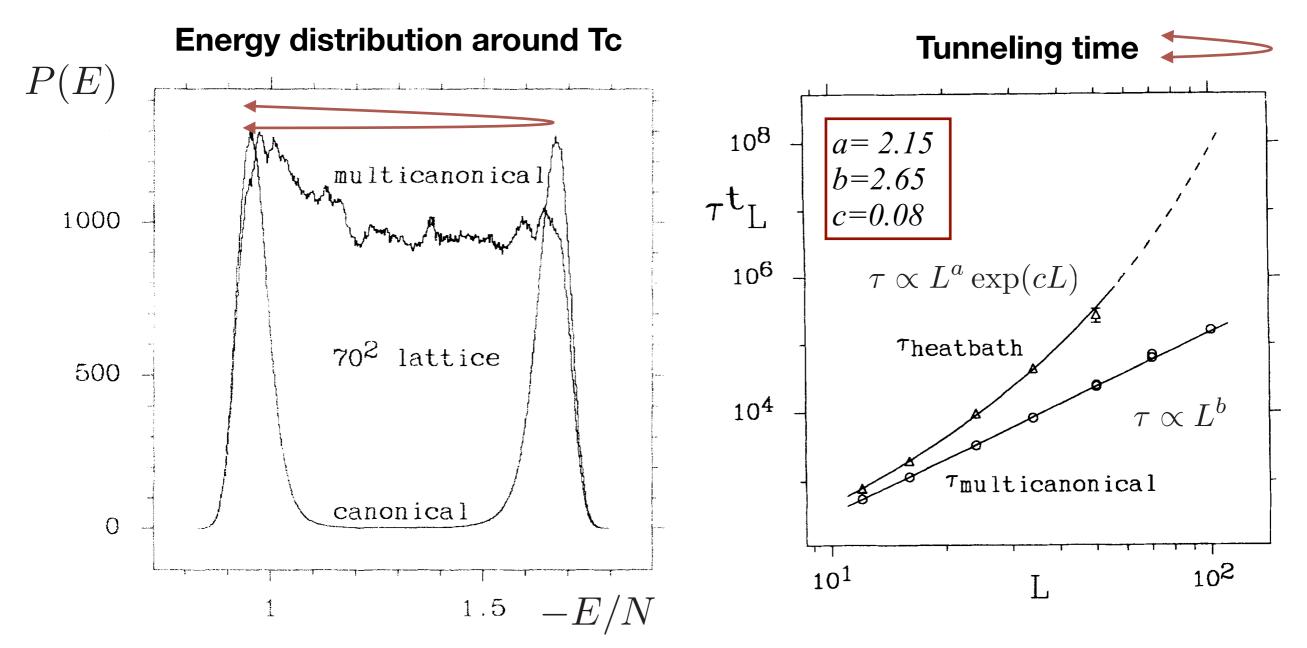
q=2: Equivalent to Ising model

 $q \leq 4$ : Continuous phase transition

q > 5: 1st order phase transition

### Multi Canonical method for q=10 Potts model

B.A. Berg and T. Neuhaus, Phys. Rev. Lett. **68**, 9 (1992)



By Multi Canonical method, the tunneling time is reduced to the power of L!

Another method to obtain the density of state:

### Random walk on the energy space

Markov Chain Monte Carlo with the probability

$$W_{\Gamma \to \Gamma'} = \min\left(\frac{g(E(\Gamma))}{g(E(\Gamma'))}, 1\right)$$
 
$$g(E) \text{ :estimate of DOS}$$

if 
$$g(E) = \rho(E)$$

This MCMC give us completely flat histogram

## Wang-Landau method:update of g(E)

F. Wang and D. P. Landau (2001)



Initially, we don't know DOS.  $\blacksquare$  Set an initial guess, e.g. g(E) = 1

Along MCMC, we update g(E) of the  $E(\Gamma)$  as

$$g_{new}(E) = g(E) \times f$$

If the multiplication factor is "gradually" reduced to f=1,

### g(E) eventually converges to $\rho(E)$ .

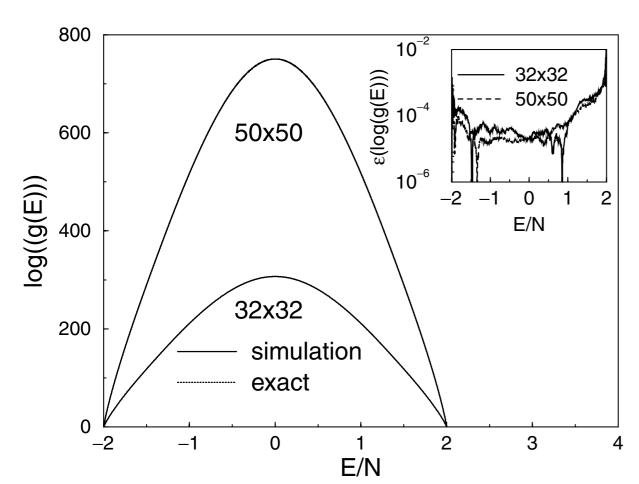
"gradual" change of f

- 1. Initially  $f = f_0$  (e.g.  $f_0 = e^1$ )
- 2. Loop i
  - If (the histogram h(E) becomes "flat"?)
    - Then, we decrease  $f_i$  as  $f_{i+1} = (f_i)^x$  (e.g. x = 1/2), and reset the histogram.
- Repeat until  $f_i$  becomes enough small (e.g.  $f \sim \exp(10^{-8})$ )

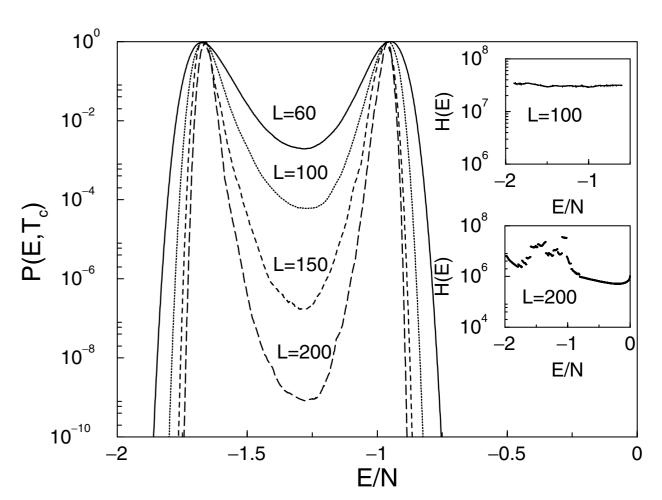
### Power of Wang-Landau method

F. Wang and D. P. Landau, Phys. Rev. Lett. 86, 2050 (2001)

#### Density of state of 2D-Ising model



#### Density of state of q=10 Potts model



We can obtain very accurate density of state by Wang-Landau method!

## Replica Exchange method

K.Hukushim and K. Nemoto, J. Phys. Soc. Jpn. 65, 1604 (1996).

## Replica exchange (parallel tempering)

A different types of extended ensemble:

Usual MC or MD considers one parameter and one realization:

$$T, \Gamma = \{S_i\}, \{\boldsymbol{q}_i, \boldsymbol{p}_i\}$$



Replica exchange method considers multiple parameter sets together with multiple realizations:

$$\{T_0,T_1,\cdots,T_M\}, \{\Gamma_0,\Gamma_1,\cdots,\Gamma_M\},\$$

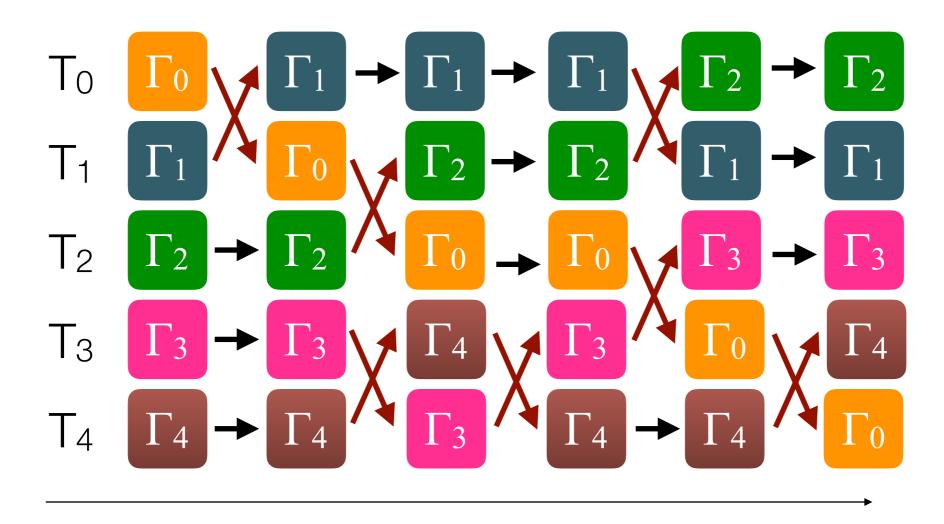


Try to sample "(M+1)-dimensional" joint-distribution

$$P(\Gamma_0,\Gamma_1,\cdots,\Gamma_M;T_0,T_1,\cdots,T_M)$$

## "Replica exchange"

Along simulation, we "exchange" the relationship between parameter and realization



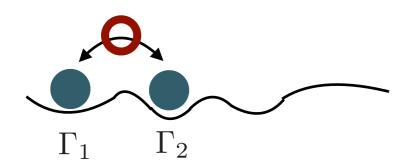
time

## Purpose of replica exchange

Free energy landscape depends on the parameter

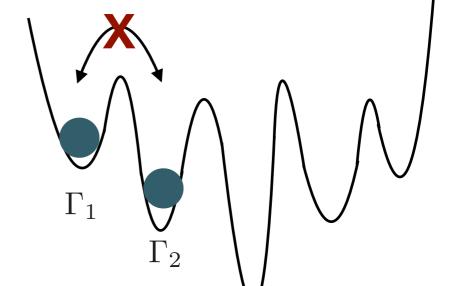
### High temperature: Th

 $\Gamma$  easily moves to other points!



### Low temperature:T<sub>I</sub>

Thardly moves to other minima!





Make a pass like:

$$\{\Gamma_1,T_l\} o \{\Gamma_1,T_h\} o \{\Gamma_2,T_h\} o \{\Gamma_2,T_l\}$$
 low high high low

<sup>\*</sup> Parameter is not necessary a temperature.

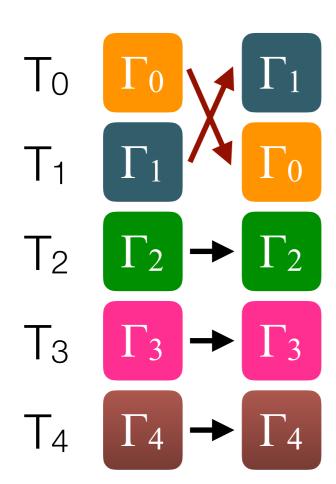
### Markov Chain Monte Carlo for Replica Exchange

### Target steady state distribution:

$$P(\Gamma_0, \Gamma_1, \cdots, \Gamma_M; T_0, T_1, \cdots, T_M) \propto e^{-\sum_i^M \beta_i E_i}$$

$$E_i \equiv \mathcal{H}(\Gamma_i)$$

### Metropolis method:



#### ${\mathcal T}$ :sequence of temperatures

$$\mathcal{T} = \{T_1, T_0, T_2, \cdots\}$$
$$\{T_0, \Gamma_0\}, \{T_1, \Gamma_1\} \to \{T_1, \Gamma_0\}, \{T_0, \Gamma_1\}$$

#### **Transition probability**

 $\mathcal{T}_{01}$ 

$$W_{\mathcal{T}_{01} \to \mathcal{T}_{10}} = \min \left( 1, \frac{P(\{\Gamma_i\}; \mathcal{T}_{10})}{P(\{\Gamma_i\}; \mathcal{T}_{01})} \right)$$

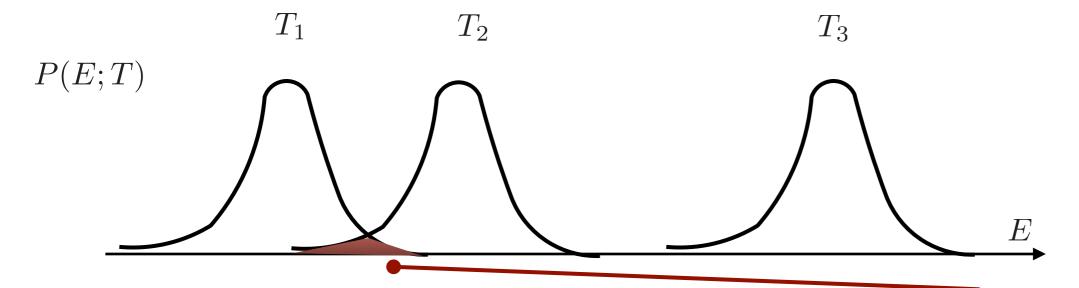
$$\frac{P(\{\Gamma_i\}; \mathcal{T}_{10})}{P(\{\Gamma_i\}; \mathcal{T}_{01})} = \frac{e^{-\beta_1 E_0 - \beta_0 E_1}}{e^{-\beta_0 E_0 - \beta_1 E_1}}$$
$$= e^{(\beta_0 - \beta_1)(E_0 - E_1)}$$

## Select of temperature sequence

$$\frac{P(\{\Gamma_i\}; \mathcal{T}_{10})}{P(\{\Gamma_i\}; \mathcal{T}_{01})} = e^{(\beta_0 - \beta_1)(E_0 - E_1)} = \frac{P(E_1; T_0)P(E_0; T_1)}{P(E_0; T_0)P(E_1; T_1)}$$

#### **Energy distribution at** *T*

P(E;T)



Almost all exchange occurs the energy region of "overwrap".

$$\{\Gamma_1, T_1\}, \{\Gamma_2, T_2\} \to \{\Gamma_1, T_2\}, \{\Gamma_2, T_1\}$$
 :acceptable!

$$\{\Gamma_2, T_2\}, \{\Gamma_3, T_3\} \rightarrow \{\Gamma_2, T_3\}, \{\Gamma_3, T_2\}$$
 :almost rejected!

For efficient exchange, we have to choose a sequence of temperatures so that the energy distributions have finite overwrap!

Usually we only exchange the nearest neighbor pairs of temperatures

## Select of temperature sequence: Example

Suppose 
$$C = \frac{dE}{dT} = \text{const.}$$

$$\frac{P(\{\Gamma_i\}; \mathcal{T}_{10})}{P(\{\Gamma_i\}; \mathcal{T}_{01})} = e^{(\beta_0 - \beta_1)(E_0 - E_1)}$$



Temperature sequence satisfying almost "flat" transition probability

$$(\beta_i - \beta_{i+1})(E_i - E_{i+1}) = \text{const.}$$

$$C\frac{(T_{i+1} - T_i)^2}{T_{i+1}T_i} = \text{const.}$$

$$T_{i+1}T_i \simeq T_i^2$$
  $T_{i+1} = \alpha T_i$  :Temperatures are geometric sequence!

#### Important notice:

Heat capacity C is an extensive quantity:  $C \sim O(N)$ 



In order to keep finite overwrap, we need to increase temperature point M as

$$M \propto \sqrt{N}$$

## Relaxation time of the replica exchange

In order to confirm the equilibration of the whole system, usually we need two criterions

- 1. The correlation time at the highest temperature is sufficiently short, e.g.  $\tau$ =O(1)
  - If a replica visits the highest temperature, it can easily change its state  $\Gamma$ .
- 2. All replicas make several (~O(10)) round trips between the lowest and the highest temperatures
  - The ensemble at the lower temperature is in the equilibrium.

The second part determines the relaxation time of the method.

$$\tau_{\rm RE} \sim {\rm round\ trip\ time}$$

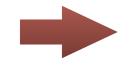
\* If the replica exchange is an random walk:

round trip time  $\propto M^2$ 

## Summary of replica exchange

### Algorithm:

- 1. Make a temperature set  $\{T_1, T_2, ..., T_M\}$
- 2. Loop n
  - (1) Do MC or MD for M replicas:  $\{\Gamma_1, \Gamma_2, ... \Gamma_M; T_1, T_2, ..., T_M\}$
  - (2) Calculate the energies of replicas
  - (3) Try replica exchange based on, e.g. Metropolis method
    - Usually we alternatively try replica exchange such as even n;  $\{1\leftrightarrow 2\}, \{3\leftrightarrow 4\}, \{5\leftrightarrow 6\}, ...$  odd n;  $\{2\leftrightarrow 3\}, \{4\leftrightarrow 5\}, \{6\leftrightarrow 7\}, ...$  Note: each exchange trial is independent
  - (4) Observe the quantities for  $\{\Gamma_1, \Gamma_2, ... \Gamma_M; T_1, T_2, ..., T_M\}$



If we already have a MC or MD programs, it is very easy to introduce the replica exchange method!

Introduction of ALPS for the report

### ALPS (Applications and Libraries for Physical Simulation)

- Set of libraries and applications for a variety of lattice models.
- Support for spin models, Hubburd model, Kondo lattice model, ...
- A lot of solvers for models:
  - Classical/Quantum Monte Carlo, Exact Diagonalization, Density Matrix Renormalization Group (DMRG), Dynamical Mean Field Theory (DMFT), Time Evolving Block Decimation (TEBD), ...
  - We can select efficient solver for your problems.
  - It can be applicable to the frontier research.

ALPS Wiki <a href="http://alps.comp-phys.org/mediawiki/index.php/Main\_Page">http://alps.comp-phys.org/mediawiki/index.php/Main\_Page</a>

- Phase transition of ultracold atoms immersed in a BEC vortex lattice
- Entanglement entropy and topological order in resonating valence-bond quantum spin liquids
- First-order topological phase transition of the Haldane-Hubbard model
- DMFT Study for Valence Fluctuations in the Extended Periodic Anderson Model
- Static and dynamical spin correlations of the S = 1/2 random-bond antiferromagnetic Heisenberg model on the triangular and kagome lattices
- Transport properties for a quantum dot coupled to normal leads with a pseudogap
- Magnetic structure and Dzyaloshinskii-Moriya interaction in the S =1/2 helical-honeycomb antiferromagnet  $\alpha$  -Cu<sub>2</sub>V<sub>2</sub>O<sub>7</sub>
- Mott transition in the triangular lattice Hubbard model: A dynamical cluster approximation study
- SU (N) Heisenberg model with multicolumn representations
- Superconductivity in the two-band Hubbard model
- Local Electron Correlations in a Two-Dimensional Hubbard Model on the Penrose Lattice

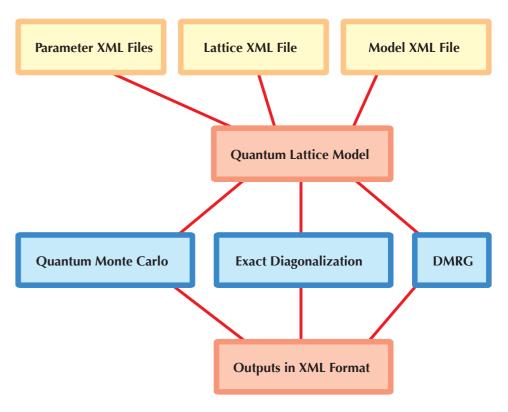
Details: <a href="http://alps.comp-phys.org/mediawiki/index.php/PapersTalks">http://alps.comp-phys.org/mediawiki/index.php/PapersTalks</a>

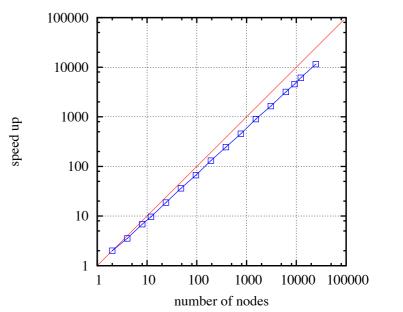


### ALPS の機能

- 入出力支援
  - 格子構造, 模型は XML を用いて柔軟に指定
  - ・全てのソルバーに共通した入出力形式
  - Python インターフェースを用意
    - Python から直接実行、グラフを作成
- 並列化
  - パラメータ並列のための並列化スケジューラ
  - ・量子モンテカルロソルバ (looper)
    - 京で20,000ノードまで良好なスケーリング
- 競合するアプリケーション: 「なし」?

#### \*MateriApps のハンズオン資料から借用





## Preparation of ALPS (If you use it at ECCS)

- Login to iMac and open "Terminal" application.
- Download ALPS binaries for ECCS from <a href="https://dl.dropboxusercontent.com/u/484163/alps-for-eccs/alps-20160816.zip">https://dl.dropboxusercontent.com/u/484163/alps-for-eccs/alps-20160816.zip</a>
  - Probably, it will be automatically decompressed.
     (If not, double click the zip file)
  - Move the folder to home (or your preferable place) cd mv Downloads/alps-20160816.
  - Run configure file

     alps-20160816/bin/alpsvars.sh

     Note! Don't forget type "." before "alps-20160816/bin/alpsvars.sh"
  - Check spinmc and simplemc spinmc --help simplemc --help

### Download of example (tutorial) files

<u>problems</u>

From ITC-LMS: <a href="https://itc-lms.ecc.u-tokyo.ac.jp/portal/login">https://portal/login</a>
or
github: <a href="https://github.com/compsci-alliance/many-body-">https://github.com/compsci-alliance/many-body-</a>

Download and decompress the example files "ALPS\_examples.zip"

 Move the folder ALPS\_examples to home (or your preferable place). In the case of ECCS iMac, cd mv Downloads/ALPS\_examples.

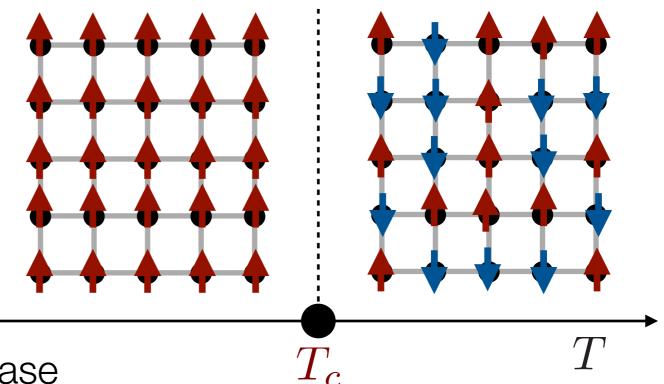
## Exercise (not a report)

Square lattice Ising model

$$\mathcal{H} = -J \sum_{\langle i,j \rangle} S_i S_j$$

• Continuous transition at  $T=T_{C}$ ,

$$T_c/J = \frac{2}{\ln(1+\sqrt{2})}$$
  
= 2.26918531...

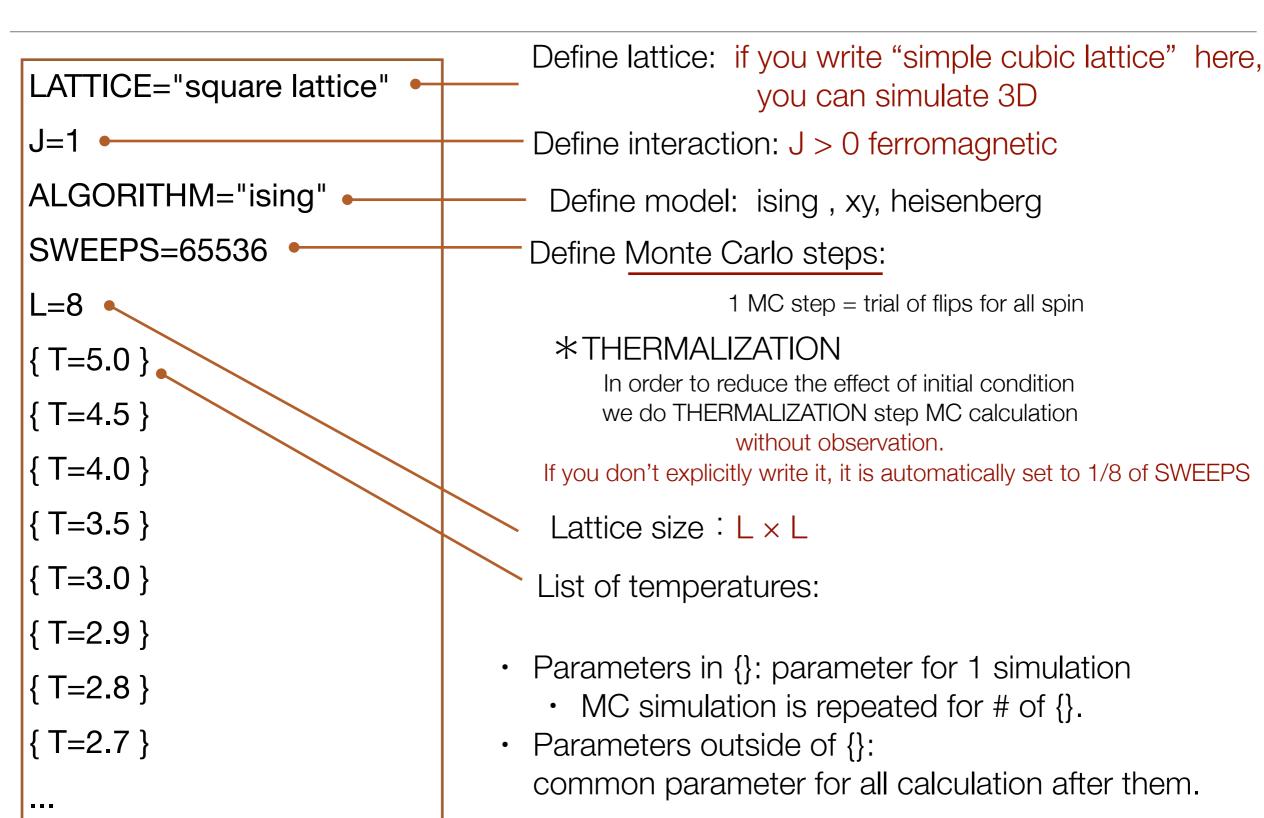


- $T > T_c$ : Para magnetic phase
- $T < T_c$ : Ferro magnetic phase
- By Monte Carlo simulation (Metropolis algorithm), see the phase transition!

## Simulation by simplemc

- simplemc: classical Monte Carlo simulator using Metropolis Algorithm
- Move to ALPS\_examples
  - cd
  - cd ALPS\_examples/simplemc
- Transform parameter file to XML format
  - parameter2xml parm9a
- Run simulation (It takes approximately five minites)
  - simplemc parm9a.in.xml
- Plot the results (Specific heat, Energy, square of the Magnetization)
  - python plot9a.py
  - (If you close three windows (graphs), python script will stop)

## Explanation of parameter file: parm9a



## Explanation of plotting file: plot9a.py

#### Python script

Extract the result from the data files: pyalps.loadMeasurements

Setting for the X and the Y axes: pyalps.collectXY

Plotting: matplotlib

```
data = pyalps.loadMeasurements(pyalps.getResultFiles(prefix='parm9a'),
    ['Specific Heat', 'Magnetization Density^2', 'Energy Density'])
for item in pyalps.flatten(data):
    item.props['L'] = int(item.props['L'])

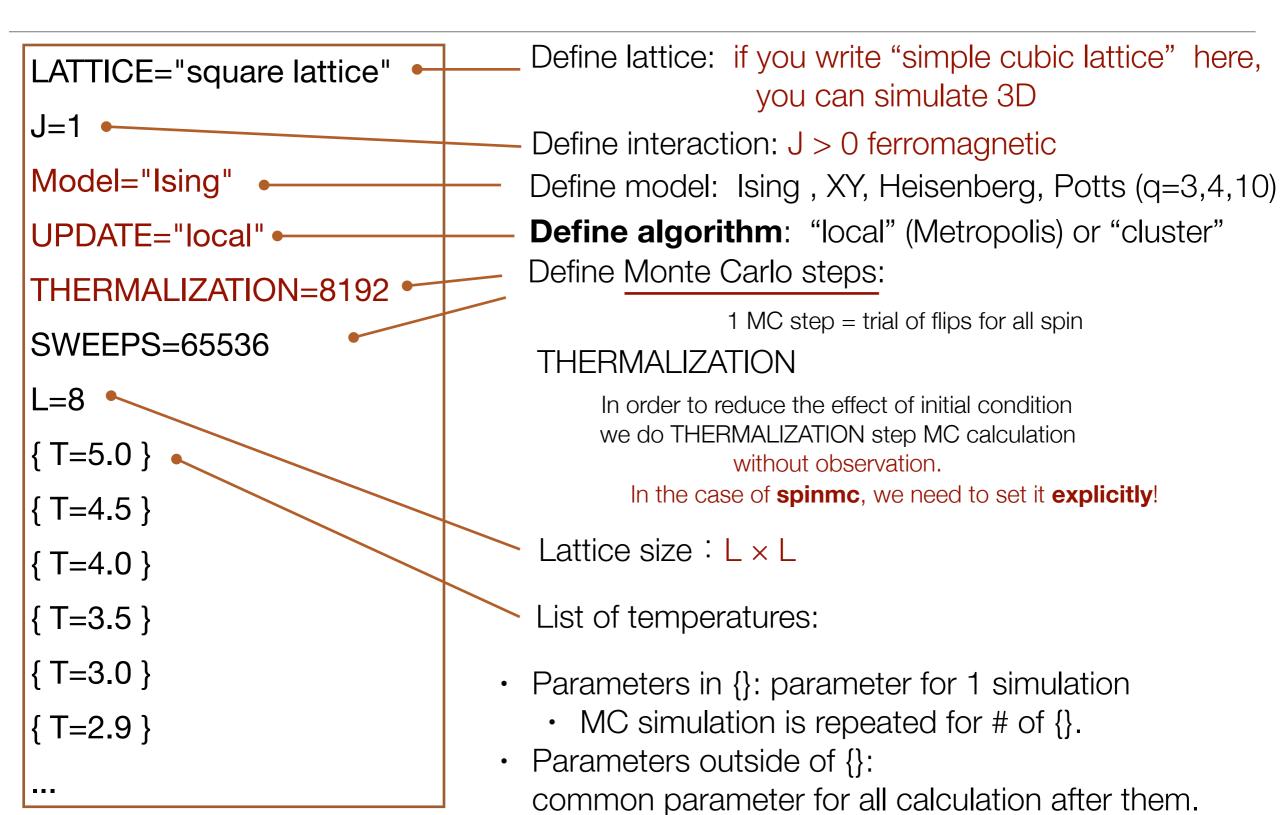
magnetization2 = pyalps.collectXY(data, x='T', y='Magnetization Density^2', foreach=['L'])
magnetization2.sort(key=lambda item: item.props['L'])

pyplot.figure()
alpsplot.plot(magnetization2)
pyplot.xlabel('Temperture $T$')
pyplot.ylabel('Magnetization Density Squared $m^2$')
pyplot.legend(loc='best')
```

## Simulation by **spinmc**

- spinmc: classical Monte Carlo simulator using Metropolis Algorithm or Cluster Algorithm
- Move to ALPS\_examples
  - cd
  - cd ALPS\_examples/spinmc
- Transform parameter file to XML format
  - parameter2xml parm9a
- Run simulation
  - spinmc --Tmin 5 parm9a.in.xml
     Note. "--Tmin n" set minimum time to check weather a simulation is finished.
     In this example, default value n=60 is too long, Thus, here I recommend to use --Tmin 5 or --Tmin 1
- Run evaluation (Different from simplemc, we need explicit evaluation for several physical quantities)
  - spinmc\_evaluate parm9a.task\*.out.xml
- Plot the results (Specific heat, Energy, square of the Magnetization)
  - python plot9a.py
  - (If you close three windows (graphs), python script will stop)

## Explanation of parameter file: parm9a



## Explanation of plotting file: plot9a.py

#### Python script

Extract the result from the data files: pyalps.loadMeasurements

Setting for the X and the Y axes: pyalps.collectXY

Plotting: matplotlib

```
data = pyalps.loadMeasurements(pyalps.getResultFiles(prefix='parm9a'),
  ['Specific Heat', 'Magnetization^2', 'Energy Density'])
for item in pyalps.flatten(data):
  item.props['L'] = int(item.props['L'])
magnetization2 = pyalps.collectXY(data, x='T', y='Magnetization^2', foreach=['L'])
magnetization2.sort(key=lambda item: item.props['L'])
pyplot.figure()
alpsplot.plot(magnetization2)
pyplot.xlabel('Temperture $T$')
pyplot.ylabel('Magnetization Density Squared $m^2$')
pyplot.legend(loc='best')
```

#### Report problem 1:

- By editing the parameter file parm9a, try to simulate the following systems
  - 1. Square lattice Ising model of larger system sizes than L=32 (e.g. L=64, 128, ...)
    - Discuss that the relationship among SWEEP, L, and error bar of physical quantities
    - Plot the "binder ratio of magnetization" and compare the crossing point of them to the true critical point.
      - It can be done by adding "Binder Ratio of Magnetization" (in the case of simpleme)
         to pyalps.loadMeasurements in plot9a.py and edit properly pyalps.collectXY
    - Try anything you can do
    - (Advanced) Try finite size scaling of the binder ratio, and specific heat.
  - 2. Cubic lattice Ising model of larger system sizes
    - Perform the same tasks with the case of the above square lattice model.
      - Note: In the case of 3D you may need longer time to simulate the model.
         Thus, the largest size becomes smaller than that of 2D.
    - (Advanced): Try XY or Heisenberg models and determine transition temperature from e.g. the crossing point of binder ratio.

## Report problem 1: Tips

- If you change the name of parameter file, you also need to edit the corresponding part of the plotting script.
- If you want to see the numbers directly, you can use python script textout9a.py.
  - If you output the numbers to a file:

    python textout9a.py > filename.txt
    (If you use the script for the binder ratio or other quantities, you need to edit it.)
- Note: if SWEEP is too small, MCMC can not correctly sample the equilibrium ensemble!. If you change the parameter, you should check the SWEEP dependence of the results.
  - (ALPS tutorial MC-01 might help you to check convergence of the results)

#### Report problem 1: Additional comments1

- You can use simpleme, spinme, free applications or your own code
  - If you use simplemc or spinmc, please attach input files to the report.
  - When you write a report by using an application not included in ALPS, please add information of the code (source code or url of the app.) in addition to the information of inputs to reproduce the results.
- Note that several quantities have different names in simplemc and spinmc.

	simplemc	spinmc
<e></e>	Energy Density	Energy Density
$< M^2 >$	Magnetization Density^2	Magnetization^2
<c></c>	Specific Heat	Specific Heat
binder ratio	Binder Ratio of Magnetization	Binder Cumulant

#### Report problem 1: Additional comments2

- The ALPS tutorials are useful to learn how to use the ALPS.
   Especially mc-01,02 and 07 are relevant.
  - http://alps.comp-phys.org/mediawiki/index.php/ ALPS 2 Tutorials:Overview
- If you install mac-osx binary, please use "Prerelease 2.3.0"
  - It exists only in "English" page. (In "Japanese" page, 2.3.0 does not exist!)
- If you install ALPS through mac-osx binary or MacPorts, "python" command appeared in previous exercises should be replaced by "alpspython".

#### Report problem 2:

- Suppose that you have a (sub) program  $MC(\Gamma, T, E)$  which perform MC update for input  $\Gamma$  at a temperature T and returns new  $\Gamma$  and its energy E.
  - 1. Make a (pseudo) program to perform a replica exchange Monte Carlo.
    - 1. Define the maximum and the minimum temperatures.
    - 2. Determine sequence of M temperatures. (You may use geometric sequence explained in today's lecture. In this case, the common ratio  $\alpha$  is determined by  $T_{\text{max}}$ ,  $T_{\text{min}}$  and M.)
    - 3. Implement the replica exchange Monte Carlo by using e.g. Metropolis method.
    - You can use c, c++, fortran, python, ..., or a pseudo code.
    - You can assume that you have a random number generator  $\mathbf{make\_random(r)}$  which return uniformly distributed random number  $r \in [0, 1)$
  - 2. (Advanced) If you have a MC or MD program for single run (or if you can write it), try to run the above program and observe the dynamics of replicas, such as turn around time, acceptance ratio of replica exchange, ... for a model you like.

#### Report problem 3 (optional)

- Write a comment to the lecture of classical many body systems, e.g.,
  - How do you feel the contents of the lecture?
    - Too easy, Boring, Too difficult, Too biased to the interest of the lecturer, ...
  - What topics do you want to learn if you have the next chance?
  - Do you have any idea to improve the quality of the lecture?
    - Tutorial using computers, Use black board, ...

#### Deadline

- Submit your report through the system of ITC-LMS
  - The deadline is July. 31st.
- If you have any troubles or questions, please freely ask me
  - at the future lectures,
  - by e-mail: <u>t-okubo@phys.s.u-tokyo.ac.jp</u>
  - or come to my office Sci. Bldg. #1 940.
     (It is better to get an appointment by e-mail.)

#### References (books)

- "A Guild to Simulations in Statistical Physics" D.P. Landau and D. Binder, Cambridge University Press.
- "Computational Physics", J. Thijssen, Cambridge University Press.
  - (「計算物理学」J.M.ティッセン著、松田和典他訳、シュ プリンガー・フェアラーク東京.
- ・ 「分子シミュレーション」上田顯著、裳華房.

#### PCOMS workshop

期日:6月7日

場所:柏の葉キャンパス

駅前サテライト

対象:

M2(博士進学予定), 博士課程の学生, 研究員、若手教員

参加申し込み・情報

5月26日(金)まで

http://pcoms.issp.u-tokyo.ac.jp/events

# 企業人材ニース vs 博士人材シース マッチングワークショップ

キャリアパス、広げてみませんか!

企業の人材ニーズと、博士人材の技術シーズをぶつけ合い、マッチングを図って、博士人材を参画企業への研究インターン実施(別紙参照)や企業連携研究に導くことを目的としています。午前中は、企業における計算機科学・計算科学の最近の活用事例も紹介いただきます。是非ご参加ください。

開催: 平成 29 年 6 月 7 日(水)10:00-19:30

場所: 東京大学フューチャーセンター2F

(柏の葉キャンパス駅前徒歩1分)

対象: 修士課程2年で博士課程進学予定の院生、

博士後期課程の院生、研究員、若手教員

など。教職員の聴講もOK。

参画: 出光興産㈱、NEC、新日鐵住金㈱、

トヨタ㈱、㈱日産アーク、

日本ゼオン㈱、富士通研究所㈱

本大DC 国内企業 博士課程を終えた後、学校で培ってきた能力をどのように社会で活かすことができるのか、企業の中で実際の業務

に近いことを行いながら知りたく思い、イ

ンターンシップに関する支援の手厚いイ

ノベーション創出人材育成プログラムに

異なるバックグラウンドを持つ研究者と 多くの議論をかわすなかで、考え方の違い を感じることも多くあり新鮮で多くの刺激 を得ることができました。また、企業の研 究機関での研究のあり方の一端を垣間 見ることができ、何よりインターンシップ先 での生活が楽しかったことが今後のキャリ アを考えるうえでよい経験となりました。

東大DC

国内企業

進行: 10:00~10:50「全固体電池における材料インフォマティクス手法を用いた新材料探索」「トヨタ自動車における計算材料科学への取り組み」(トヨタ自動車)

10:50~11:40 「社会課題解決のための高性能データ分析技術」(NEC)

13:00~13:10 ガイダンス(PCoMS、イノベーション創出人材育成事業・インターン実施に関して)

応募しました。

13:10~15:10 企業人材ニーズ説明(20分/1社 予定)

15:30~17:30 博士人材シーズ説明(参加者よりショートプレゼン&ポスター発表を予定)

17:30~19:30 企業説明ブース巡回・情報交換会

申込: <a href="http://pcoms.issp.u-tokyo.ac.jp/events">http://pcoms.issp.u-tokyo.ac.jp/events</a> (締切:平成 29 年 5 月 26 日(金)正午)