

# Lecture 8

## Training Neural Networks & Convolutional Neural Networks

# Review

We looked in detail at:

- Activation Functions (use ReLU)
- Data Preprocessing (images: subtract mean)
- Weight Initialization (use Xavier init)
- Batch Normalization (use)
- Gradient Checking
- Babysitting the Learning process
- Hyperparameter Optimization (random sample hyperparams, in log space when appropriate)

# Hyperparameter Optimization

# Cross-validation strategy

I like to do **coarse** -> **fine** cross-validation in stages

**First stage:** only a few epochs to get rough idea of what params work

**Second stage:** longer running time, finer search

... (repeat as necessary)

Tip for detecting explosions in the solver:

If the cost is ever  $> 3 \times$  original cost, break out early

# For example: run coarse search for 5 epochs

```
max_count = 100
for count in xrange(max_count):
    reg = 10**uniform(-5, 5)
    lr = 10**uniform(-3, -6)

    trainer = ClassifierTrainer()
    model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
    trainer = ClassifierTrainer()
    best_model_local, stats = trainer.train(X_train, y_train, X_val, y_val,
                                           model, two_layer_net,
                                           num_epochs=5, reg=reg,
                                           update='momentum', learning_rate_decay=0.9,
                                           sample_batches = True, batch_size = 100,
                                           learning_rate=lr, verbose=False)
```

note it's best to optimize  
in log space!

```
val_acc: 0.412000, lr: 1.405206e-04, reg: 4.793564e-01, (1 / 100)
val_acc: 0.214000, lr: 7.231888e-06, reg: 2.321281e-04, (2 / 100)
val_acc: 0.208000, lr: 2.119571e-06, reg: 8.011857e+01, (3 / 100)
val_acc: 0.196000, lr: 1.551131e-05, reg: 4.374936e-05, (4 / 100)
val_acc: 0.079000, lr: 1.753300e-05, reg: 1.200424e+03, (5 / 100)
val_acc: 0.223000, lr: 4.215128e-05, reg: 4.196174e+01, (6 / 100)
val_acc: 0.441000, lr: 1.750259e-04, reg: 2.110807e-04, (7 / 100)
val_acc: 0.241000, lr: 6.749231e-05, reg: 4.226413e+01, (8 / 100)
val_acc: 0.482000, lr: 4.296863e-04, reg: 6.642555e-01, (9 / 100)
val_acc: 0.079000, lr: 5.401602e-06, reg: 1.599828e+04, (10 / 100)
val_acc: 0.154000, lr: 1.618508e-06, reg: 4.925252e-01, (11 / 100)
```

nice

# Now run finer search...

```
max_count = 100
for count in xrange(max_count):
    reg = 10**uniform(-5, 5)
    lr = 10**uniform(-3, -6)
```

adjust range

```
max_count = 100
for count in xrange(max_count):
    reg = 10**uniform(-4, 0)
    lr = 10**uniform(-3, -4)
```

val_acc: 0.527000, lr: 5.340517e-04, reg: 4.097824e-01, (0 / 100)
val_acc: 0.492000, lr: 2.279484e-04, reg: 9.991345e-04, (1 / 100)
val_acc: 0.512000, lr: 8.680827e-04, reg: 1.349727e-02, (2 / 100)
val_acc: 0.461000, lr: 1.028377e-04, reg: 1.220193e-02, (3 / 100)
val_acc: 0.460000, lr: 1.113730e-04, reg: 5.244309e-02, (4 / 100)
val_acc: 0.498000, lr: 9.477776e-04, reg: 2.001293e-03, (5 / 100)
val_acc: 0.469000, lr: 1.484369e-04, reg: 4.328313e-01, (6 / 100)
val_acc: 0.522000, lr: 5.586261e-04, reg: 2.312685e-04, (7 / 100)
val_acc: 0.530000, lr: 5.808183e-04, reg: 8.259964e-02, (8 / 100)
val_acc: 0.489000, lr: 1.979168e-04, reg: 1.010889e-04, (9 / 100)
val_acc: 0.490000, lr: 2.036031e-04, reg: 2.406271e-03, (10 / 100)
val_acc: 0.475000, lr: 2.021162e-04, reg: 2.287807e-01, (11 / 100)
val_acc: 0.460000, lr: 1.135527e-04, reg: 3.905040e-02, (12 / 100)
val_acc: 0.515000, lr: 6.947668e-04, reg: 1.562808e-02, (13 / 100)
val_acc: 0.531000, lr: 9.471549e-04, reg: 1.433895e-03, (14 / 100)
val_acc: 0.509000, lr: 3.140888e-04, reg: 2.857518e-01, (15 / 100)
val_acc: 0.514000, lr: 6.438349e-04, reg: 3.033781e-01, (16 / 100)
val_acc: 0.502000, lr: 3.921784e-04, reg: 2.707126e-04, (17 / 100)
val_acc: 0.509000, lr: 9.752279e-04, reg: 2.850865e-03, (18 / 100)
val_acc: 0.500000, lr: 2.412048e-04, reg: 4.997821e-04, (19 / 100)
val_acc: 0.466000, lr: 1.319314e-04, reg: 1.189915e-02, (20 / 100)
val_acc: 0.516000, lr: 8.039527e-04, reg: 1.528291e-02, (21 / 100)

**53%** - relatively good  
for a 2-layer neural net  
with 50 hidden neurons.

# Now run finer search...

```
max_count = 100
for count in xrange(max_count):
    reg = 10**uniform(-5, 5)
    lr = 10**uniform(-3, -6)
```

adjust range

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max_count = 100
for count in xrange(max_count):
    reg = 10**uniform(-4, 0)
    lr = 10**uniform(-3, -4)
```

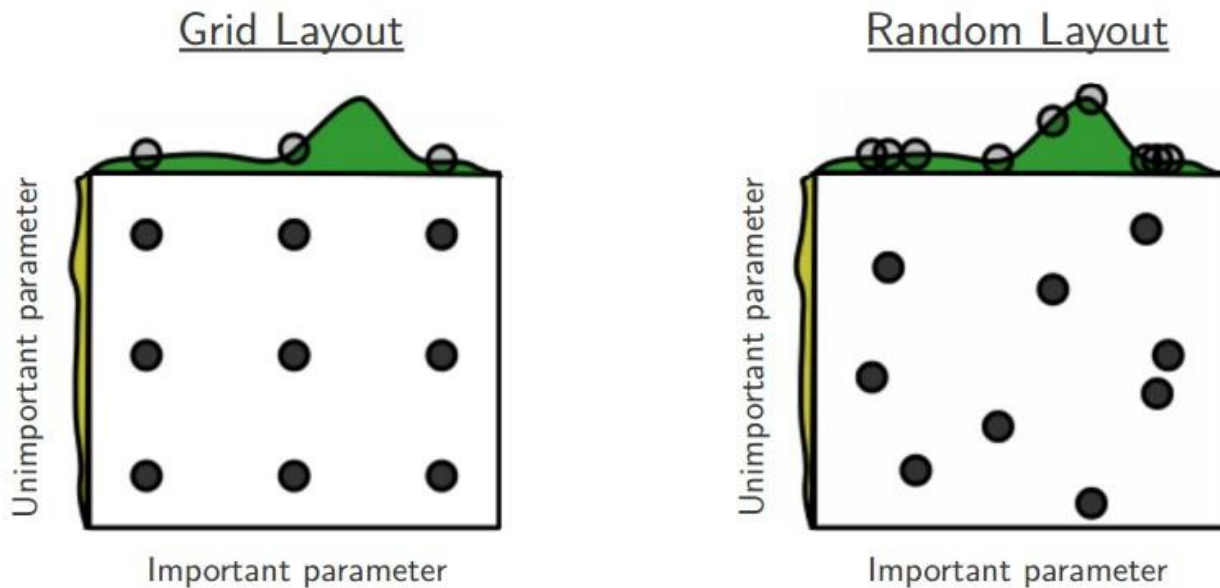
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val_acc: 0.516000, lr: 8.039527e-04, reg: 1.528291e-02, (21 / 100)

**53%** - relatively good  
for a 2-layer neural net  
with 50 hidden neurons.

But this best cross-  
validation result is  
worrying. Why?



# Random Search vs. Grid Search

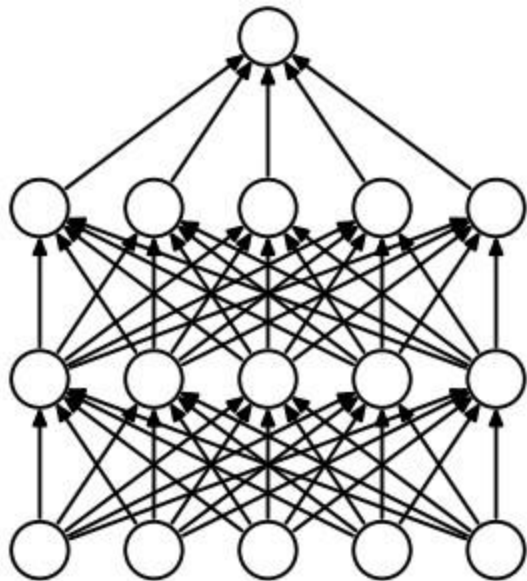


*Random Search for Hyper-Parameter Optimization*  
Bergstra and Bengio, 2012

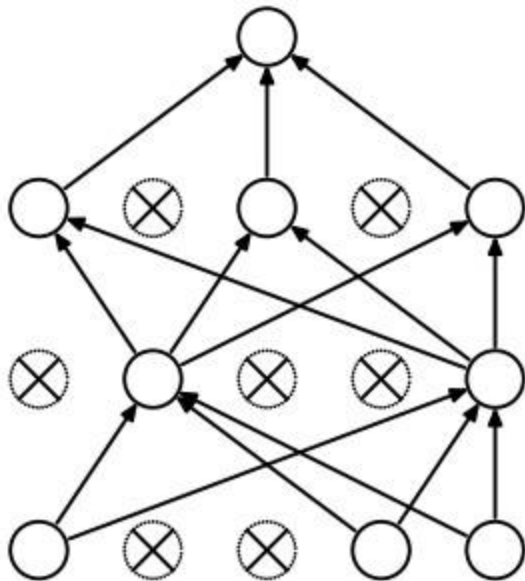


# Regularization: **Dropout**

“randomly set some neurons to zero in the forward pass”



(a) Standard Neural Net



(b) After applying dropout.

*[Srivastava et al., 2014]*

```
p = 0.5 # probability of keeping a unit active. higher = less dropout
```

```
def train_step(X):
```

```
    """ X contains the data """
```

```
    # forward pass for example 3-layer neural network
```

```
    H1 = np.maximum(0, np.dot(W1, X) + b1)
```

```
    U1 = np.random.rand(*H1.shape) < p # first dropout mask
```

```
    H1 *= U1 # drop!
```

```
    H2 = np.maximum(0, np.dot(W2, H1) + b2)
```

```
    U2 = np.random.rand(*H2.shape) < p # second dropout mask
```

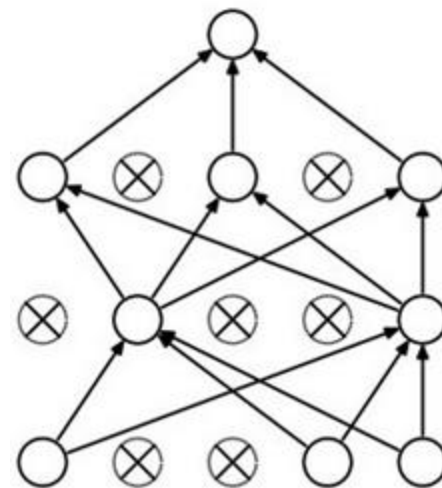
```
    H2 *= U2 # drop!
```

```
    out = np.dot(W3, H2) + b3
```

```
    # backward pass: compute gradients... (not shown)
```

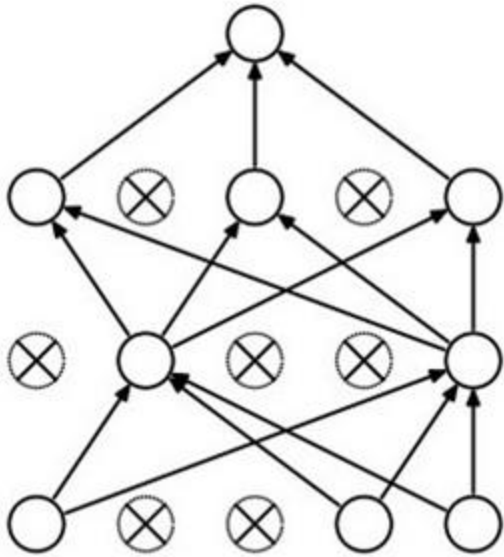
```
    # perform parameter update... (not shown)
```

Example forward pass with a 3-layer network using dropout



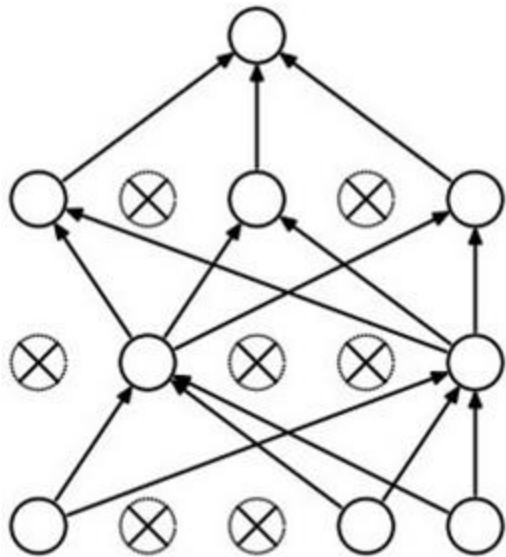
Waaaait a second...

How could this possibly be a good idea?



# Waaaaait a second...

## How could this possibly be a good idea?



Forces the network to have a redundant representation.

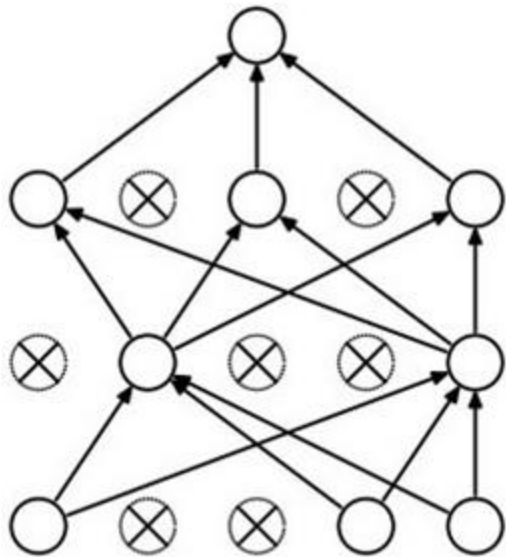


# Training with occlusions?



Waaaait a second...

How could this possibly be a good idea?



Another interpretation:

Dropout is training a large ensemble of models (that share parameters).

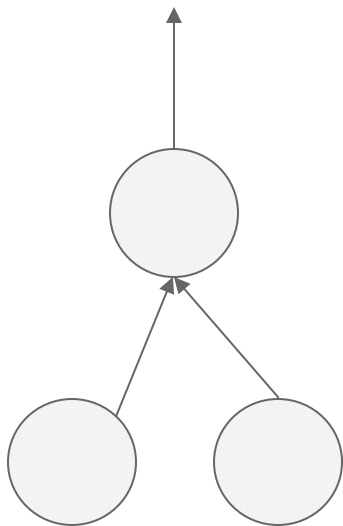
Each binary mask is one model, gets trained on only ~one datapoint.



# At test time....

Can in fact do this with a single forward pass! (approximately)

Leave all input neurons turned on (no dropout).



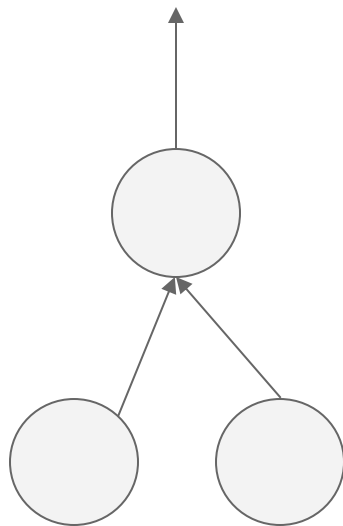
(this can be shown to be an approximation to evaluating the whole ensemble)



# At test time....

Can in fact do this with a single forward pass! (approximately)

Leave all input neurons turned on (no dropout).



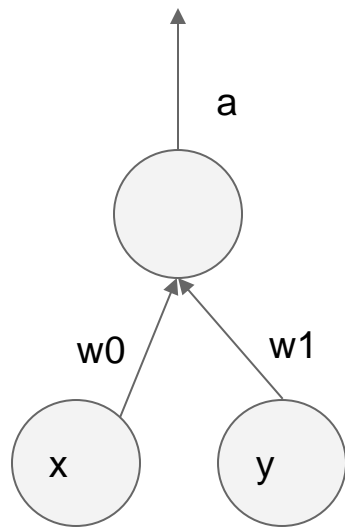
Q: Suppose that with all inputs present at test time the output of this neuron is  $x$ .

What would its output be during training time, in expectation? (e.g. if  $p = 0.5$ )

# At test time....

Can in fact do this with a single forward pass! (approximately)

Leave all input neurons turned on (no dropout).



during test:  $a = w0*x + w1*y$

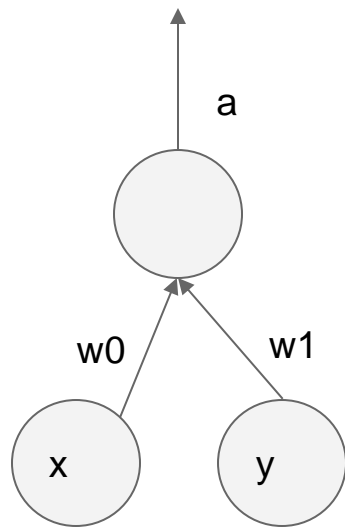
during train:

$$\begin{aligned} E[a] &= \frac{1}{4} * (w0*0 + w1*0 \\ &\quad w0*0 + w1*y \\ &\quad w0*x + w1*0 \\ &\quad w0*x + w1*y) \\ &= \frac{1}{4} * (2 w0*x + 2 w1*y) \\ &= \frac{1}{2} * (w0*x + w1*y) \end{aligned}$$

# At test time....

Can in fact do this with a single forward pass! (approximately)

Leave all input neurons turned on (no dropout).



during test:  $a = w_0 * x + w_1 * y$

during train:

$$E[a] = \frac{1}{4} * (w_0 * 0 + w_1 * 0$$

$$w_0 * 0 + w_1 * y$$

$$w_0 * x + w_1 * 0$$

$$w_0 * x + w_1 * y)$$

$$= \frac{1}{4} * (2 w_0 * x + 2 w_1 * y)$$

$$= \frac{1}{2} * (w_0 * x + w_1 * y)$$

With  $p=0.5$ , using all inputs in the forward pass would inflate the activations by 2x from what the network was “used to” during training!  
=> Have to compensate by scaling the activations back down by  $\frac{1}{2}$

# We can do something approximate analytically

```
def predict(X):  
    # ensembled forward pass  
    H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations  
    H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations  
    out = np.dot(W3, H2) + b3
```

At test time all neurons are active always

=> We must scale the activations so that for each neuron:

output at test time = expected output at training time

# Dropout Summary

```
""" Vanilla Dropout: Not recommended implementation (see notes below) """

p = 0.5 # probability of keeping a unit active. higher = less dropout

def train_step(X):
    """ X contains the data """

    # forward pass for example 3-layer neural network
    H1 = np.maximum(0, np.dot(W1, X) + b1)
    U1 = np.random.rand(*H1.shape) < p # first dropout mask
    H1 *= U1 # drop!
    H2 = np.maximum(0, np.dot(W2, H1) + b2)
    U2 = np.random.rand(*H2.shape) < p # second dropout mask
    H2 *= U2 # drop!
    out = np.dot(W3, H2) + b3

    # backward pass: compute gradients... (not shown)
    # perform parameter update... (not shown)

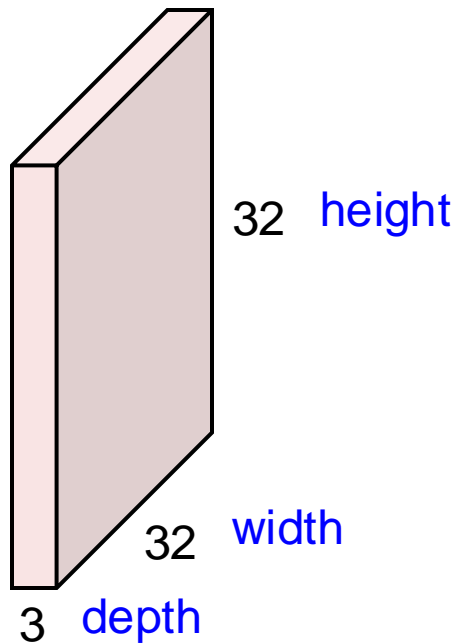
def predict(X):
    # ensembled forward pass
    H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations
    H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
    out = np.dot(W3, H2) + b3
```

drop in forward pass

scale at test time

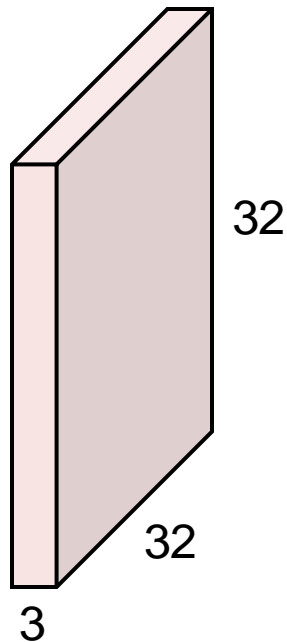
# Convolution Layer

32x32x3 image



# Convolution Layer

32x32x3 image



5x5x3 filter

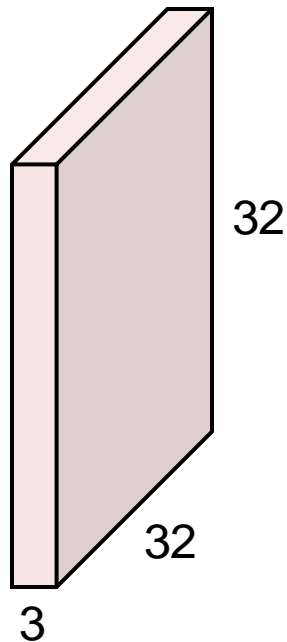


**Convolve** the filter with the image  
i.e. “slide over the image spatially,  
computing dot products”



# Convolution Layer

32x32x3 image



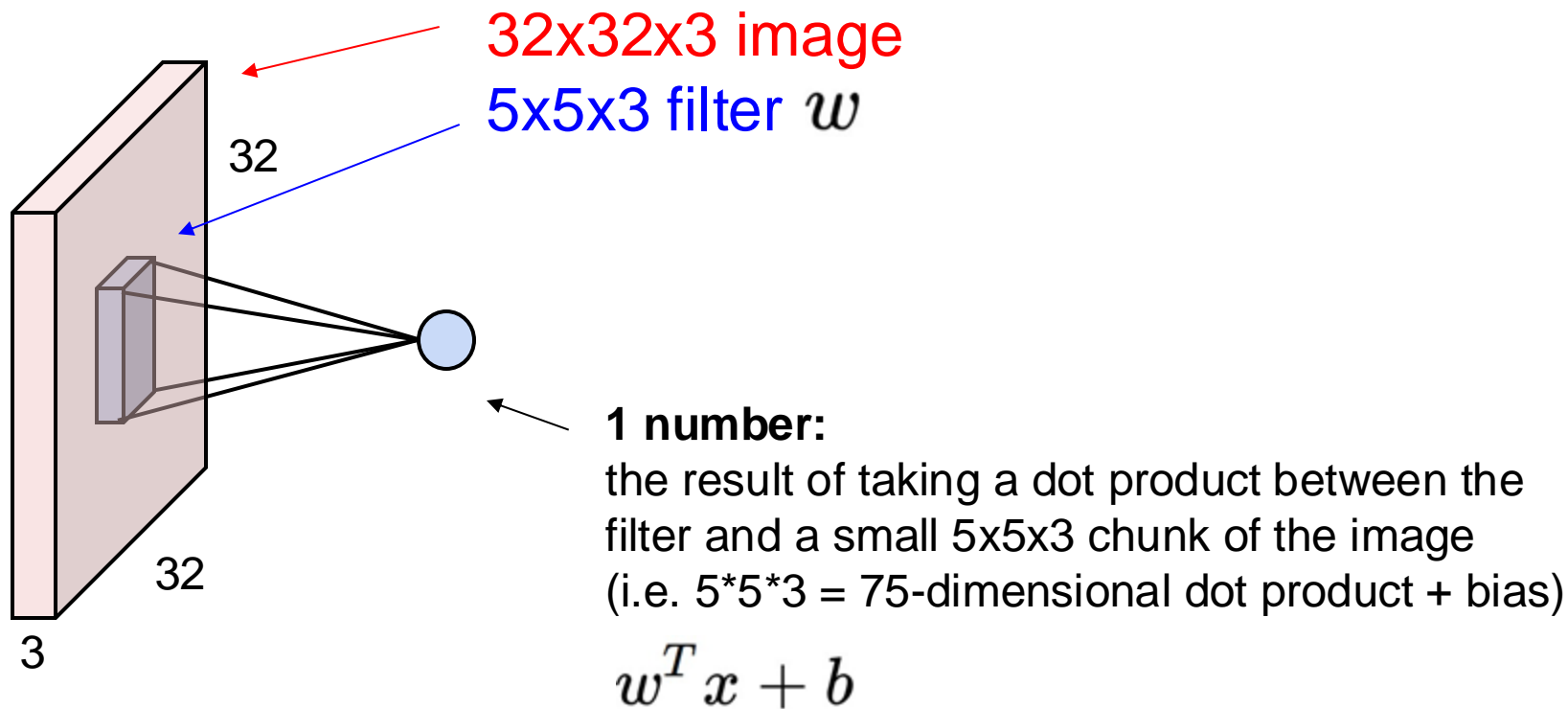
Filters always extend the full depth of the input volume

5x5x3 filter

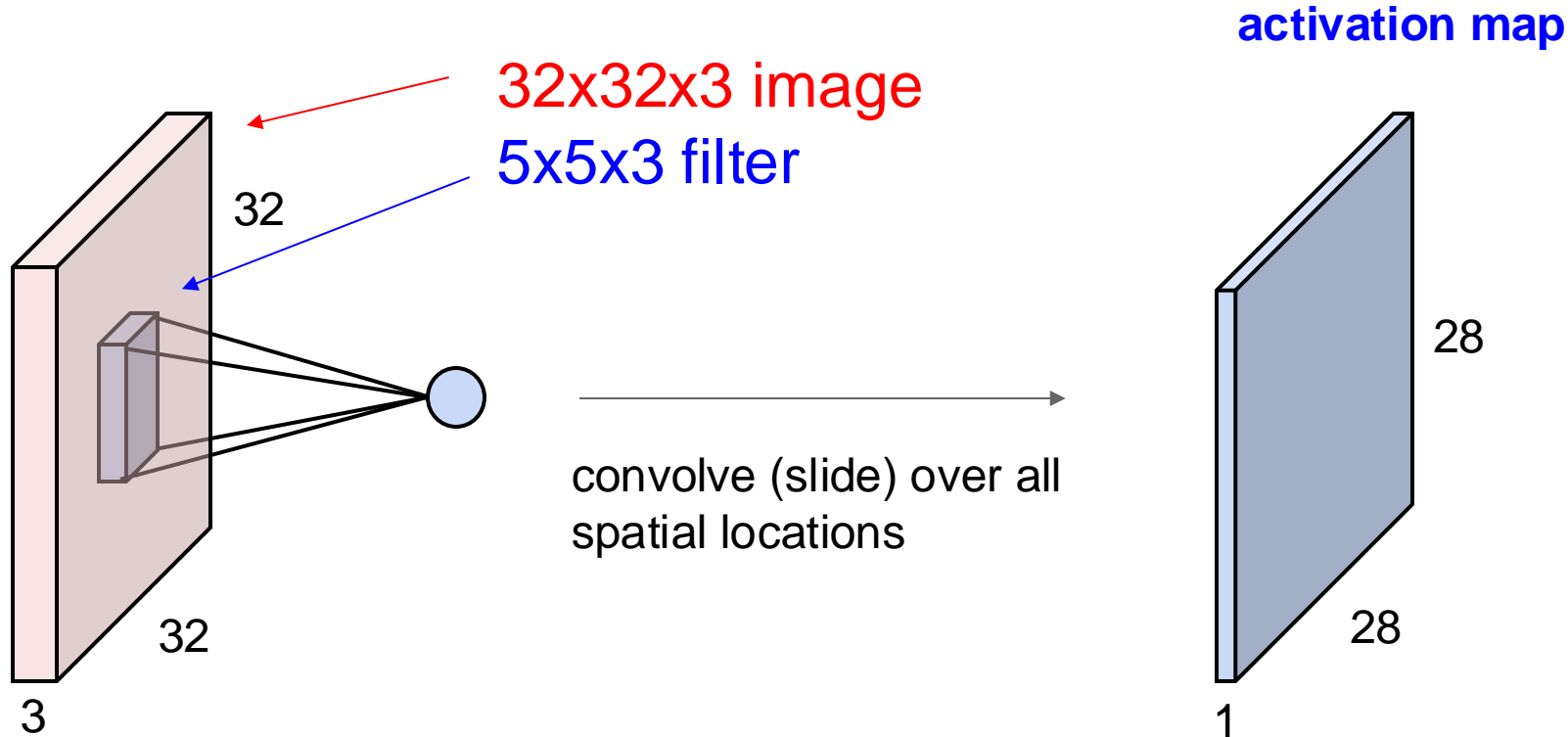


**Convolve** the filter with the image  
i.e. “slide over the image spatially,  
computing dot products”

# Convolution Layer

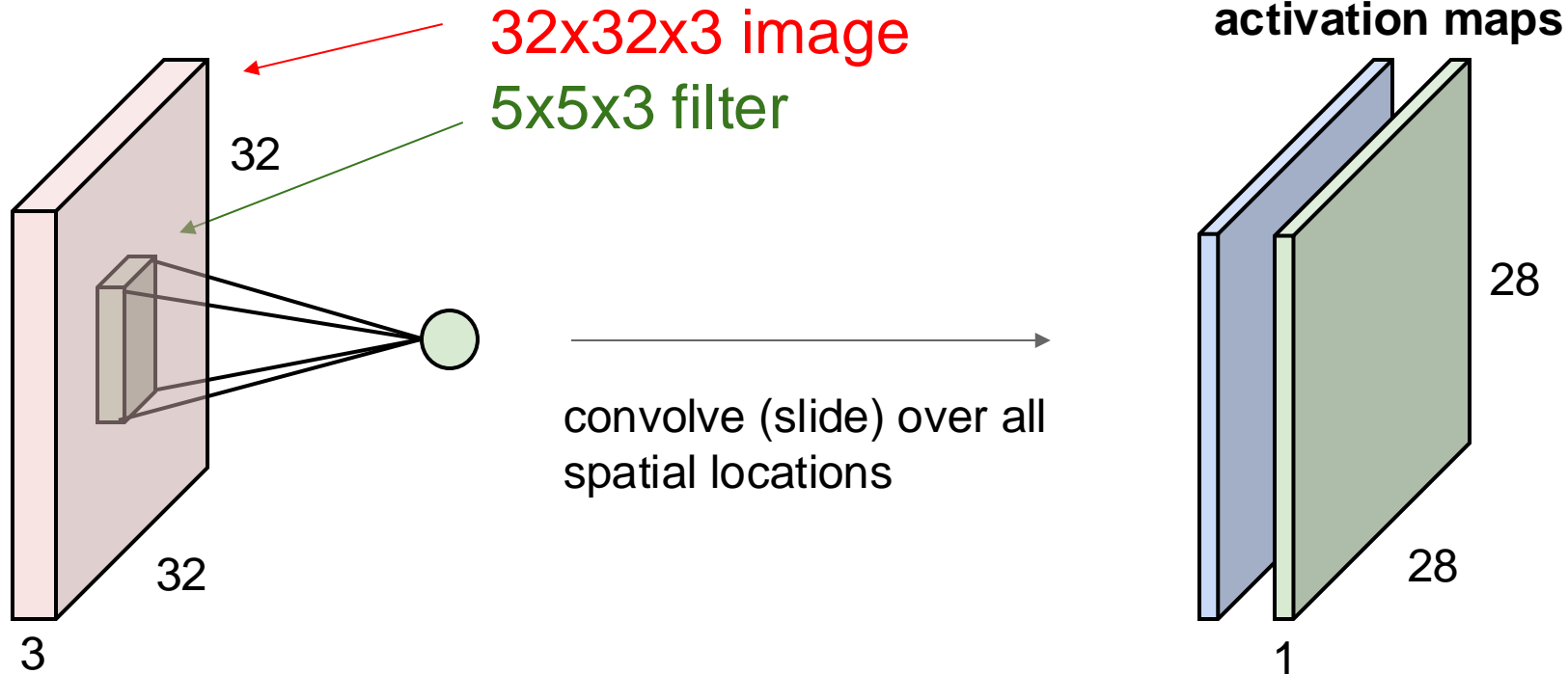


# Convolution Layer

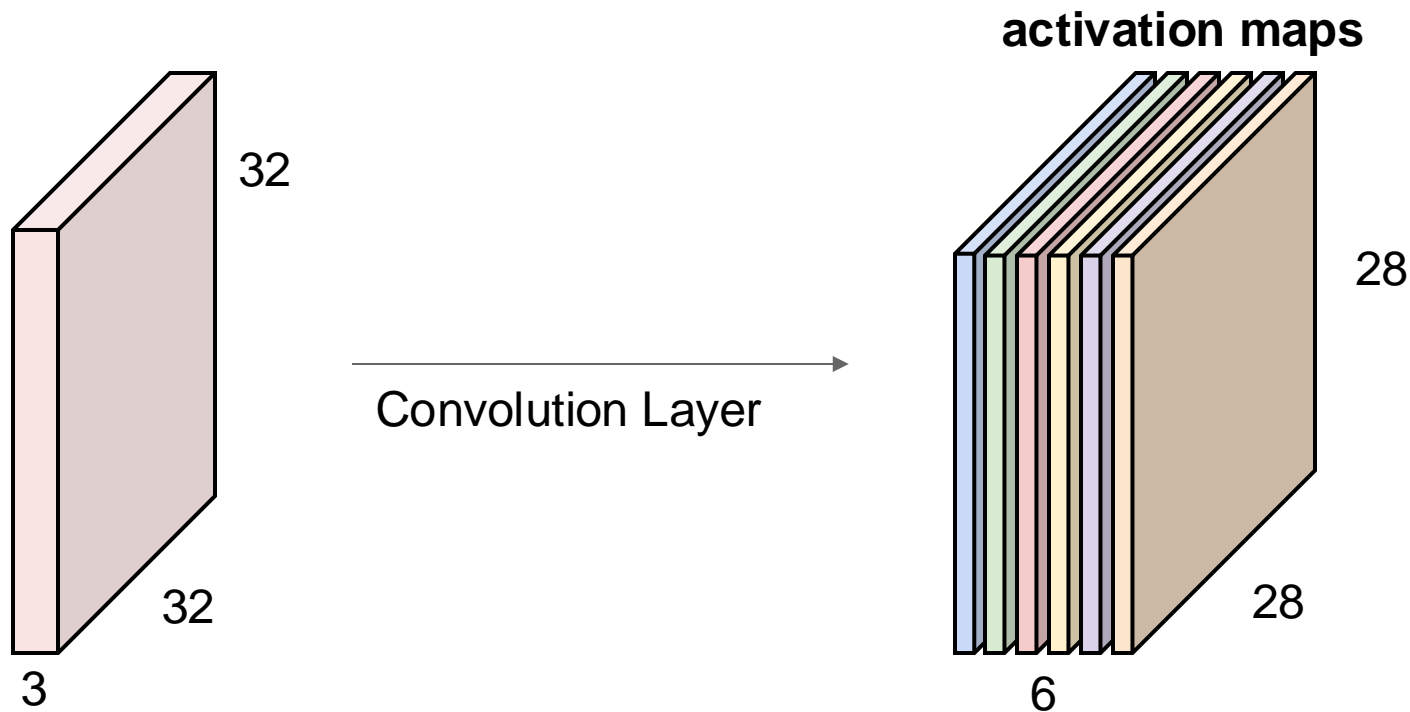


# Convolution Layer

consider a second, **green** filter

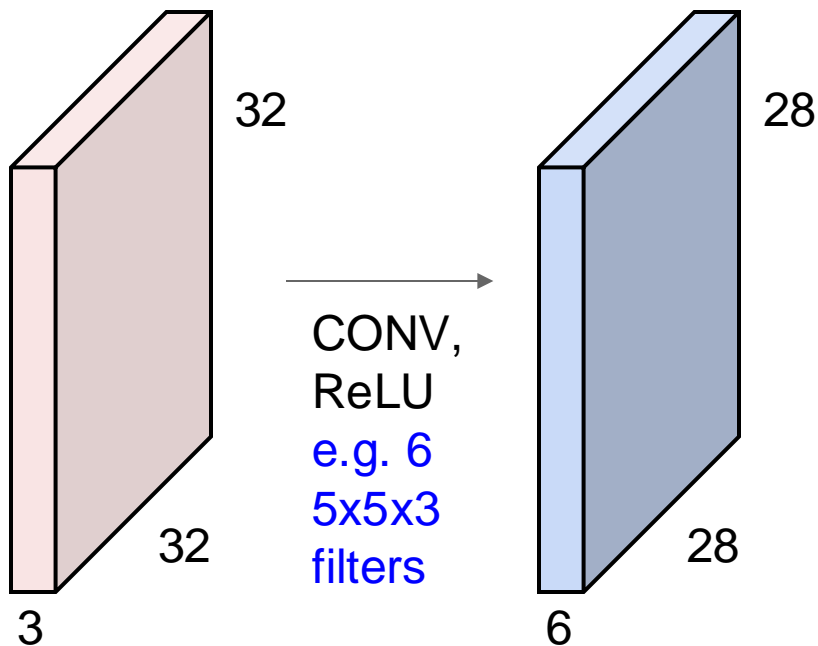


For example, if we had 6 5x5 filters, we'll get 6 separate activation maps:

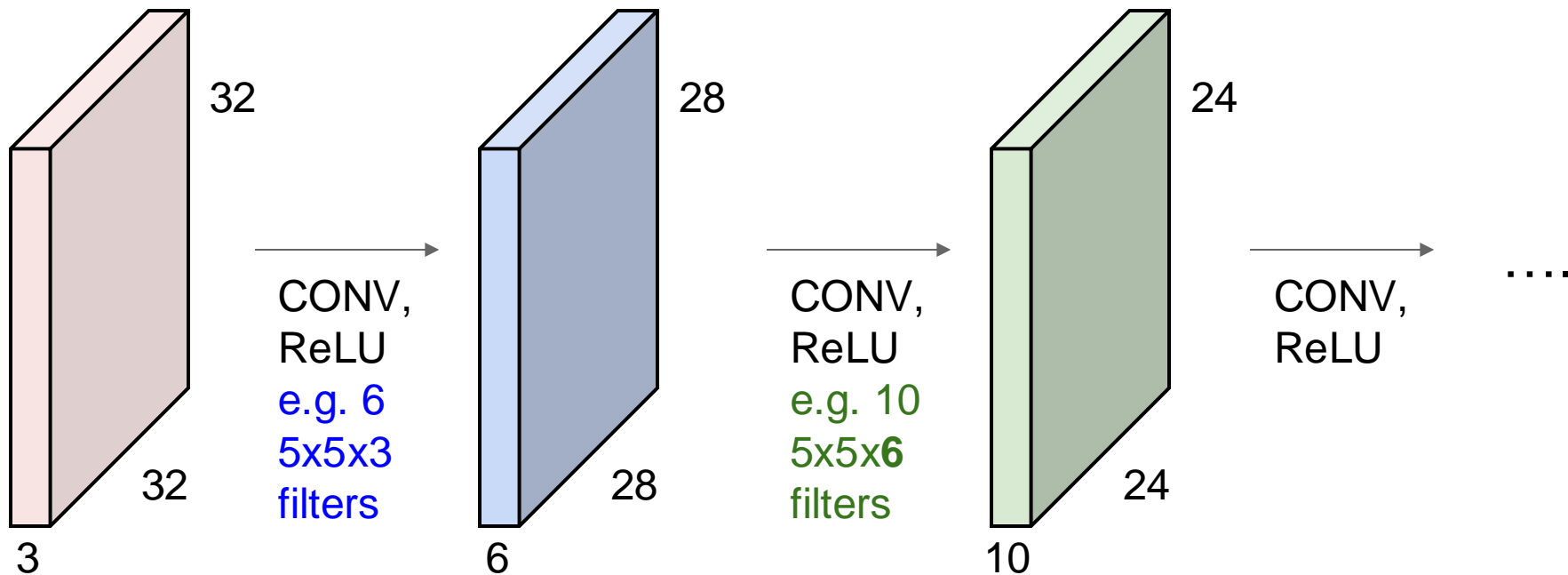


We stack these up to get a “new image” of size 28x28x6!

**Preview:** ConvNet is a sequence of Convolution Layers, interspersed with activation functions



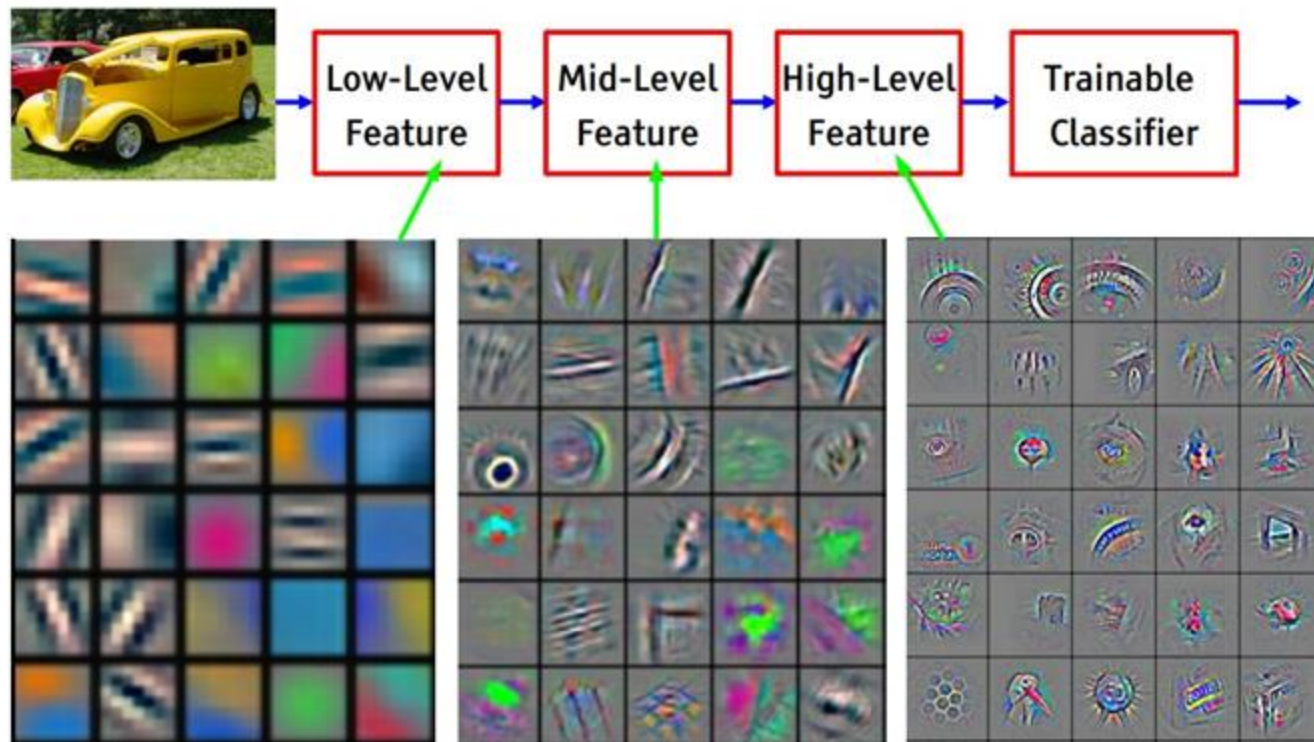
**Preview:** ConvNet is a sequence of Convolutional Layers, interspersed with activation functions





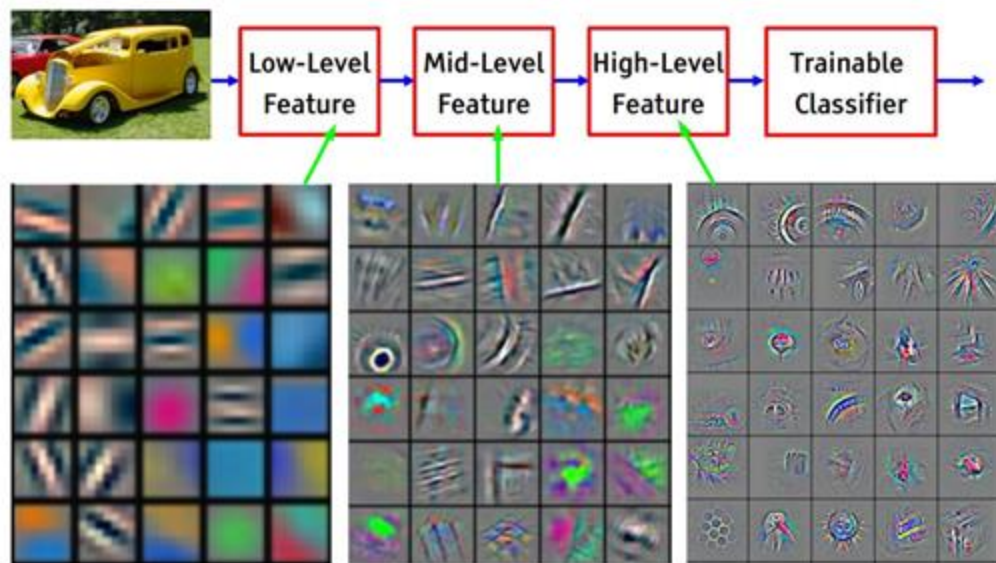
# Preview

[From recent Yann  
LeCun slides]



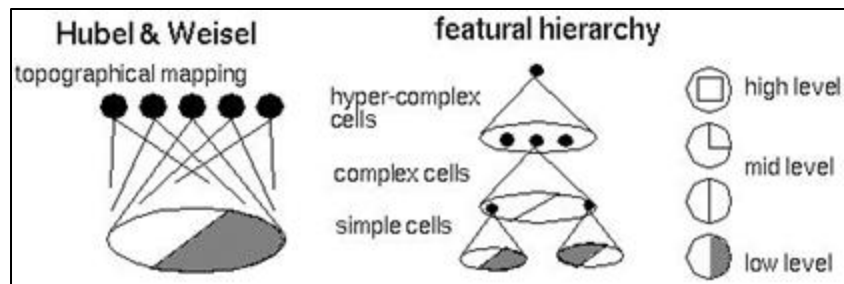
Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

# Preview



[From recent Yann LeCun slides]

Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]



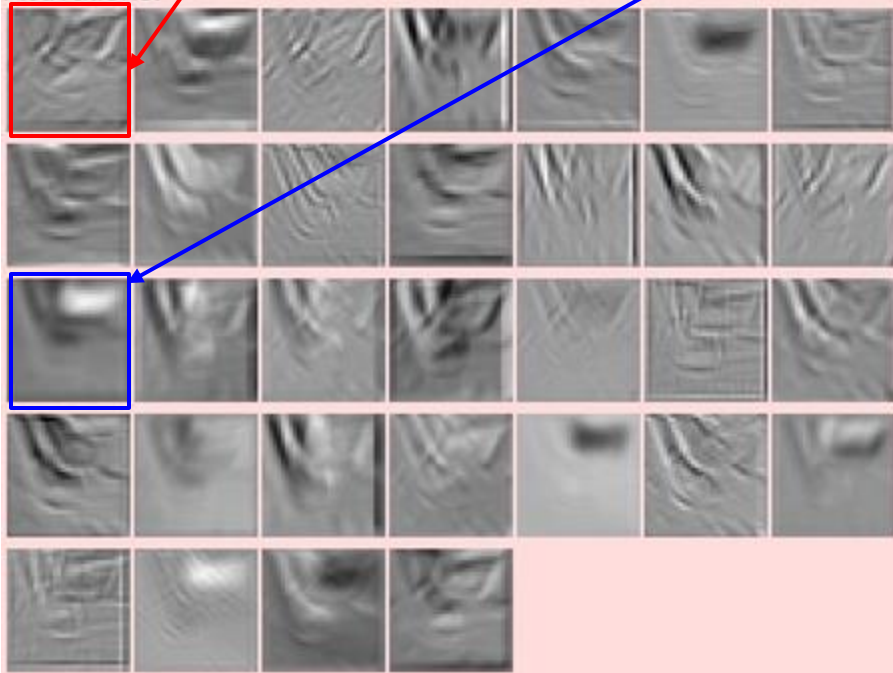


one filter =>  
one activation map



example 5x5 filters  
(32 total)

Activations:



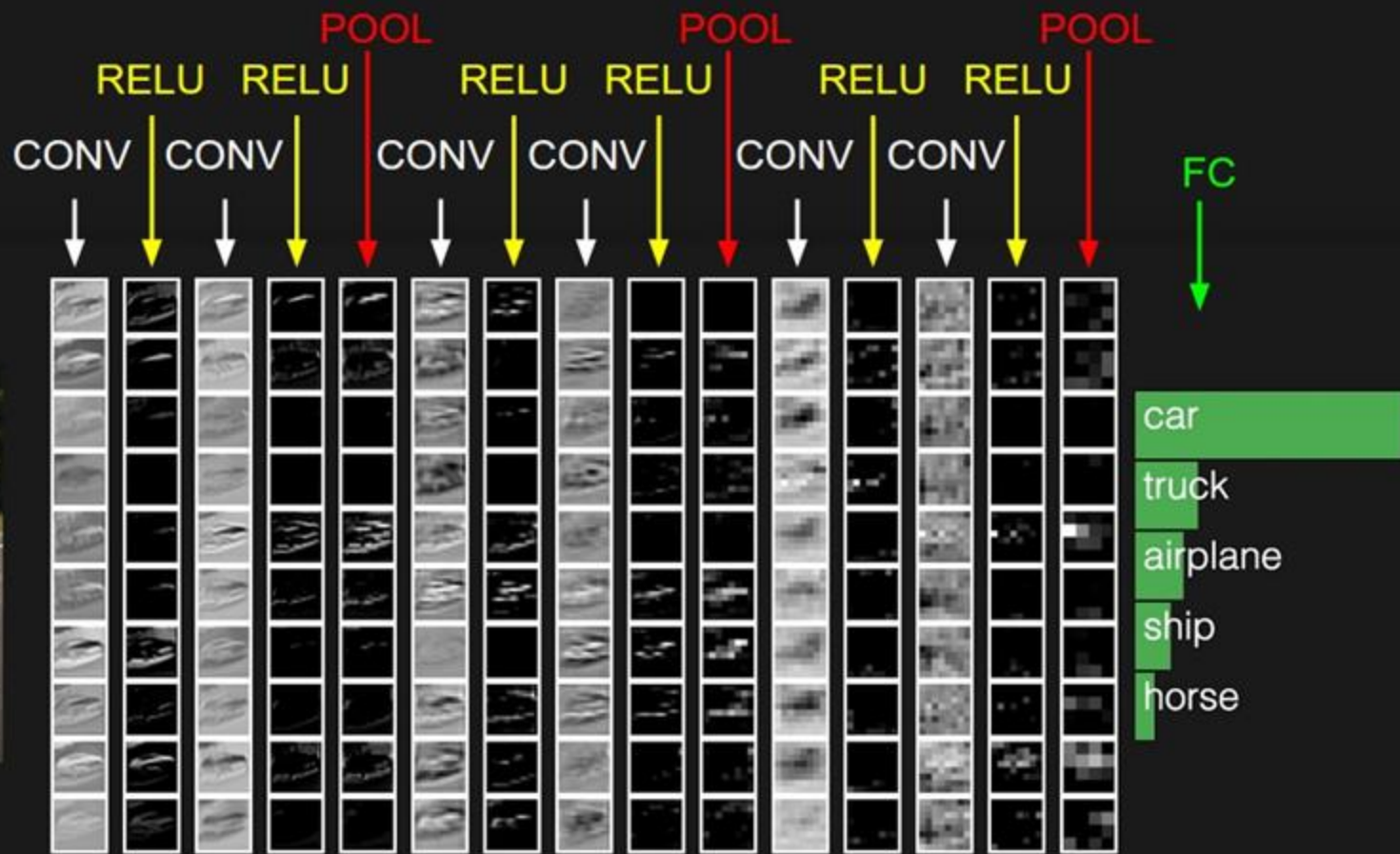
We call the layer convolutional  
because it is related to convolution  
of two signals:

$$f[x,y] * g[x,y] = \sum_{n_1=-\infty}^{\infty} \sum_{n_2=-\infty}^{\infty} f[n_1,n_2] \cdot g[x-n_1,y-n_2]$$

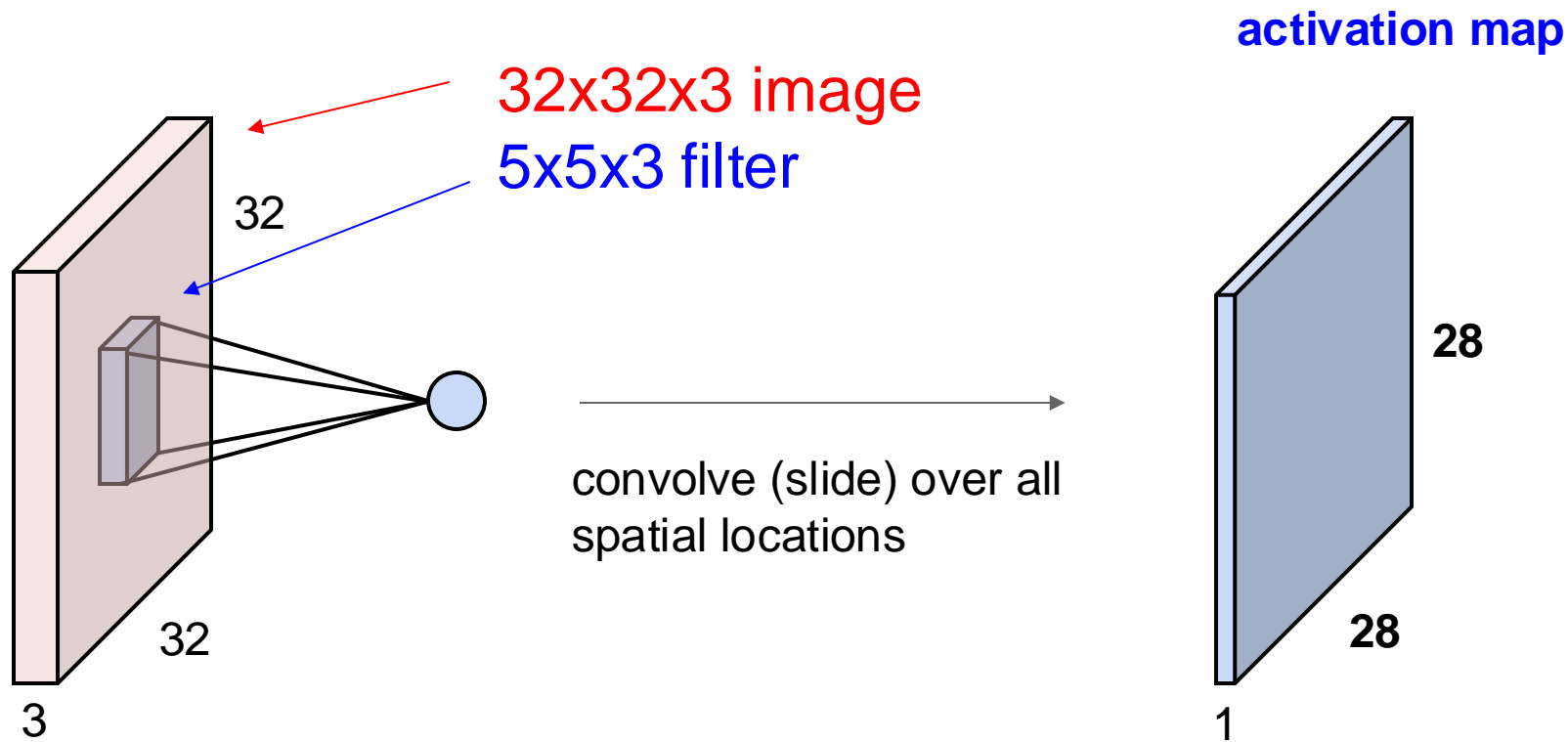


elementwise multiplication and sum of  
a filter and the signal (image)

preview:

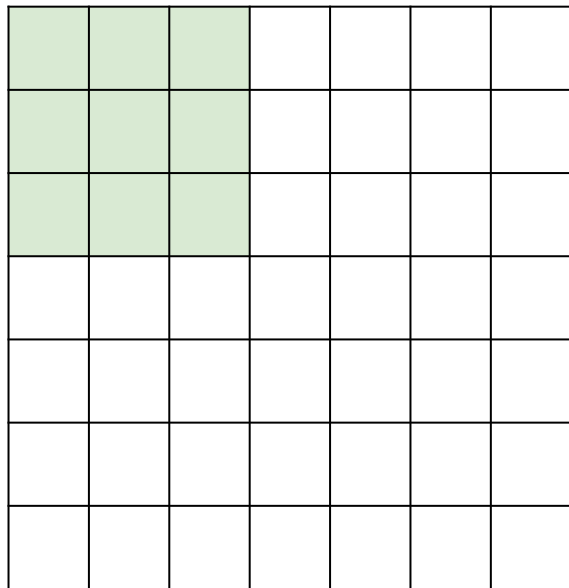


## A closer look at spatial dimensions:



## A closer look at spatial dimensions:

7

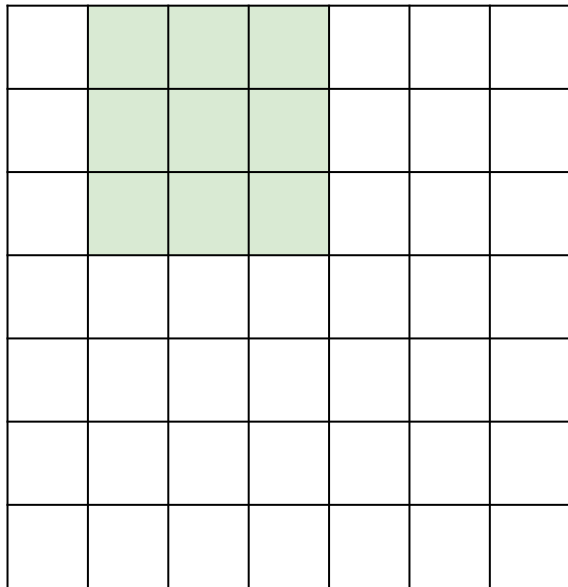


7

7x7 input (spatially)  
assume 3x3 filter

## A closer look at spatial dimensions:

7



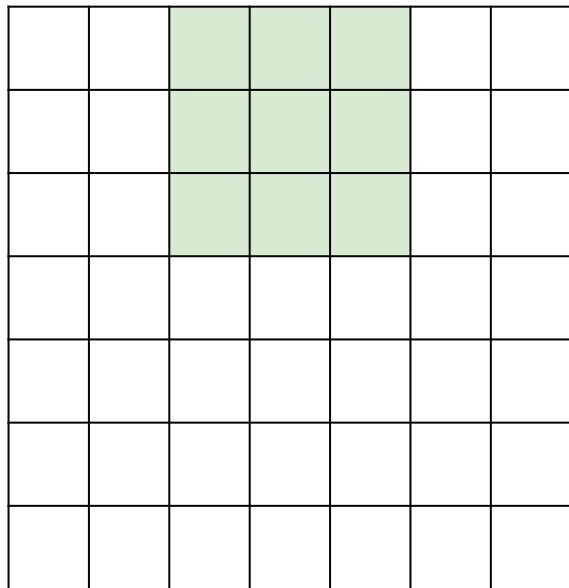
7

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assume 3x3 filter



## A closer look at spatial dimensions:

7

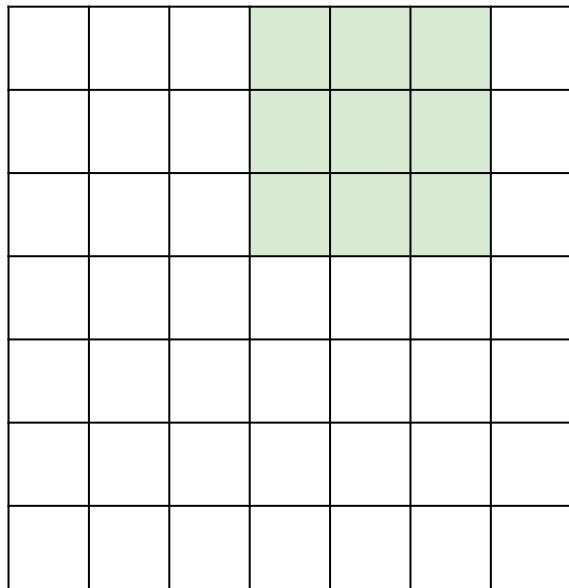


7x7 input (spatially)  
assume 3x3 filter

7

## A closer look at spatial dimensions:

7



7

7x7 input (spatially)  
assume 3x3 filter

## A closer look at spatial dimensions:

7

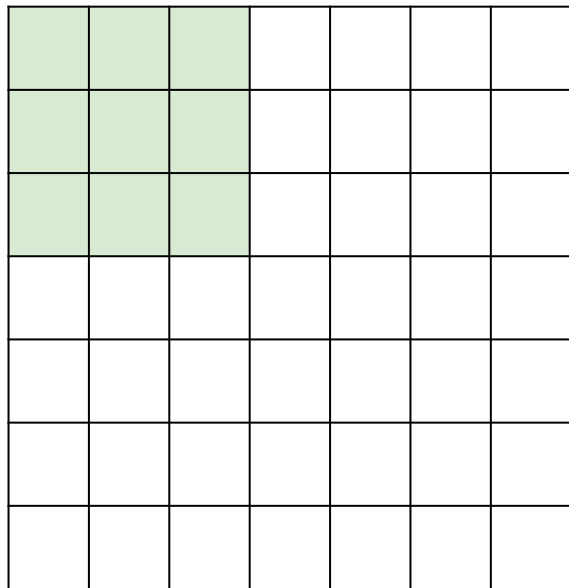

7

7x7 input (spatially)  
assume 3x3 filter

**=> 5x5 output**

A closer look at spatial dimensions:

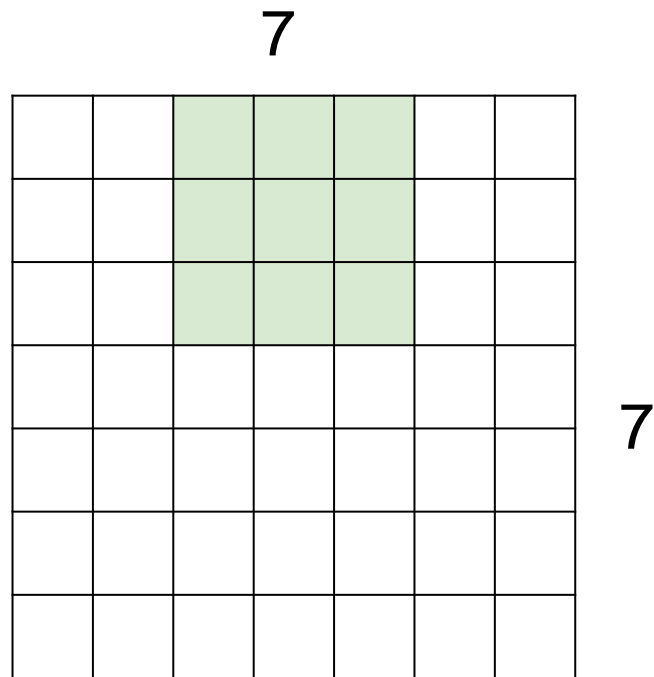
7



7

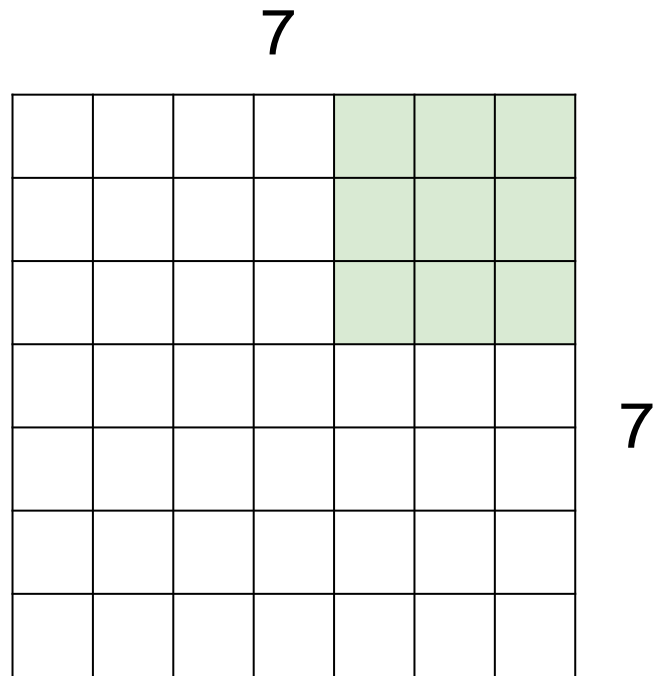
7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 2**

## A closer look at spatial dimensions:



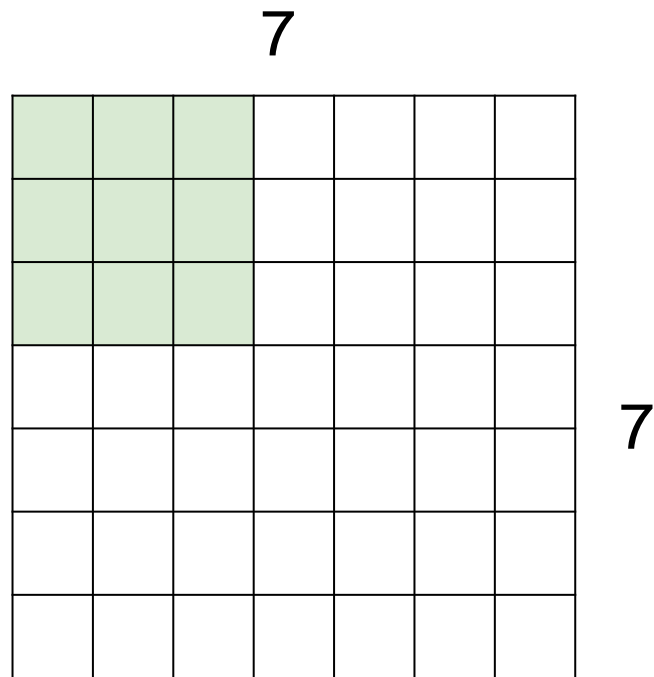
7x7 input (spatially)  
assume 3x3 filter  
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A closer look at spatial dimensions:



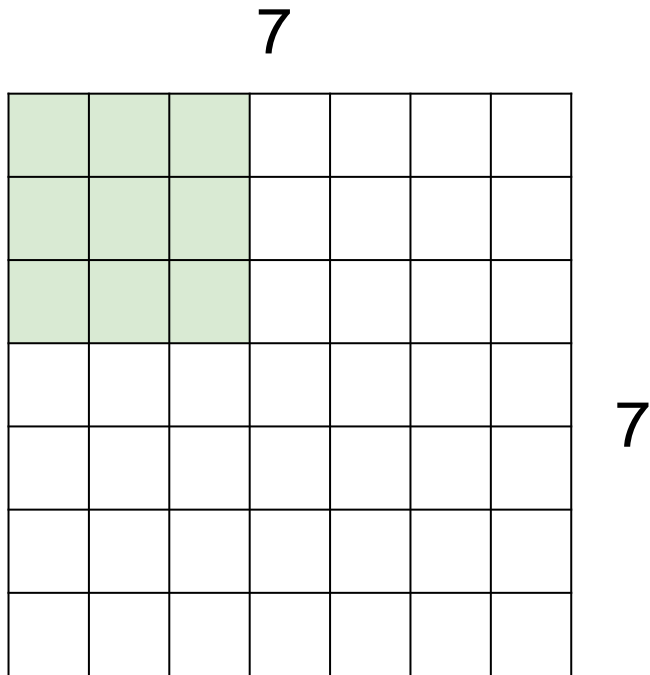
7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 2**  
**=> 3x3 output!**

A closer look at spatial dimensions:



7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 3?**

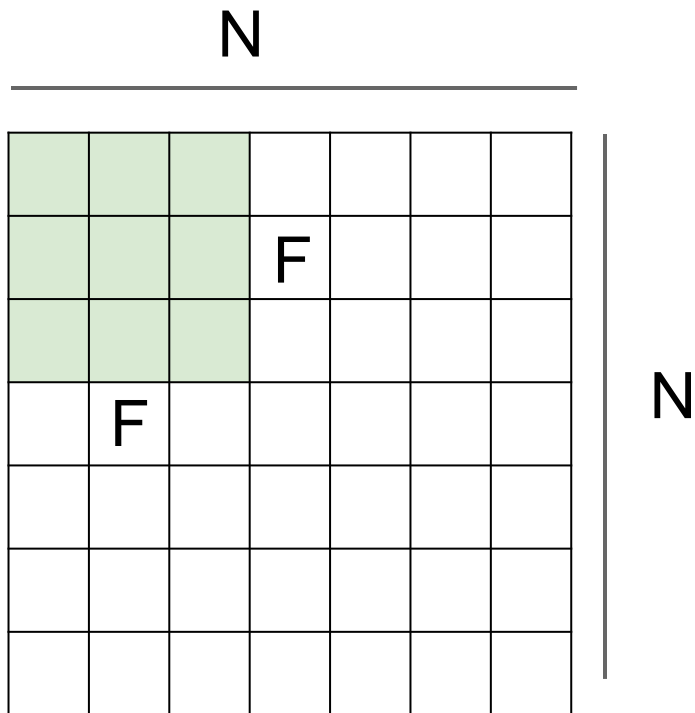
## A closer look at spatial dimensions:



7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 3?**

**doesn't fit!**  
cannot apply 3x3 filter on  
7x7 input with stride 3.





Output size:  
 **$(N - F) / \text{stride} + 1$**

e.g.  $N = 7, F = 3$ :

stride 1  $\Rightarrow (7 - 3)/1 + 1 = 5$

stride 2  $\Rightarrow (7 - 3)/2 + 1 = 3$

stride 3  $\Rightarrow (7 - 3)/3 + 1 = 2.33 \therefore \backslash$

# In practice: Common to zero pad the border

0	0	0	0	0	0			
0								
0								
0								
0								

e.g. input 7x7

**3x3** filter, applied with **stride 1**

**pad with 1 pixel** border => what is the output?

(recall:)

$$(N - F) / \text{stride} + 1$$

# In practice: Common to zero pad the border

0	0	0	0	0	0			
0								
0								
0								
0								

e.g. input 7x7

**3x3** filter, applied with **stride 1**

**pad with 1 pixel** border => what is the output?

**7x7 output!**

# In practice: Common to zero pad the border

0	0	0	0	0	0			
0								
0								
0								
0								

e.g. input 7x7

**3x3** filter, applied with **stride 1**

**pad with 1 pixel** border => what is the output?

**7x7 output!**

in general, common to see CONV layers with stride 1, filters of size  $F \times F$ , and zero-padding with  $(F-1)/2$ . (will preserve size spatially)

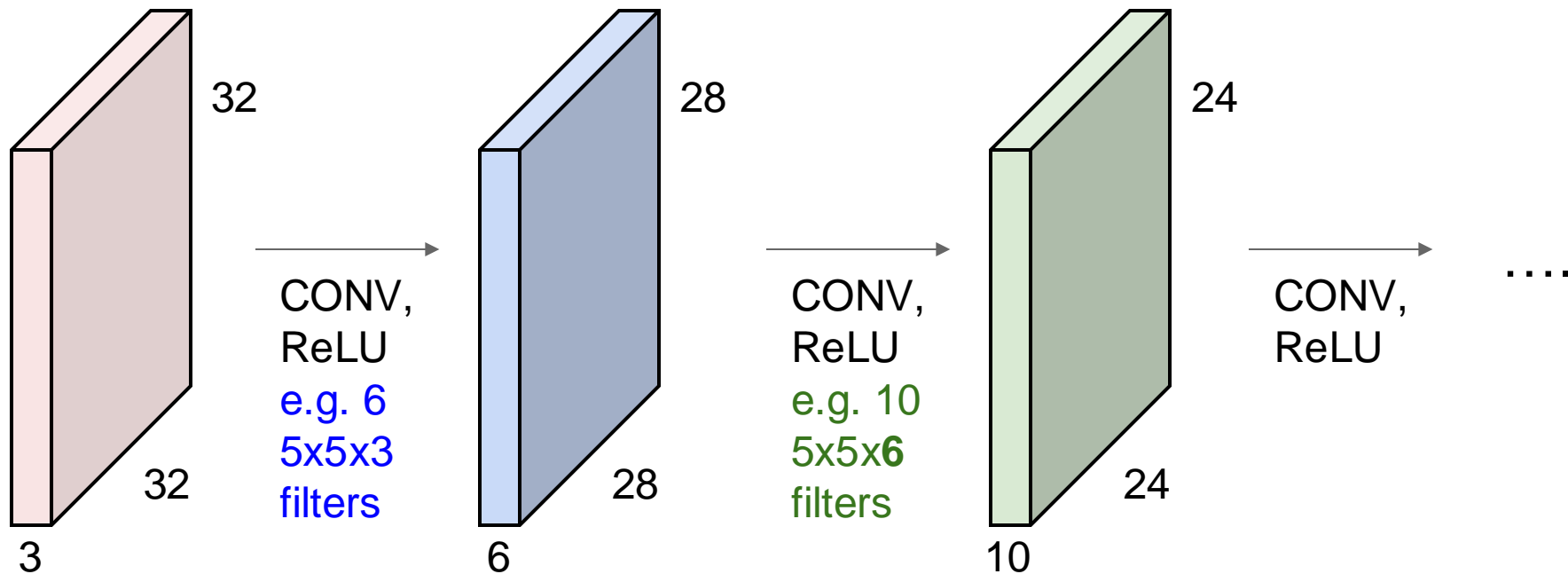
e.g.  $F = 3 \Rightarrow$  zero pad with 1

$F = 5 \Rightarrow$  zero pad with 2

$F = 7 \Rightarrow$  zero pad with 3

## Remember back to...

E.g. 32x32 input convolved repeatedly with 5x5 filters shrinks volumes spatially! (32 -> 28 -> 24 ...). Shrinking too fast is not good, doesn't work well.

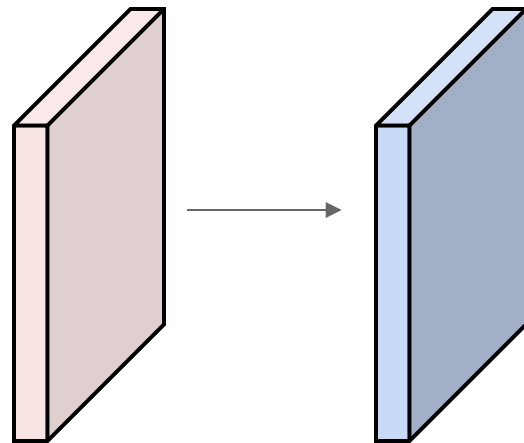


Examples time:

Input volume: **32x32x3**

10 5x5 filters with stride 1, pad 2

Output volume size: ?



Examples time:

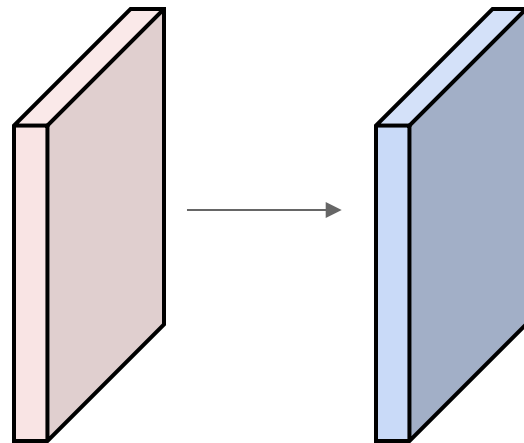
Input volume: **32x32x3**

**10** **5x5** filters with stride **1**, pad **2**

Output volume size:

$(32+2*2-5)/1+1 = 32$  spatially, so

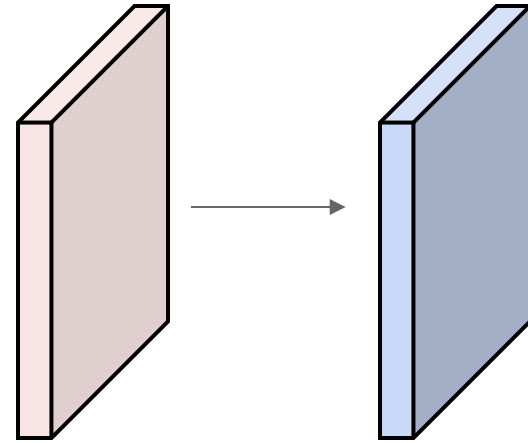
**32x32x10**



Examples time:

Input volume: **32x32x3**

10 5x5 filters with stride 1, pad 2



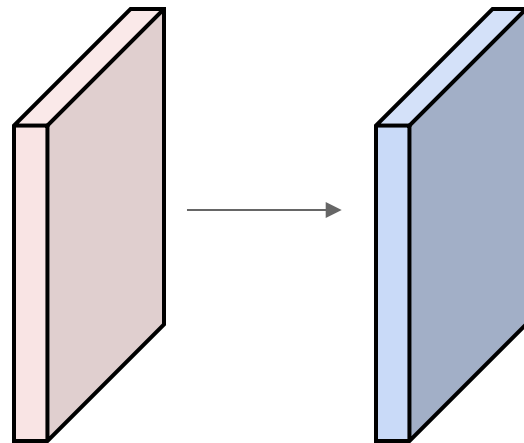
Number of parameters in this layer?



Examples time:

Input volume: **32x32x3**

**10** **5x5** filters with stride 1, pad 2



Number of parameters in this layer?

each filter has  $5*5*3 + 1 = 76$  params (+1 for bias)

=>  $76*10 = 760$

**Summary.** To summarize, the Conv Layer:

- Accepts a volume of size  $W_1 \times H_1 \times D_1$
- Requires four hyperparameters:
  - Number of filters  $K$ ,
  - their spatial extent  $F$ ,
  - the stride  $S$ ,
  - the amount of zero padding  $P$ .
- Produces a volume of size  $W_2 \times H_2 \times D_2$  where:
  - $W_2 = (W_1 - F + 2P)/S + 1$
  - $H_2 = (H_1 - F + 2P)/S + 1$  (i.e. width and height are computed equally by symmetry)
  - $D_2 = K$
- With parameter sharing, it introduces  $F \cdot F \cdot D_1$  weights per filter, for a total of  $(F \cdot F \cdot D_1) \cdot K$  weights and  $K$  biases.
- In the output volume, the  $d$ -th depth slice (of size  $W_2 \times H_2$ ) is the result of performing a valid convolution of the  $d$ -th filter over the input volume with a stride of  $S$ , and then offset by  $d$ -th bias.

## Common settings:

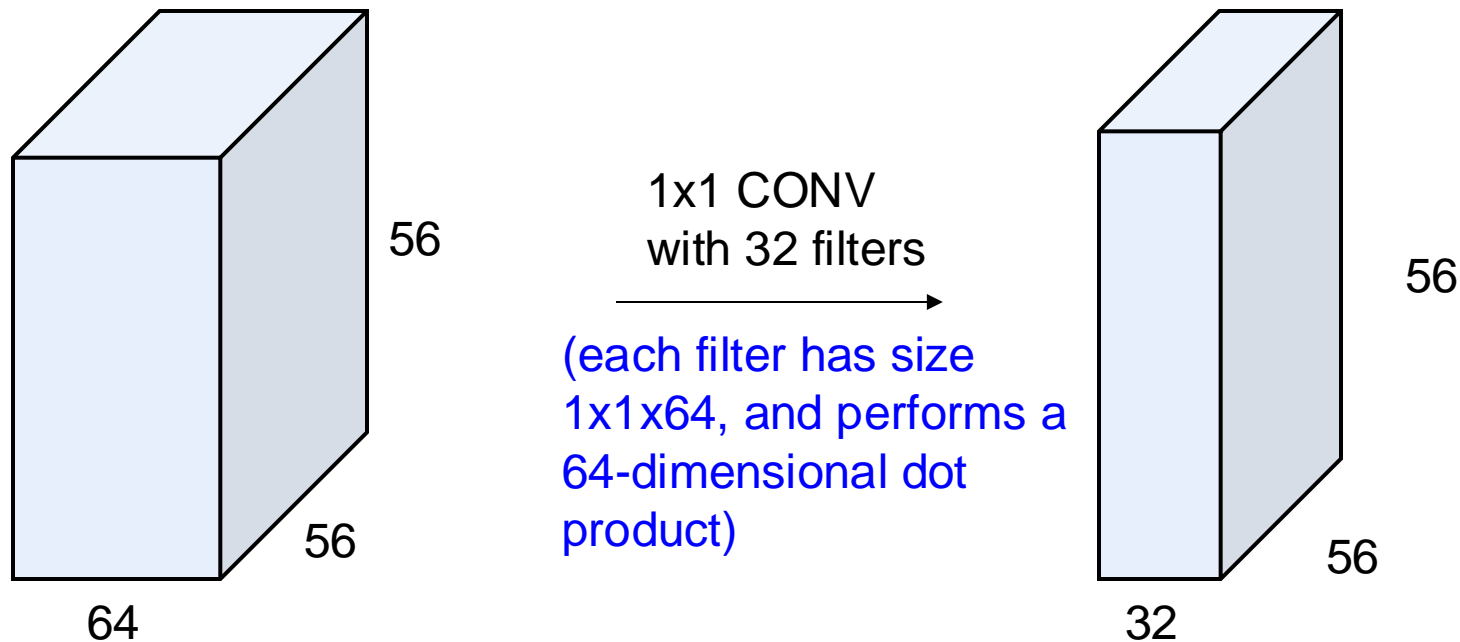
**Summary.** To summarize, the Conv Layer:

- Accepts a volume of size  $W_1 \times H_1 \times D_1$
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$K = (\text{powers of 2, e.g. 32, 64, 128, 512})$

- $F = 3, S = 1, P = 1$
- $F = 5, S = 1, P = 2$
- $F = 5, S = 2, P = ?$  (whatever fits)
- $F = 1, S = 1, P = 0$

(btw, 1x1 convolution layers make perfect sense)



# Example:

## nn.Conv2d in PyTorch

```
class torch.nn.Conv2d(in_channels, out_channels, kernel_size, stride=1, padding=0, dilation=1, groups=1, bias=True) [source]
```

Applies a 2D convolution over an input signal composed of several input planes.

In the simplest case, the output value of the layer with input size  $(N, C_{in}, H, W)$  and output  $(N, C_{out}, H_{out}, W_{out})$  can be precisely described as:

$$out(N_i, C_{out_j}) = bias(C_{out_j}) + \sum_{k=0}^{C_{in}-1} weight(C_{out_j}, k) \star input(N_i, k)$$

where  $\star$  is the valid 2D **cross-correlation** operator

**Summary.** To summarize, the Conv Layer:

- Accepts a volume of size  $W_1 \times H_1 \times D_1$
- Requires four hyperparameters:
  - Number of filters  $K$ ,
  - their spatial extent  $F$ ,
  - the stride  $S$ ,
  - the amount of zero padding  $P$ .

Parameters:

- **in\_channels** (*int*) – Number of channels in the input image
- **out\_channels** (*int*) – Number of channels produced by the convolution
- **kernel\_size** (*int or tuple*) – Size of the convolving kernel
- **stride** (*int or tuple, optional*) – Stride of the convolution. Default: 1
- **padding** (*int or tuple, optional*) – Zero-padding added to both sides of the input. Default: 0
- **dilation** (*int or tuple, optional*) – Spacing between kernel elements. Default: 1
- **groups** (*int, optional*) – Number of blocked connections from input channels to output channels. Default: 1
- **bias** (*bool, optional*) – If True, adds a learnable bias to the output. Default: True

Shape:

- Input:  $(N, C_{in}, H_{in}, W_{in})$
- Output:  $(N, C_{out}, H_{out}, W_{out})$  where
$$H_{out} = \text{floor}((H_{in} + 2 * padding[0] - dilation[0] * (kernel\_size[0] - 1) - 1) / stride[0] + 1)$$
$$W_{out} = \text{floor}((W_{in} + 2 * padding[1] - dilation[1] * (kernel\_size[1] - 1) - 1) / stride[1] + 1)$$

Variables:

- **weight** (*Tensor*) – the learnable weights of the module of shape  $(out\_channels, in\_channels, kernel\_size[0], kernel\_size[1])$
- **bias** (*Tensor*) – the learnable bias of the module of shape  $(out\_channels)$

Examples:

```
>>> # With square kernels and equal stride
>>> m = nn.Conv2d(16, 33, 3, stride=2)
>>> # non-square kernels and unequal stride and with padding
>>> m = nn.Conv2d(16, 33, (3, 5), stride=(2, 1), padding=(4, 2))
>>> # non-square kernels and unequal stride and with padding and dilation
>>> m = nn.Conv2d(16, 33, (3, 5), stride=(2, 1), padding=(4, 2), dilation=(3, 1))
>>> input = autograd.Variable(torch.randn(20, 16, 50, 100))
>>> output = m(input)
```

# Example:

## vl\_nnconv in MatConvNet

### VL\_NNCONV - CNN convolution.

$Y = \text{VL\_NNCONV}(X, F, B)$  computes the convolution of the image  $X$  with the filter bank  $F$  and biases  $B$ . If  $B$  is the empty matrix, then no biases are added. If  $F$  is the empty matrix, then the function does not filter the image, but still adds the biases and applies downsampling and padding as explained below.

$X$  is an array of dimension  $H \times W \times C \times N$  where  $(H, W)$  are the height and width of the image stack,  $C$  is the number of feature channels, and  $N$  is the number of images in the batch.

$F$  is an array of dimension  $FW \times FH \times FC \times K$  where  $(FH, FW)$  are the filter height and width and  $K$  the number of filters in the bank.  $FC$  is the number of feature channels in each filter and must match the number of feature channels  $C$  in  $X$ . Alternatively,  $FC$  can

- divide\* the  $C$ ; in this case, filters are assumed to form  $G=C/FC$
- groups\* of equal size (where  $G$  must divide  $K$ ). Each group of

filters works on a consecutive subset of feature channels of the input array  $X$ .

$[DX, DF, DB] = \text{VL\_NNCONV}(X, F, B, DY)$  computes the derivatives of the operator projected onto  $P$ .  $DX$ ,  $DF$ ,  $DB$ , and  $DY$  have the same dimensions as  $X$ ,  $F$ ,  $B$ , and  $Y$ , respectively. In particular, if  $B$  is the empty matrix, then  $DB$  is also empty.

$\text{VL\_NNCONV}()$  implements a special *fully-connected* mode: when the support of the filters matches exactly the support of the input image, the code uses an optimized path for faster computation.

$\text{VL\_NNCONV}(\dots, \text{'option'}, \text{value}, \dots)$  accepts the following options:

- **Stride** [1]

Set the output stride or downsampling factor. If the value is a scalar, then the same stride is applied to both vertical and horizontal directions; otherwise, passing [STRIDEY STRIDEX] allows specifying different downsampling factors for each direction.

- **Pad** [0]

Set the amount of input padding. Input images are padded with zeros by this number of pixels before the convolution is computed. Passing [TOP BOTTOM LEFT RIGHT] allows specifying different padding amounts for the top, bottom, left, and right sides respectively. Passing a single scalar applies the same padding to all borders.

- **Dilate** [1]

Set the kernel dilation factor. Passing [DILATEY DILATEX] allows specifying different dilation factors for  $Y$  and  $X$ . Filters are dilated by inserting  $\text{DILATE}-1$  zeros between filter elements. For example, the filter

**Summary.** To summarize, the Conv Layer:

- Accepts a volume of size  $W_1 \times H_1 \times D_1$
- Requires four hyperparameters:
  - Number of filters  $K$ ,
  - their spatial extent  $F$ ,
  - the stride  $S$ ,
  - the amount of zero padding  $P$ .

# Example:

## Convolution in Caffe

**Summary.** To summarize, the Conv Layer:

- Accepts a volume of size  $W_1 \times H_1 \times D_1$
- Requires four hyperparameters:
  - Number of filters  $K$ ,
  - their spatial extent  $F$ ,
  - the stride  $S$ ,
  - the amount of zero padding  $P$ .

```
layer {
  name: "conv1"
  type: "Convolution"
  bottom: "data"
  top: "conv1"
  # learning rate and decay multipliers for the filters
  param { lr_mult: 1 decay_mult: 1 }
  # learning rate and decay multipliers for the biases
  param { lr_mult: 2 decay_mult: 0 }
  convolution_param {
    num_output: 96      # learn 96 filters
    kernel_size: 11     # each filter is 11x11
    stride: 4           # step 4 pixels between each filter application
    weight_filler {
      type: "gaussian" # initialize the filters from a Gaussian
      std: 0.01        # distribution with stdev 0.01 (default mean: 0)
    }
    bias_filler {
      type: "constant" # initialize the biases to zero (0)
      value: 0
    }
  }
}
```



# Example:

## [tf.nn.conv2d](#) in TensorFlow

```
conv2d(  
    input,  
    filter,  
    strides,  
    padding,  
    use_cudnn_on_gpu=None,  
    data_format=None,  
    name=None  
)
```

**Summary.** To summarize, the Conv Layer:

- Accepts a volume of size  $W_1 \times H_1 \times D_1$
- Requires four hyperparameters:
  - Number of filters  $K$ ,
  - their spatial extent  $F$ ,
  - the stride  $S$ ,
  - the amount of zero padding  $P$ .

Args:

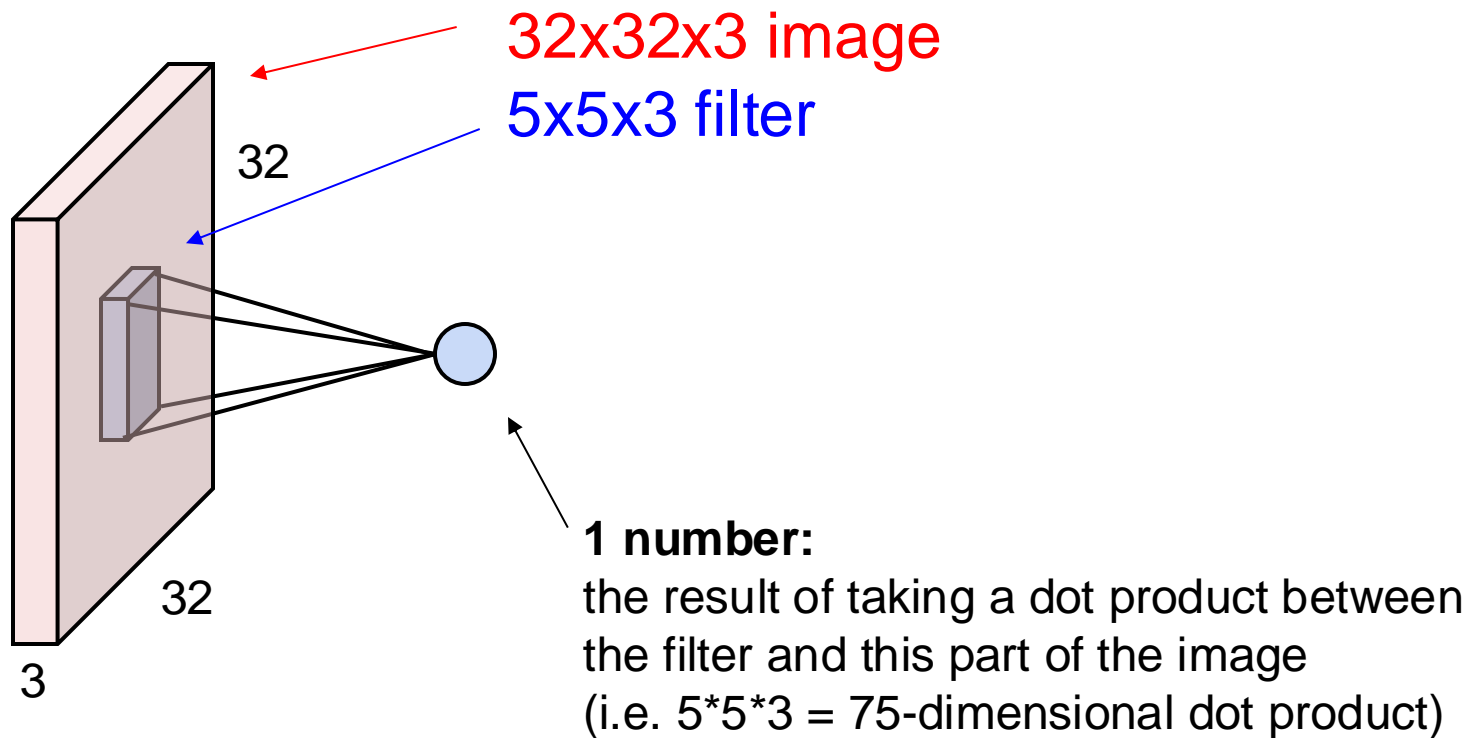
- **input**: A `Tensor`. Must be one of the following types: `half`, `float32`. A 4-D tensor. The dimension order is interpreted according to the value of `data_format`, see below for details.
- **filter**: A `Tensor`. Must have the same type as `input`. A 4-D tensor of shape `[filter_height, filter_width, in_channels, out_channels]`
- **strides**: A list of `ints`. 1-D tensor of length 4. The stride of the sliding window for each dimension of `input`. The dimension order is determined by the value of `data_format`, see below for details.
- **padding**: A `string` from: "SAME", "VALID". The type of padding algorithm to use.
- **use\_cudnn\_on\_gpu**: An optional `bool`. Defaults to `True`.
- **data\_format**: An optional `string` from: "NHWC", "NCHW". Defaults to "NHWC". Specify the data format of the input and output data. With the default format "NHWC", the data is stored in the order of: [batch, height, width, channels]. Alternatively, the format could be "NCHW", the data storage order of: [batch, channels, height, width].
- **name**: A name for the operation (optional).

Returns:

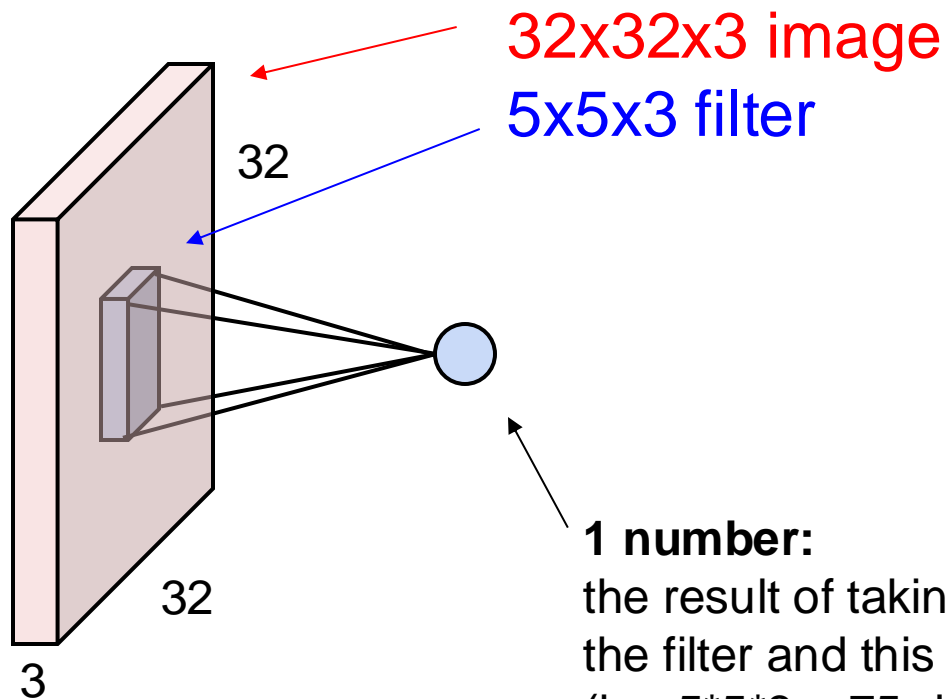
A `Tensor`. Has the same type as `input`. A 4-D tensor. The dimension order is determined by the value of `data_format`, see below for details.



# The brain/neuron view of CONV Layer



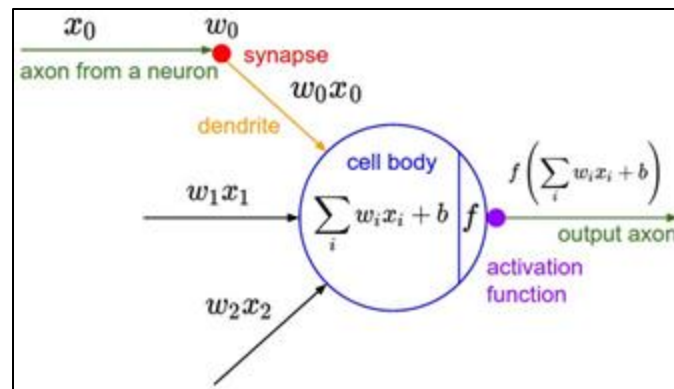
# The brain/neuron view of CONV Layer



32x32x3 image  
5x5x3 filter

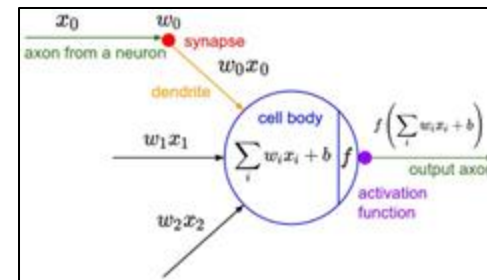
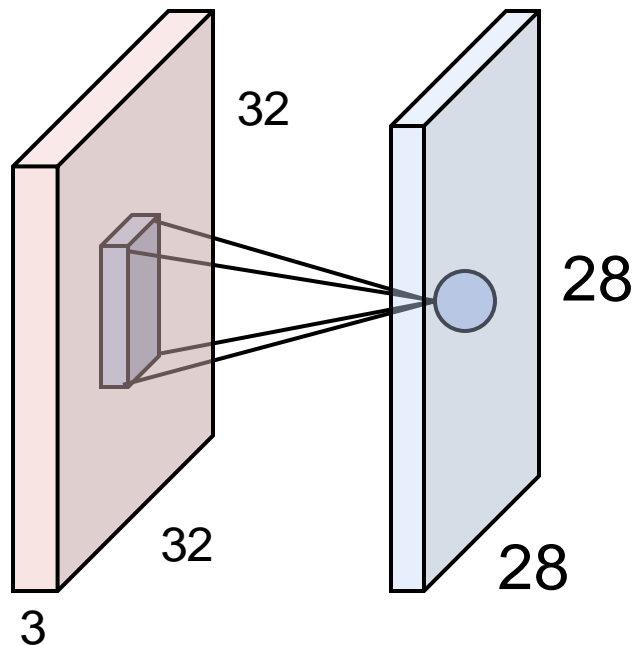
**1 number:**

the result of taking a dot product between  
the filter and this part of the image  
(i.e.  $5 \times 5 \times 3 = 75$ -dimensional dot product)



It's just a neuron with local connectivity...

# The brain/neuron view of CONV Layer



An activation map is a 28x28 sheet of neuron outputs:

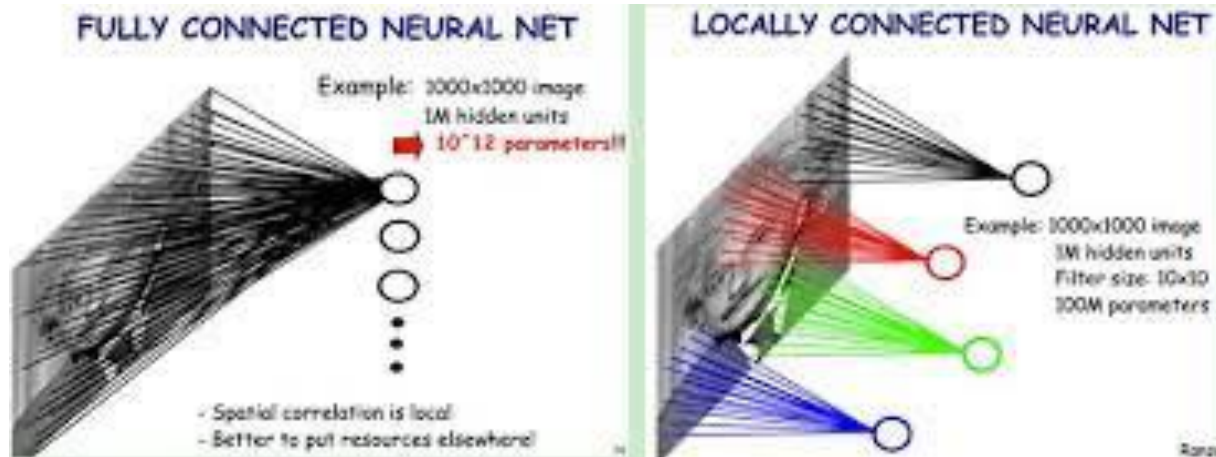
1. Each is connected to a small region in the input
  2. All of them share parameters
- A major advantage of CONV layer!

“5x5 filter” -> “5x5 receptive field for each neuron”

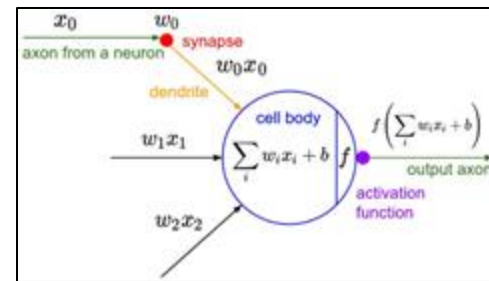
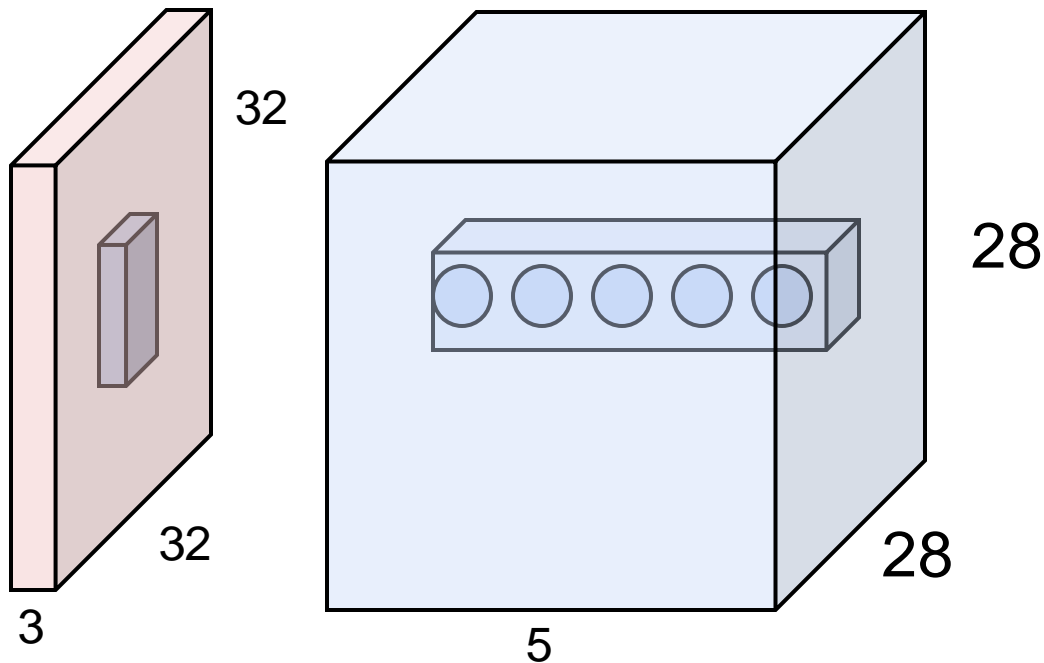
# How could we make a standard neural network have local connectivity?

- Instead of have a connection from every unit in a hidden layer to the whole image, what if we only had connections to things that were “nearby”?
- Have to define a notion of “nearness”.
- Give every unit coordinates in 3 dimensions (like layers in the brain).
- Now, introduce a penalty that makes the weights smaller when the connections are across a greater distance.
- This will naturally lead to local connectivity.
- Project idea!

# Fully versus locally connected units



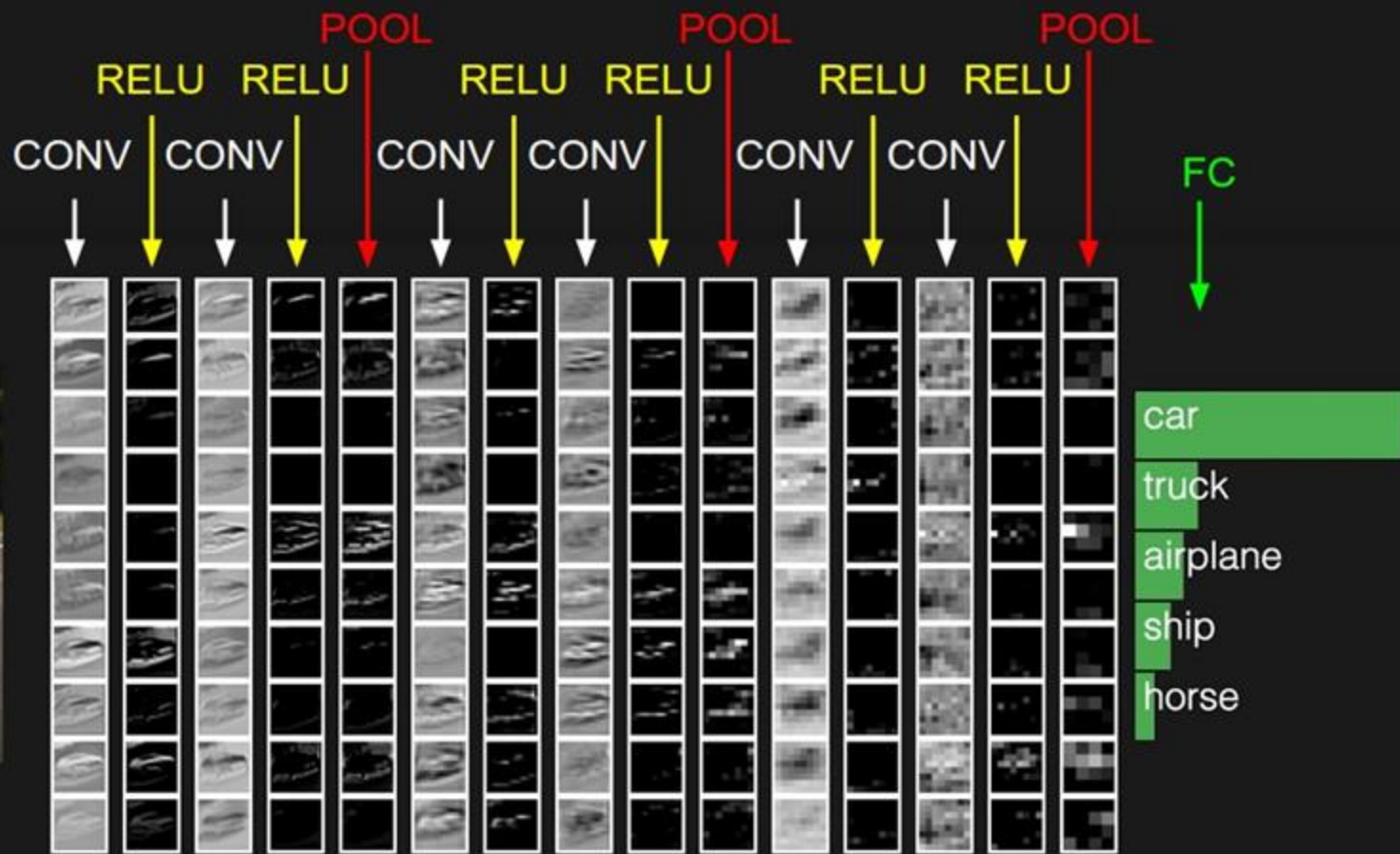
# The brain/neuron view of CONV Layer



E.g. with 5 filters,  
CONV layer consists of  
neurons arranged in a 3D grid  
(28x28x5)

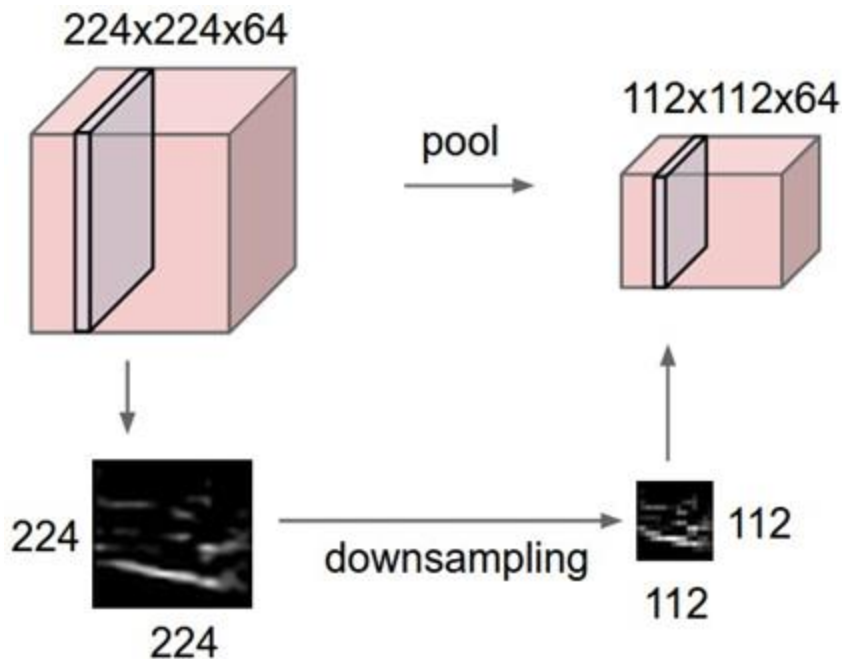
There will be 5 different  
neurons all looking at the same  
region in the input volume

two more layers to go: POOL/FC



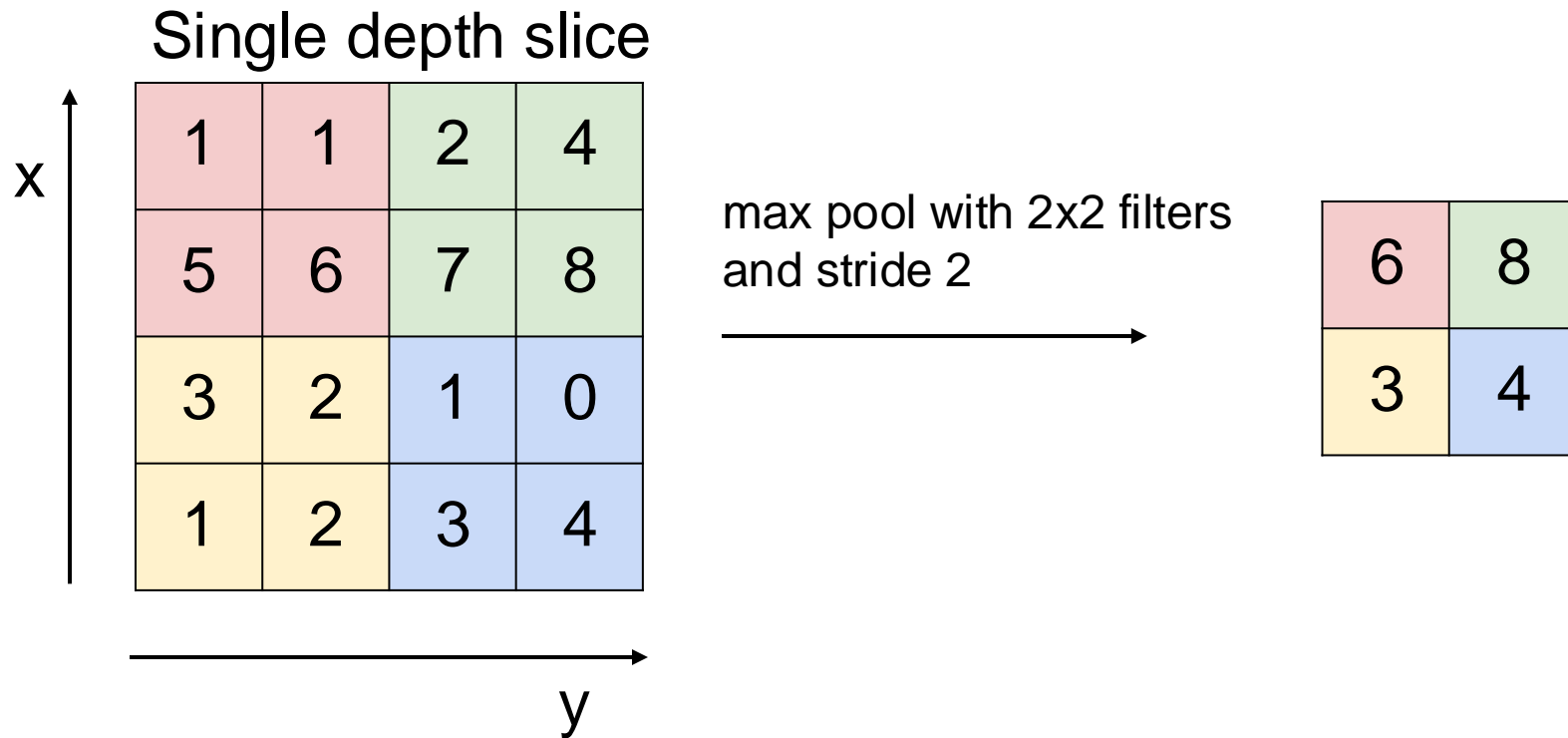
# Pooling layer

- makes the representations smaller and more manageable
- operates over each activation map independently:





# MAX POOLING



- Accepts a volume of size  $W_1 \times H_1 \times D_1$
- Requires three hyperparameters:
  - their spatial extent  $F$ ,
  - the stride  $S$ ,
- Produces a volume of size  $W_2 \times H_2 \times D_2$  where:
  - $W_2 = (W_1 - F)/S + 1$
  - $H_2 = (H_1 - F)/S + 1$
  - $D_2 = D_1$
- Introduces zero parameters since it computes a fixed function of the input
- Note that it is not common to use zero-padding for Pooling layers

## Common settings:

$$F = 2, S = 2$$

$$F = 3, S = 2$$

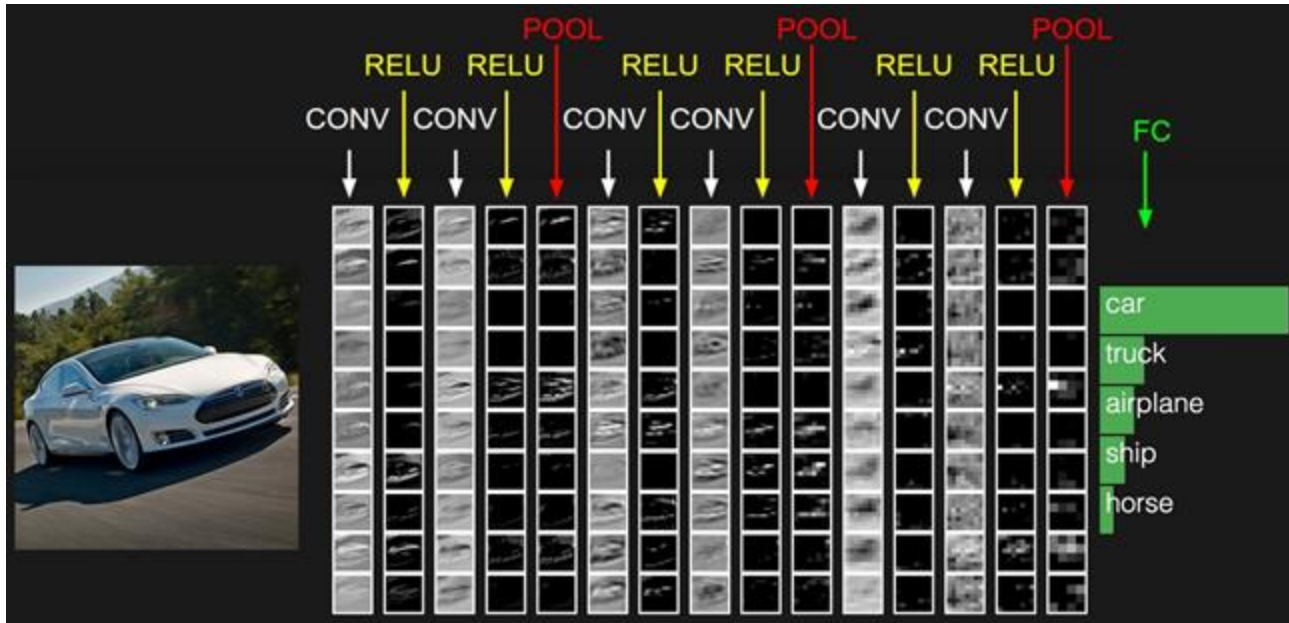
- Accepts a volume of size  $W_1 \times H_1 \times D_1$
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  - $D_2 = D_1$
- Introduces zero parameters since it computes a fixed function of the input
- Note that it is not common to use zero-padding for Pooling layers

# Why do we need pooling?

- Pool information by increasing **receptive field**
- Provide some spatial invariance

## Fully Connected Layer (FC layer)

- Contains neurons that connect to the entire input volume, as in ordinary Neural Networks

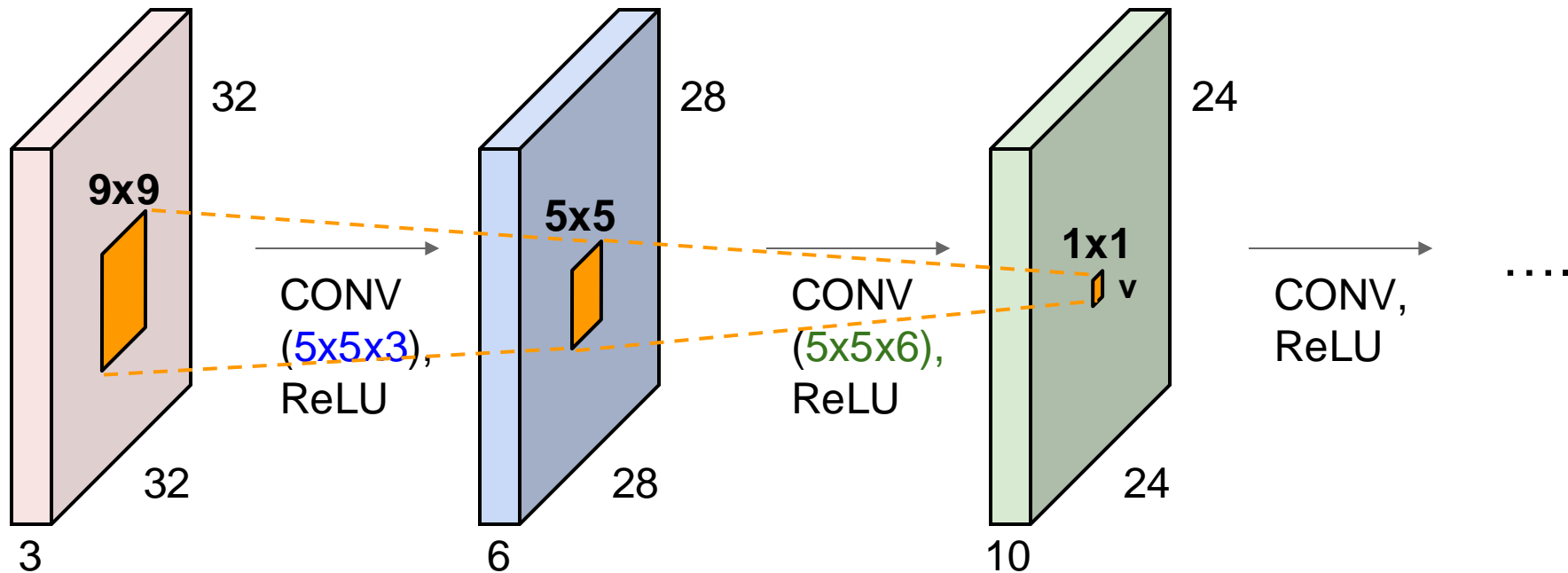


## [ConvNetJS demo: training on CIFAR-10]

<http://cs.stanford.edu/people/karpathy/convnetjs/demo/cifar10.html>

## Receptive field

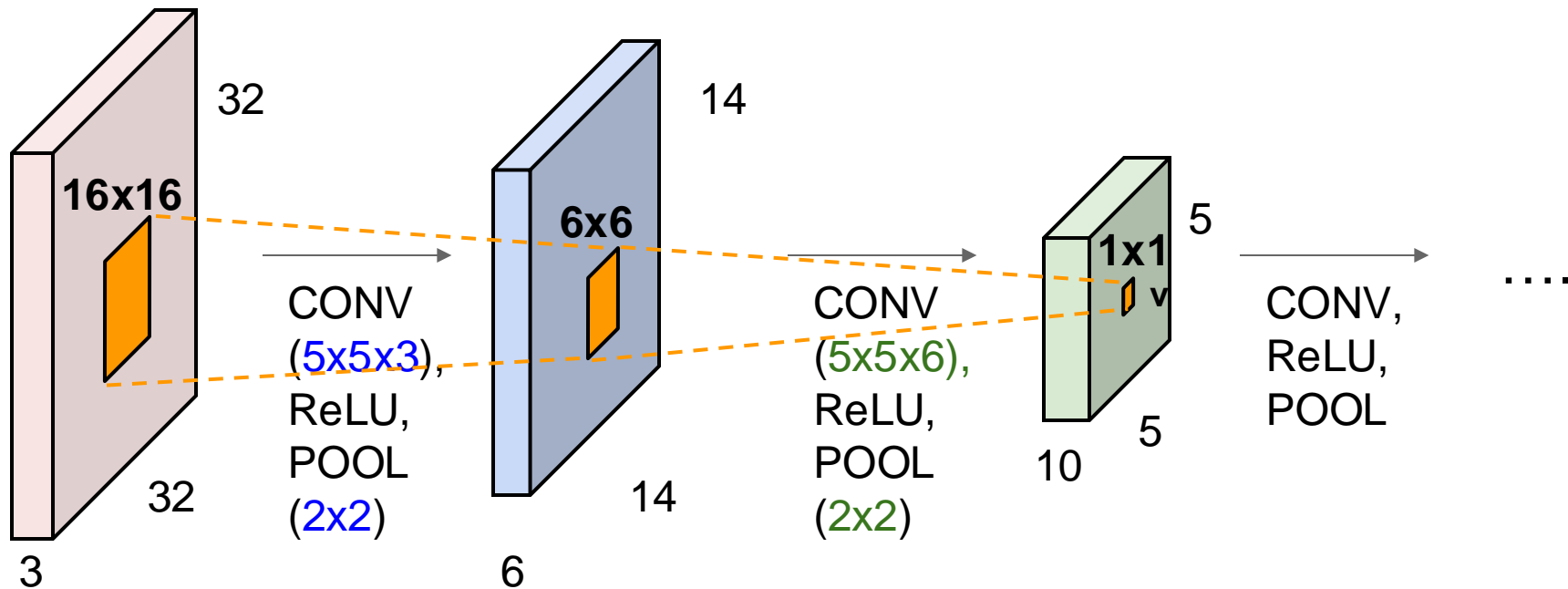
Which pixels in the input image have impact on the value of  $v$ ?



## Receptive field

Which pixels in the input image have impact on the value of  $v$ ?

With POOL Layers?





# Dilated convolution, for even larger receptive fields

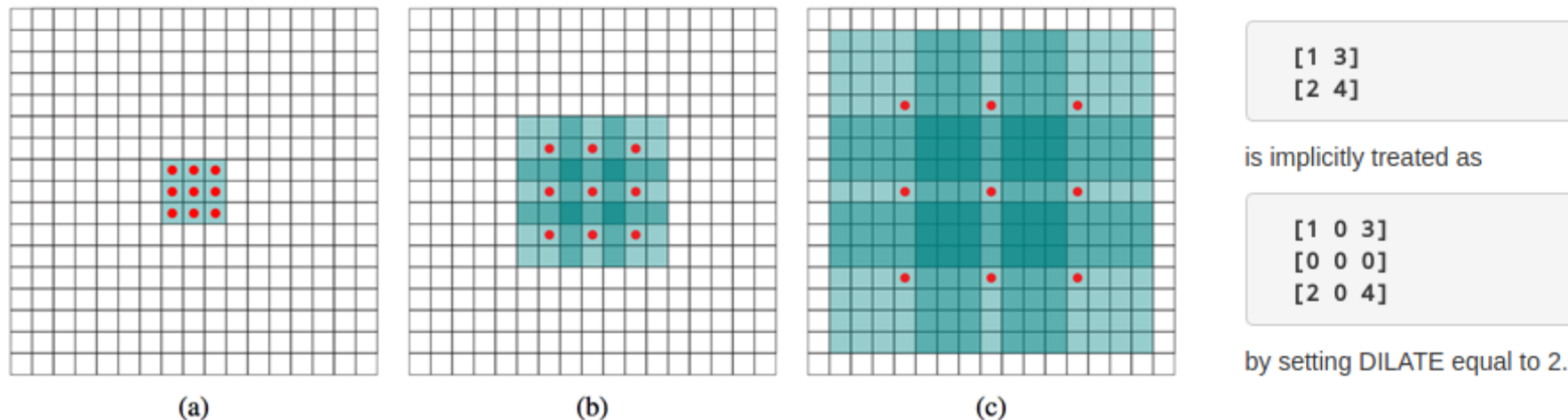
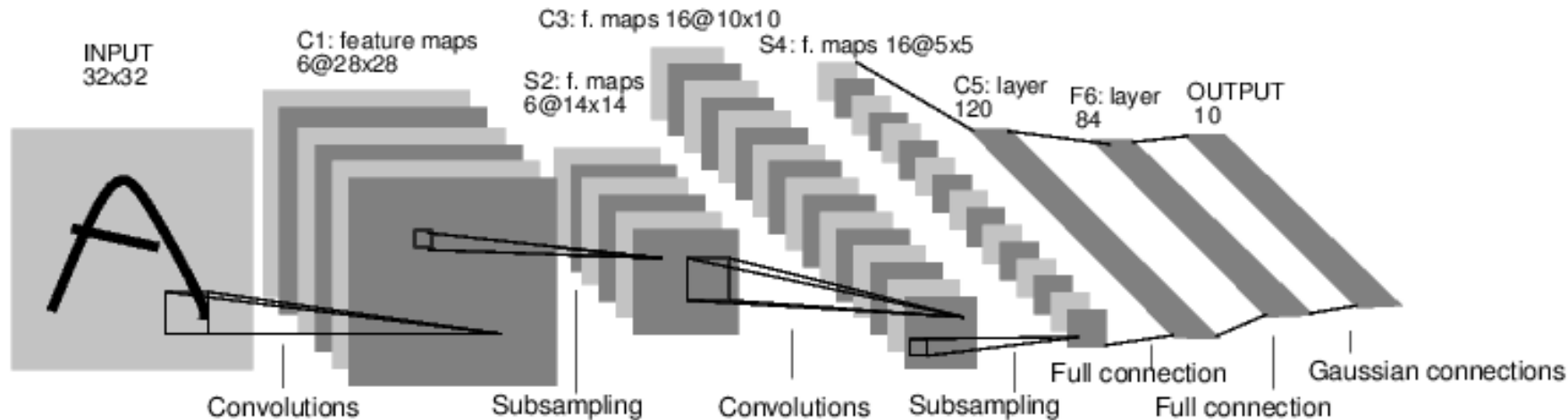


Figure 1: Systematic dilation supports exponential expansion of the receptive field without loss of resolution or coverage. (a)  $F_1$  is produced from  $F_0$  by a 1-dilated convolution; each element in  $F_1$  has a receptive field of  $3 \times 3$ . (b)  $F_2$  is produced from  $F_1$  by a 2-dilated convolution; each element in  $F_2$  has a receptive field of  $7 \times 7$ . (c)  $F_3$  is produced from  $F_2$  by a 4-dilated convolution; each element in  $F_3$  has a receptive field of  $15 \times 15$ . The number of parameters associated with each layer is identical. The receptive field grows exponentially while the number of parameters grows linearly.

**Multi-Scale Context Aggregation by Dilated Convolutions**, Fisher Yu, Vladlen Koltun

# Case Study: LeNet-5

[LeCun et al., 1998]



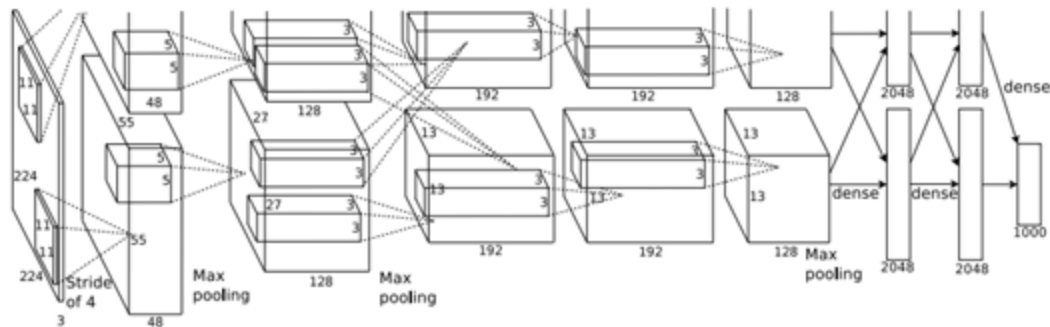
Conv filters were 5x5, applied at stride 1

Subsampling (Pooling) layers were 2x2 applied at stride 2

i.e. architecture is [CONV-POOL-CONV-POOL-CONV-FC]

# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

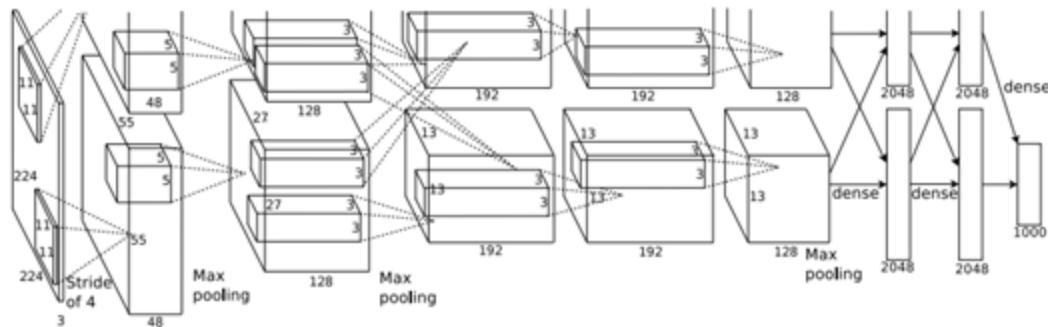
**First layer (CONV1):** 96 11x11 filters applied at stride 4

=>

Q: what is the output volume size? Hint:  $(227-11)/4+1 = 55$

# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

**First layer (CONV1):** 96 11x11 filters applied at stride 4

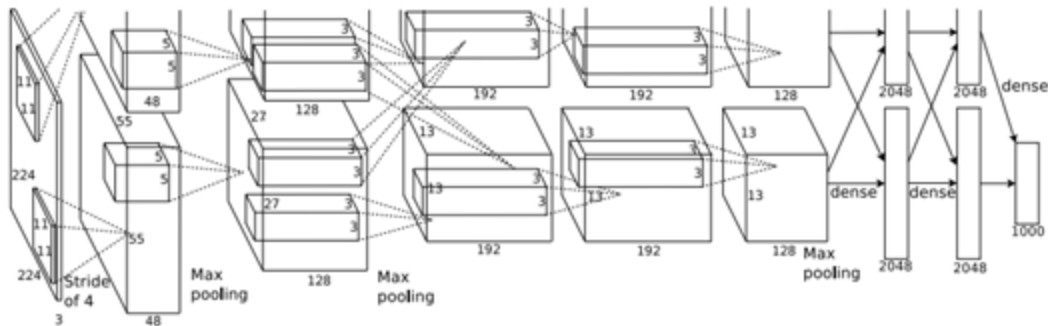
=>

Output volume **[55x55x96]**

Q: What is the total number of parameters in this layer?

# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

**First layer (CONV1):** 96 11x11 filters applied at stride 4

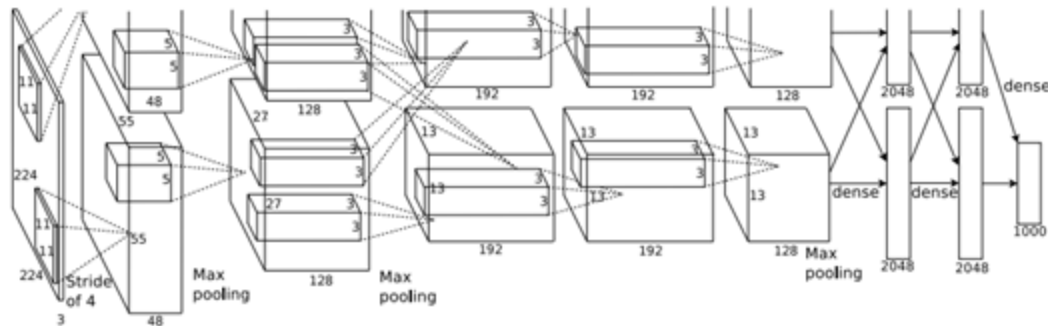
=>

Output volume **[55x55x96]**

Parameters:  $(11*11*3)*96 = \mathbf{35K}$

# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

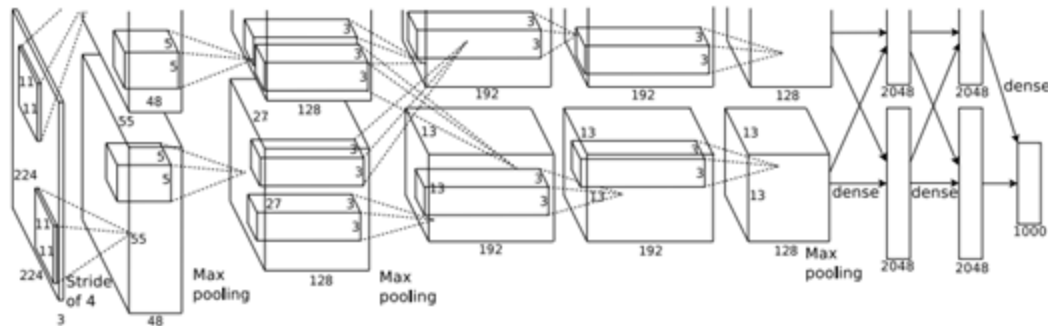
After CONV1: 55x55x96

**Second layer (POOL1):** 3x3 filters applied at stride 2

Q: what is the output volume size? Hint:  $(55-3)/2+1 = 27$

# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

After CONV1: 55x55x96

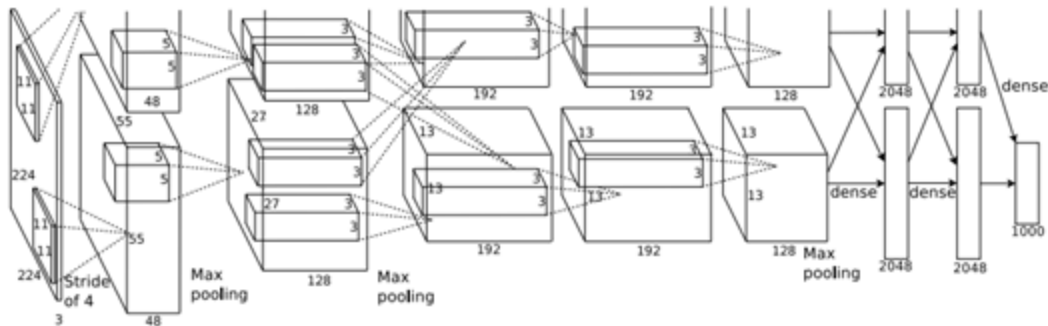
**Second layer (POOL1):** 3x3 filters applied at stride 2

Output volume: 27x27x96

Q: what is the number of parameters in this layer?

# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

After CONV1: 55x55x96

**Second layer (POOL1):** 3x3 filters applied at stride 2

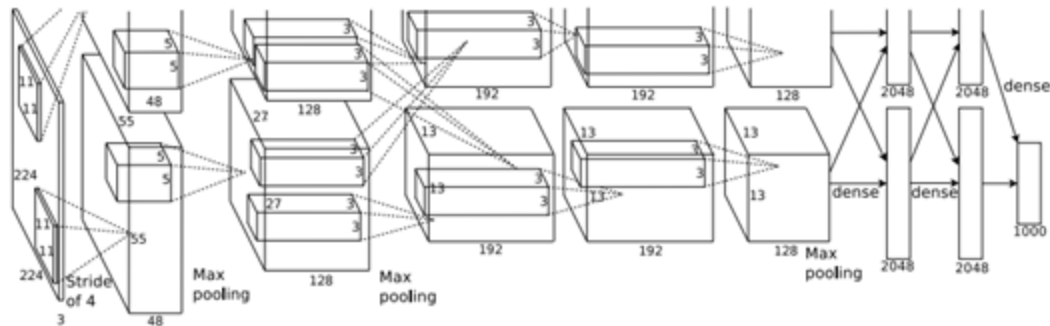
Output volume: 27x27x96

Parameters: 0!



# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

After CONV1: 55x55x96

After POOL1: 27x27x96

...

# Case Study: AlexNet

[Krizhevsky et al. 2012]

Full (simplified) AlexNet architecture:

[227x227x3] INPUT

[55x55x96] **CONV1**: 96 11x11 filters at stride 4, pad 0

[27x27x96] **MAX POOL1**: 3x3 filters at stride 2

[27x27x96] **NORM1**: Normalization layer

[27x27x256] **CONV2**: 256 5x5 filters at stride 1, pad 2

[13x13x256] **MAX POOL2**: 3x3 filters at stride 2

[13x13x256] **NORM2**: Normalization layer

[13x13x384] **CONV3**: 384 3x3 filters at stride 1, pad 1

[13x13x384] **CONV4**: 384 3x3 filters at stride 1, pad 1

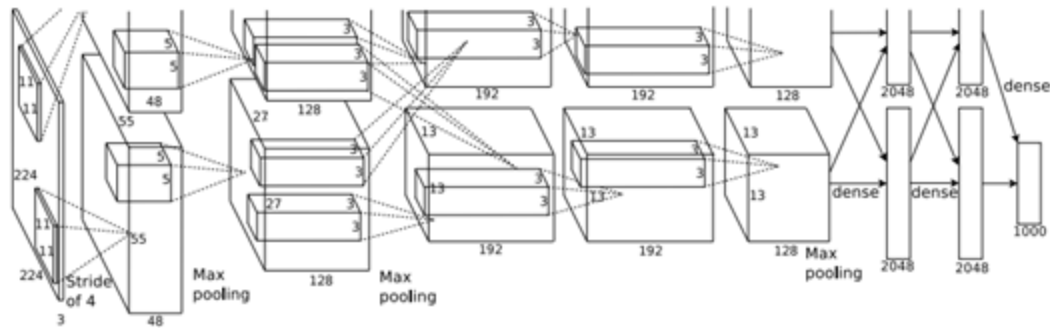
[13x13x256] **CONV5**: 256 3x3 filters at stride 1, pad 1

[6x6x256] **MAX POOL3**: 3x3 filters at stride 2

[4096] **FC6**: 4096 neurons

[4096] **FC7**: 4096 neurons

[1000] **FC8**: 1000 neurons (class scores)



# Case Study: AlexNet

[Krizhevsky et al. 2012]

Full (simplified) AlexNet architecture:

[227x227x3] INPUT

[55x55x96] **CONV1**: 96 11x11 filters at stride 4, pad 0

[27x27x96] **MAX POOL1**: 3x3 filters at stride 2

[27x27x96] **NORM1**: Normalization layer

[27x27x256] **CONV2**: 256 5x5 filters at stride 1, pad 2

[13x13x256] **MAX POOL2**: 3x3 filters at stride 2

[13x13x256] **NORM2**: Normalization layer

[13x13x384] **CONV3**: 384 3x3 filters at stride 1, pad 1

[13x13x384] **CONV4**: 384 3x3 filters at stride 1, pad 1

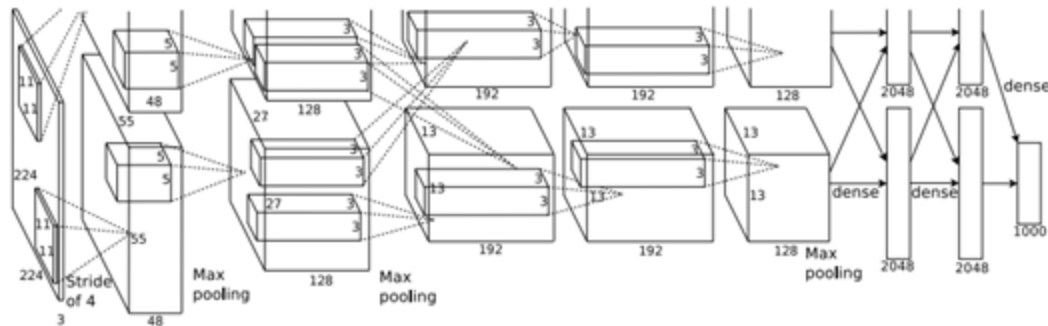
[13x13x256] **CONV5**: 256 3x3 filters at stride 1, pad 1

[6x6x256] **MAX POOL3**: 3x3 filters at stride 2

[4096] **FC6**: 4096 neurons

[4096] **FC7**: 4096 neurons

[1000] **FC8**: 1000 neurons (class scores)



## Details/Retrospectives:

- first use of ReLU
- used Norm layers (not common anymore)
- heavy data augmentation
- dropout 0.5
- batch size 128
- SGD Momentum 0.9
- Learning rate 1e-2, reduced by 10 manually when val accuracy plateaus
- L2 weight decay 5e-4
- 7 CNN ensemble: 18.2% -> 15.4%

# Case Study: VGGNet

[Simonyan and Zisserman, 2014]

Only 3x3 CONV stride 1, pad 1  
and 2x2 MAX POOL stride 2

best model

11.2% top 5 error in ILSVRC 2013

->

7.3% top 5 error

ConvNet Configuration					
A	A-LRN	B	C	D	E
11 weight layers	11 weight layers	13 weight layers	16 weight layers	16 weight layers	19 weight layers
input (224 × 224 RGB image)					
conv3-64	conv3-64 LRN	conv3-64 <b>conv3-64</b>	conv3-64 conv3-64	conv3-64 conv3-64	conv3-64 conv3-64
maxpool					
conv3-128	conv3-128	conv3-128 <b>conv3-128</b>	conv3-128 conv3-128	conv3-128 conv3-128	conv3-128 conv3-128
maxpool					
conv3-256 conv3-256	conv3-256 conv3-256	conv3-256 conv3-256	conv3-256 conv3-256 <b>conv1-256</b>	conv3-256 conv3-256 <b>conv3-256</b>	conv3-256 conv3-256 conv3-256 <b>conv3-256</b>
maxpool					
conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512 <b>conv1-512</b>	conv3-512 conv3-512 <b>conv3-512</b>	conv3-512 conv3-512 conv3-512 <b>conv3-512</b>
maxpool					
conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512 <b>conv1-512</b>	conv3-512 conv3-512 <b>conv3-512</b>	conv3-512 conv3-512 conv3-512 <b>conv3-512</b>
maxpool					
FC-4096					
FC-4096					
FC-1000					
soft-max					

Table 2: Number of parameters (in millions).

Network	A,A-LRN	B	C	D	E
Number of parameters	133	133	134	138	144

INPUT: [224x224x3] memory:  $224*224*3=150\text{K}$  params: 0 (not counting biases)

CONV3-64: [224x224x64] memory:  $224*224*64=3.2\text{M}$  params:  $(3*3*3)*64 = 1,728$

CONV3-64: [224x224x64] memory:  $224*224*64=3.2\text{M}$  params:  $(3*3*64)*64 = 36,864$

POOL2: [112x112x64] memory:  $112*112*64=800\text{K}$  params: 0

CONV3-128: [112x112x128] memory:  $112*112*128=1.6\text{M}$  params:  $(3*3*64)*128 = 73,728$

CONV3-128: [112x112x128] memory:  $112*112*128=1.6\text{M}$  params:  $(3*3*128)*128 = 147,456$

POOL2: [56x56x128] memory:  $56*56*128=400\text{K}$  params: 0

CONV3-256: [56x56x256] memory:  $56*56*256=800\text{K}$  params:  $(3*3*128)*256 = 294,912$

CONV3-256: [56x56x256] memory:  $56*56*256=800\text{K}$  params:  $(3*3*256)*256 = 589,824$

CONV3-256: [56x56x256] memory:  $56*56*256=800\text{K}$  params:  $(3*3*256)*256 = 589,824$

POOL2: [28x28x256] memory:  $28*28*256=200\text{K}$  params: 0

CONV3-512: [28x28x512] memory:  $28*28*512=400\text{K}$  params:  $(3*3*256)*512 = 1,179,648$

CONV3-512: [28x28x512] memory:  $28*28*512=400\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

CONV3-512: [28x28x512] memory:  $28*28*512=400\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

POOL2: [14x14x512] memory:  $14*14*512=100\text{K}$  params: 0

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CONV3-512: [14x14x512] memory:  $14*14*512=100\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

POOL2: [7x7x512] memory:  $7*7*512=25\text{K}$  params: 0

FC: [1x1x4096] memory: 4096 params:  $7*7*512*4096 = 102,760,448$

FC: [1x1x4096] memory: 4096 params:  $4096*4096 = 16,777,216$

FC: [1x1x1000] memory: 1000 params:  $4096*1000 = 4,096,000$

ConvNet Configuration			
B	C	D	
13 weight layers	16 weight layers	16 weight layers	19
put (224 × 224 RGB image)			
conv3-64	conv3-64	conv3-64	cc
<b>conv3-64</b>	conv3-64	conv3-64	cc
maxpool			
conv3-128	conv3-128	conv3-128	co
<b>conv3-128</b>	conv3-128	conv3-128	co
maxpool			
conv3-256	conv3-256	conv3-256	co
conv3-256	conv3-256	conv3-256	co
	<b>conv1-256</b>	<b>conv3-256</b>	co
		<b>conv3-256</b>	co
maxpool			
conv3-512	conv3-512	conv3-512	co
conv3-512	conv3-512	conv3-512	co
	<b>conv1-512</b>	<b>conv3-512</b>	co
		<b>conv3-512</b>	co
maxpool			
conv3-512	conv3-512	conv3-512	co
conv3-512	conv3-512	conv3-512	co
	<b>conv1-512</b>	<b>conv3-512</b>	co
		<b>conv3-512</b>	co
maxpool			
FC-4096			
FC-4096			
FC-1000			
soft-max			

INPUT: [224x224x3] memory:  $224*224*3=150\text{K}$  params: 0 (not counting biases)

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CONV3-64: [224x224x64] memory:  $224*224*64=3.2\text{M}$  params:  $(3*3*64)*64 = 36,864$

POOL2: [112x112x64] memory:  $112*112*64=800\text{K}$  params: 0

CONV3-128: [112x112x128] memory:  $112*112*128=1.6\text{M}$  params:  $(3*3*64)*128 = 73,728$

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POOL2: [56x56x128] memory:  $56*56*128=400\text{K}$  params: 0

CONV3-256: [56x56x256] memory:  $56*56*256=800\text{K}$  params:  $(3*3*128)*256 = 294,912$

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POOL2: [7x7x512] memory:  $7*7*512=25\text{K}$  params: 0

FC: [1x1x4096] memory: 4096 params:  $7*7*512*4096 = 102,760,448$

FC: [1x1x4096] memory: 4096 params:  $4096*4096 = 16,777,216$

FC: [1x1x1000] memory: 1000 params:  $4096*1000 = 4,096,000$

**TOTAL memory: 24M \* 4 bytes  $\sim$  93MB / image** (only forward!  $\sim$ \*2 for bwd)

**TOTAL params: 138M parameters**

ConvNet Configuration			
B	C	D	
13 weight layers	16 weight layers	16 weight layers	19
put (224 × 224 RGB image)			
conv3-64	conv3-64	conv3-64	cc
<b>conv3-64</b>	conv3-64	conv3-64	cc
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<b>conv3-128</b>	conv3-128	conv3-128	co
maxpool			
conv3-256	conv3-256	conv3-256	co
conv3-256	conv3-256	conv3-256	co
	<b>conv1-256</b>	<b>conv3-256</b>	co
			co
maxpool			
conv3-512	conv3-512	conv3-512	co
conv3-512	conv3-512	conv3-512	co
	<b>conv1-512</b>	<b>conv3-512</b>	co
			co
maxpool			
conv3-512	conv3-512	conv3-512	co
conv3-512	conv3-512	conv3-512	co
	<b>conv1-512</b>	<b>conv3-512</b>	co
			co
maxpool			
FC-4096			
FC-4096			
FC-1000			
soft-max			



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FC: [1x1x1000] memory: 1000 params:  $4096*1000 = 4,096,000$

**TOTAL memory:**  $24\text{M} * 4 \text{ bytes} \approx 93\text{MB} / \text{image}$  (only forward!  $\sim 2$  for bwd)

**TOTAL params:** 138M parameters

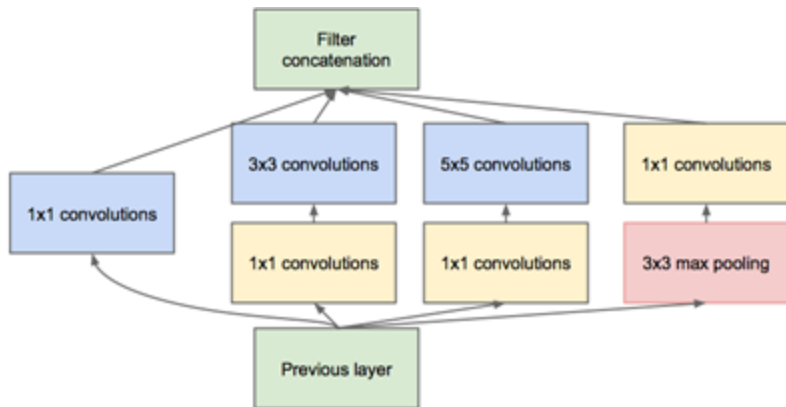
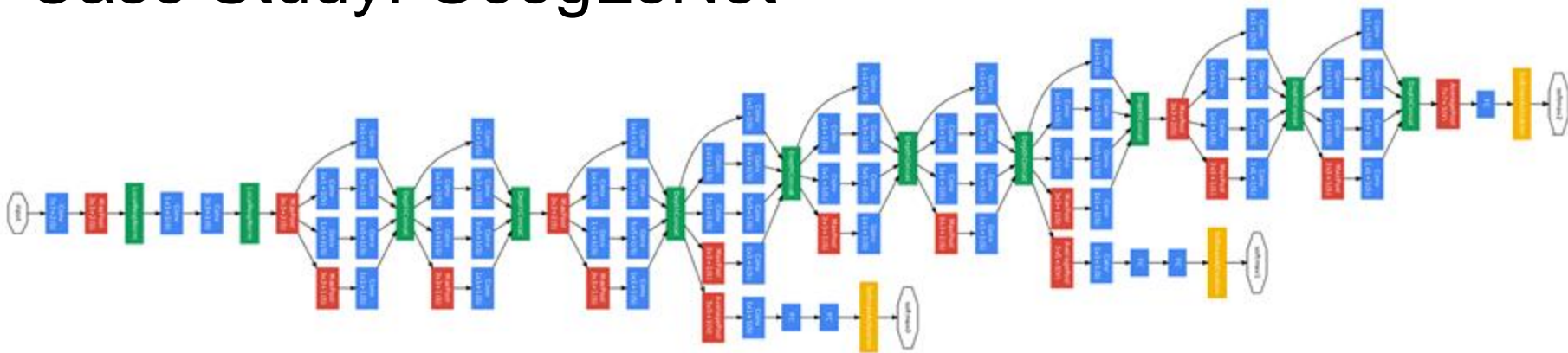
Note:

Most memory is in early CONV

Most params are in late FC

# Case Study: GoogLeNet

[Szegedy et al., 2014]



## Inception module

ILSVRC 2014 winner (6.7% top 5 error)



# Case Study: GoogLeNet

type	patch size/ stride	output size	depth	#1×1	#3×3 reduce	#3×3	#5×5 reduce	#5×5	pool proj	params	ops
convolution	7×7/2	112×112×64	1							2.7K	34M
max pool	3×3/2	56×56×64	0								
convolution	3×3/1	56×56×192	2		64	192				112K	360M
max pool	3×3/2	28×28×192	0								
inception (3a)		28×28×256	2	64	96	128	16	32	32	159K	128M
inception (3b)		28×28×480	2	128	128	192	32	96	64	380K	304M
max pool	3×3/2	14×14×480	0								
inception (4a)		14×14×512	2	192	96	208	16	48	64	364K	73M
inception (4b)		14×14×512	2	160	112	224	24	64	64	437K	88M
inception (4c)		14×14×512	2	128	128	256	24	64	64	463K	100M
inception (4d)		14×14×528	2	112	144	288	32	64	64	580K	119M
inception (4e)		14×14×832	2	256	160	320	32	128	128	840K	170M
max pool	3×3/2	7×7×832	0								
inception (5a)		7×7×832	2	256	160	320	32	128	128	1072K	54M
inception (5b)		7×7×1024	2	384	192	384	48	128	128	1388K	71M
avg pool	7×7/1	1×1×1024	0								
dropout (40%)		1×1×1024	0								
linear		1×1×1000	1							1000K	1M
softmax		1×1×1000	0								

Fun features:

- Only 5 million params!  
(Removes FC layers completely)

**Compared to AlexNet:**

- 12X less params
- 2x more compute
- 6.67% (vs. 16.4%)

# Case Study: ResNet [He et al., 2015]

ILSVRC 2015 winner (3.6% top 5 error)

Microsoft Research

MSRA @ ILSVRC & COCO 2015 Competitions

- **1st places in all five main tracks**
  - ImageNet Classification: “Ultra-deep” (quote Yann) **152-layer** nets
  - ImageNet Detection: **16%** better than 2nd
  - ImageNet Localization: **27%** better than 2nd
  - COCO Detection: **11%** better than 2nd
  - COCO Segmentation: **12%** better than 2nd

According to [Google Scholar Metrics](#), as of June 2017:

- “Deep Residual Learning for Image Recognition” is **the most cited paper** published in CVPR 2016.

*Deep Residual Learning for Image Recognition*

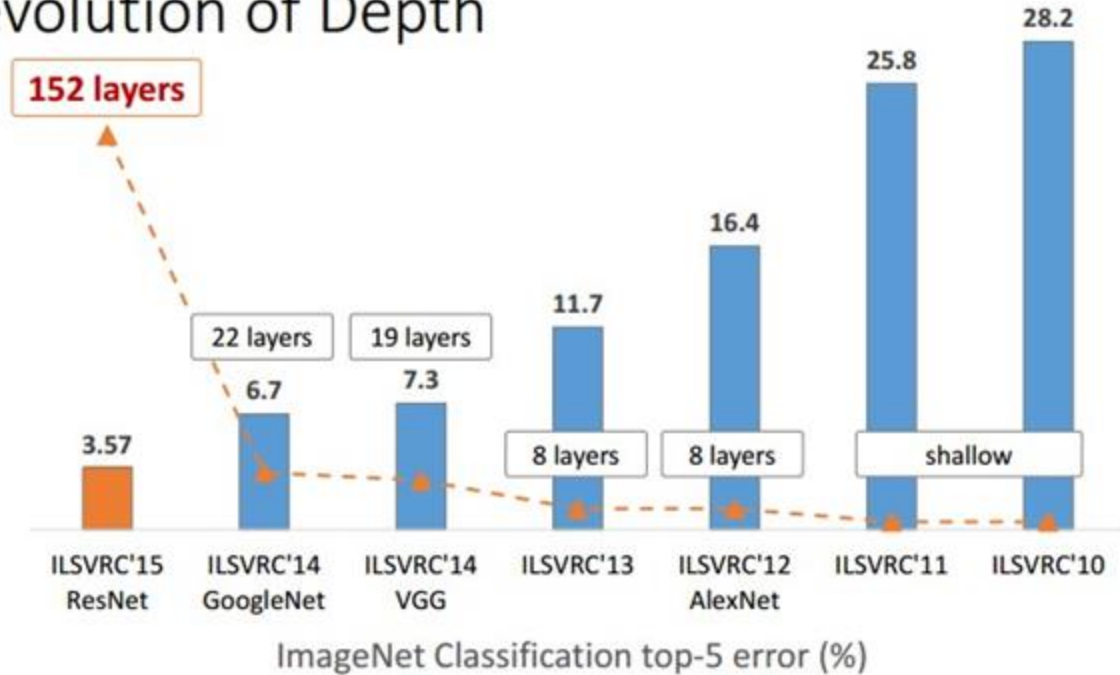
**Kaiming He**, Xiangyu Zhang, Shaoqing Ren, and Jian Sun

IEEE Conference on Computer Vision and Pattern Recognition (CVPR), 2016 (Oral). [CVPR Best Paper Award](#)

[arXiv](#) [code/models](#) [talk](#) slides: [ILSVRC workshop](#) [ICML tutorial](#) [CVPR oral](#)

[ILSVRC](#) & [COCO](#) competitions 2015: we won the **1st places** in ImageNet classification, ImageNet detection, ImageNet localization, COCO detection, and COCO segmentation!

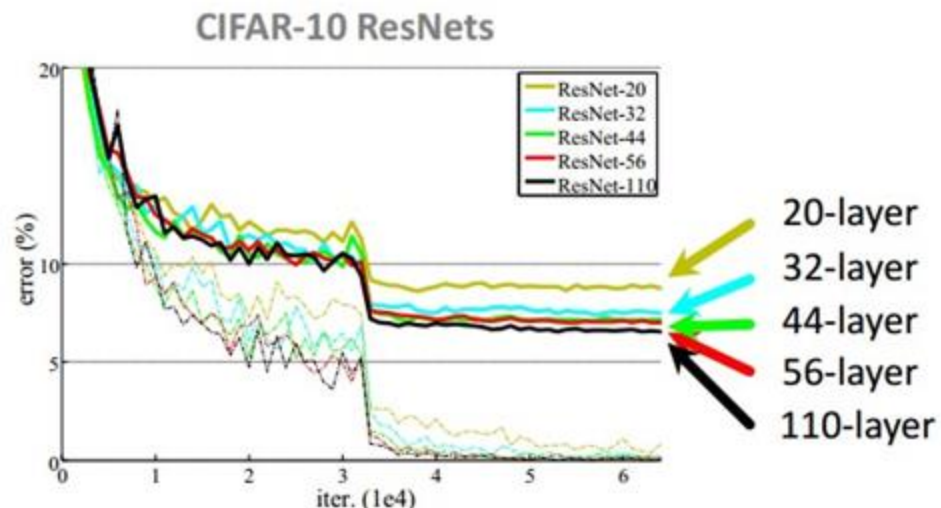
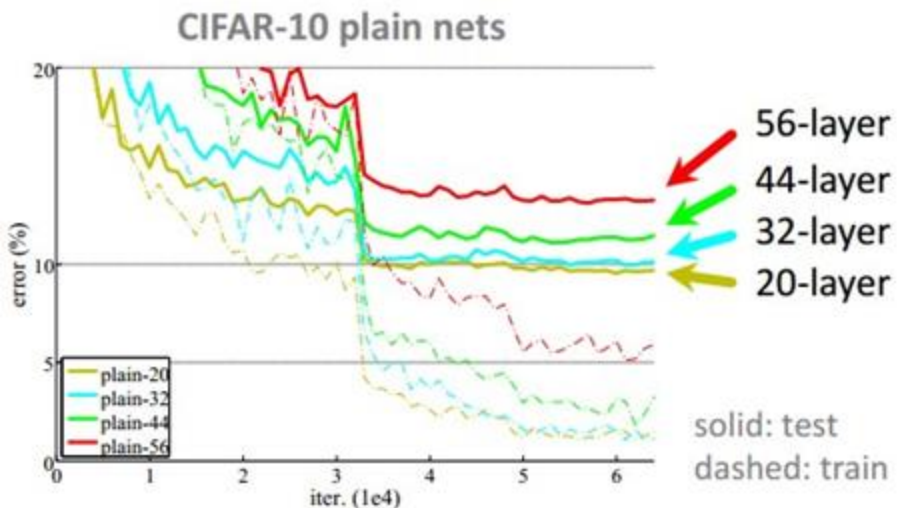
# Revolution of Depth



Kaiming He, Xiangyu Zhang, Shaoqing Ren, & Jian Sun. "Deep Residual Learning for Image Recognition". arXiv 2015.

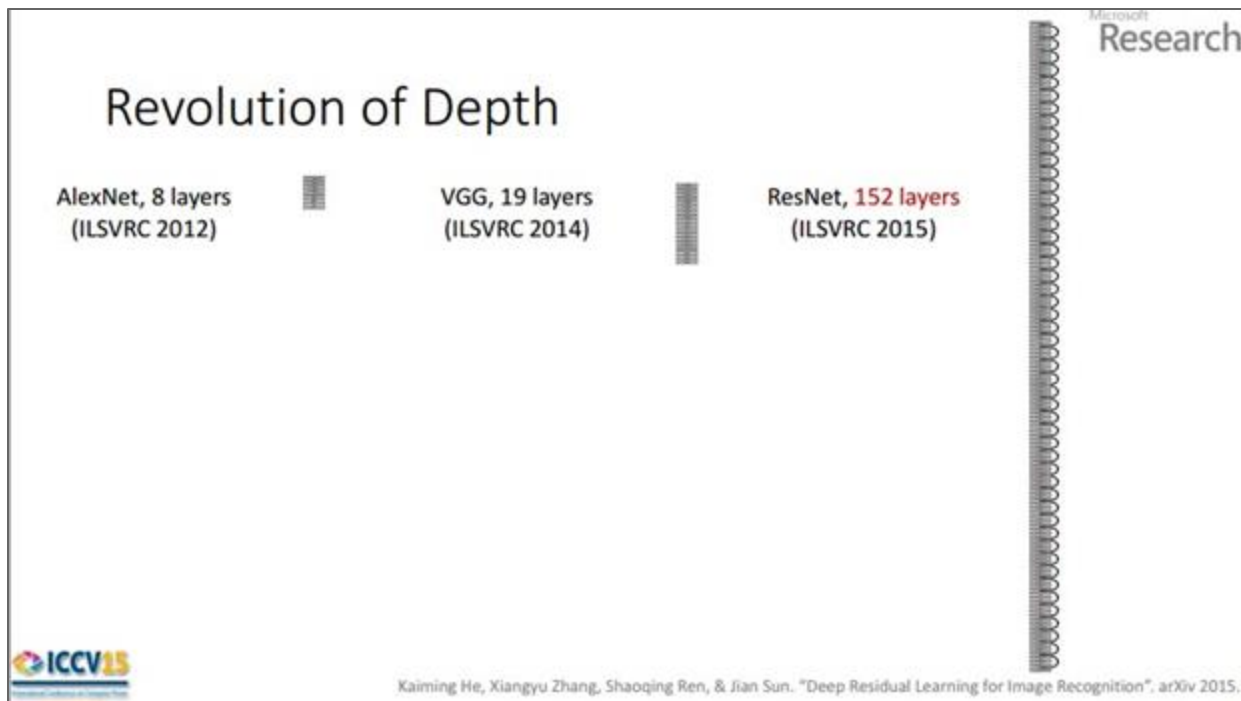
(slide from Kaiming He's recent presentation)

# CIFAR-10 experiments



# Case Study: ResNet [He et al., 2015]

ILSVRC 2015 winner (3.6% top 5 error)



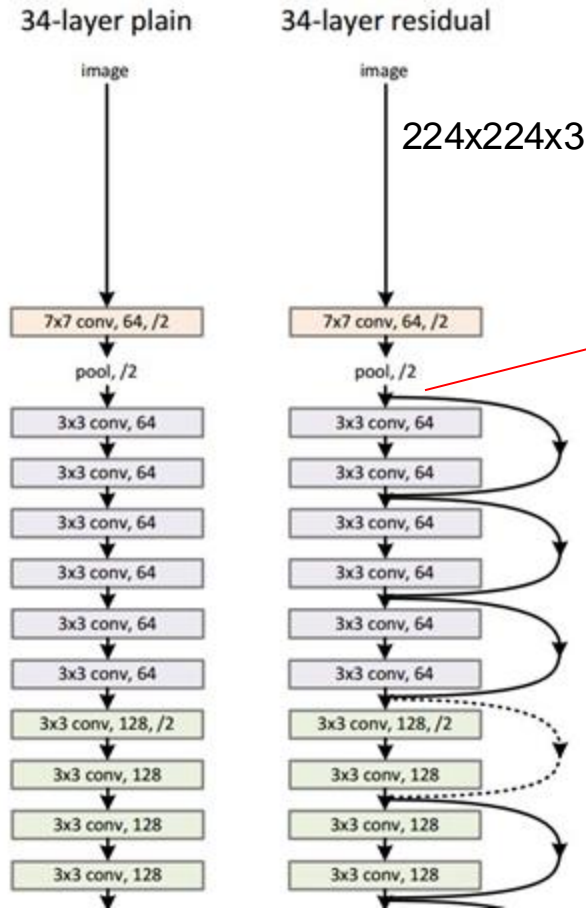
2-3 weeks of training  
on 8 GPU machine

at runtime: faster  
than a VGGNet!  
(even though it has  
8x more layers)

(slide from Kaiming He's presentation)

# Case Study: ResNet

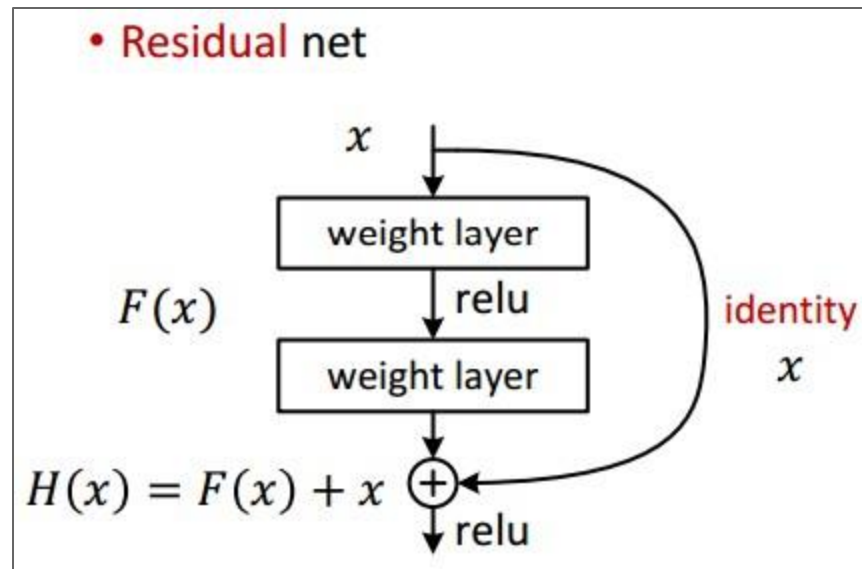
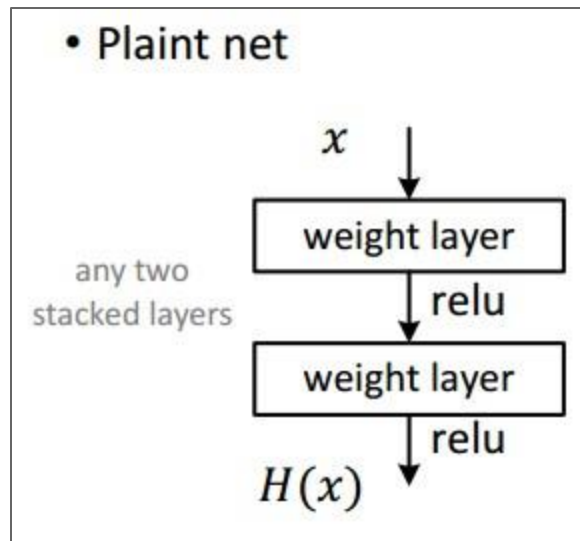
[He et al., 2015]



spatial dimension  
only 56x56!

# Case Study: ResNet

[He et al., 2015]



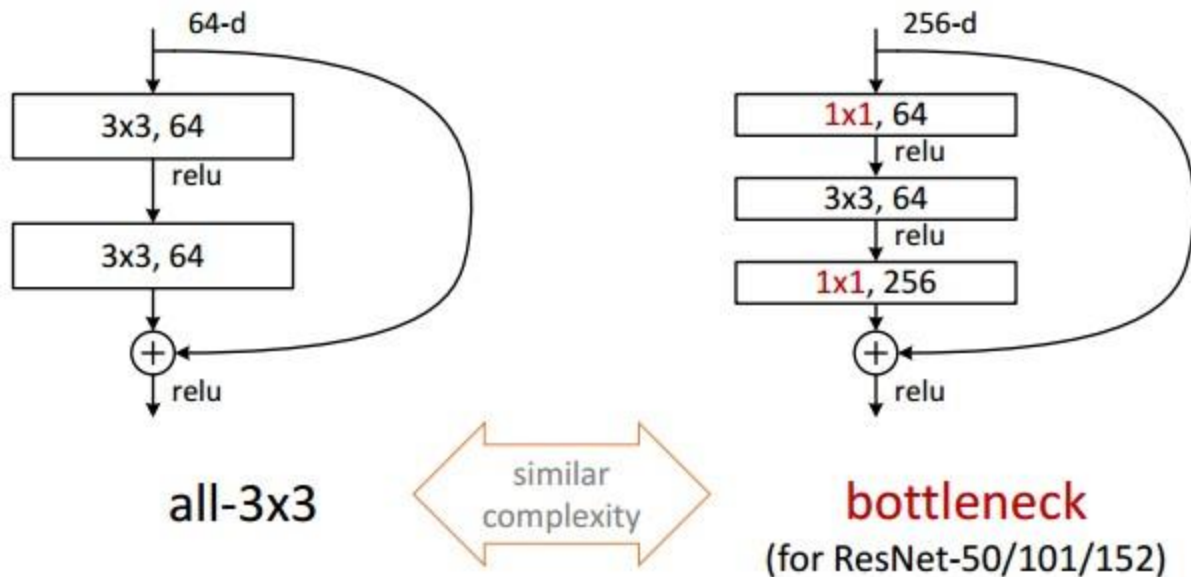
# Case Study: ResNet *[He et al., 2015]*

- Batch Normalization after every CONV layer
- Xavier/2 initialization from He et al.
- SGD + Momentum (0.9)
- Learning rate: 0.1, divided by 10 when validation error plateaus
- Mini-batch size 256
- Weight decay of  $1e-5$
- No dropout used



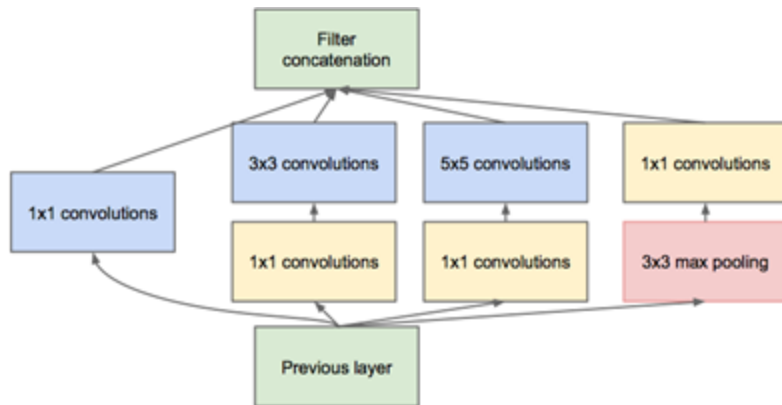
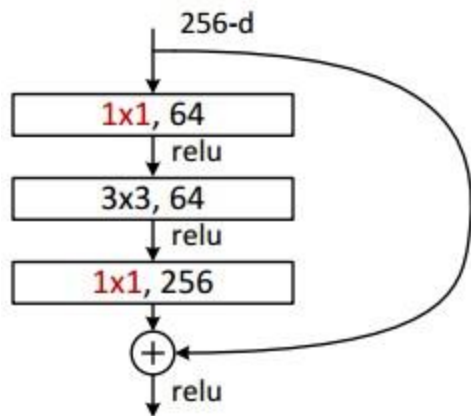
# Case Study: ResNet

[He et al., 2015]



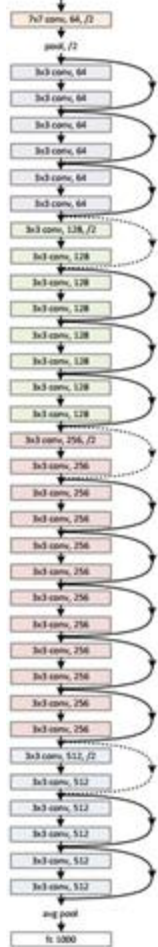
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(this trick is also used in GoogLeNet)

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layer name	output size	18-layer	34-layer	50-layer	101-layer	152-layer
conv1	112×112	7×7, 64, stride 2				
conv2_x	56×56	3×3 max pool, stride 2				
		$\begin{bmatrix} 3 \times 3, 64 \\ 3 \times 3, 64 \end{bmatrix} \times 2$	$\begin{bmatrix} 3 \times 3, 64 \\ 3 \times 3, 64 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$
conv3_x	28×28	$\begin{bmatrix} 3 \times 3, 128 \\ 3 \times 3, 128 \end{bmatrix} \times 2$	$\begin{bmatrix} 3 \times 3, 128 \\ 3 \times 3, 128 \end{bmatrix} \times 4$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 8$
conv4_x	14×14	$\begin{bmatrix} 3 \times 3, 256 \\ 3 \times 3, 256 \end{bmatrix} \times 2$	$\begin{bmatrix} 3 \times 3, 256 \\ 3 \times 3, 256 \end{bmatrix} \times 6$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 6$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 23$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 36$
conv5_x	7×7	$\begin{bmatrix} 3 \times 3, 512 \\ 3 \times 3, 512 \end{bmatrix} \times 2$	$\begin{bmatrix} 3 \times 3, 512 \\ 3 \times 3, 512 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$
	1×1	average pool, 1000-d fc, softmax				
FLOPs		$1.8 \times 10^9$	$3.6 \times 10^9$	$3.8 \times 10^9$	$7.6 \times 10^9$	$11.3 \times 10^9$

# Summary

- ConvNets stack CONV, POOL, FC layers
- Trend towards smaller filters and deeper architectures
- Trend towards getting rid of POOL/FC layers (just CONV)
- Typical architectures look like  
 **$[(\text{CONV-RELU})^N \text{- POOL?}]^M \text{- (FC-RELU)}^K, \text{SOFTMAX}$**   
where N is usually up to  $\sim 5$ , M is large,  $0 \leq K \leq 2$ .
  - but recent advances such as ResNet/GoogLeNet challenge this paradigm