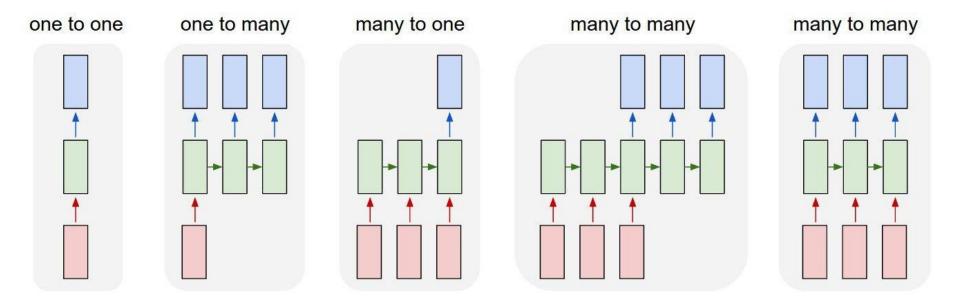
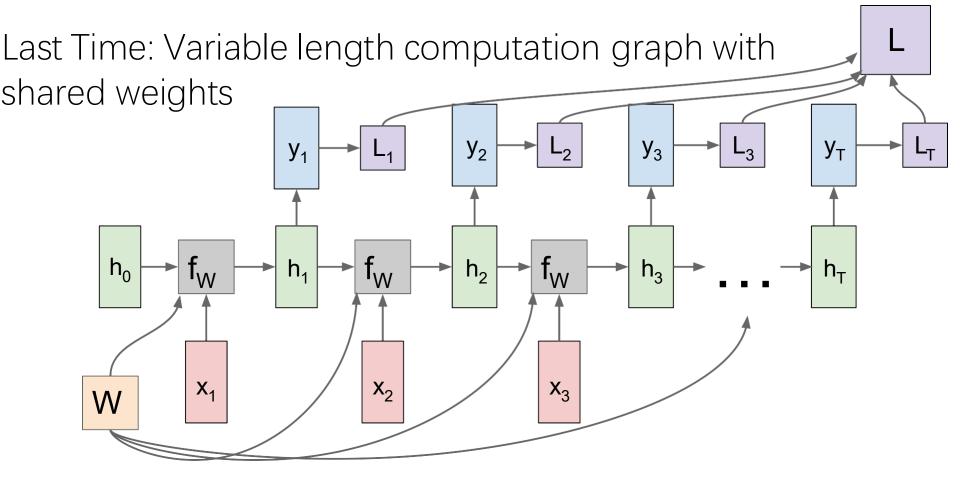
# Lecture 17: Attention and Transformers

# **Project Presentation:**

All teams are required to present in person; however, teams with online students have the option to present either in person or online. Presentations will take place over the last three days, with the presentation order determined randomly.

#### Last Time: Recurrent Neural Networks

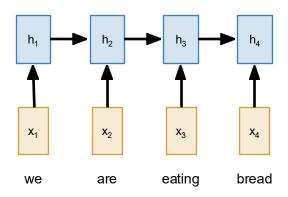




**Input**: Sequence  $x_1, \dots x_T$ 

**Output**: Sequence y<sub>1</sub>, ..., y<sub>T</sub>,

**Encoder:**  $h_t = f_W(x_t, h_{t-1})$ 



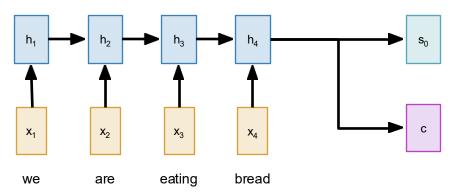
**Input**: Sequence  $x_1, ... x_T$ 

**Output**: Sequence y<sub>1</sub>, ..., y<sub>T</sub>,

From final hidden state predict:

**Encoder:**  $h_t = f_W(x_t, h_{t-1})$  Initial decoder state  $s_0$ 

**Context vector** c (often c=h<sub>T</sub>)

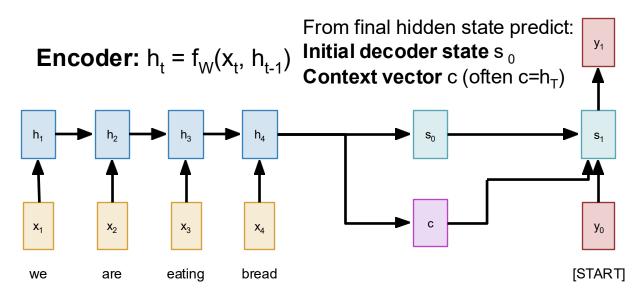


**Input**: Sequence  $x_1, \dots x_T$ 

**Output**: Sequence y<sub>1</sub>, ..., y<sub>T</sub>,

**Decoder:**  $s_t = g_U(y_{t-1}, s_{t-1}, c)$ 

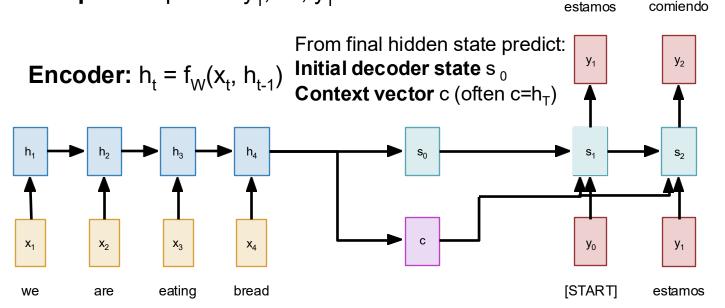
estamos



**Input**: Sequence  $x_1, \dots x_T$ 

Output: Sequence y<sub>1</sub>, ..., y<sub>T</sub>,

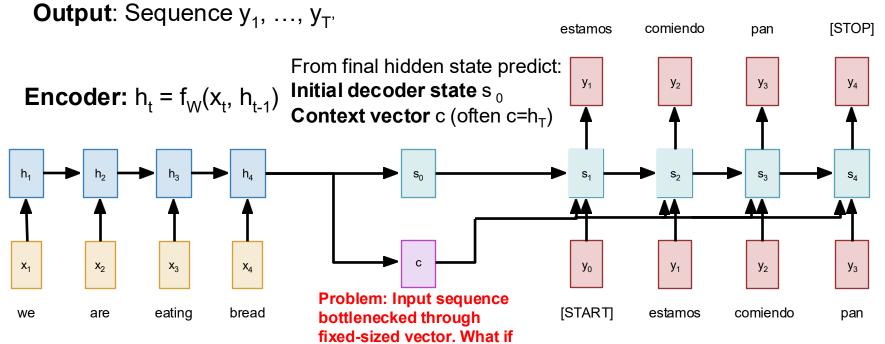
**Decoder:**  $s_t = g_U(y_{t-1}, s_{t-1}, c)$ 



**Decoder:**  $s_t = g_{l,l}(y_{t-1}, s_{t-1}, c)$ **Input**: Sequence  $x_1, \dots x_T$ Output: Sequence y<sub>1</sub>, ..., y<sub>T</sub>, [STOP] estamos comiendo pan From final hidden state predict: Initial decoder state s<sub>0</sub> **Encoder:**  $h_t = f_W(x_t, h_{t-1})$ Context vector c (often c=h<sub>⊤</sub>)  $X_1$  $X_3$ **y**<sub>2</sub> **y**<sub>3</sub> eating bread [START] comiendo we are estamos pan

**Input**: Sequence  $x_1, \dots x_T$ 

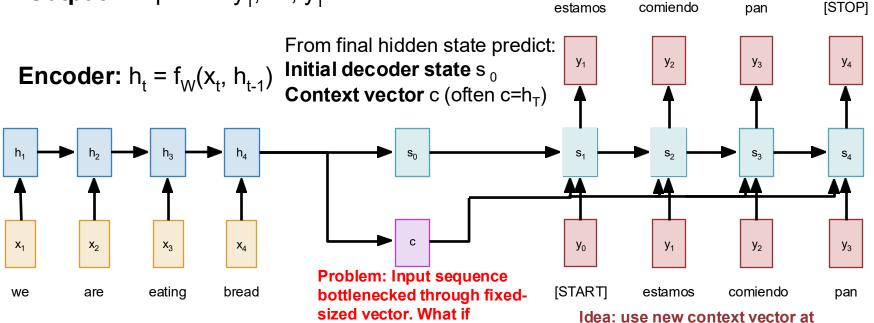
**Decoder:**  $s_t = g_{l,l}(y_{t-1}, s_{t-1}, c)$ 



**Input**: Sequence  $x_1, \dots x_T$ 

**Output**: Sequence  $y_1, ..., y_T$ 

**Decoder:**  $s_t = g_U(y_{t-1}, s_{t-1}, c)$ 



Chuang Gan and TAs

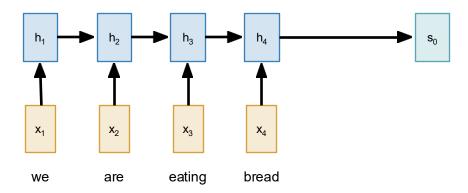
Lecture 17 - 11

each step of decoder!

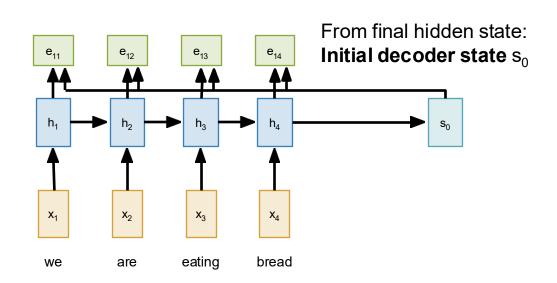
**Input**: Sequence  $x_1, ... x_T$ 

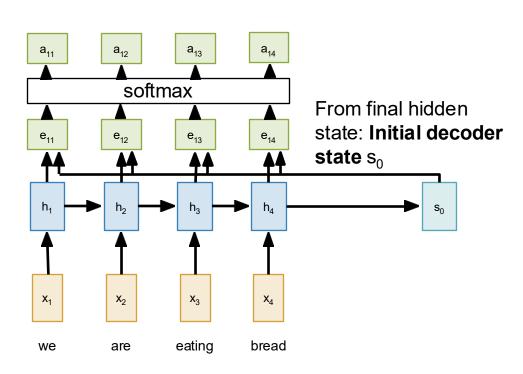
**Output**: Sequence y<sub>1</sub>, ..., y<sub>T</sub>,

**Encoder:** 
$$h_t = f_W(x_t, h_{t-1})$$
 From final hidden state:  
Initial decoder state  $s_0$ 



Compute (scalar) **alignment scores**  $e_{t,i} = f_{att}(s_{t-1}, h_i)$  ( $f_{att}$  is an MLP)

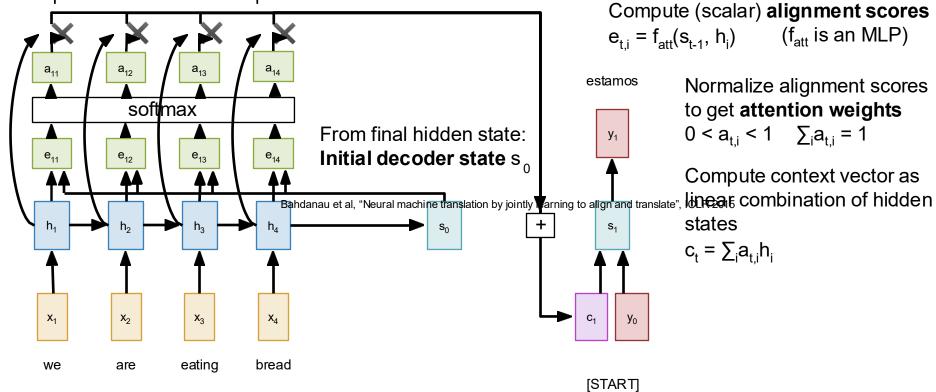


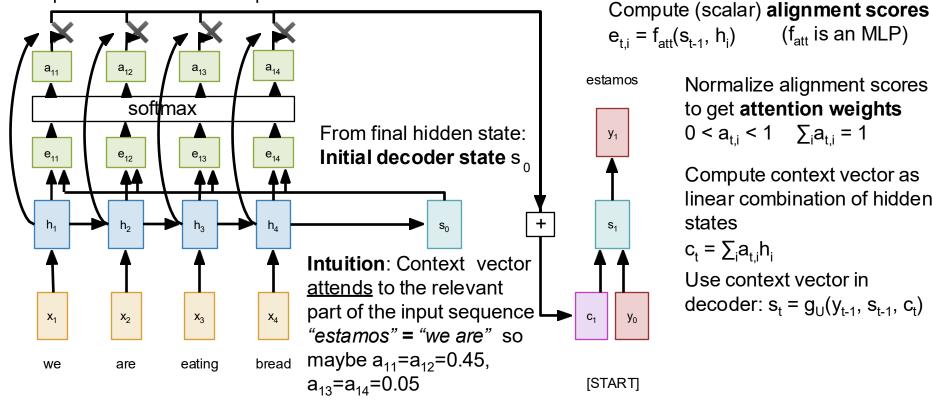


Compute (scalar) **alignment scores**  $e_{t,i} = f_{att}(s_{t-1}, h_i)$  ( $f_{att}$  is an MLP)

Normalize alignment scores to get **attention weights**  $0 < a_{ti} < 1$   $\sum_{i} a_{ti} = 1$ 







Normalize alignment scores to get attention weights

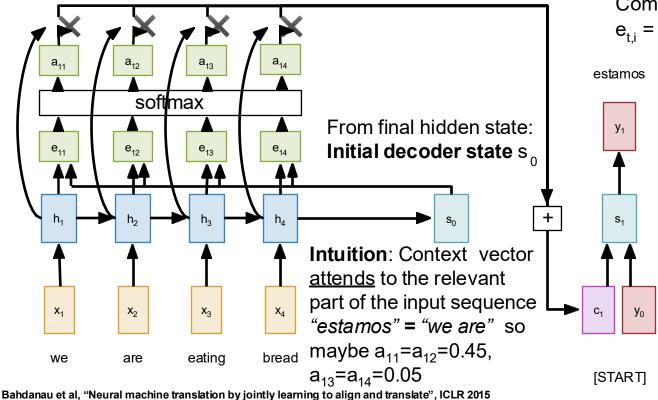
(f<sub>att</sub> is an MLP)

$$0 < a_{t,i} < 1$$
  $\sum_{i} a_{t,i} = 1$ 

Compute context vector as linear combination of hidden states

$$c_t = \sum_i a_{t,i} h_i$$

Use context vector in decoder:  $s_t = g_{11}(y_{t-1}, s_{t-1}, c_t)$ 



Compute (scalar) **alignment scores**  $e_{t,i} = f_{att}(s_{t-1}, h_i)$  ( $f_{att}$  is an MLP)

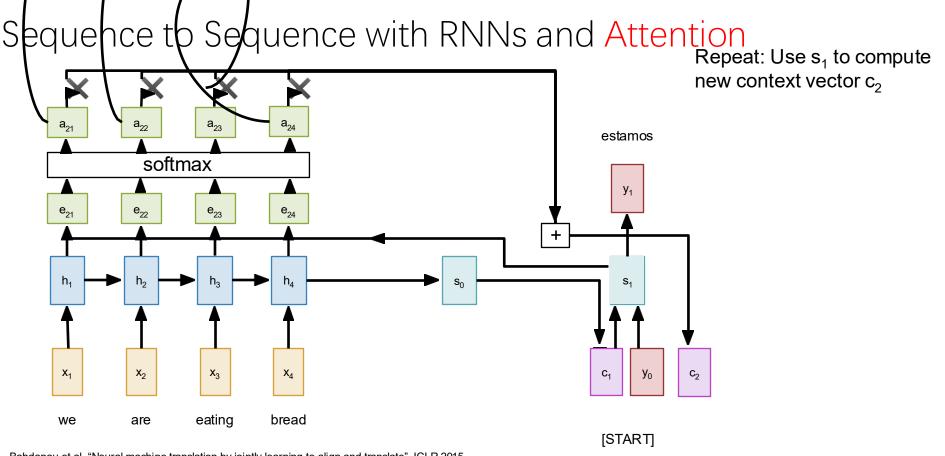
Normalize alignment scores to get **attention weights**  $0 < a_{ti} < 1$   $\sum_{i} a_{ti} = 1$ 

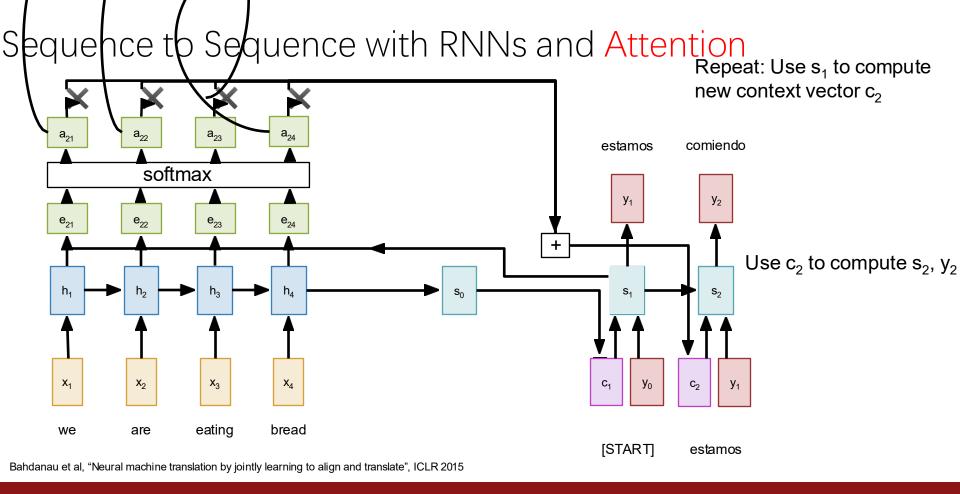
Compute context vector as linear combination of hidden states

$$c_t = \sum_i a_{t,i} h_i$$

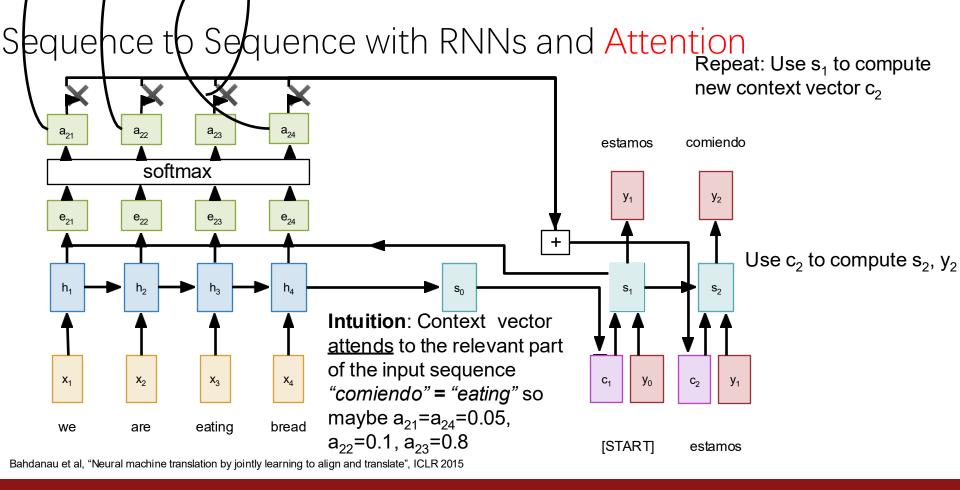
Use context vector in decoder:  $s_t = g_U(y_{t-1}, s_{t-1}, c_t)$ 

This is all differentiable! No supervision on attention weights – backprop through everything





Chuang Gan and TAs
Some slides kindly provided by Fei-Fei Li, Jiajun Wu, Erik Learned-Miller



# Sequence to Sequence with RNNs and Attention Use a different context vector in each timestep of decoder

- Input sequence not bottlenecked through single vector

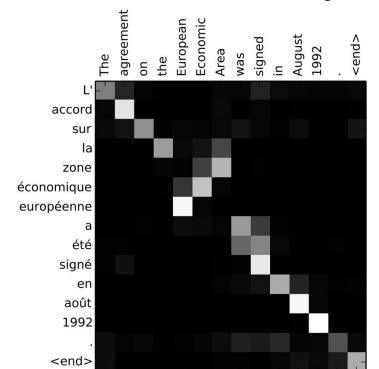
estamos comiendo pan [STOP] At each timestep of decoder, context vector "looks at" different parts of the input sequence  $X_2$  $X_3$  $X_4$  $C_2$  $C_3$  $X_1$ **y**<sub>2</sub> C<sub>4</sub> **y**<sub>3</sub> eating bread we are [START] estamos comiendo pan

**Example**: English to French translation

**Input**: "The agreement on the European Economic Area was signed in August 1992."

**Output**: "L'accord sur la zone économique européenne a été signé en août 1992."

Visualize attention weights a<sub>t,i</sub>



**Example**: English to French translation

Input: "The agreement on the European Economic Area was signed in August 1992."

Output: "L'accord sur la zone économique européenne a été signé en août 1992."

Diagonal attention means words correspond in order

Diagonal attention means words correspond in order

accord sur zone économique européenne été signé août 1992

Visualize attention weights a<sub>+</sub>;

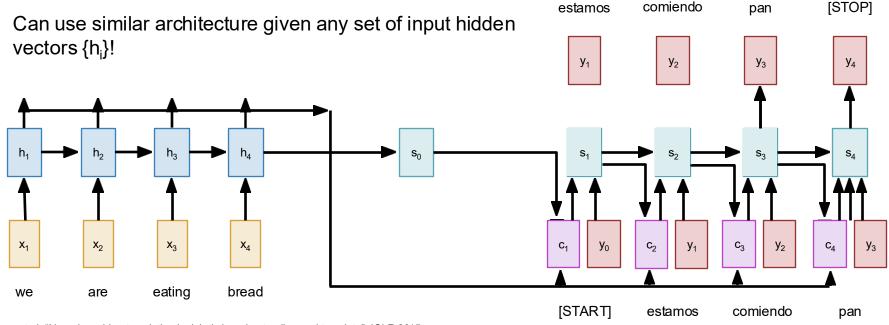
**Example**: English to French translation

Input: "The agreement on the European Economic Area was signed in August 1992."

Output: "L'accord sur la zone économique européenne a été signé en août 1992."

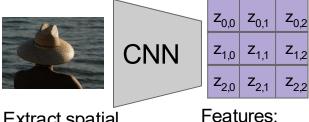
Visualize attention weights a<sub>ti</sub> accord **Diagonal attention means** sur words correspond in order zone Attention figures out économique different word orders européenne été signé août **Diagonal attention means** 1992 words correspond in order <end>

The decoder doesn't use the fact that h<sub>i</sub> form an ordered sequence – it just treats them as an unordered set {h<sub>i</sub>}



Input: Image I

**Output:** Sequence  $y = y_1, y_2, ..., y_T$ 



Extract spatial features from a pretrained CNN

Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

 $H \times W \times D$ 

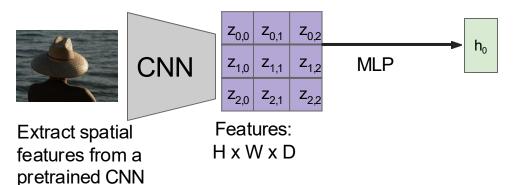
Input: Image I

**Output:** Sequence  $\mathbf{y} = \mathbf{y}_1, \mathbf{y}_2, ..., \mathbf{y}_T$ 

**Encoder**:  $h_0 = f_w(z)$ 

where **z** is spatial CNN features

fw(.) is an MLP

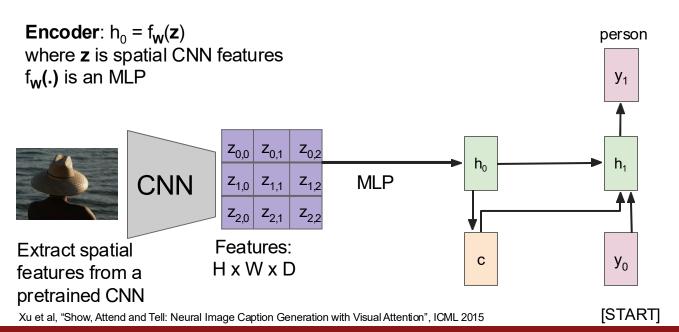


Input: Image I

**Output:** Sequence  $y = y_1, y_2, ..., y_T$ 

**Decoder**:  $y_t = g_v(y_{t-1}, h_{t-1}, c)$ 

where context vector c is often  $c = h_0$ 



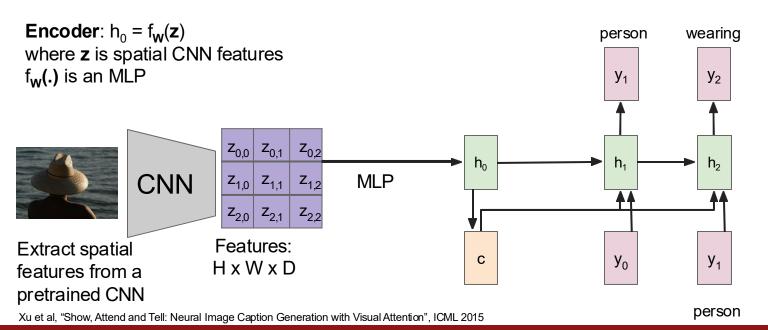
Chuang Gan and TAs

Input: Image I

**Output:** Sequence  $y = y_1, y_2, ..., y_T$ 

**Decoder**:  $y_t = g_V(y_{t-1}, h_{t-1}, c)$ 

where context vector c is often  $c = h_0$ 



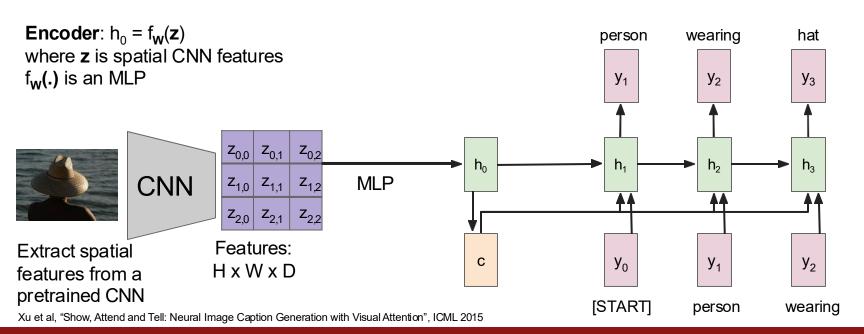
Chuang Gan and TAs

Input: Image I

**Output:** Sequence  $y = y_1, y_2, ..., y_T$ 

**Decoder**:  $y_t = g_V(y_{t-1}, h_{t-1}, c)$ 

where context vector c is often  $c = h_0$ 



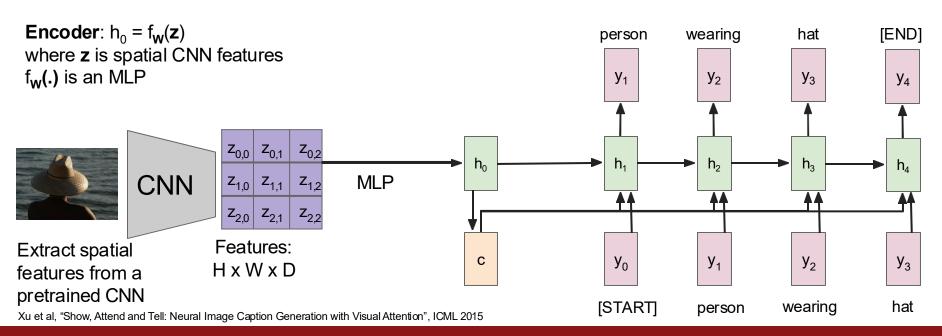
Chuang Gan and TAs

Input: Image I

**Output:** Sequence  $\mathbf{y} = \mathbf{y}_1, \mathbf{y}_2, ..., \mathbf{y}_T$ 

**Decoder**:  $y_t = g_V(y_{t-1}, h_{t-1}, c)$ 

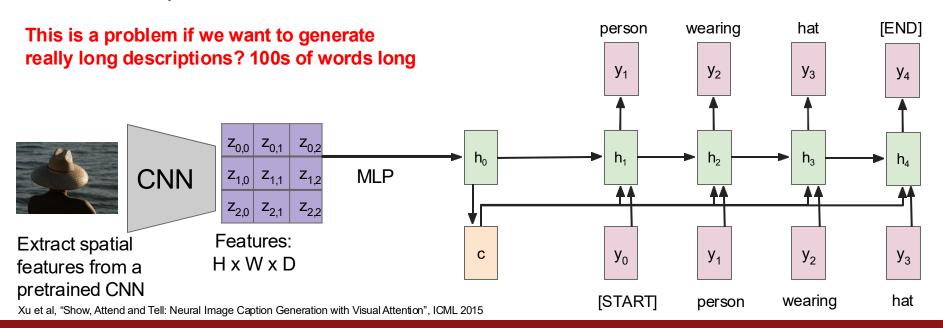
where context vector c is often  $c = h_0$ 



Chuang Gan and TAs

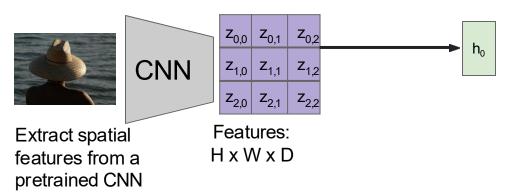
#### Problem: Input is "bottlenecked" through c

Model needs to encode everything it wants to say within c

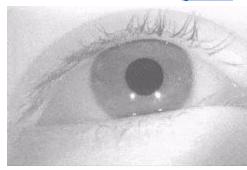


Attention idea: New context vector at every time step.

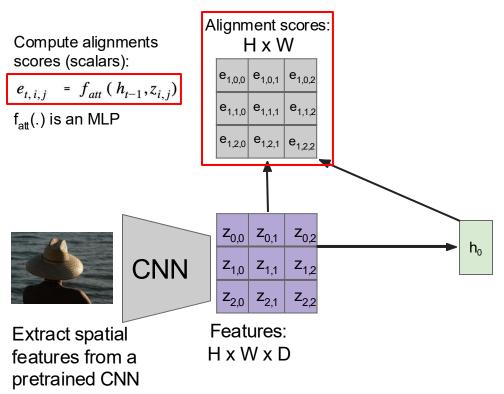
Each context vector will attend to different image regions

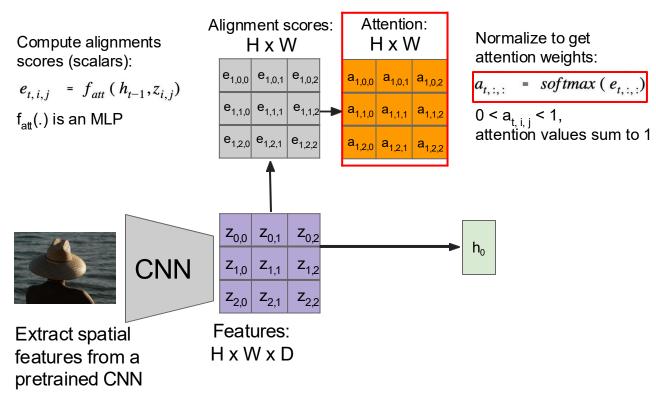


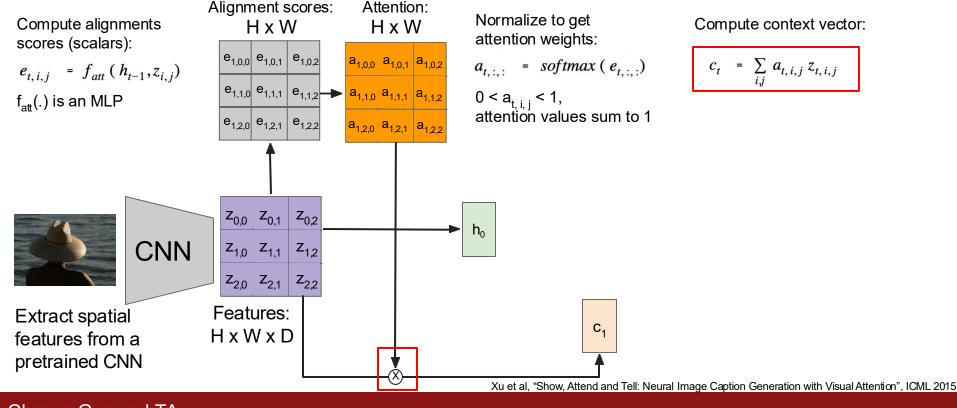
gif source



**Attention Saccades in humans** 





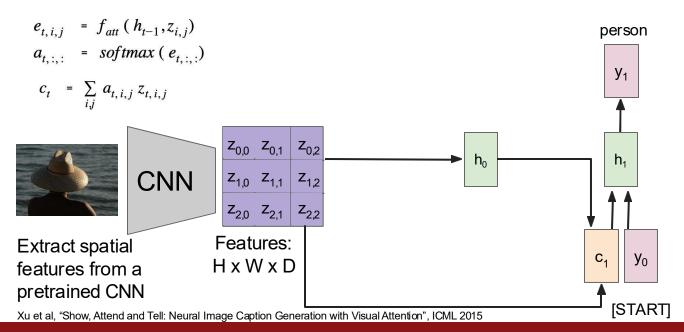


Chuang Gan and TAs

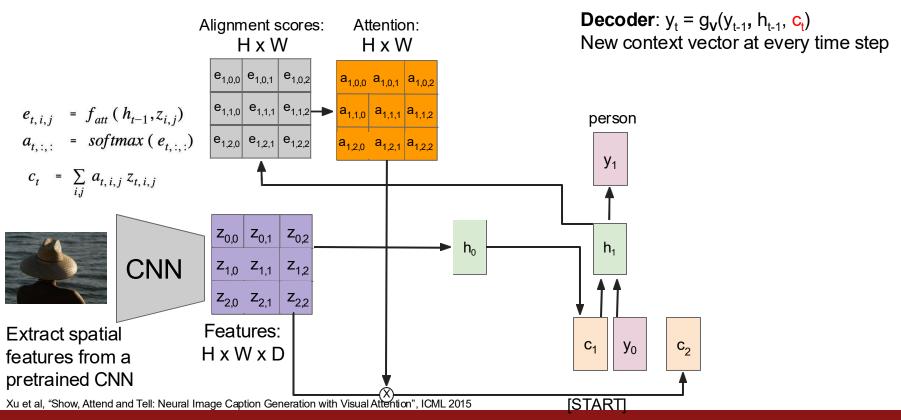
Some slides kindly provided by Fei-Fei Li, Jiajun Wu, Erik Learned-Miller

Each timestep of decoder uses a different context vector that looks at different parts of the input image

**Decoder**:  $y_t = g_v(y_{t-1}, h_{t-1}, c_t)$ New context vector at every time step



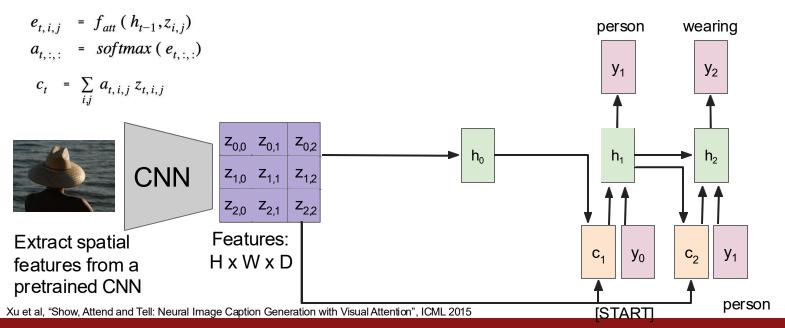
Chuang Gan and TAs



Chuang Gan and TAs

Each timestep of decoder uses a different context vector that looks at different parts of the input image

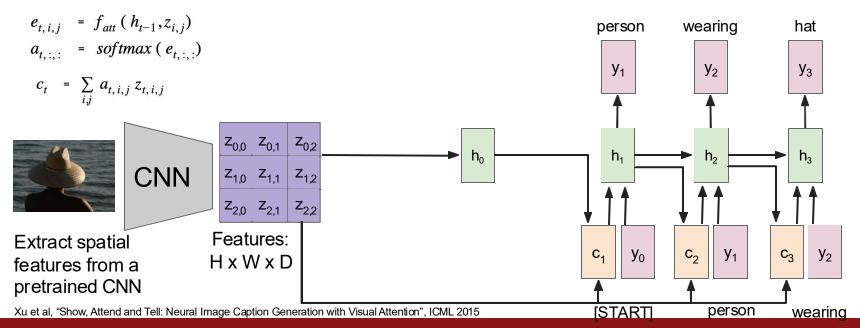
**Decoder**:  $y_t = g_v(y_{t-1}, h_{t-1}, c_t)$ New context vector at every time step



Chuang Gan and TAs

Each timestep of decoder uses a different context vector that looks at different parts of the input image

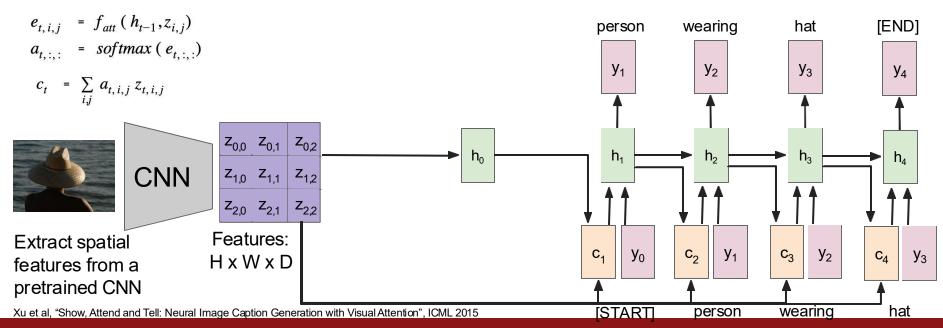
**Decoder**:  $y_t = g_v(y_{t-1}, h_{t-1}, c_t)$ New context vector at every time step



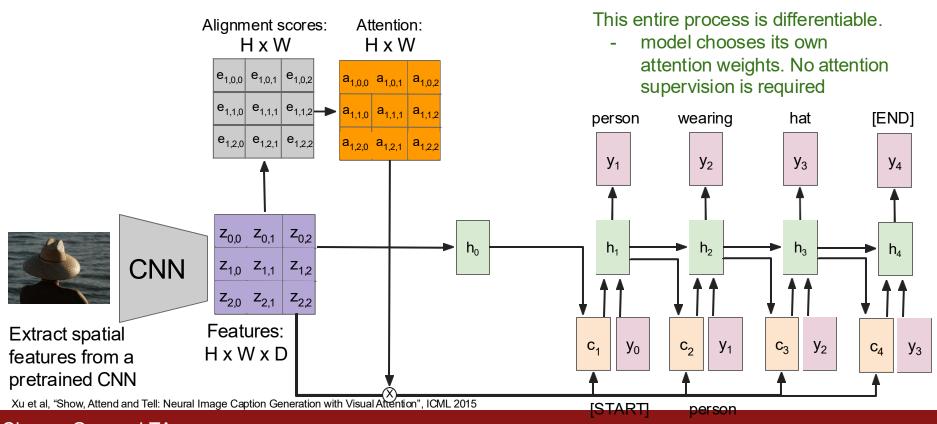
Chuang Gan and TAs

Each timestep of decoder uses a different context vector that looks at different parts of the input image

**Decoder**:  $y_t = g_v(y_{t-1}, h_{t-1}, c_t)$ New context vector at every time step



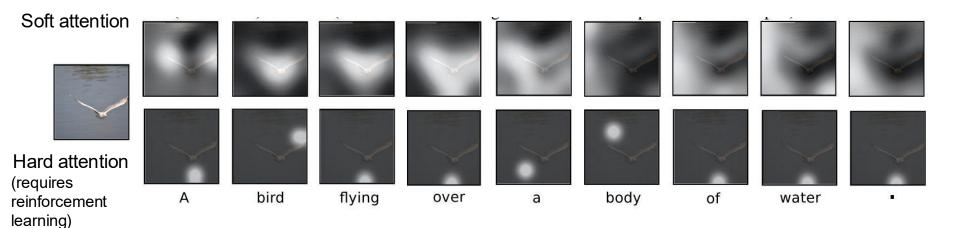
Chuang Gan and TAs



Chuang Gan and TAs

Some slides kindly provided by Fei-Fei Li, Jiajun Wu, Erik Learned-Miller

## Image Captioning with Attention



Xu et al, "Show, Attend, and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015
Figure copyright Kelvin Xu, Jimmy Lei Ba, Jamie Kiros, Kyunghyun Cho, Aaron Courville, Ruslan Salakhutdinov, Richard S. Zemel, and Yoshua Benchio, 2015. Reproduced with permission.

## Image Captioning with Attention



A woman is throwing a frisbee in a park.



A dog is standing on a hardwood floor.



A <u>stop</u> sign is on a road with a mountain in the background.



A little <u>girl</u> sitting on a bed with a teddy bear.



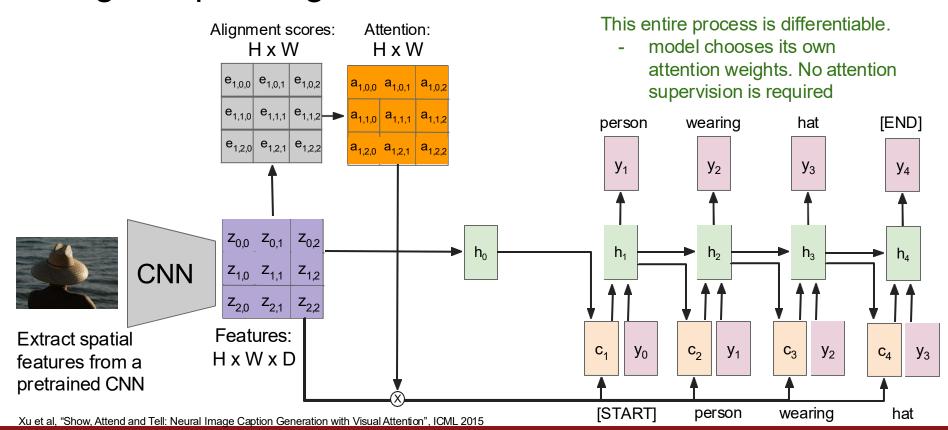
A group of <u>people</u> sitting on a boat in the water.



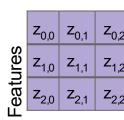
A giraffe standing in a forest with trees in the background.

Xu et al, "Show, Attend, and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

Figure copyright Kelvin Xu, Jimmy Lei Ba, Jamie Kiros, Kyunghyun Cho, Aaron Courville, Ruslan Salakhutdinov, Richard S. Zemel, and Yoshua Benchio, 2015. Reproduced with permission.



Chuang Gan and TAs



Inputs:

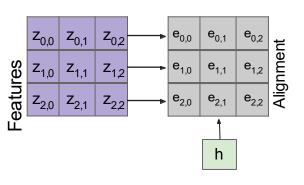
Features: **z** (shape: H x W x D)

Query: **h** (shape: D)

h

#### Operations:

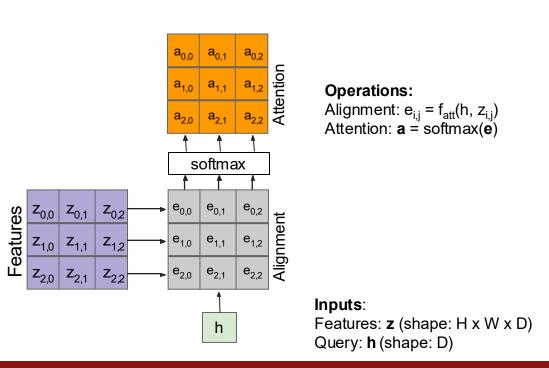
Alignment:  $e_{i,j} = f_{att}(h, z_{i,j})$ 

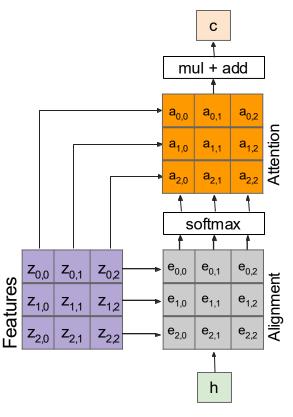


Inputs:

Features: **z** (shape: H x W x D)

Query: **h** (shape: D)





#### **Outputs:**

context vector: **c** (shape: D)

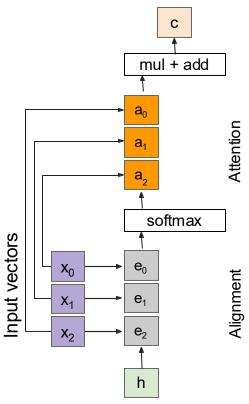
#### **Operations:**

Alignment:  $e_{i,j} = f_{att}(h, z_{i,j})$ Attention:  $\mathbf{a} = \text{softmax}(\mathbf{e})$ Output:  $\mathbf{c} = \sum_{i,j} a_{i,j} z_{i,j}$ 

Inputs:

Features: **z** (shape: H x W x D)

Query: h (shape: D)



#### **Outputs:**

context vector: **c** (shape: D)

#### **Operations:**

Alignment:  $e_i = f_{att}(h, x_i)$ Attention:  $\mathbf{a} = \text{softmax}(\mathbf{e})$ Output:  $\mathbf{c} = \sum_i a_i x_i$ 

Inputs:

Input vectors: **x** (shape: N x D)

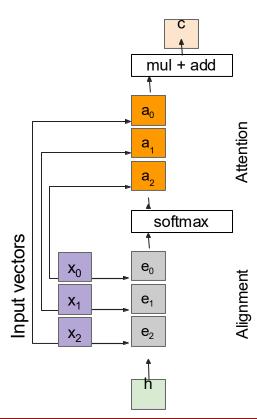
Query: **h** (shape: D)

Attention operation is **permutation invariant.** 

- Doesn't care about ordering of the features
  - Stretch H x W = N into N vectors

Chuang Gan and TAs

Miller



#### **Outputs:**

context vector: **c** (shape: D)

#### Operations:

Alignment:  $e_i = h \cdot x_i$ Attention:  $\mathbf{a} = \text{softmax}(\mathbf{e})$ Output:  $\mathbf{c} = \sum_i a_i x_i$ 

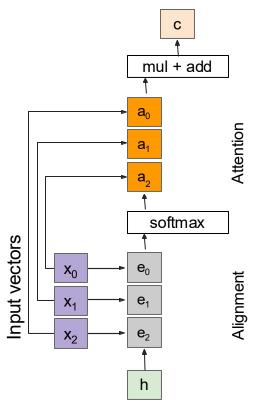
### Change f<sub>att</sub>(.) to a simple dot product

 only works well with key & value transformation trick (will mention in a few slides)

#### Inputs:

Input vectors: **x** (shape: N x D)

Query: **h** (shape: D)



#### Outputs:

context vector: **c** (shape: D)

#### **Operations:**

Alignment:  $e_i = h \cdot x_i / \sqrt{D}$ Attention:  $\mathbf{a} = \text{softmax}(\mathbf{e})$ Output:  $\mathbf{c} = \sum_i a_i x_i$ 

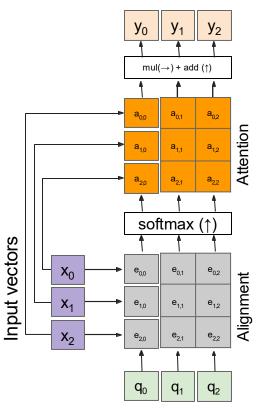
#### Inputs:

Input vectors: **x** (shape: N x D)

Query: h (shape: D)

Change f<sub>att</sub>(.) to a scaled simple dot product

- Larger dimensions means more terms in the dot product sum.
- So, the variance of the logits is higher.
   Large magnitude vectors will produce much higher logits.
- So, the post-softmax distribution has lower-entropy, assuming logits are IID.
- Ultimately, these large magnitude vectors will cause softmax to peak and assign very little weight to all others
- Divide by √D to reduce effect of large magnitude vectors



#### **Outputs:**

context vectors: **y** (shape: D)

#### **Operations:**

Alignment:  $e_{i,j} = q_j \cdot x_i / \sqrt{D}$ Attention:  $\mathbf{a} = \text{softmax}(\mathbf{e})$ Output:  $y_i = \sum_i a_{i,i} x_i$ 

#### Multiple query vectors

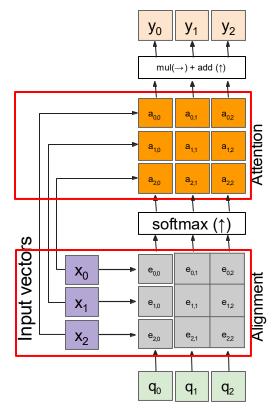
 each query creates a new output context vector

Inputs:

Input vectors: **x** (shape: N x D)

Queries: **q** (shape: M x D)

Multiple query vectors



#### **Outputs:**

context vectors: **y** (shape: D)

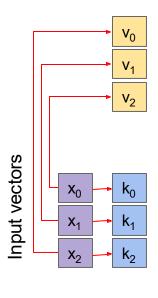
#### **Operations:**

Alignment:  $e_{i,j} = q_j \cdot x_i / \sqrt{D}$ Attention:  $\mathbf{a} = \text{softmax}(\mathbf{e})$ Output:  $y_i = \sum_i a_{i,i} x_i$  Notice that the input vectors are used for both the alignment as well as the attention calculations

 We can add more expressivity to the layer by adding a different FC layer before each of the two steps.

Inputs:

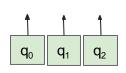
Input vectors: **x** (shape: N x D) Queries: **q** (shape: M x D)



#### **Operations:**

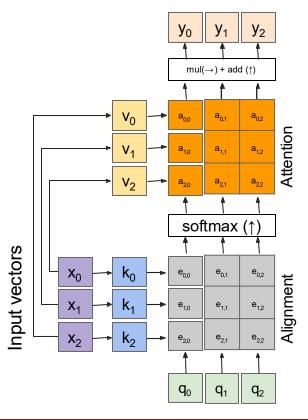
Key vectors:  $\mathbf{k} = \mathbf{x}\mathbf{W}_{\mathbf{k}}$ Value vectors:  $\mathbf{v} = \mathbf{x}\mathbf{W}_{\mathbf{v}}$  Notice that the input vectors are used for both the alignment as well as the attention calculations

 We can add more expressivity to the layer by adding a different FC layer before each of the two steps.



Inputs:

Input vectors:  $\mathbf{x}$  (shape: N x D) Queries:  $\mathbf{q}$  (shape: M x  $\mathbf{D}_k$ )



#### **Outputs:**

context vectors: **y** (shape: D<sub>v</sub>)

#### **Operations:**

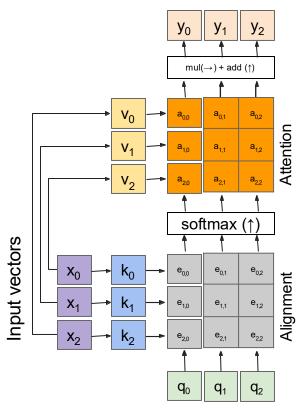
Key vectors:  $\mathbf{k} = \mathbf{x} \mathbf{W}_{\mathbf{k}}$ Value vectors:  $\mathbf{v} = \mathbf{x} \mathbf{W}_{\mathbf{v}}$ Alignment:  $\mathbf{e}_{i,j} = \mathbf{q}_{j} \cdot \mathbf{k}_{i} / \sqrt{D}$ Attention:  $\mathbf{a} = \operatorname{softmax}(\mathbf{e})$ Output:  $\mathbf{y}_{i} = \sum_{i} \mathbf{a}_{i,i} \mathbf{v}_{i}$  The input and output dimensions can now change depending on the key and value FC layers

Notice that the input vectors are used for both the alignment as well as the attention calculations.

 We can add more expressivity to the layer by adding a different FC layer before each of the two steps.

#### Inputs:

Input vectors:  $\mathbf{x}$  (shape: N x D) Queries:  $\mathbf{q}$  (shape: M x  $\mathbf{D}_k$ )



#### **Outputs:**

context vectors:  $\mathbf{y}$  (shape:  $D_{v}$ )

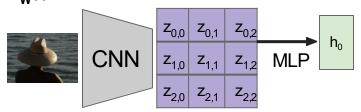
#### **Operations:**

Key vectors:  $\mathbf{k} = \mathbf{x} \mathbf{W}_{\mathbf{k}}$ Value vectors:  $\mathbf{v} = \mathbf{x} \mathbf{W}_{\mathbf{v}}$ Alignment:  $\mathbf{e}_{i,j} = \mathbf{q}_{j} \cdot \mathbf{k}_{i} / \sqrt{D}$ Attention:  $\mathbf{a} = \operatorname{softmax}(\mathbf{e})$ Output:  $\mathbf{y}_{i} = \sum_{i} \mathbf{a}_{i,i} \mathbf{v}_{i}$  Recall that the query vector was a function of the input vectors

**Encoder**:  $h_0 = f_{\mathbf{W}}(\mathbf{z})$ 

where **z** is spatial CNN features

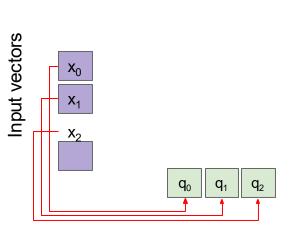
f<sub>w</sub>(.) is an MLP



#### Inputs:

Input vectors:  $\mathbf{x}$  (shape: N x D) Queries:  $\mathbf{q}$  (shape: M x  $\mathbf{p}_k$ )

## Self attention layer



#### Operations:

Key vectors:  $\mathbf{k} = \mathbf{x} \mathbf{W}_{\mathbf{k}}$ Value vectors:  $\mathbf{v} = \mathbf{x} \mathbf{W}_{\mathbf{v}}$ Query vectors:  $\mathbf{q} = \mathbf{x} \mathbf{W}_{\mathbf{q}}$ Alignment:  $\mathbf{e}_{\mathbf{i},\mathbf{j}} = \mathbf{q}_{\mathbf{j}} \cdot \mathbf{k}_{\mathbf{i}} / \sqrt{D}$ Attention:  $\mathbf{a} = \text{softmax}(\mathbf{e})$ 

Output:  $y_j = \sum_i a_{i,j} v_i$ 

We can calculate the query vectors from the input vectors, therefore, defining a "self-attention" layer.

Instead, query vectors are calculated using a FC layer.

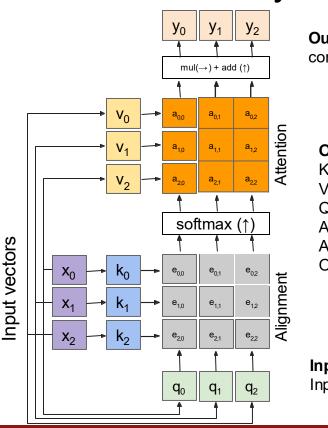
No input query vectors anymore

#### Inputs:

Input vectors: **x** (shape: N x D)

Queries: **q** (shape: M x D<sub>k</sub>)

## Self attention layer



#### **Outputs:**

context vectors:  $\mathbf{y}$  (shape:  $\mathbf{D}_{v}$ )

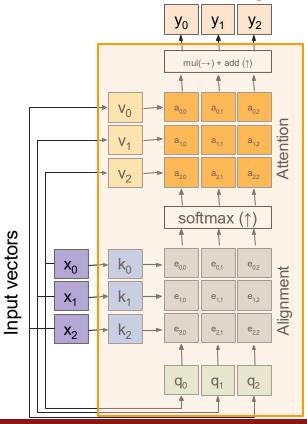
#### **Operations:**

Key vectors:  $\mathbf{k} = \mathbf{x} \mathbf{W}_{\mathbf{k}}$ Value vectors:  $\mathbf{v} = \mathbf{x} \mathbf{W}_{\mathbf{v}}$ Query vectors:  $\mathbf{q} = \mathbf{x} \mathbf{W}_{\mathbf{q}}$ Alignment:  $\mathbf{e}_{i,j} = \mathbf{q}_j \cdot \mathbf{k}_i / \sqrt{D}$ Attention:  $\mathbf{a} = \text{softmax}(\mathbf{e})$ Output:  $\mathbf{y}_i = \sum_i \mathbf{a}_{i,i} \mathbf{v}_i$ 

#### Inputs:

Input vectors: **x** (shape: N x D)

## Self attention layer - attends over sets of inputs

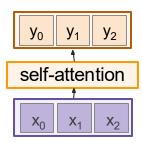


#### **Outputs:**

context vectors:  $\mathbf{y}$  (shape:  $\mathbb{D}_{v}$ )

#### **Operations:**

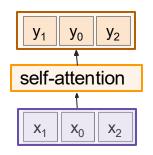
Key vectors:  $\mathbf{k} = \mathbf{x} \mathbf{W}_{\mathbf{k}}$ Value vectors:  $\mathbf{v} = \mathbf{x} \mathbf{W}_{\mathbf{v}}$ Query vectors:  $\mathbf{q} = \mathbf{x} \mathbf{W}_{\mathbf{q}}$ Alignment:  $\mathbf{e}_{i,j} = \mathbf{q}_j \cdot \mathbf{k}_i / \sqrt{D}$ Attention:  $\mathbf{a} = \text{softmax}(\mathbf{e})$ Output:  $\mathbf{y}_i = \sum_i \mathbf{a}_{i,i} \mathbf{v}_i$ 

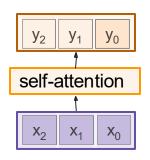


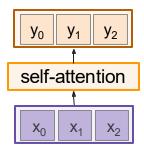
#### Inputs:

Input vectors: **x** (shape: N x D)

## Self attention layer - attends over sets of inputs



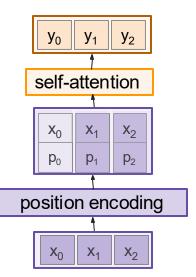




Permutation equivariant

Self-attention layer doesn't care about the orders of the inputs!

**Problem:** How can we encode ordered sequences like language or spatially ordered image features?



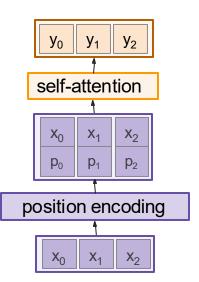
Concatenate/add special positional encoding  $p_i$  to each input vector  $x_i$ 

We use a function *pos*:  $N \rightarrow R^d$  to process the position j of the vector into a d-dimensional vector

So, 
$$p_i = pos(j)$$

#### Desiderata of pos(.):

- 1. It should output a **unique** encoding for each time-step (word's position in a sentence)
- Distance between any two time-steps should be consistent across sentences with different lengths.
- 3. Our model should generalize to **longer** sentences without any efforts. Its values should be bounded.
- 4. It must be **deterministic**.



Concatenate special positional encoding  $\mathbf{p}_i$  to each input vector  $\mathbf{x}_i$ 

We use a function *pos*:  $N \rightarrow \mathbb{R}^d$  to process the position j of the vector into a d-dimensional vector

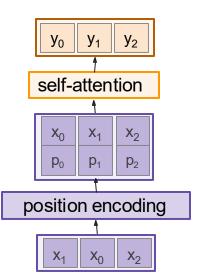
So, 
$$p_i = pos(j)$$

#### Options for pos(.)

- 1. Learn a lookup table:
  - Learn parameters to use for pos(t) for t ε [0, T)
  - Lookup table contains T x d parameters.

#### Desiderata of pos(.):

- 1. It should output a **unique** encoding for each time-step (word's position in a sentence)
- **2. Distance** between any two time-steps should be consistent across sentences with different lengths.
- 3. Our model should generalize to **longer** sentences without any efforts. Its values should be bounded.
- 4. It must be **deterministic**.



Concatenate special positional encoding  $p_i$  to each input vector  $x_i$ 

We use a function  $pos: N \rightarrow \mathbb{R}^d$  to process the position j of the vector into a d-dimensional vector

So, 
$$p_i = pos(j)$$

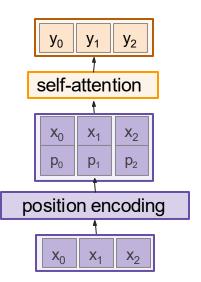
#### Options for pos(.)

- 1. Learn a lookup table:
  - Learn parameters to use for pos(t) for t ε [0, T)
  - Lookup table contains T x d parameters.
- 2. Design a fixed function with the desiderata

$$\mathbf{p(t)} = egin{bmatrix} \sin(\omega_1.\,t) \\ \cos(\omega_1.\,t) \\ \sin(\omega_2.\,t) \\ \cos(\omega_2.\,t) \\ & \vdots \\ \sin(\omega_{d/2}.\,t) \\ \cos(\omega_{d/2}.\,t) \end{bmatrix}_d$$

where 
$$\omega_k=rac{1}{10000^{2k/d}}$$

Vaswani et al, "Attention is all you need", NeurIPS 2017



Concatenate special positional encoding  $\mathbf{p}_i$  to each input vector  $\mathbf{x}_i$ 

We use a function *pos*:  $N \rightarrow R^d$  to process the position j of the vector into a d-dimensional vector

So, 
$$p_i = pos(j)$$

#### Options for pos(.)

- Learn a lookup table:
  - Learn parameters to use for pos(t) for t ε [0, T)
  - Lookup table contains T x d parameters.
- 2. Design a fixed function with the desiderata

# $\mathbf{p(t)} = egin{bmatrix} \sin(\omega_1.t) \ \cos(\omega_1.t) \ & \sin(\omega_2.t) \ & \cos(\omega_2.t) \ & \vdots \ & \sin(\omega_{d/2}.t) \ \end{pmatrix}$

 $\cos(\omega_{d/2}.\,t)$ 

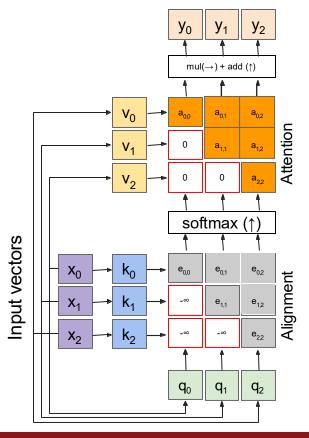
#### Intuition:

where  $\omega_k = rac{1}{10000^{2k/d}}$ 

image source

Vaswani et al, "Attention is all you need", NeurIPS 2017

## Masked self-attention layer



#### **Outputs:**

context vectors:  $\mathbf{y}$  (shape:  $D_{v}$ )

#### Operations:

Key vectors:  $\mathbf{k} = \mathbf{x} \mathbf{W}_{\mathbf{k}}$ Value vectors:  $\mathbf{v} = \mathbf{x} \mathbf{W}_{\mathbf{v}}$ Query vectors:  $\mathbf{q} = \mathbf{x} \mathbf{W}_{\mathbf{q}}$ Alignment:  $\mathbf{e}_{i,j} = \mathbf{q}_j \cdot \mathbf{k}_i / \sqrt{D}$ Attention:  $\mathbf{a} = \operatorname{softmax}(\mathbf{e})$ Output:  $\mathbf{y}_i = \sum_i \mathbf{a}_{i,i} \mathbf{v}_i$ 

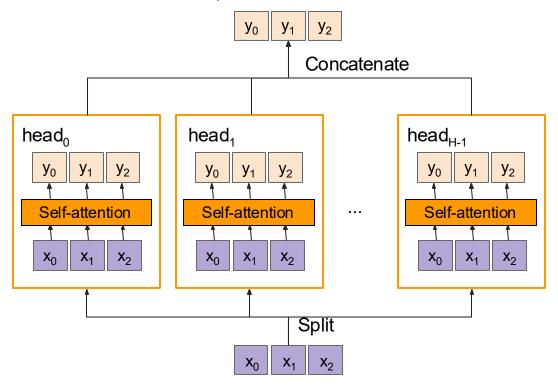
#### Inputs:

Input vectors: **x** (shape: N x D)

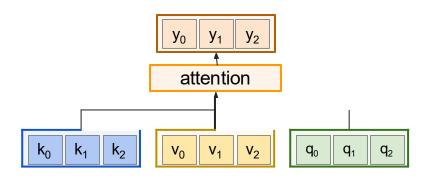
- Prevent vectors from looking at future vectors.
- Manually set alignment scores to -infinity

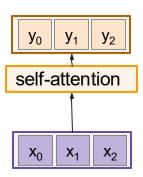
## Multi-head self-attention layer

- Multiple self-attention heads in parallel



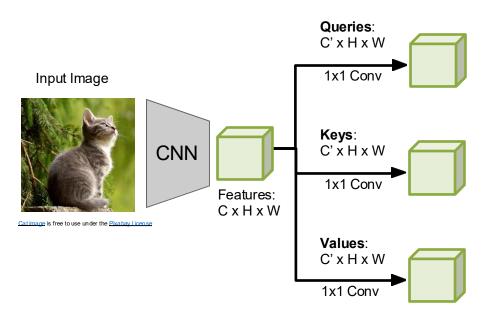
## General attention versus self-attention

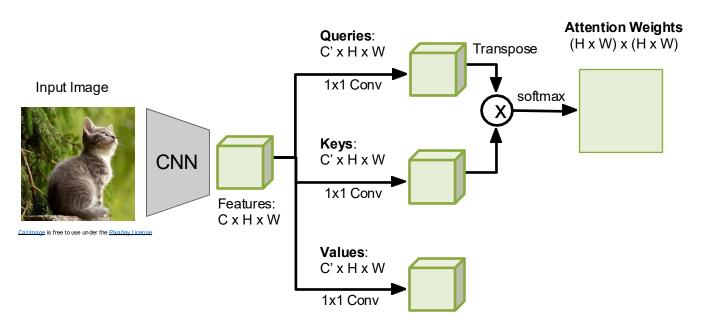


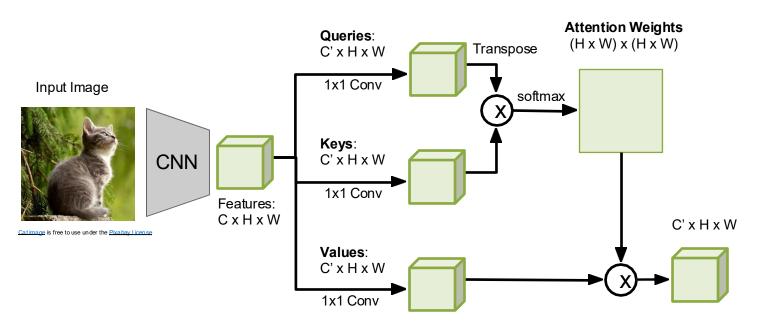


#### Input Image

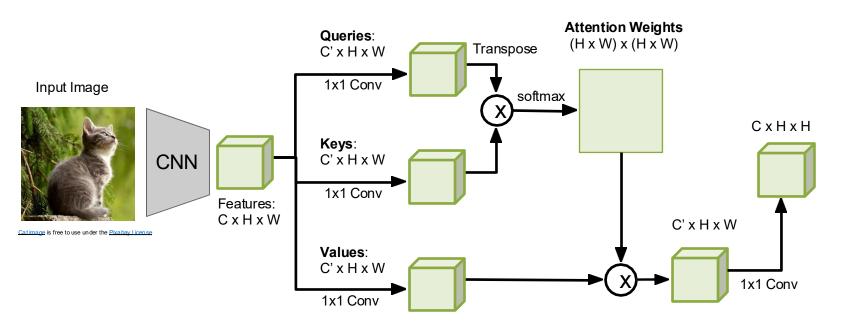








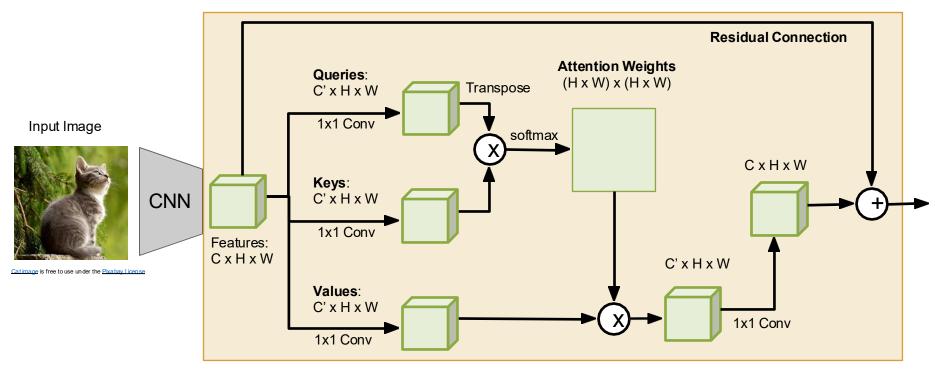
## Example: CNN with Self-Attention



Zhang et al, "Self-Attention Generative Adversarial Networks", ICML 2018

Slide credit Justin Johnson

## Example: CNN with Self-Attention



Self-Attention Module

Zhang et al, "Self-Attention Generative Adversarial Networks", ICML 2018

## Comparing RNNs to Transformer

#### **RNNs**

- (+) LSTMs work reasonably well for long sequences.
- (-) Expects an ordered sequences of inputs
- (-) Sequential computation: subsequent hidden states can only be computed after the previous ones are done.

#### Transformer:

- (+) Good at long sequences. Each attention calculation looks at all inputs.
- (+) Can operate over unordered sets or ordered sequences with positional encodings.
- (+) Parallel computation: All alignment and attention scores for all inputs can be done in parallel.
- (-) Requires a lot of memory: N x M alignment and attention scalers need to be calculated and stored for a single self-attention head. (but GPUs are getting bigger and better)

#### **Attention Is All You Need**

Ashish Vaswani\* Google Brain avaswani@google.com

> Llion Jones\* Google Research llion@google.com

Noam Shazeer\* Google Brain noam@google.com

Google Research nikip@google.com

Niki Parmar\*

Google Research usz@google.com

Jakob Uszkoreit\*

Łukasz Kaiser\* Google Brain

lukaszkaiser@google.com

Illia Polosukhin\* ‡ illia.polosukhin@gmail.com

Aidan N. Gomez\* †

University of Toronto

aidan@cs.toronto.edu

"ImageNet Moment for Natural Language Processing"

#### Pretraining:

Download a lot of text from the internet

Train a giant Transformer model for language modeling

#### **Finetuning:**

Fine-tune the Transformer on your own NLP task

Chuang Gan and TAs Some slides kindly provided by Fei-Fei Li, Jiajun Wu, Erik Learned-Miller

Lecture 17 - 76

# On the Opportunities and Risks of Foundation Models

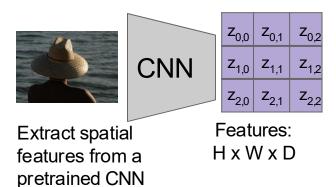
Rishi Bommasani\* Drew A. Hudson Ehsan Adeli Russ Altman Simran Arora Sydney von Arx Michael S. Bernstein Jeannette Bohg Antoine Bosselut Emma Brunskill Erik Brynjolfsson Shyamal Buch Dallas Card Rodrigo Castellon Niladri Chatterji Annie Chen Kathleen Creel Jared Quincy Davis Dorottya Demszky Chris Donahue Moussa Doumbouya Esin Durmus Stefano Ermon John Etchemendy Kawin Ethayarajh Li Fei-Fei Chelsea Finn Trevor Gale Lauren Gillespie Karan Goel Noah Goodman Shelby Grossman Neel Guha Tatsunori Hashimoto Peter Henderson John Hewitt Daniel E. Ho Jenny Hong Kyle Hsu Jing Huang Thomas Icard Saahil Jain Dan Jurafsky Pratyusha Kalluri Siddharth Karamcheti Geoff Keeling Fereshte Khani Omar Khattab Pang Wei Koh Mark Krass Ranjay Krishna Rohith Kuditipudi Ananya Kumar Faisal Ladhak Mina Lee Tony Lee Jure Leskovec Isabelle Levent Xiang Lisa Li Xuechen Li Tengyu Ma Ali Malik Christopher D. Manning Suvir Mirchandani Eric Mitchell Zanele Munyikwa Suraj Nair Avanika Narayan Deepak Narayanan Ben Newman Allen Nie Juan Carlos Niebles Hamed Nilforoshan Julian Nyarko Giray Ogut Laurel Orr Isabel Papadimitriou Joon Sung Park Chris Piech Eva Portelance Christopher Potts Aditi Raghunathan Rob Reich Hongyu Ren Frieda Rong Yusuf Roohani Camilo Ruiz Jack Ryan Christopher Ré Dorsa Sadigh Shiori Sagawa Keshav Santhanam Andy Shih Krishnan Srinivasan Alex Tamkin Rohan Taori Armin W. Thomas Florian Tramèr Rose E. Wang William Wang Bohan Wu Jiajun Wu Yuhuai Wu Sang Michael Xie Michihiro Yasunaga Jiaxuan You Matei Zaharia Michael Zhang Tianyi Zhang Xikun Zhang Yuhui Zhang Lucia Zheng Kaitlyn Zhou Percy Liang\*1

Center for Research on Foundation Models (CRFM)
Stanford Institute for Human-Centered Artificial Intelligence (HAI)
Stanford University

## Image Captioning using Transformers

Input: Image I

**Output:** Sequence  $y = y_1, y_2, ..., y_T$ 

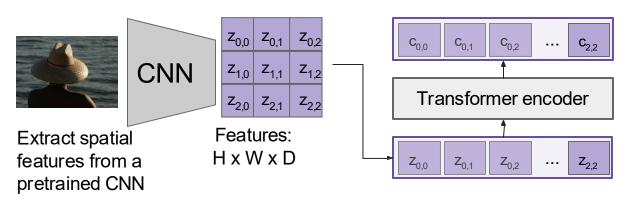


## Image Captioning using Transformers

Input: Image I

**Output:** Sequence  $y = y_1, y_2,..., y_T$ 

**Encoder**:  $\mathbf{c} = T_{\mathbf{w}}(\mathbf{z})$  where  $\mathbf{z}$  is spatial CNN features  $T_{\mathbf{w}}(.)$  is the transformer encoder



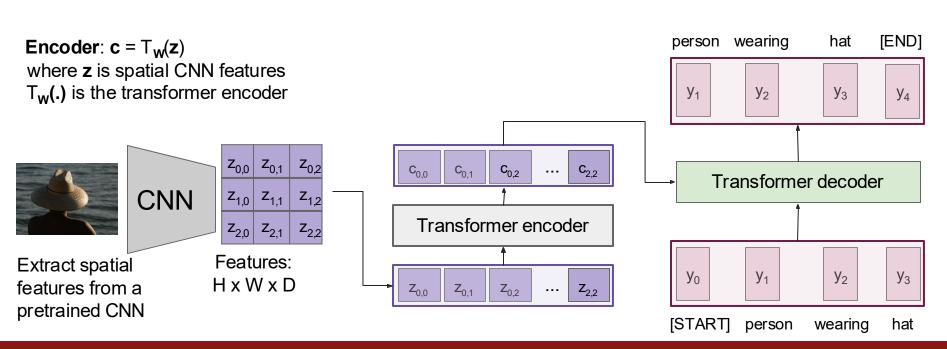
## Image Captioning using Transformers

Input: Image I

**Output:** Sequence  $\mathbf{y} = \mathbf{y}_1, \mathbf{y}_2, ..., \mathbf{y}_T$ 

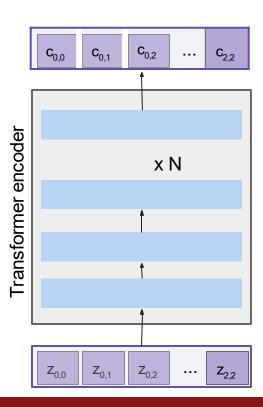
**Decoder**:  $y_t = T_D(y_{0:t-1}, c)$ 

where  $T_D(.)$  is the transformer decoder



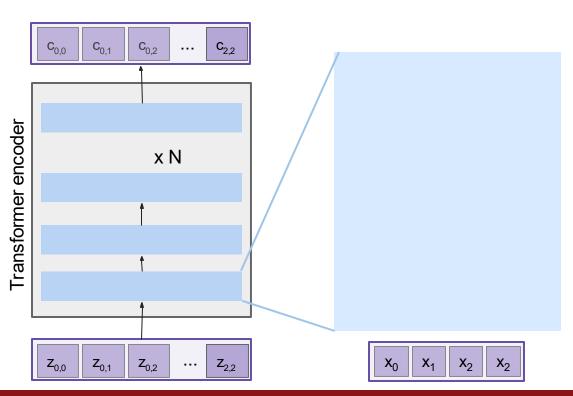
Chuang Gan and TAs

Lecture 17 - 80

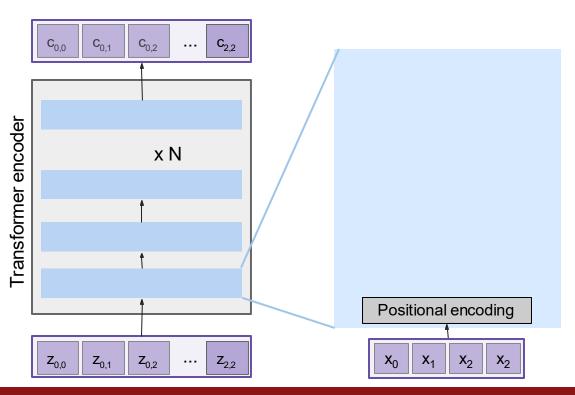


Made up of N encoder blocks.

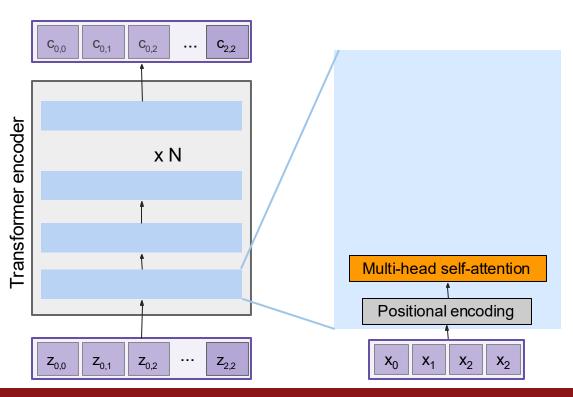
In vaswani et al. N = 6,  $D_q$ = 512



Let's dive into one encoder block



Add positional encoding



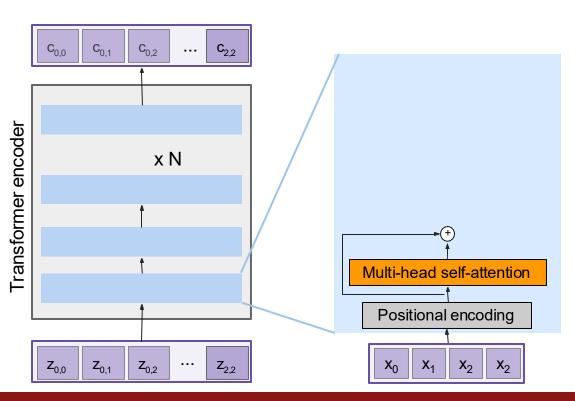
Attention attends over all the vectors

Add positional encoding

Vaswani et al, "Attention is all you need", NeurIPS 2017

Chuang Gan and TAs Some slides kindly provided by Fei-Fei Li, Jiajun Wu, Erik Learned-Miller

Lecture 17 - 84



Residual connection

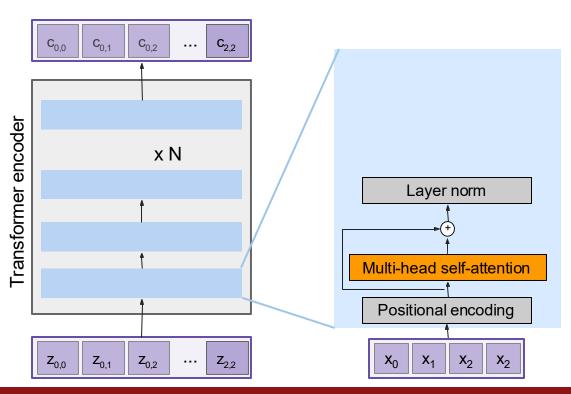
Attention attends over all the vectors

Add positional encoding

Vaswani et al, "Attention is all you need", NeurIPS 2017

Chuang Gan and TAs Some slides kindly provided by Fei-Fei Li, Jiajun Wu, Erik Learned-Miller

Lecture 17 - 85

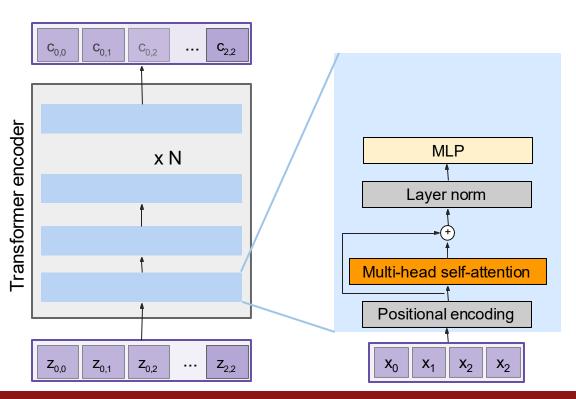


LayerNorm over each vector individually

Residual connection

Attention attends over all the vectors

Add positional encoding



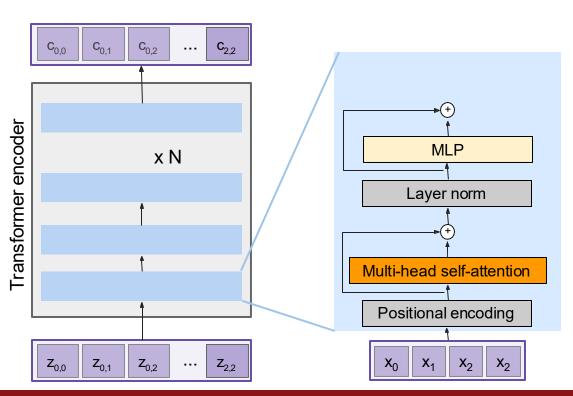
MLP over each vector individually

LayerNorm over each vector individually

Residual connection

Attention attends over all the vectors

Add positional encoding



#### Residual connection

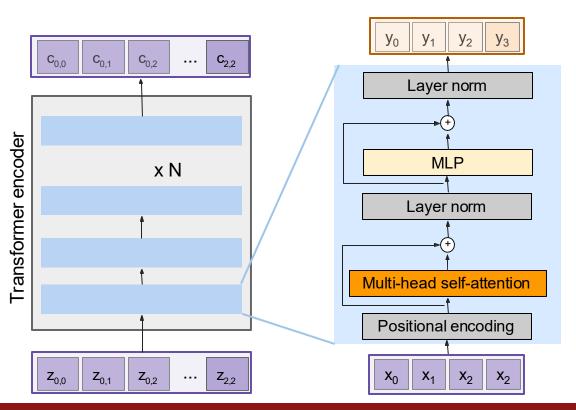
MLP over each vector individually

LayerNorm over each vector individually

Residual connection

Attention attends over all the vectors

Add positional encoding



#### **Transformer Encoder Block:**

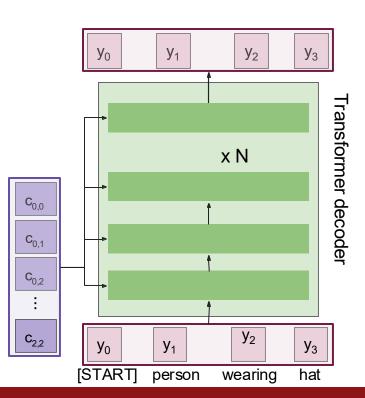
Inputs: Set of vectors x
Outputs: Set of vectors y

Self-attention is the only interaction between vectors.

Layer norm and MLP operate independently per vector.

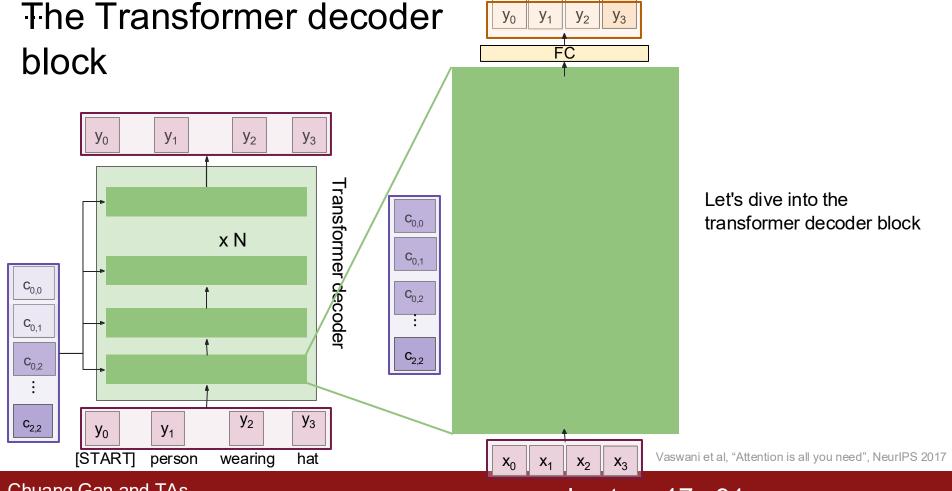
Highly scalable, highly parallelizable, but high memory usage.

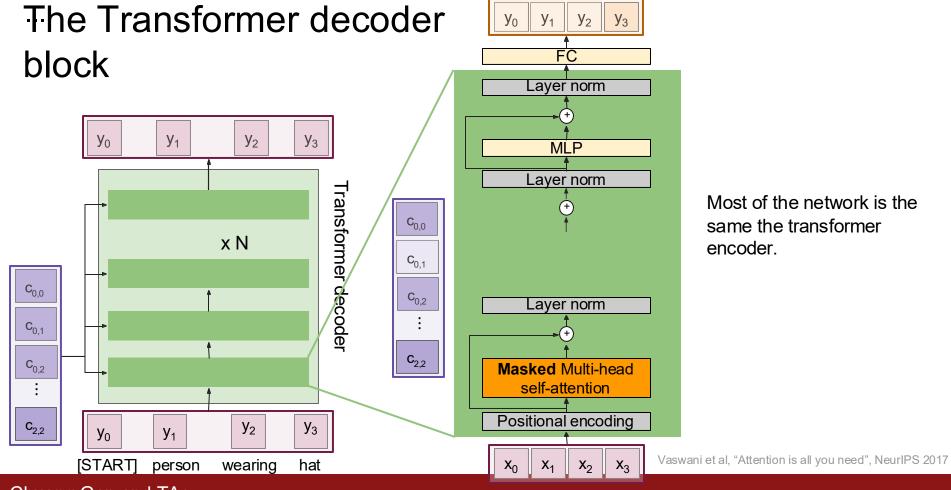
person wearing hat [END]

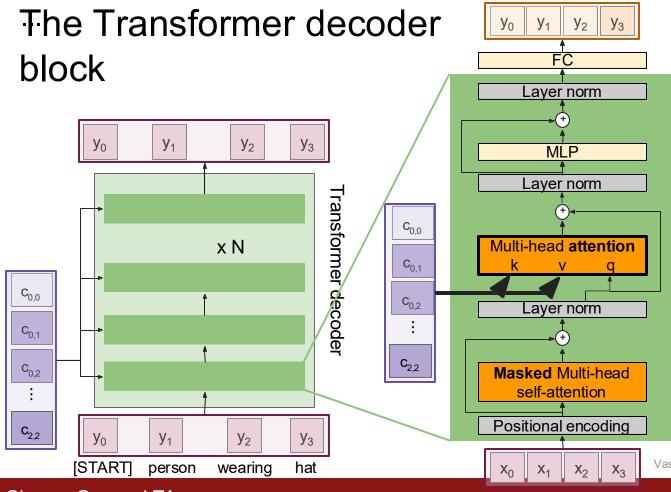


Made up of N decoder blocks.

In vaswani et al. N = 6,  $D_d = 512$ 

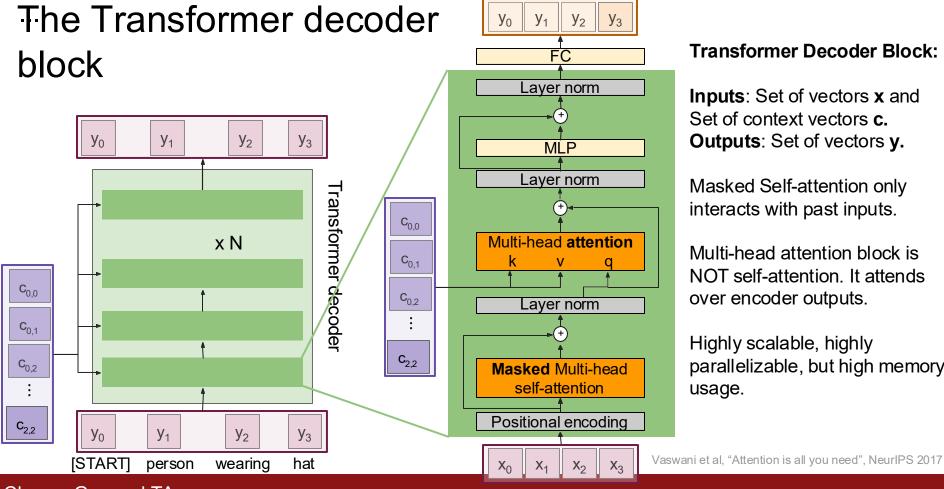






Multi-head attention block attends over the transformer encoder outputs.

For image captioning, this is how we inject image features into the decoder.



**Transformer Decoder Block:** 

**Inputs**: Set of vectors **x** and Set of context vectors **c**. Outputs: Set of vectors y.

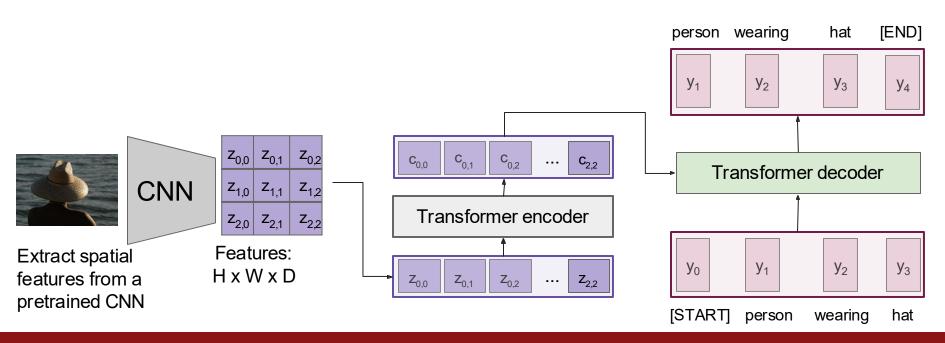
Masked Self-attention only interacts with past inputs.

Multi-head attention block is NOT self-attention. It attends over encoder outputs.

Highly scalable, highly parallelizable, but high memory usage.

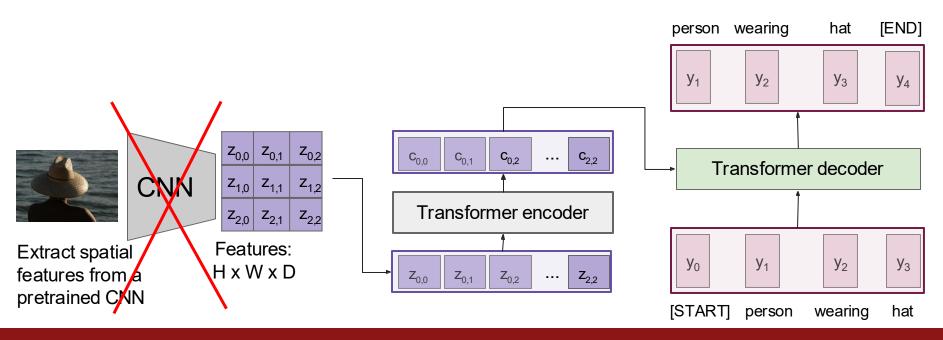
## Image Captioning using transformers

No recurrence at all



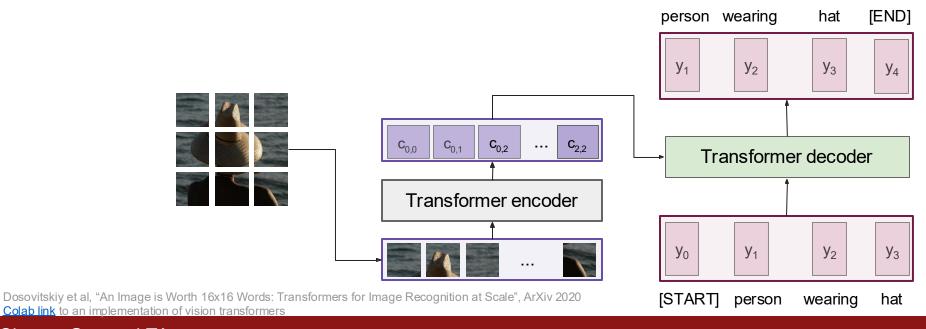
## Image Captioning using transformers

- Perhaps we don't need convolutions at all?



## Image Captioning using transformers

- Transformers from pixels to language



### Vision Transformers vs. ResNets

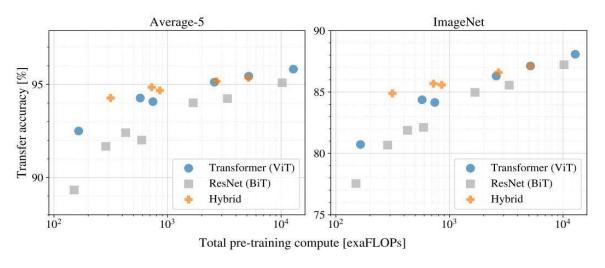
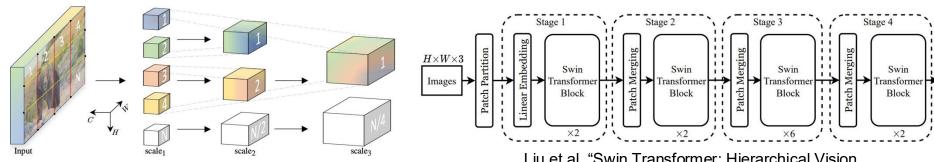


Figure 5: Performance versus cost for different architectures: Vision Transformers, ResNets, and hybrids. Vision Transformers generally outperform ResNets with the same computational budget. Hybrids improve upon pure Transformers for smaller model sizes, but the gap vanishes for larger models.

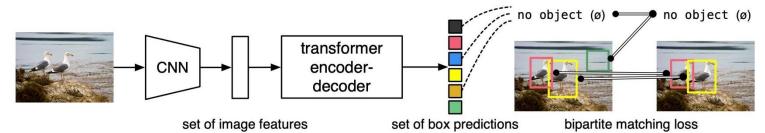
Dosovitskiy et al, "An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale", ArXiv 2020 Colab link to an implementation of vision transformers

#### **Vision Transformers**



Fan et al, "Multiscale Vision Transformers", ICCV 2021

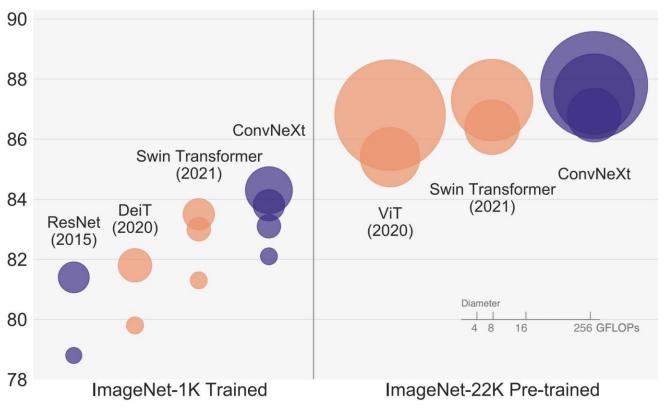
Liu et al, "Swin Transformer: Hierarchical Vision Transformer using Shifted Windows", CVPR 2021



Carion et al, "End-to-End Object Detection with Transformers", ECCV 2020

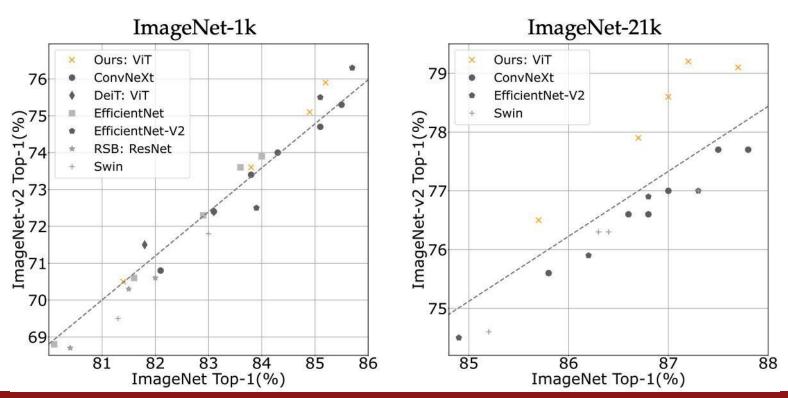
#### ConvNets strike back!

ImageNet-1K Acc.



#### DeiT III: Revenge of the ViT

Hugo Touvron\*,† Matthieu Cord† Hervé Jégou\*



# Summary

- Adding attention to RNNs allows them to "attend" to different parts of the input at every time step
- The **general attention layer** is a new type of layer that can be used to design new neural network architectures
- **Transformers** are a type of layer that uses **self-attention** and layer norm.
  - It is highly scalable and highly parallelizable
  - Faster training, larger models, better performance across vision and language tasks
  - They are quickly replacing RNNs, LSTMs, and may(?) even replace convolutions.