

Introduction to Networks

Aaron Clauset

 @aaronclauset

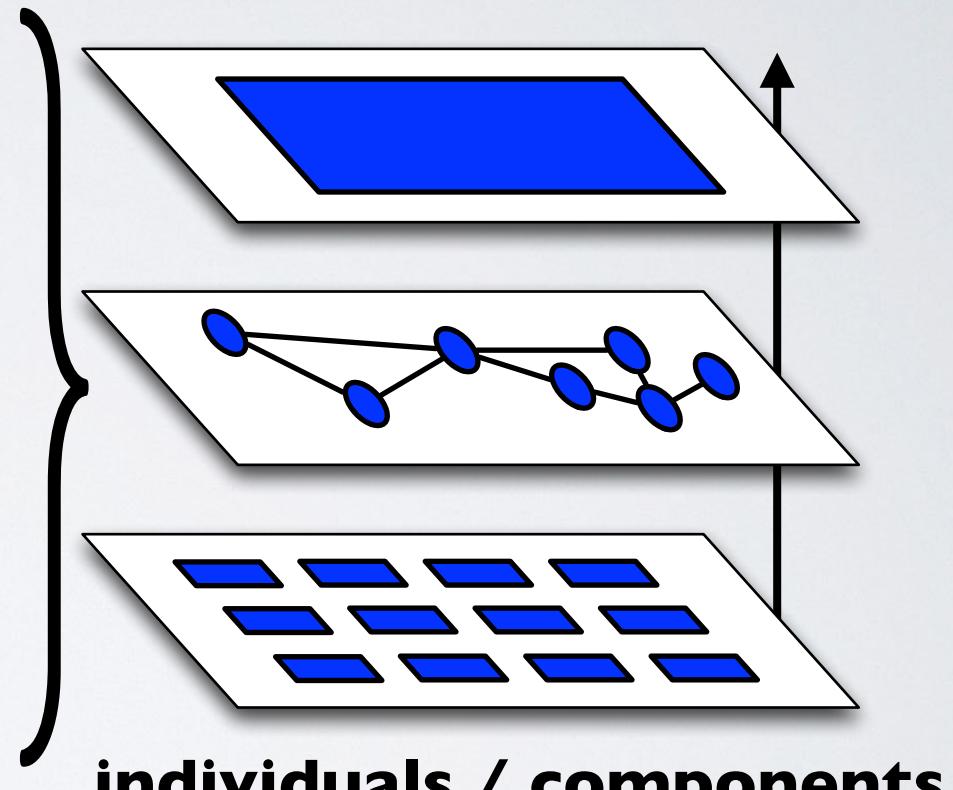
Associate Professor of Computer Science
University of Colorado Boulder
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what are networks?

what are networks?

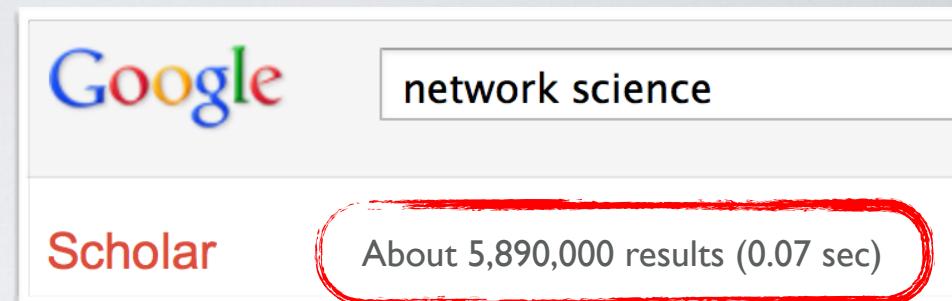
- an approach
- a mathematical representation
- provide structure to complexity
- *structure above* individuals / components
- *structure below* system / population

system / population



this lecture

- build intuition
- highlight a few concepts & questions
- provide some examples
- pointers to further study
- not a substitute for technical coursework



it's a big field now

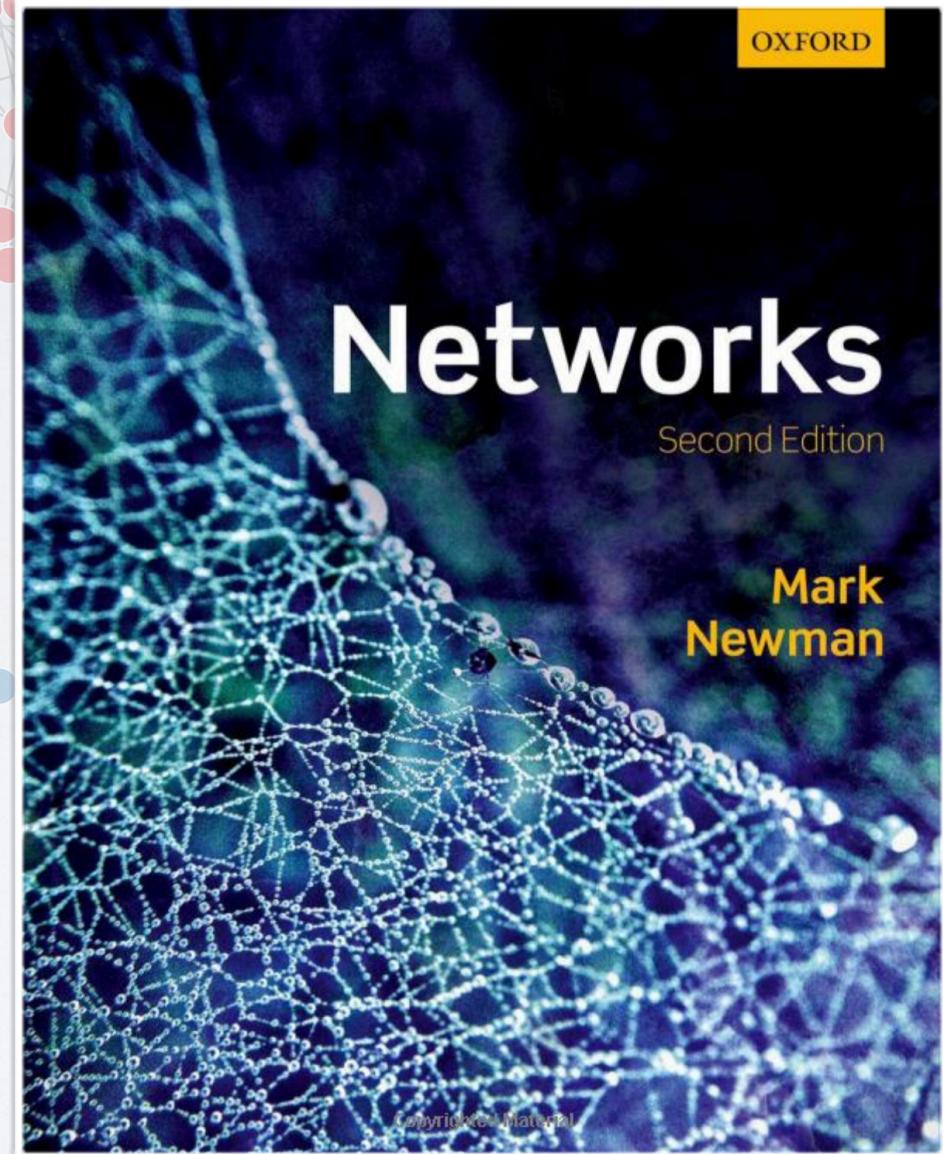


Mark Newman

Professor of Physics
University of Michigan

External Faculty
Santa Fe Institute

<http://www-personal.umich.edu/~mejn/>





University of Colorado **Boulder**

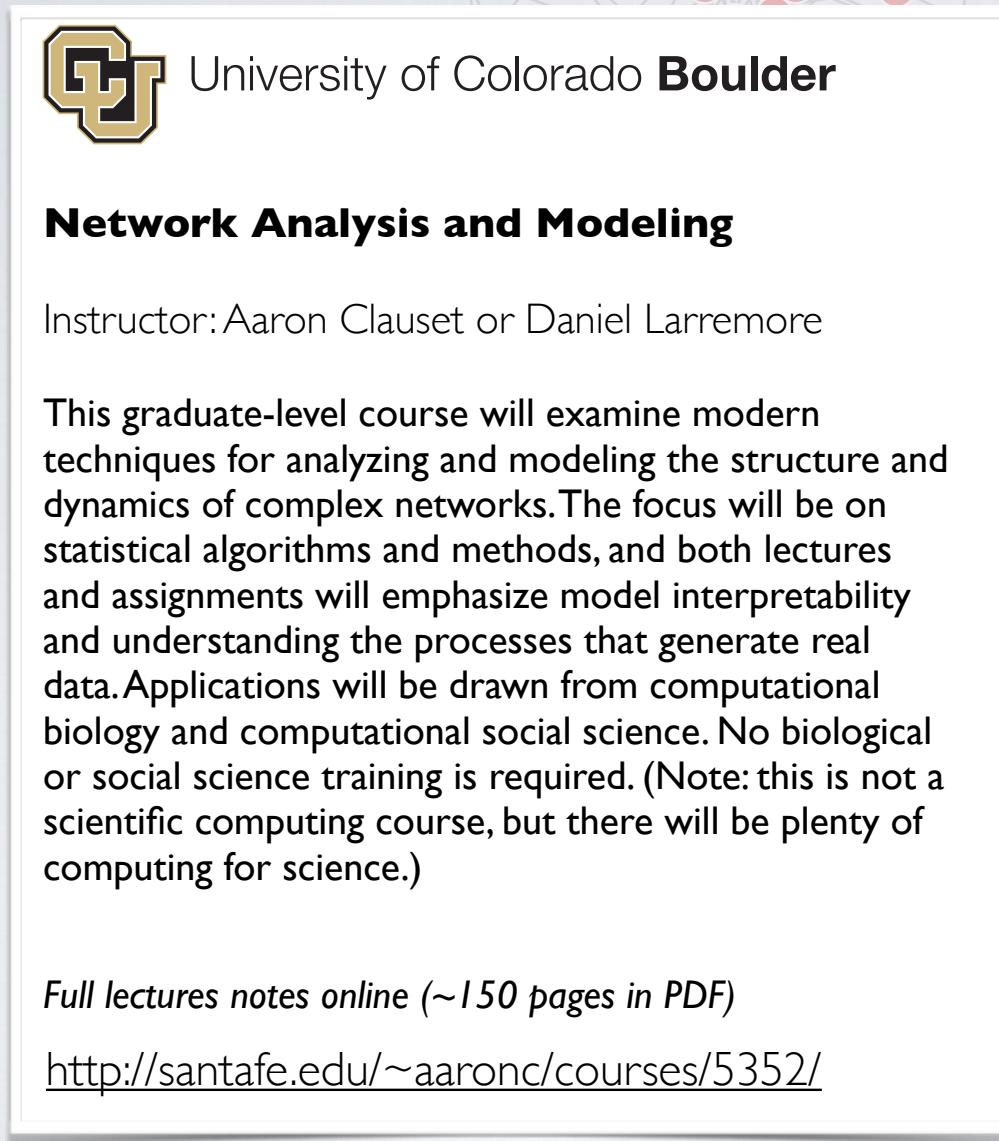
Network Analysis and Modeling

Instructor: Aaron Clauset or Daniel Larremore

This graduate-level course will examine modern techniques for analyzing and modeling the structure and dynamics of complex networks. The focus will be on statistical algorithms and methods, and both lectures and assignments will emphasize model interpretability and understanding the processes that generate real data. Applications will be drawn from computational biology and computational social science. No biological or social science training is required. (Note: this is not a scientific computing course, but there will be plenty of computing for science.)

Full lectures notes online (~150 pages in PDF)

<http://santafe.edu/~aarond/courses/5352/>



Software

R

Python

Matlab

NetworkX [python]

graph-tool [python, c++]

GraphLab [python, c++]

Standalone editors

UCI-Net

NodeXL

Gephi

Pajek

Network Workbench

Cytoscape

yEd graph editor

Graphviz

Network data sets

Colorado Index of Complex Networks

The screenshot shows a web browser window for 'icon.colorado.edu/#!/'. The title bar says 'icon.colorado.edu/#!/'. The main content area has a dark header with 'Index of Complex Networks' on the left and 'NETWORKS', 'ABOUT', and 'SUGGEST...' tabs on the right. Below the header, there's a large white area with some text and a bar chart.

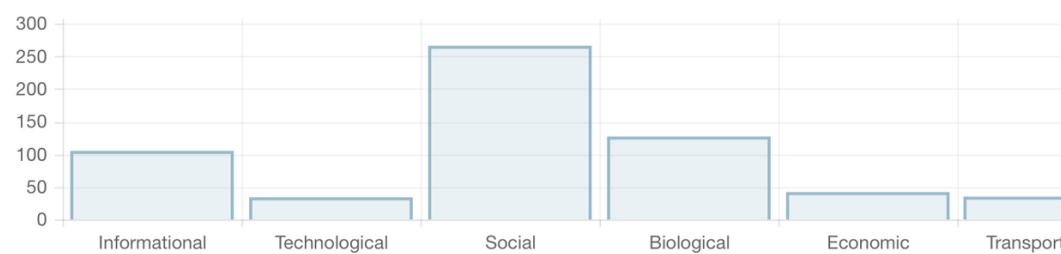
The Colorado Index of Complex Networks (ICON)

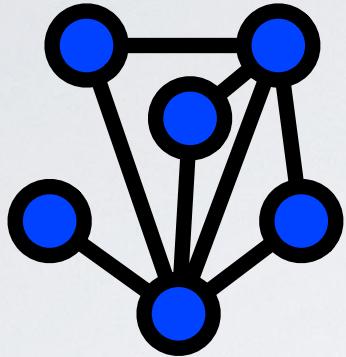
ICON is a comprehensive index of research-quality network data sets from all domains of networks, including social, web, information, biological, ecological, connectome, transportation, and technological networks.

Each network record in the index is annotated with and searchable or browsable by its graph properties, description, size, etc., and many records include links to multiple networks. The contents of ICON are curated by volunteer experts from Prof. Aaron Clauset's research group at the University of Colorado Boulder.

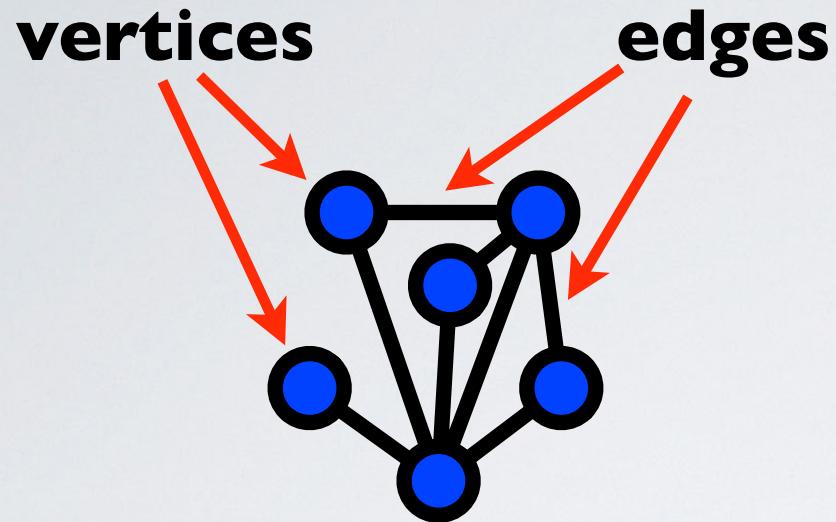
Click on the [NETWORKS tab](#) above to get started.

Entries found: 609 Networks found: 4419





🤔 **the two most fundamental
questions in network science**



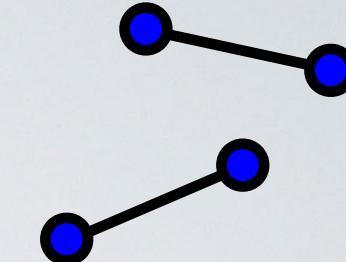
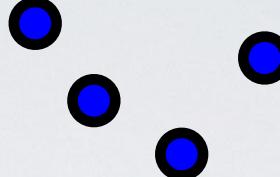
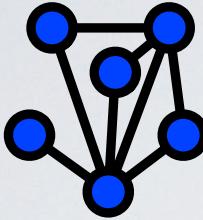
what is a vertex?

V distinct objects (vertices / nodes / actors)

when are two vertices connected?

$$E \subseteq V \times V$$

pairwise relations (edges / links / ties)

informational telecommunications**transportation****network**

Internet(1)

Internet(2)

software

World Wide Web

documents

power grid transmission

rail system

road network(1)

road network(2)

airport network

friendship network

sexual network

metabolic network

protein-interaction network

gene regulatory network

neuronal network

food web

vertex

computer

autonomous system (ISP)

function

web page

article, patent, or legal case

generating or relay station

rail station

intersection

named road

airport

person

person

metabolite

protein

gene

neuron

species

edge

IP network adjacency

BGP connection

function call

hyperlink

citation

transmission line

railroad tracks

pavement

intersection

non-stop flight

friendship

intercourse

metabolic reaction

bonding

regulatory effect

synapse

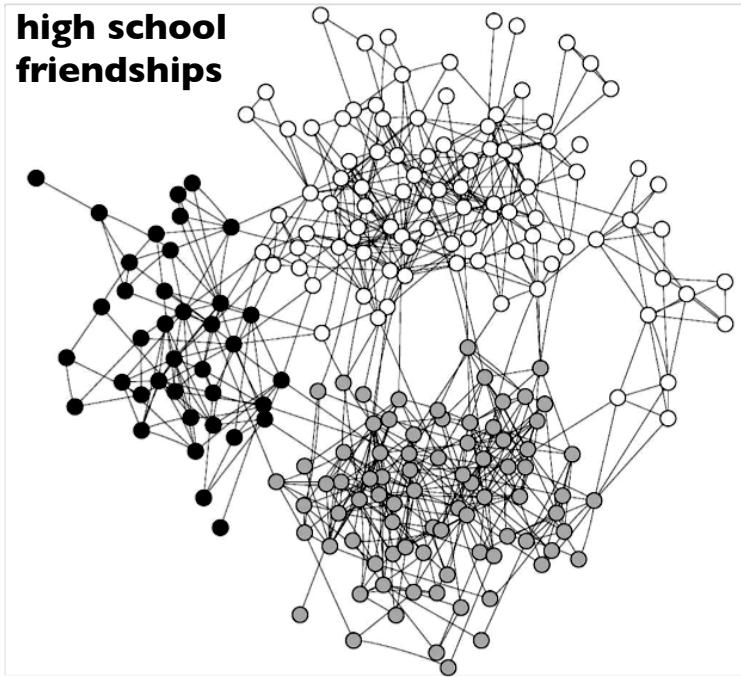
predation or resource transfer

social**biological**

social networks

vertex: a person

edge: friendship, collaborations, sexual contacts, communication, authority, exchange, etc.

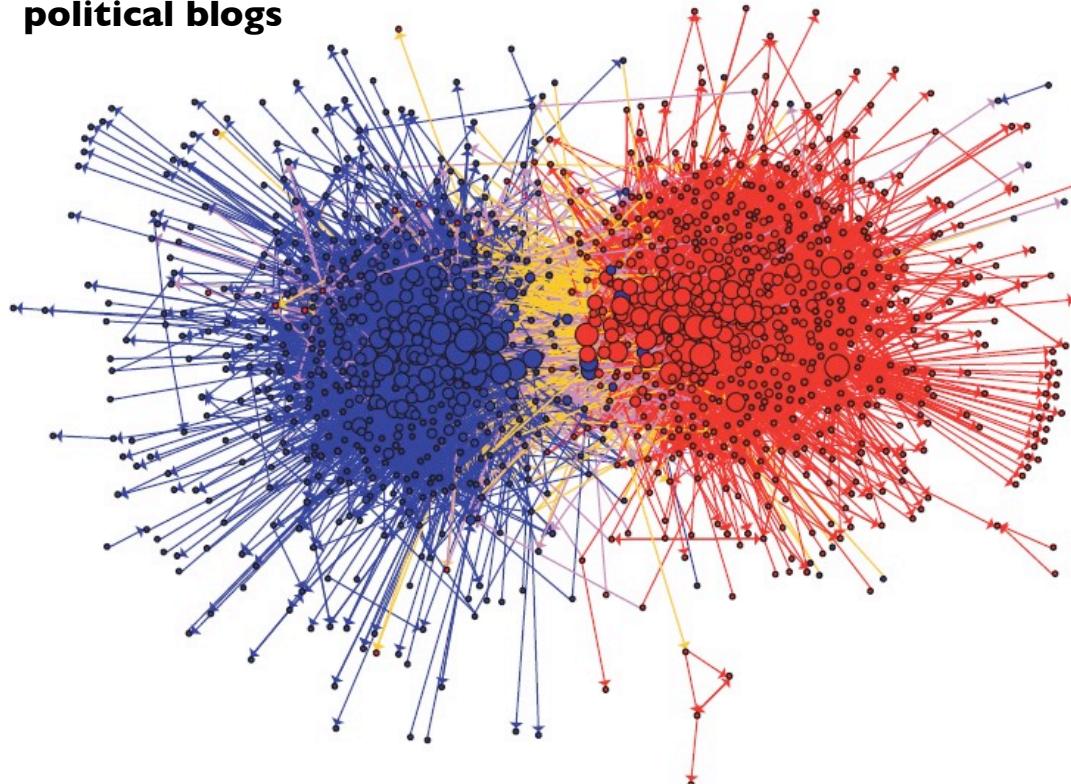


information networks

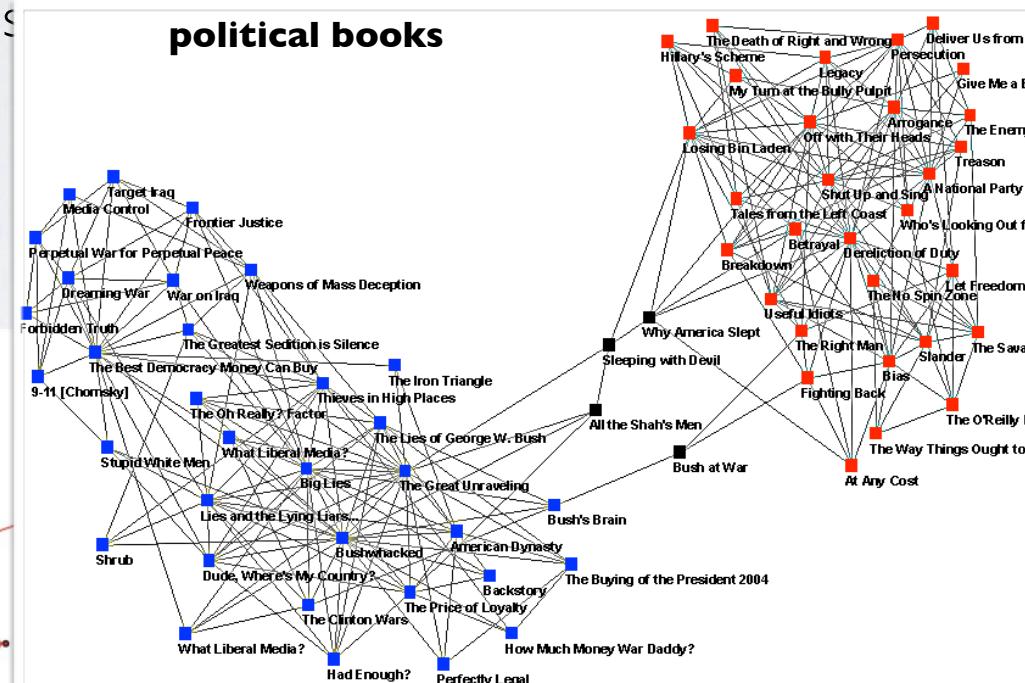
vertex: books, blogs, webpages, etc.

edge: citations, hyperlinks, recommendations
similarity, etc.

political blogs



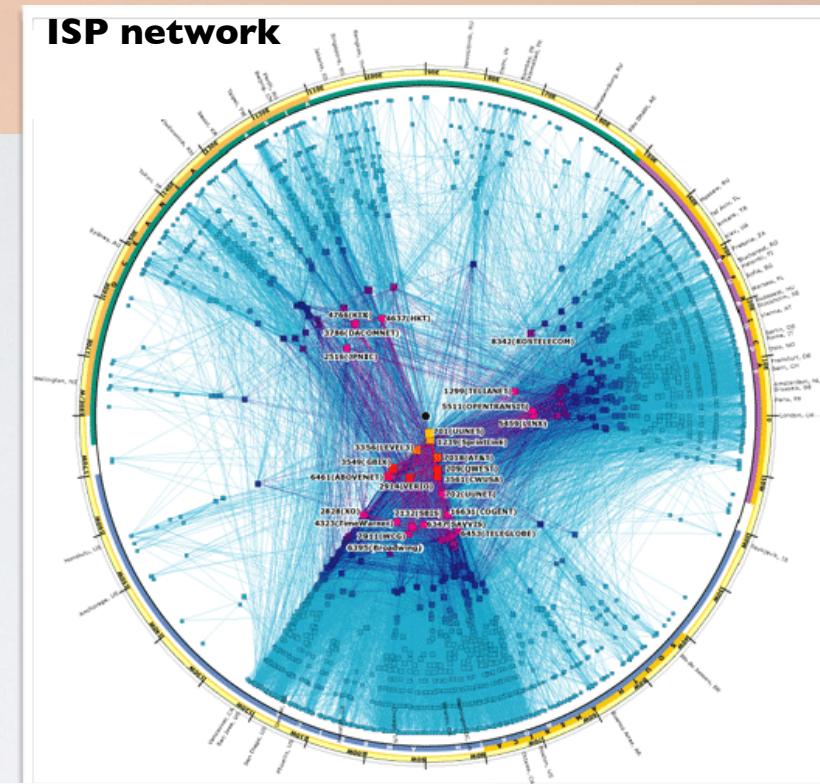
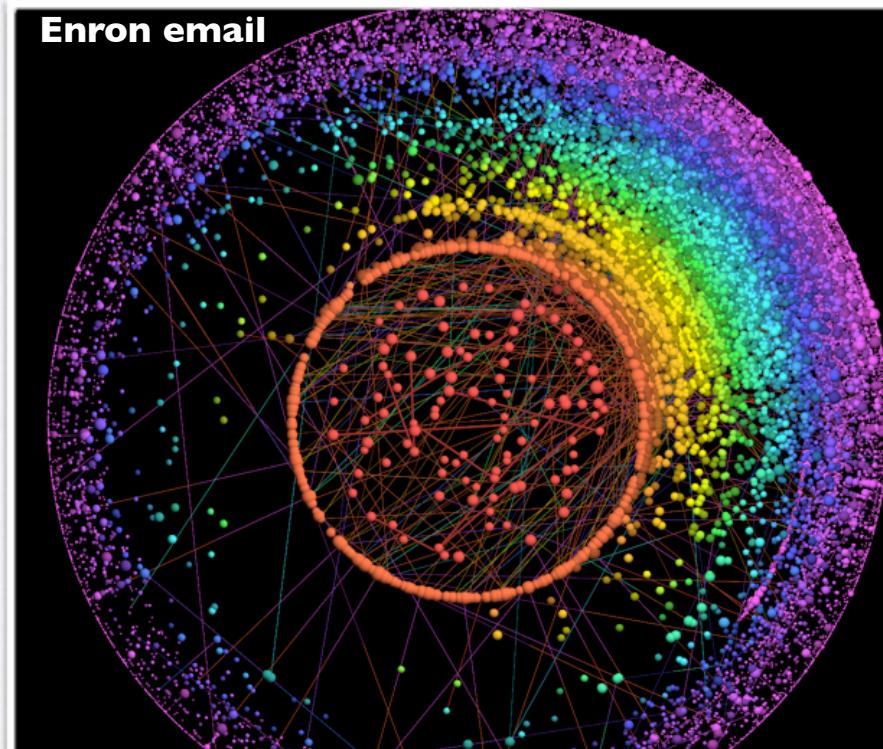
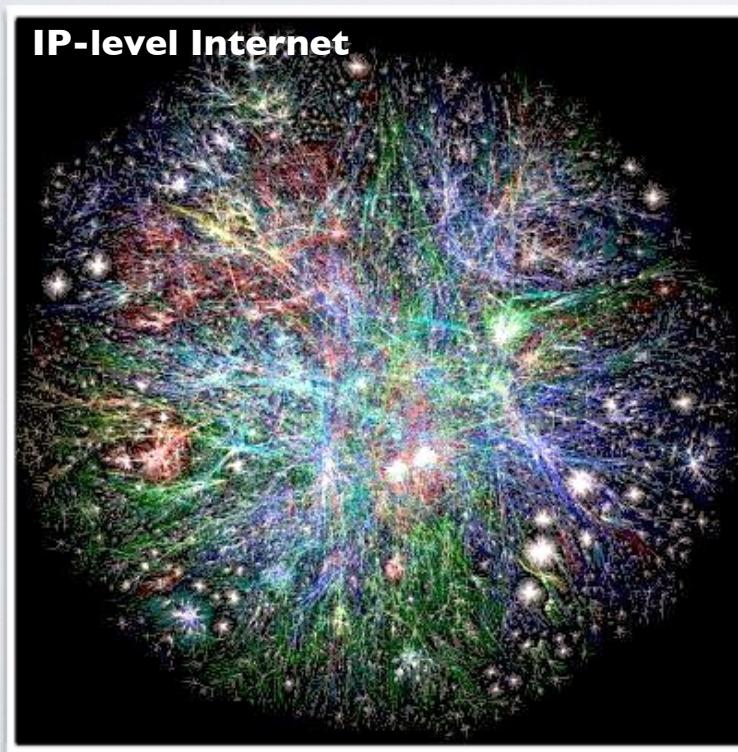
political books



communication networks

vertex: network router, ISP, email address, mobile phone number, etc.

edge: exchange of information



transportation networks

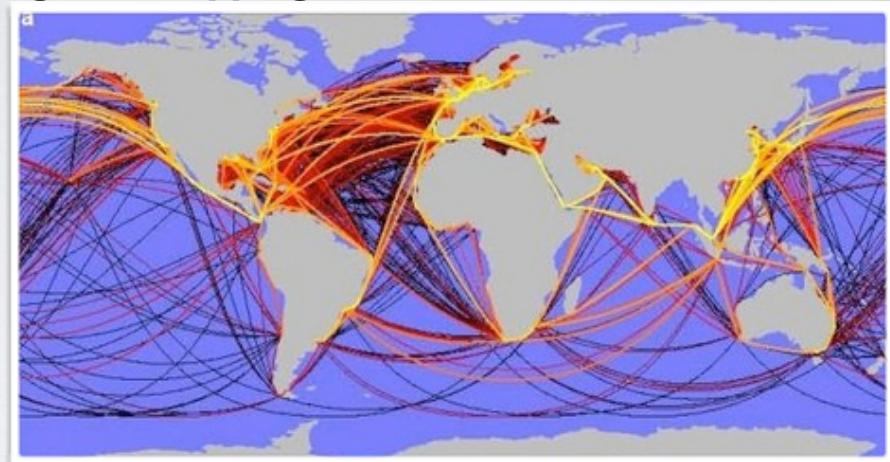
vertex: city, airport, junction, railway station, river confluence, etc.

edge: physical transportation of material



US Interstates

global shipping



global air traffic

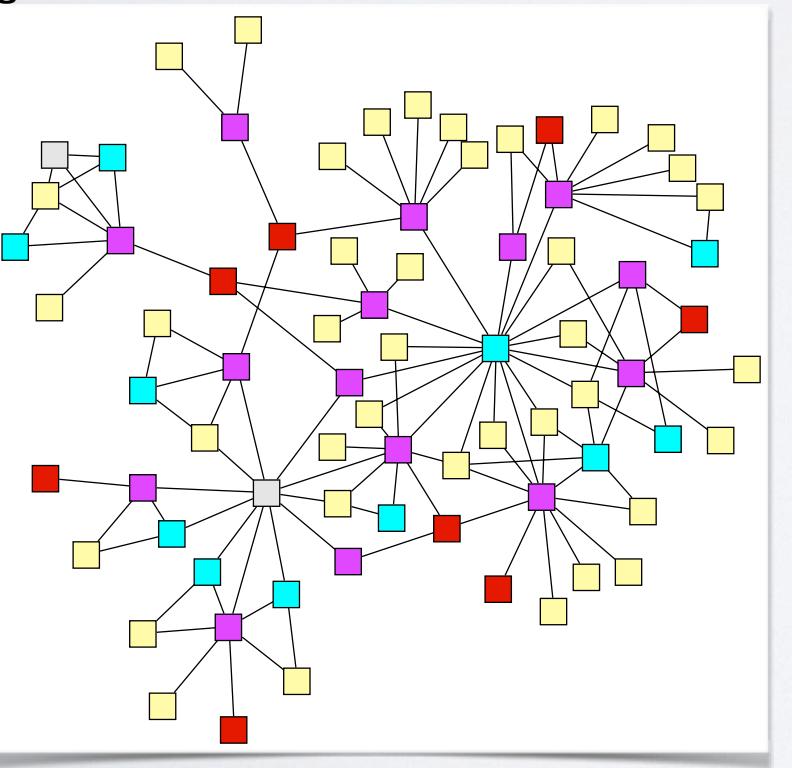


biological networks

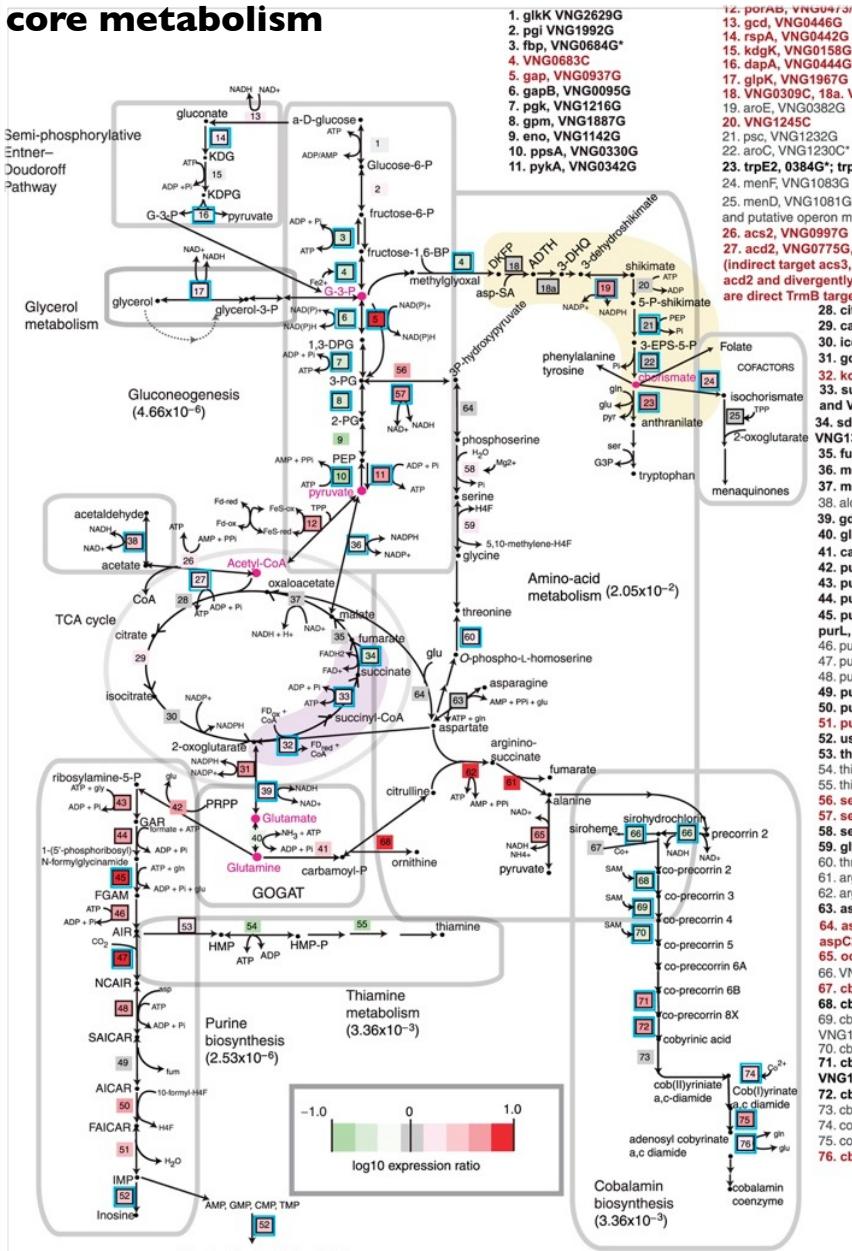
vertex: species, metabolic, protein, gene, neuron, etc.

edge: predation, chemical reaction, binding, regulation, activation, etc.

grassland foodweb

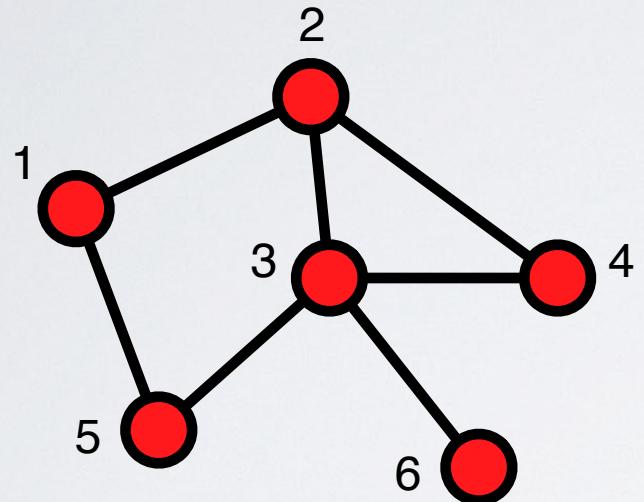


core metabolism



representing networks

a simple network

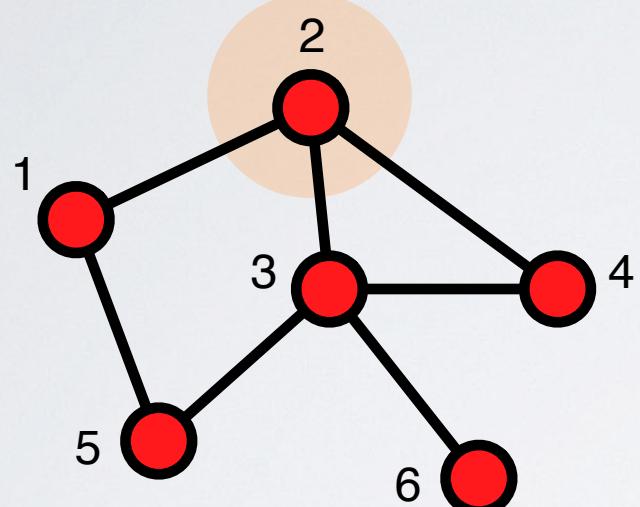


undirected

unweighted

no self-loops

a *simple* network



undirected

unweighted

no self-loops

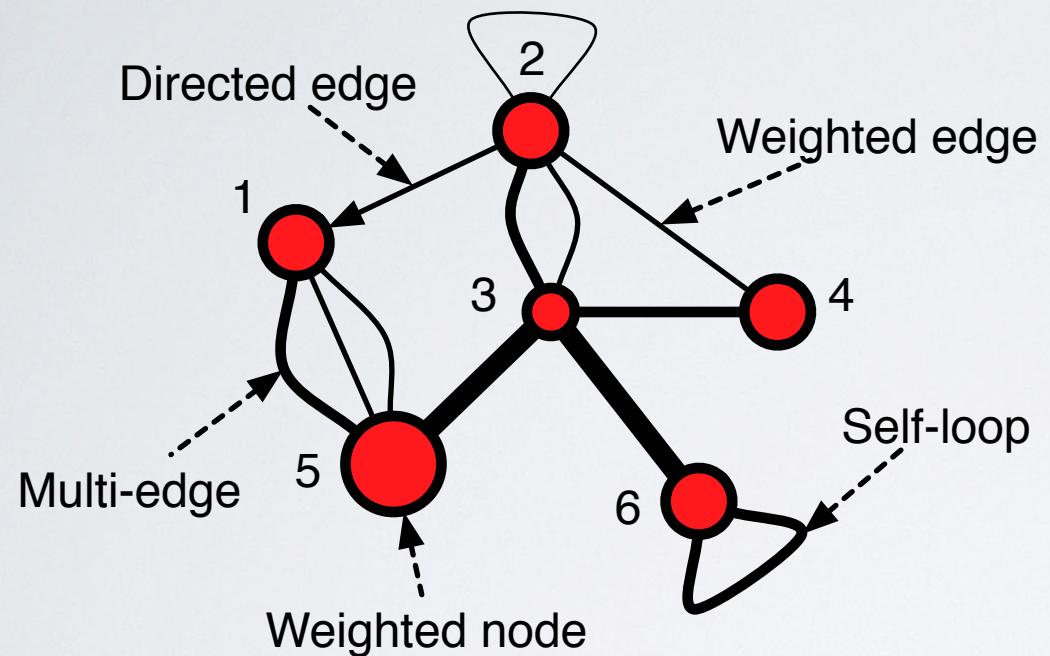
adjacency matrix

A	1	2	3	4	5	6
1	0	1	0	0	1	0
2	1	0	1	1	0	0
3	0	1	0	1	1	1
4	0	1	1	0	0	0
5	1	0	1	0	0	0
6	0	0	1	0	0	0

adjacency list

A
$1 \rightarrow \{2, 5\}$
$2 \rightarrow \{1, 3, 4\}$
$3 \rightarrow \{2, 4, 5, 6\}$
$4 \rightarrow \{2, 3\}$
$5 \rightarrow \{1, 3\}$
$6 \rightarrow \{3\}$

a less simple network

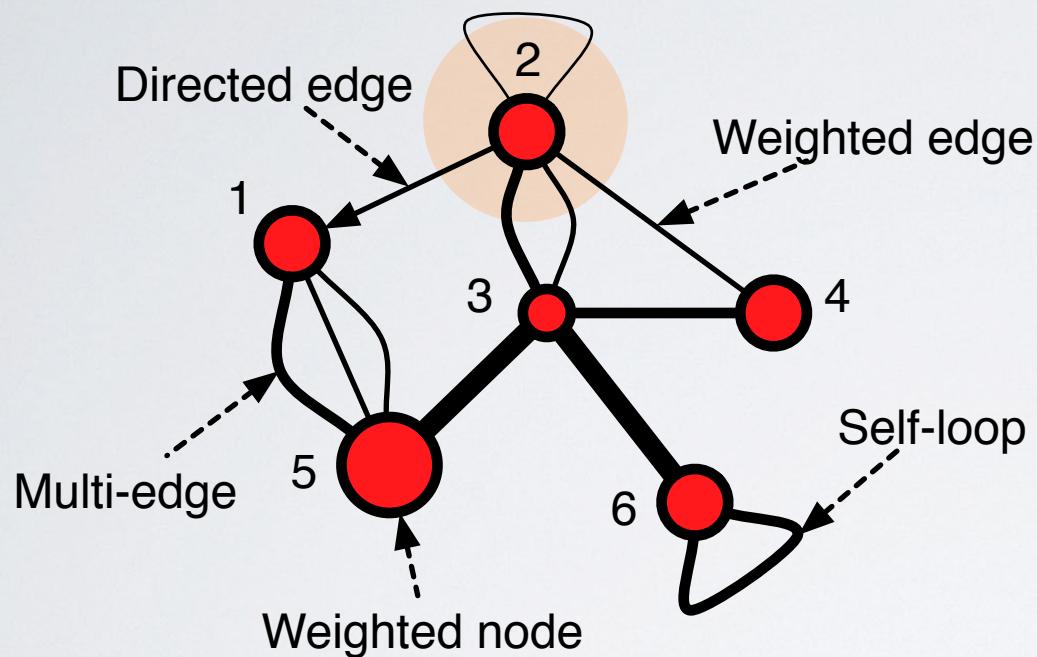


~~undirected~~

~~unweighted~~

~~no self loops~~

a less simple network



adjacency matrix

A	1	2	3	4	5	6
1	0	0	0	0	{1, 1, 2}	0
2	1	$\frac{1}{2}$	{2, 1}	1	0	0
3	0	{2, 1}	0	2	4	4
4	0	1	2	0	0	0
5	{1, 1, 2}	0	4	0	0	0
6	0	0	4	0	0	2

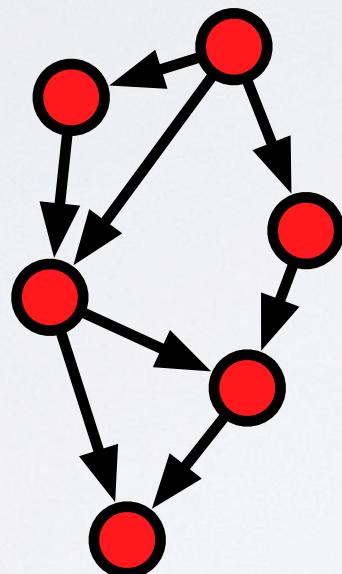
adjacency list

A
1 $\rightarrow \{(5, 1), (5, 1), (5, 2)\}$
2 $\rightarrow \{(1, 1), (2, \frac{1}{2}), (3, 2), (3, 1), (4, 1)\}$
3 $\rightarrow \{(2, 2), (2, 1), (4, 2), (5, 4), (6, 4)\}$
4 $\rightarrow \{(2, 1), (3, 2)\}$
5 $\rightarrow \{(1, 1), (1, 1), (1, 2), (3, 4)\}$
6 $\rightarrow \{(3, 4), (6, 2)\}$

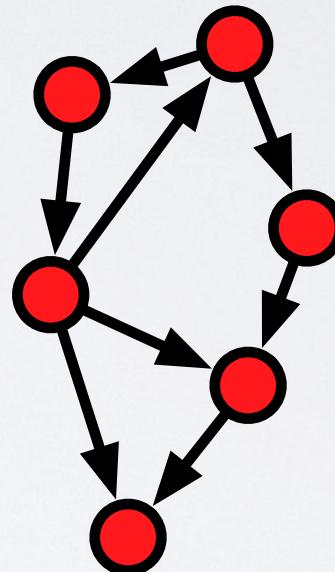
directed networks

$$A_{ij} \neq A_{ji}$$

citation networks
foodwebs*
epidemiological
others?



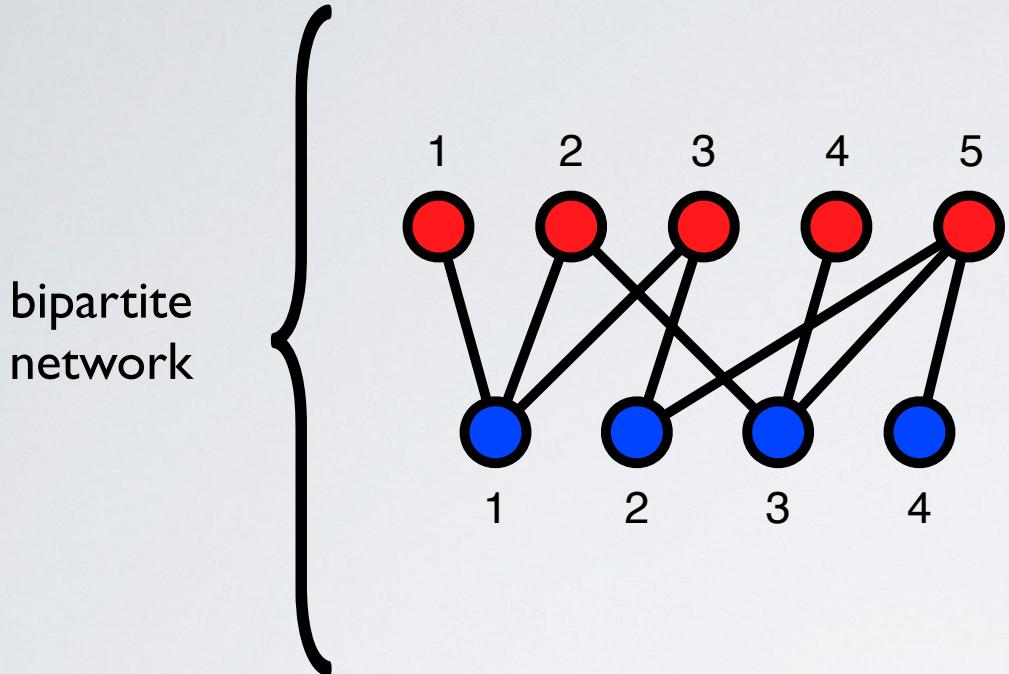
directed acyclic graph



directed graph

WWW
friendship?
flows of goods,
information
economic exchange
dominance
neuronal
transcription
time travelers

bipartite networks



no within-type edges

authors & papers

actors & movies/scenes

musicians & albums

people & online groups

people & corporate boards

people & locations (checkins)

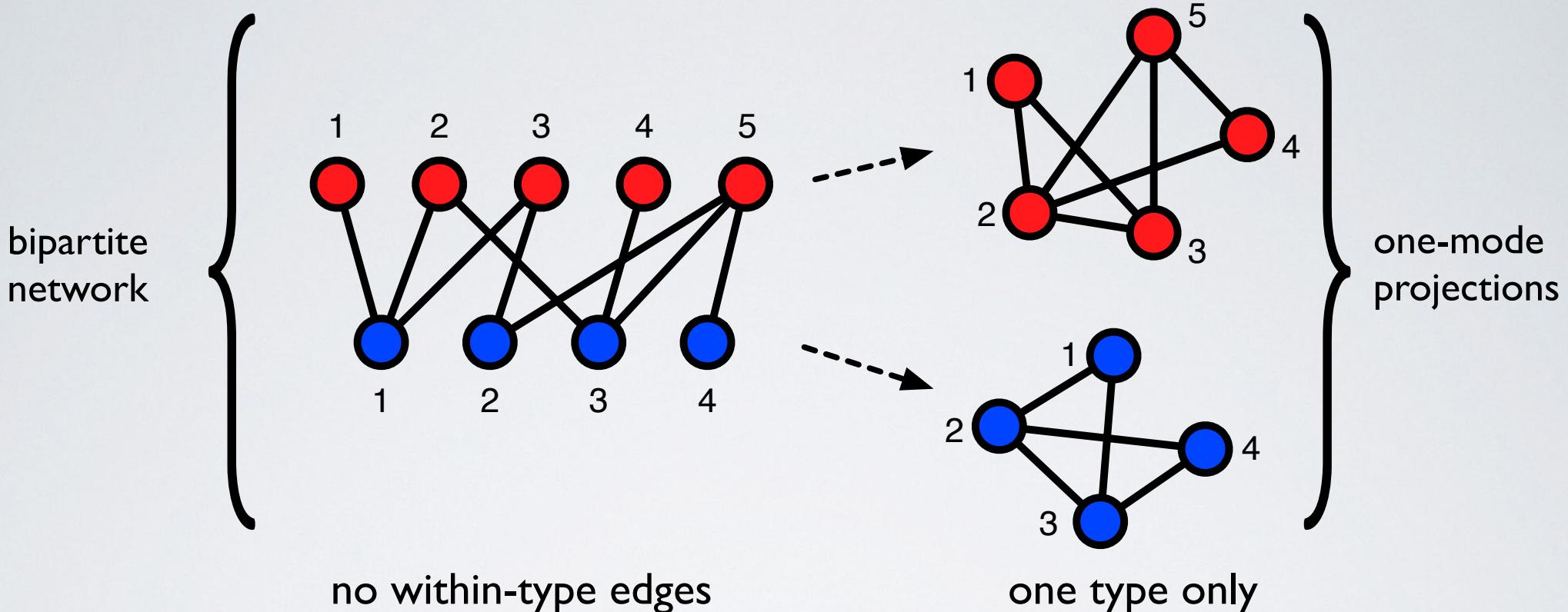
metabolites & reactions

genes & substrings

words & documents

plants & pollinators

bipartite networks



authors & papers

actors & movies/scenes

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people & online groups

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people & locations (checkins)

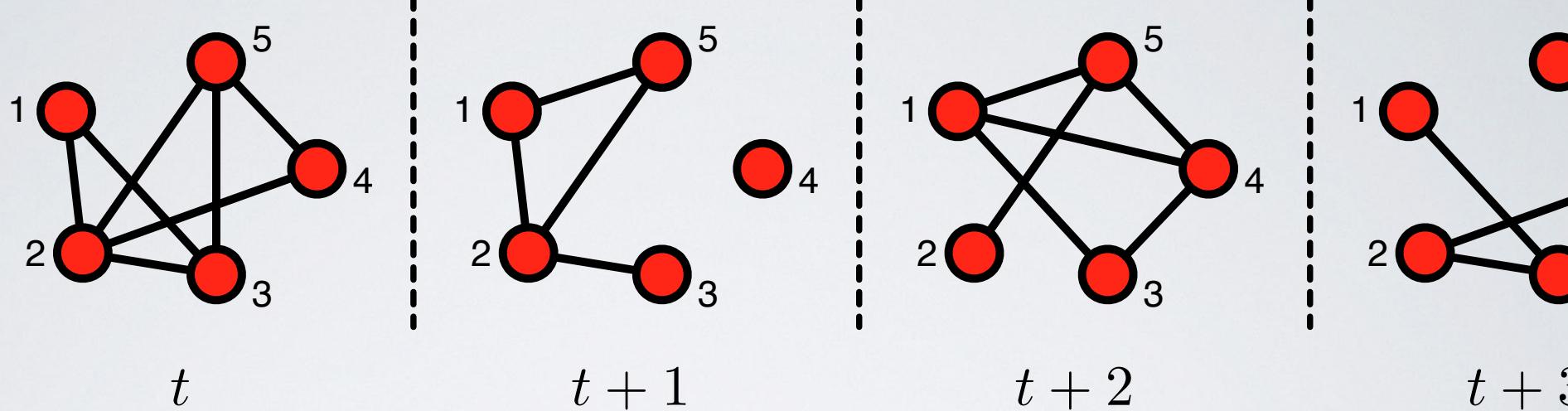
metabolites & reactions

genes & substrings

words & documents

plants & pollinators

temporal networks



any network over time; comes in two flavors

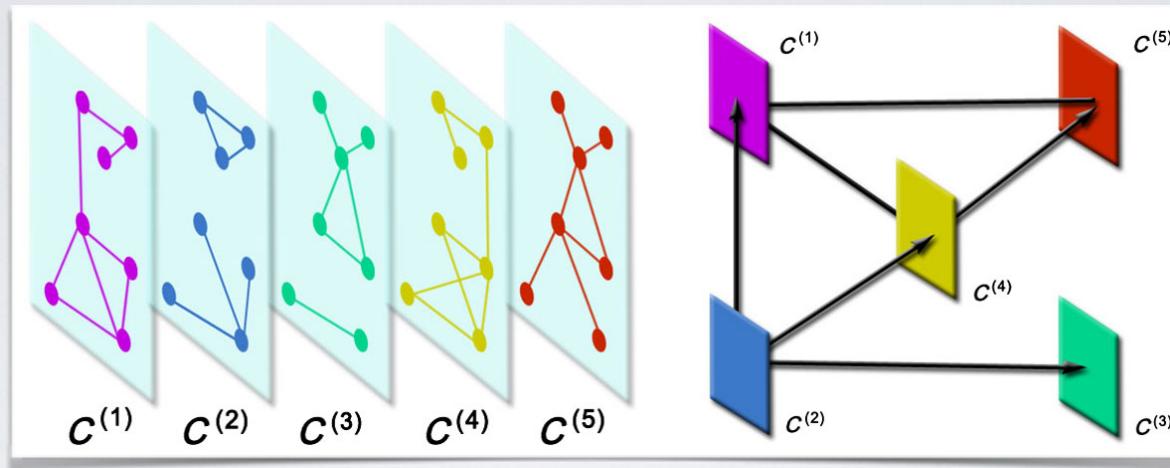
1. discrete time (snapshots), edges (i, j, t)
2. continuous time, edges $(i, j, t_s, \Delta t)$

physical proximity over time

transportation connections over time

social interactions over time

multiplex or multilayer networks



multiple network "layers"

each layer has same set of nodes V

but different sets of edges $\{E_1, E_2, \dots, E_\ell\}$

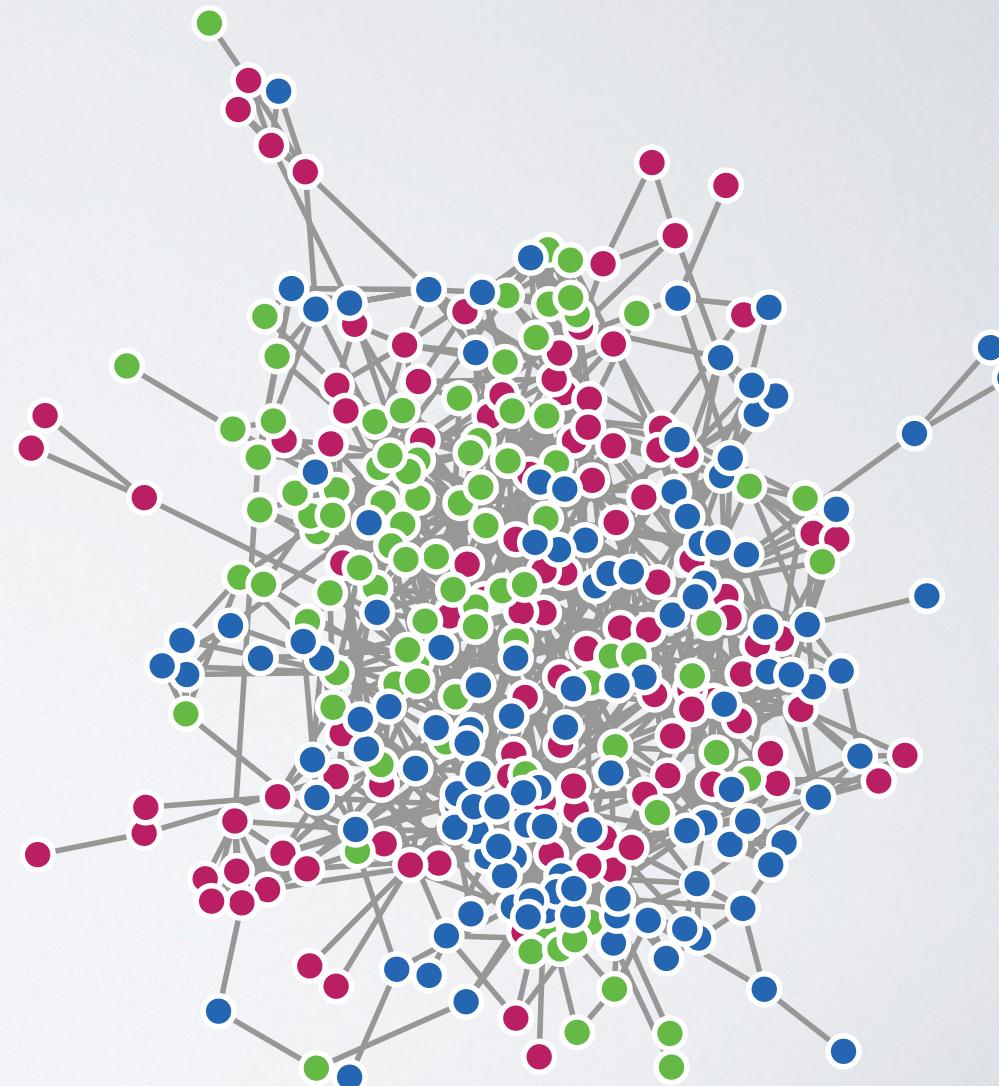
different types of transportation within a city

different types of social interactions (trust, socializing, co-located, etc.)

interactions on different social media platforms

analyzing networks

what real networks look like...



analyzing networks

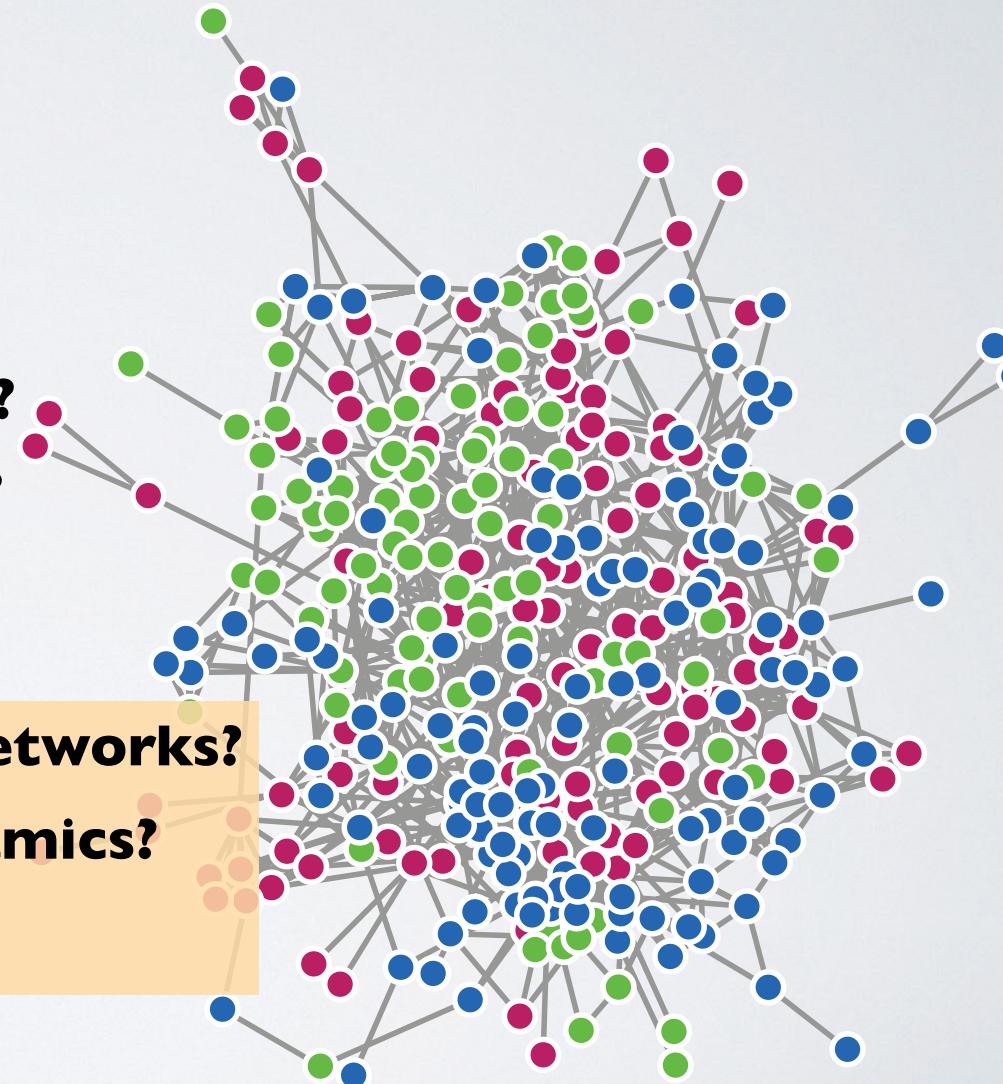
what real networks look like...

questions:

- **how are the edges organized?**
- **how do vertices differ?**
- **does network location matter?**
- **are there underlying patterns?**

what we want to know

- **what processes shape these networks?**
- **how does network shape dynamics?**
- **how can we tell?**



analyzing networks

what we want : understand its structure

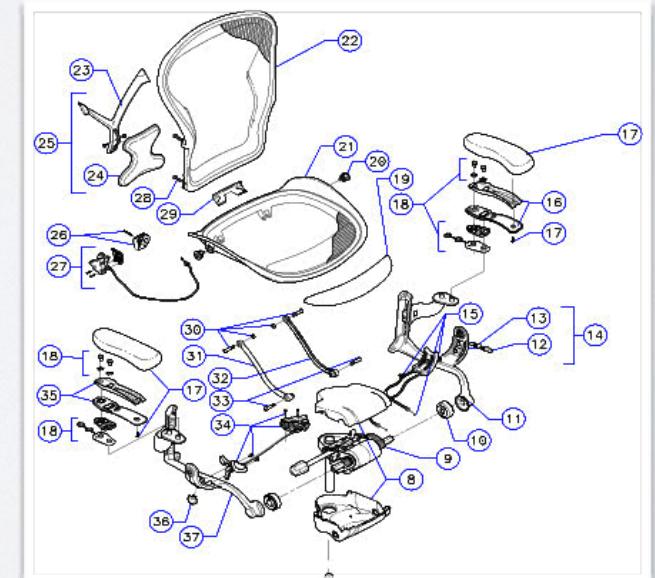
$$f : \text{object} \rightarrow \{\theta_1, \dots, \theta_k\}$$

- **what are the fundamental parts?**
- **how are these parts organized?**
- **where are the degrees of freedom $\vec{\theta}$?**
- **how can we define an abstract class?**
- **structure — dynamics — function?**

what does **local-level structure** look like?

what does **large-scale structure** look like?

how does **structure constrain** function?



analyzing networks

6 major approaches

- I. **exploratory data analysis:** count & compare all the things (degree distributions, centrality scores, community detection, etc.)

analyzing networks

6 major approaches

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2. **simple regressions:** convert network structure into node-level features, and do traditional explanatory modeling

analyzing networks

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analyzing networks

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analyzing networks

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5. **predictive models:** fit parametric model of network structure & use it to predict missing or future data (edges, labels, etc.)

analyzing networks

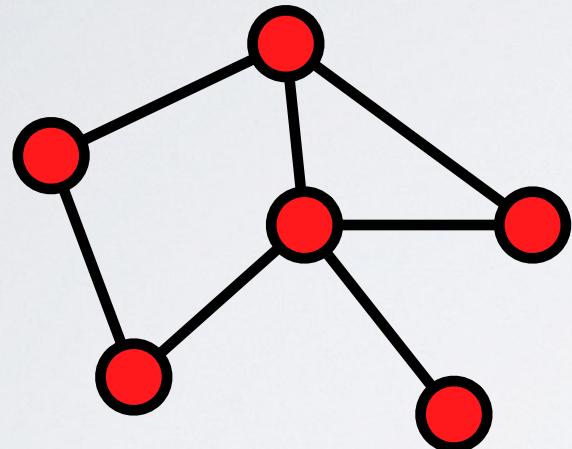
6 major approaches

- ★ 1. **exploratory data analysis:** count & compare all the things (degree distributions, centrality scores, community detection, etc.)
- ★ 2. **simple regressions:** convert network structure into node-level features, and do traditional explanatory modeling
- ★ 3. **null models:** use some kind of random graph to identify non-random patterns as deviations from the null
- ★ 4. **mechanisms / simulations:** explain structural or dynamical patterns as caused by specific process
- ★ 5. **predictive models:** fit parametric model of network structure & use it to predict missing or future data (edges, labels, etc.)
- ★ 6. **network experiments:** manipulate structure and measure node-level or graph-level behavior as function of changes

analyzing networks

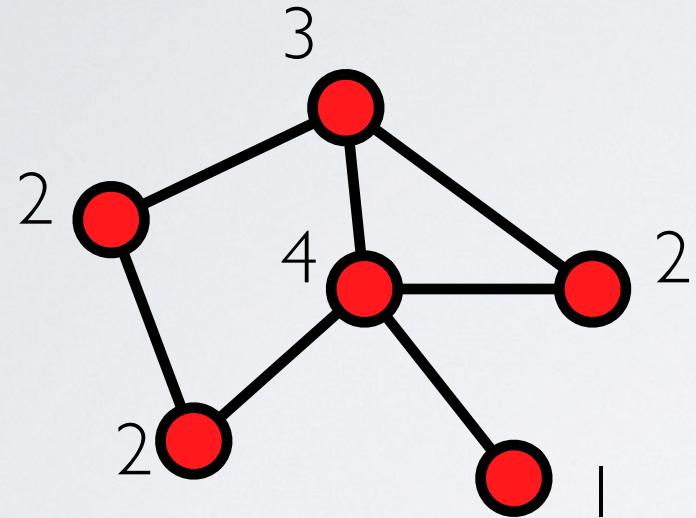
- degrees & distributions
- network position & centrality scores
- some applications

degree distributions



degree

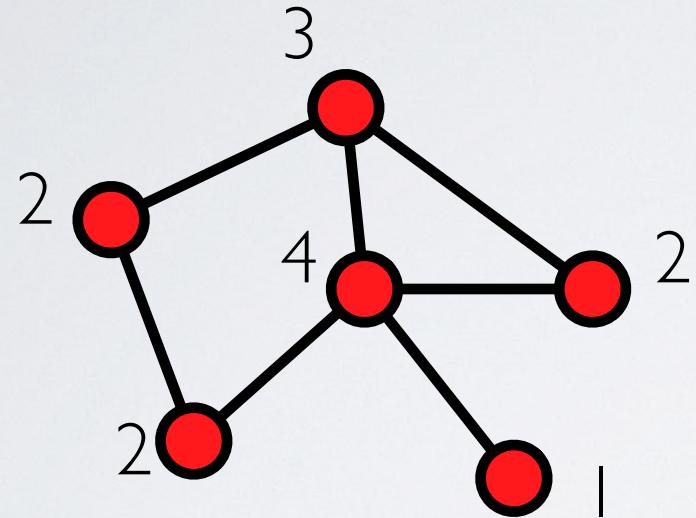
degree distributions



degree:
number of connections k

$$k_i = \sum_j A_{ij}$$

degree distributions



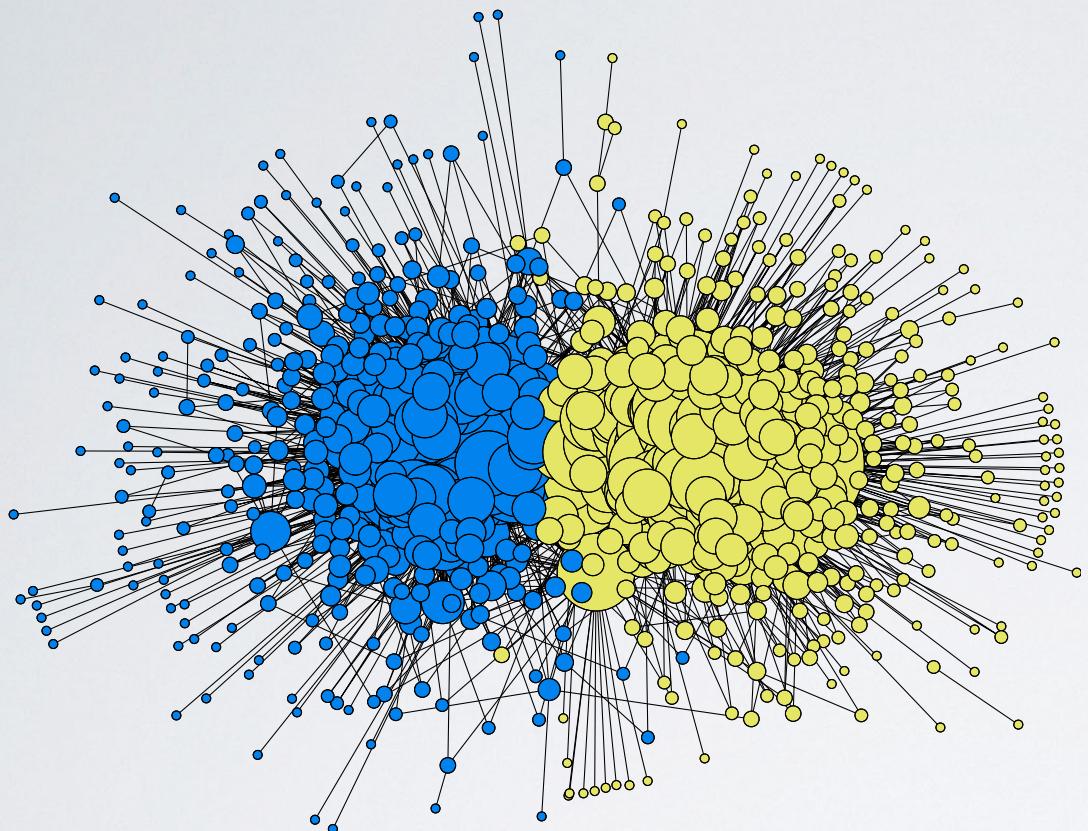
degree:
number of connections k

$$k_i = \sum_j A_{ij}$$

degree sequence : $\{1, 2, 2, 2, 3, 4\}$

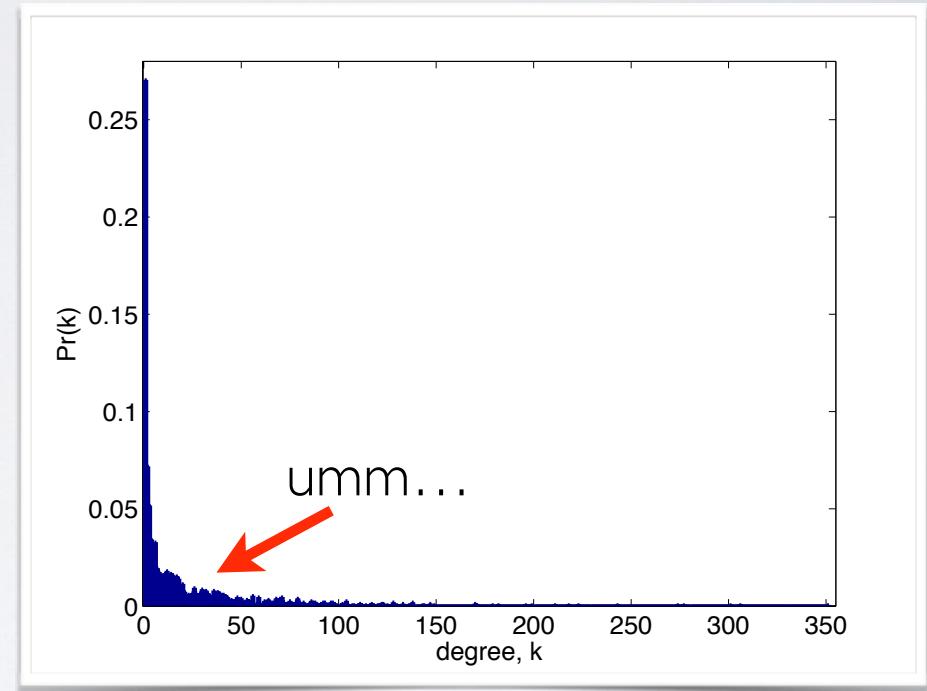
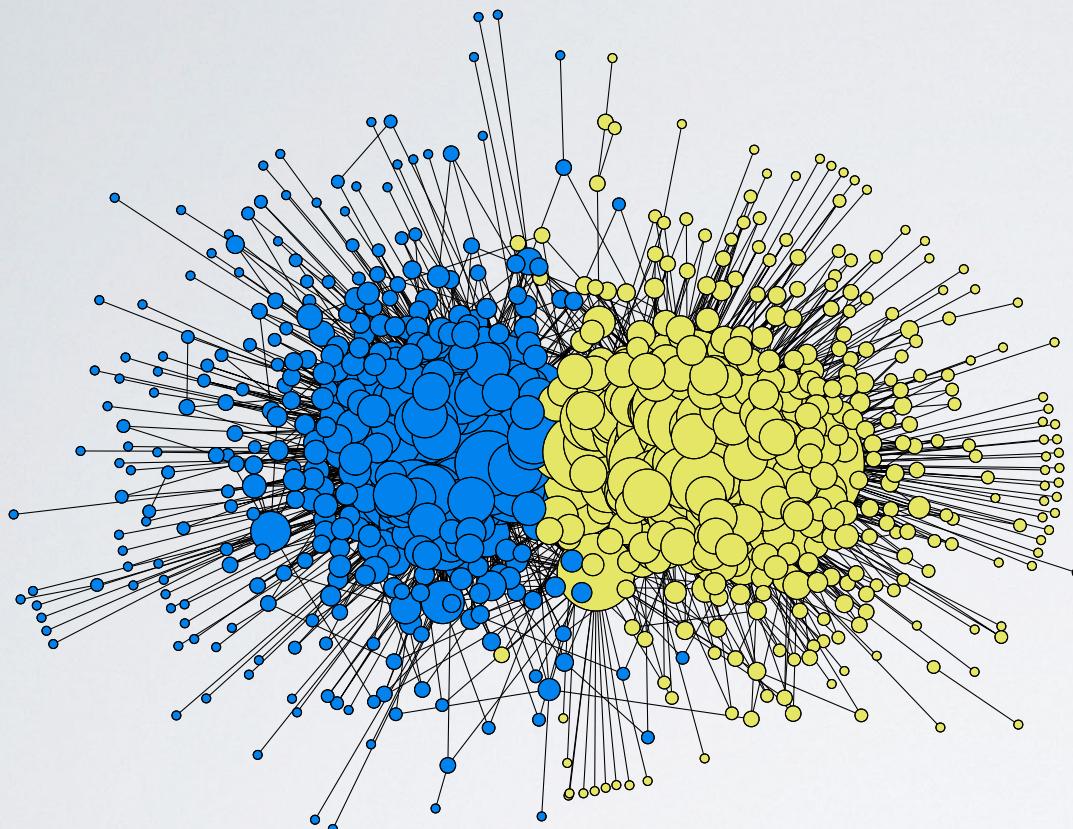
degree distribution : $\Pr(k) = \left[\left(1, \frac{1}{6}\right), \left(2, \frac{3}{6}\right), \left(3, \frac{1}{6}\right), \left(4, \frac{1}{6}\right) \right]$

degree distributions

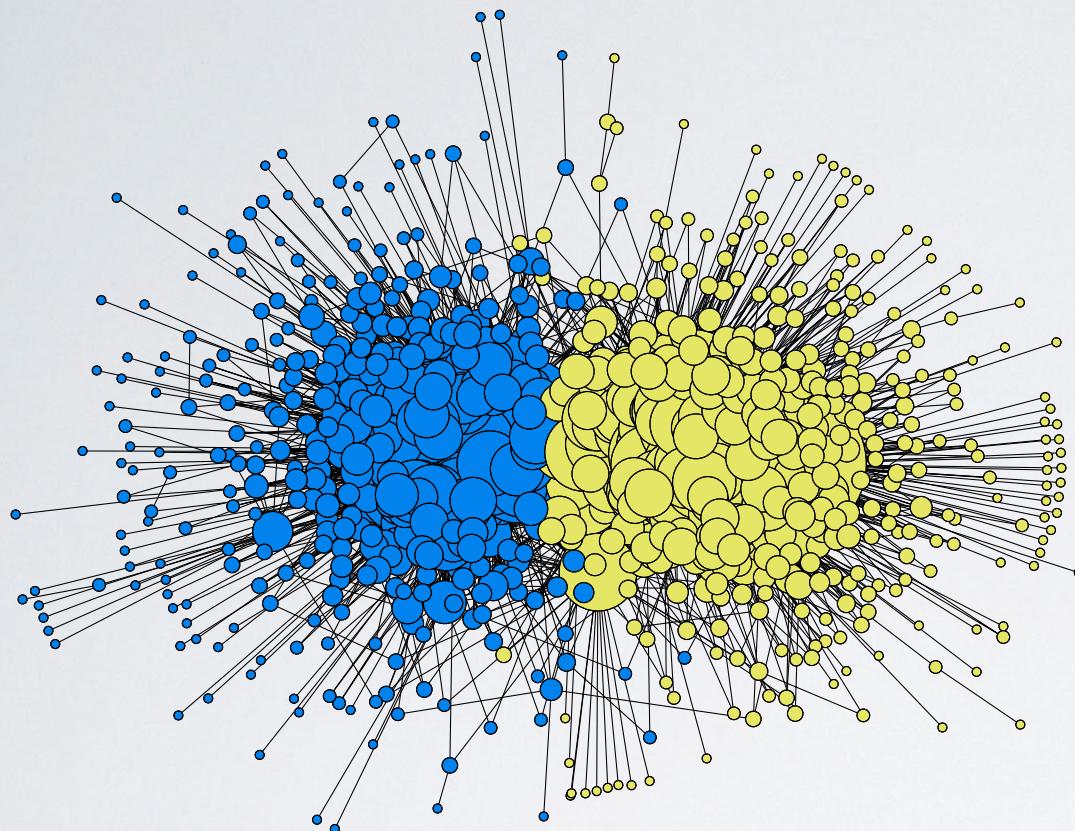


political blogs

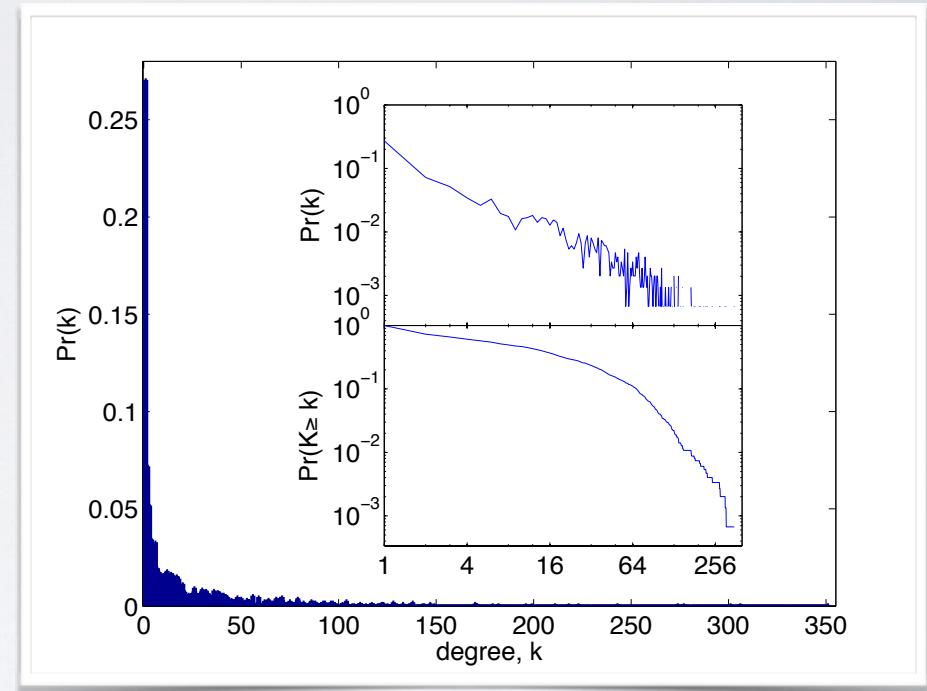
degree distributions



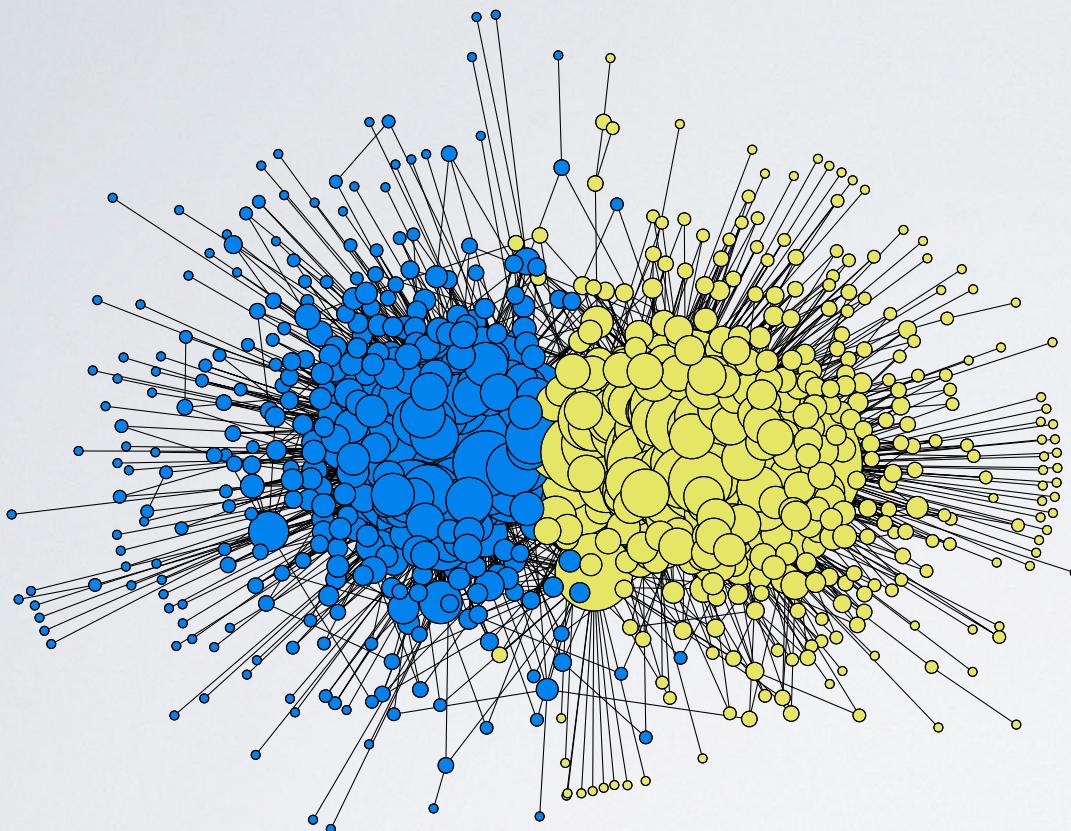
degree distributions



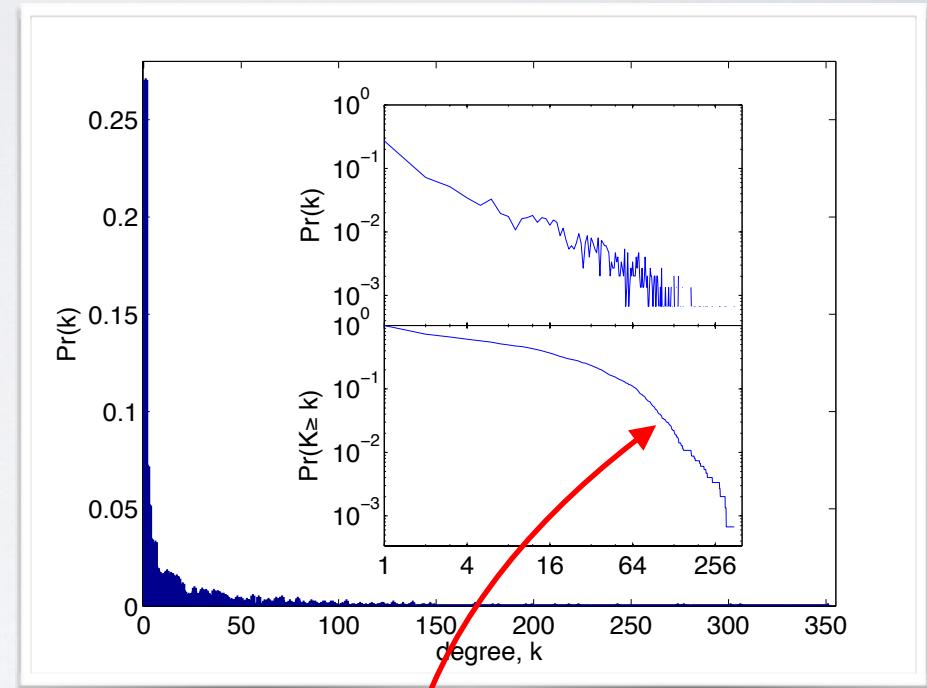
political blogs



degree distributions



political blogs

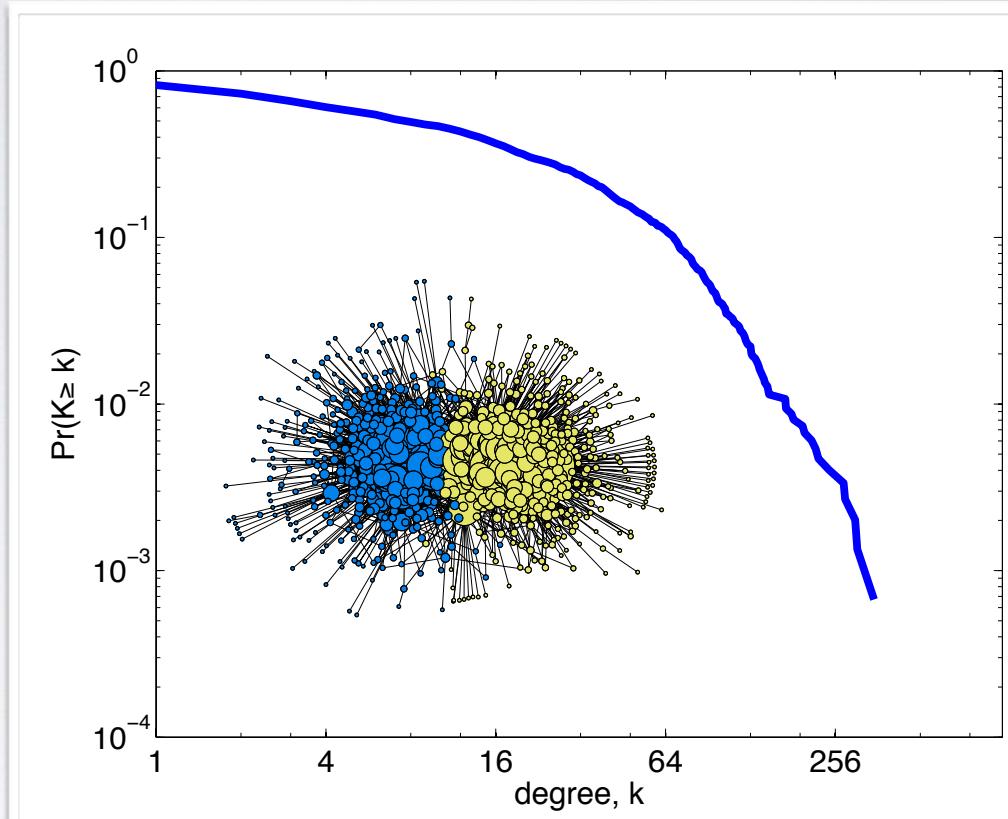


🤔 is this a power law?

degree distributions

🤔 fun facts I:

- nearly all real networks exhibit a ***heavy-tailed degree distribution***
- **very few** networks exhibit perfect power-law degree distributions
- **some** distributions exhibit power-law tails
- power laws are cool!
but identifying them in data
(and not confusing them for other things) ***requires statistics***



degree distributions

🤔 fun facts 2:

- **degree distribution** is the first-order description of network structure
- **degree heterogeneity** alone drives interesting phenomena ("friendship paradox", spreading dynamics, etc.)
- **degree heterogeneity** alone explains many other network patterns (various centralities, disassortativity, etc.)
- the **configuration model** is how to tell : random graph model with specified degree sequence



airport network & global epidemics

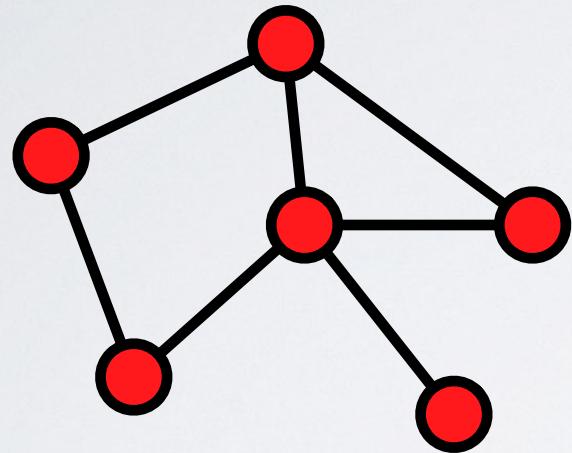
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Configuring Random Graph Models with Fixed Degree Sequences*

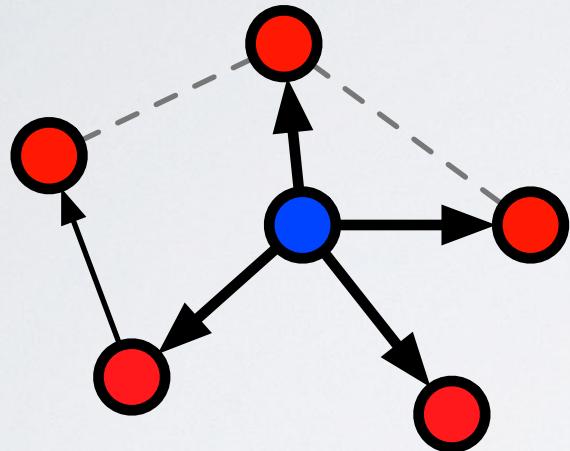
Bailey K. Fosdick[†]
Daniel B. Larremore[‡]
Joel Nishimura[§]
Johan Ugander[¶]

network position



position

network position



position = centrality:
structural vs. dynamical importance

geometric

harmonic centrality

closeness centrality

betweenness centrality

degree centrality

eigenvector centrality

PageRank

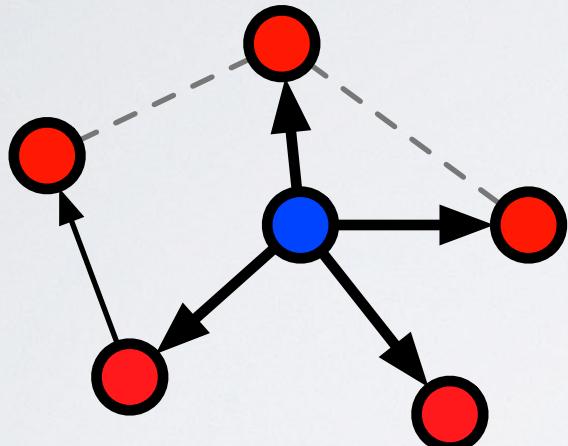
Katz centrality

many many more...



structural importance = cheap
estimate of dynamical importance
(aka "influence")

network position



position = centrality:
structural vs. dynamical importance

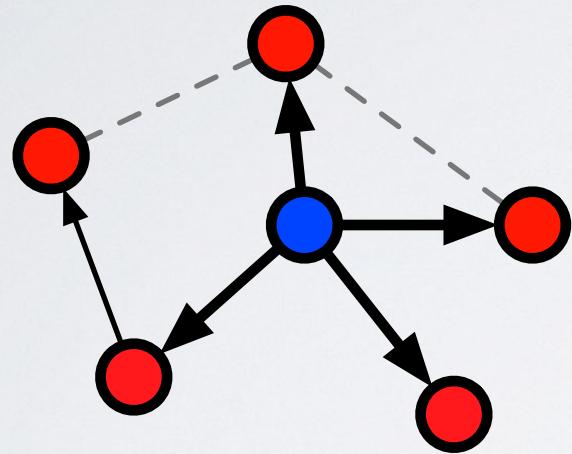
centrality = unsupervised node ranking

$$f: G \rightarrow \overrightarrow{v}$$



there are an infinite number of choices of f !
most are correlated
choose f that is most meaningful for downstream analysis

network position



position = centrality:

harmonic, closeness centrality

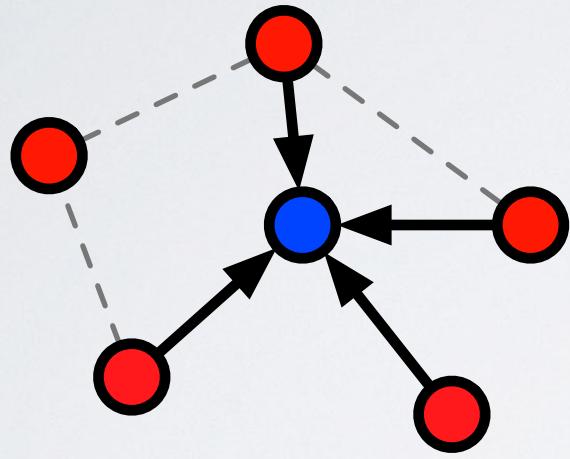
importance = being in “center” of the network

$$\text{harmonic} \quad c_i = \frac{1}{n-1} \sum_{j \neq i} \frac{1}{d_{ij}}$$

length of shortest path

distance: $d_{ij} = \begin{cases} \ell_{ij} & \text{if } j \text{ reachable from } i \\ \infty & \text{otherwise} \end{cases}$

network position



position = centrality:

PageRank, Katz, eigenvector centrality

importance = sum of importances of nodes that point at you*

$$I_i = \sum_{j \rightarrow i} \frac{I_j}{k_j}$$

or the right eigenvector of

$$\mathbf{Ax} = \lambda \mathbf{x}$$

network position

Robust Action and the Rise of the Medici, 1400–1434

John F. Padgett and Christopher K. Ansell
University of Chicago



Duomo

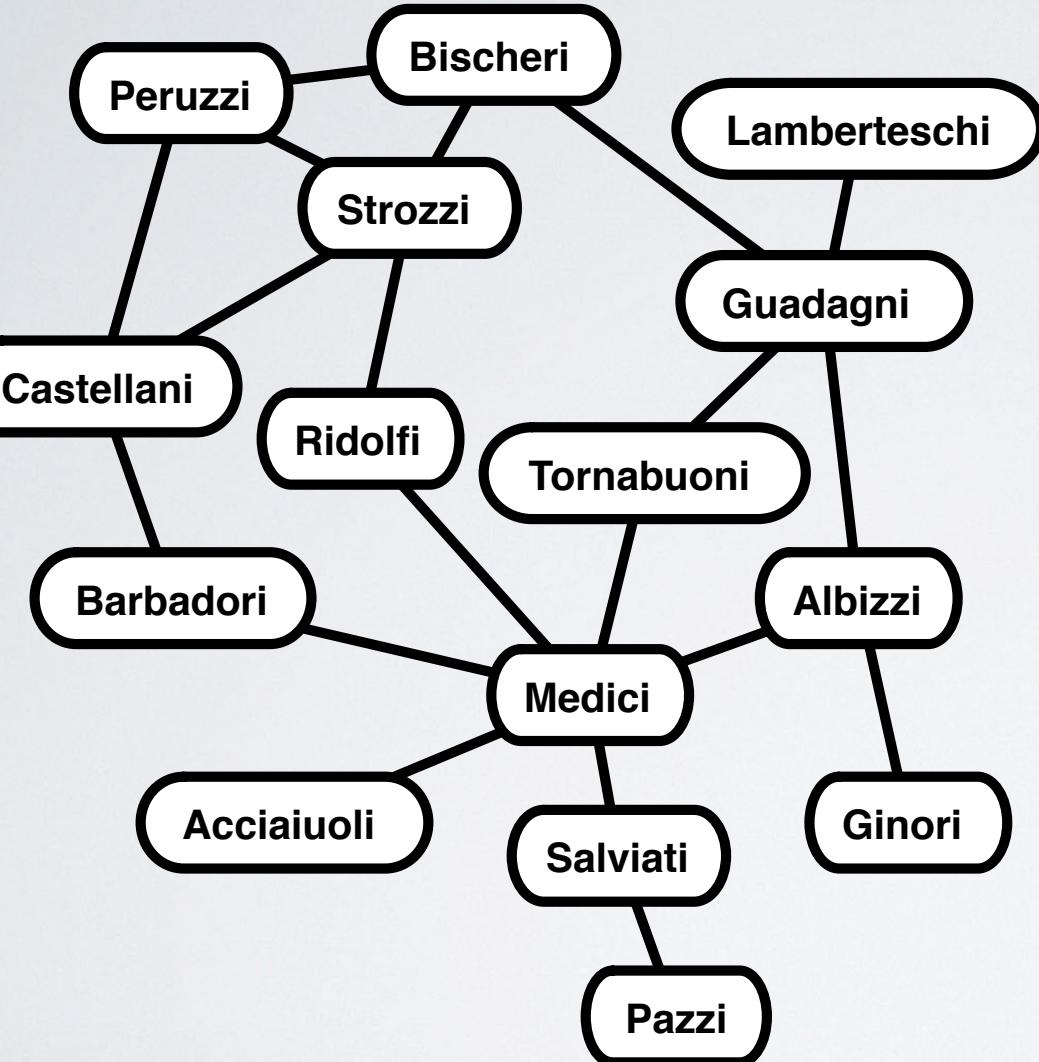


Palazzo Medici



Giovanni de Medici

network position

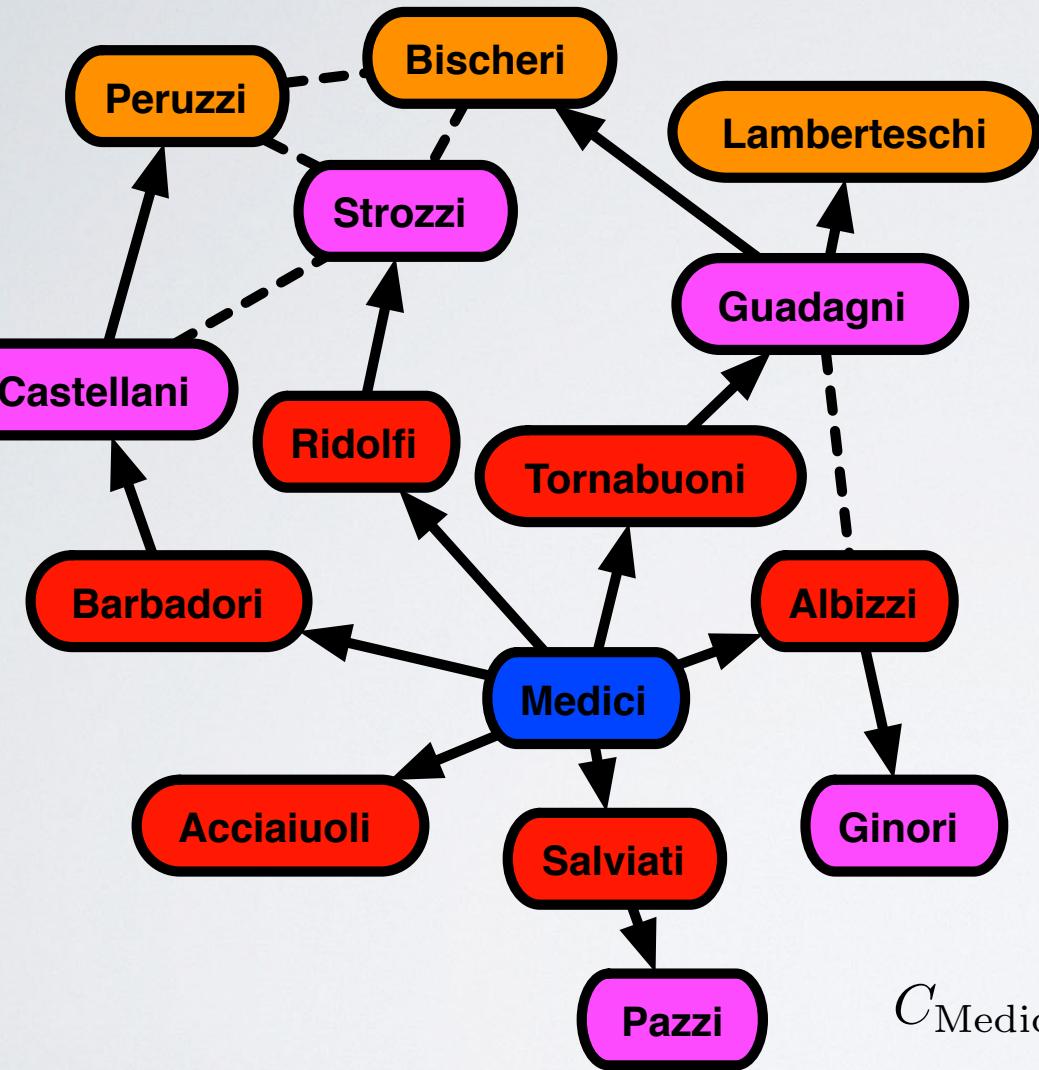


nodes: Florence families

edges: inter-family marriages

which family is most central?

network position



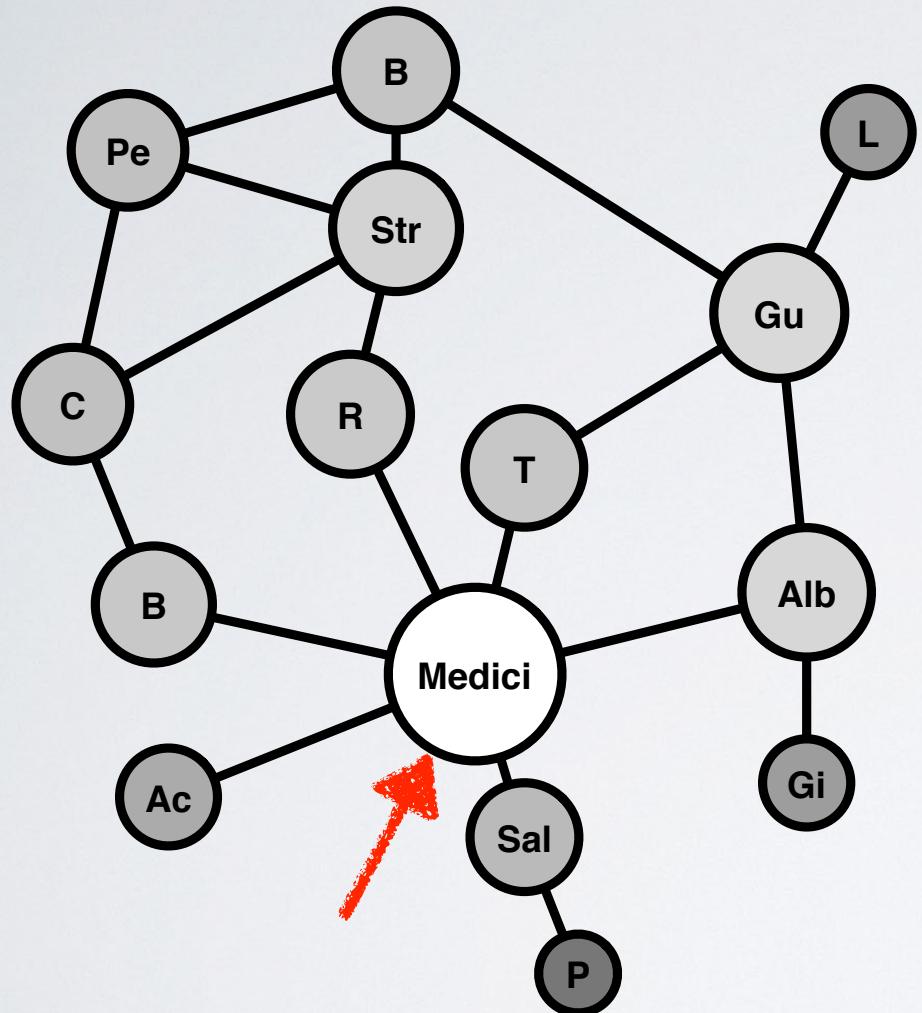
nodes: Florence families

edges: inter-family marriages

which family is most central?
Medici.

$$C_{\text{Medici}} = 6 \left(\frac{1}{1} \right) + 5 \left(\frac{1}{2} \right) + 3 \left(\frac{1}{3} \right)$$
$$= 9.5$$

network position

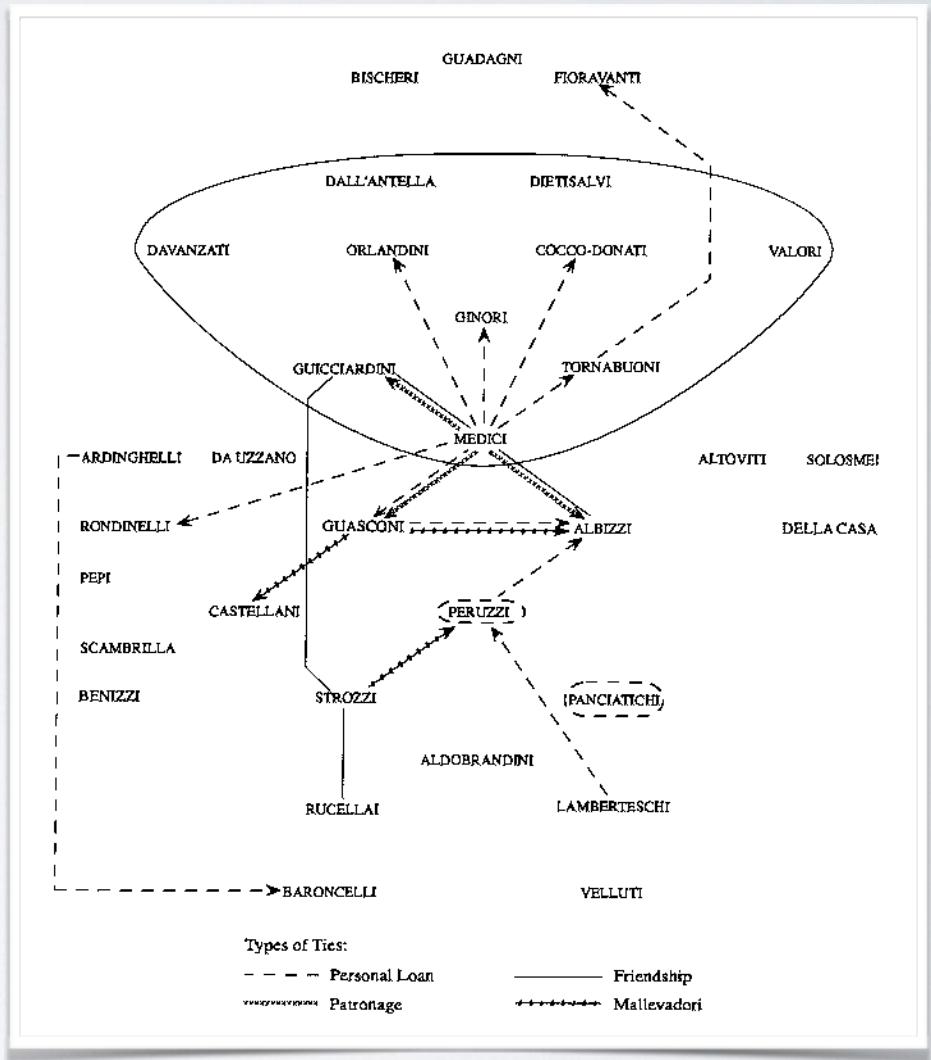
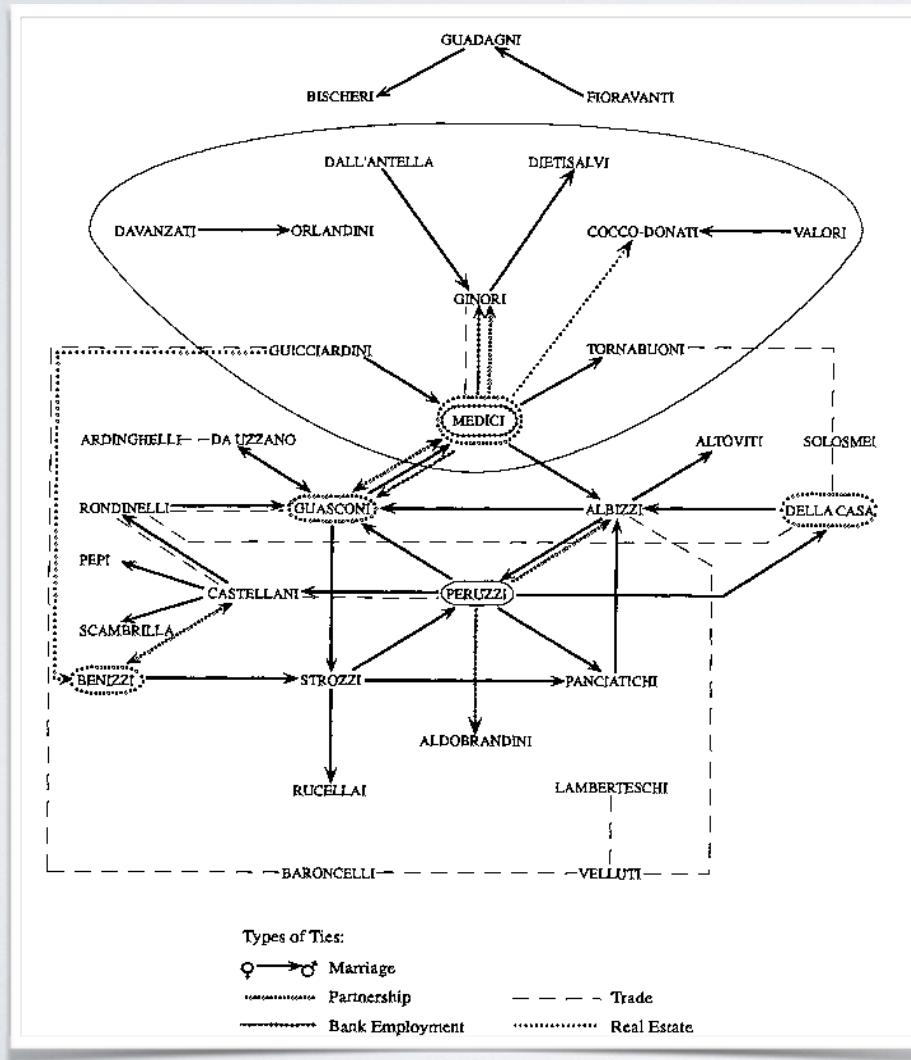


Medici	9.5
Guadagni	7.92
Albizzi	7.83
Strozzi	7.67
Ridolfi	7.25
Bischeri	7.2
Tornabuoni	7.17
Barbadori	7.08
Peruzzi	6.87
Castellani	6.87
Salviati	6.58
Acciaiuoli	5.92
Ginori	5.33
Lamberteschi	5.28
Pazzi	4.77



network position

actually, it's complicated...



[1] Marriage edges were only one type of inter-family interaction; hence, centrality on them alone is a simplification, and the deeper questions are about dynamics (how did the full network assemble over time?) and about function (was network position causally related to Medici dominance?).

let's apply these network concepts

RESEARCH ARTICLE

NETWORK SCIENCES

Systematic inequality and hierarchy in faculty hiring networks

Aaron Clauset,^{1,2,3*} Samuel Arbesman,⁴ Daniel B. Larremore^{5,6}

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10.1126/sciadv.1400005

let's apply these network concepts

RESEARCH ARTICLE

NETWORK SCIENCES

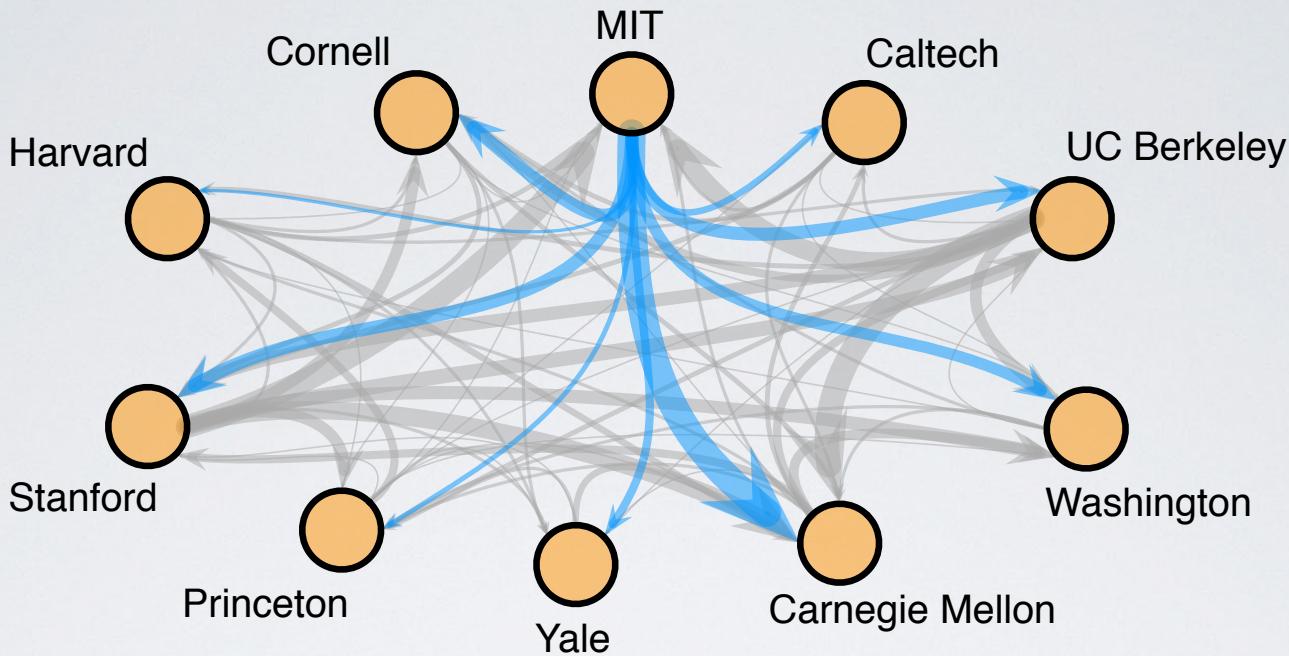
Systematic inequality and hierarchy in faculty hiring networks

Aaron Clauset,^{1,2,3*} Samuel Arbesman,⁴ Daniel B. Larremore^{5,6}

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faculty market is a *network*

- vertices are PhD-granting universities
- consumers \leftrightarrow producers
- v hires from u , add an edge $u \rightarrow v$



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collecting the data

complete, hand-curated data for
19,000 tenure-track faculty
across 461 departments in

- Computer Science (205 depts)
- Business (112)
- History (144)

roughly 5000 hours of manual data
collection

```
>>> record 1059
# facultyName : James H. Martin
# email      :
# sex        : M
# department : Computer Science
# place      : University of Colorado, Boulder
# current    : Full Professor
# [Education]
# degree     : BS
# place      : Columbia University
# field      : Computer Science
# years      : ????-1981
# [Education]
# degree     : PhD
# place      : UC Berkeley
# field      : Computer Science
# years      : ????-1988
# [Faculty]
# rank       : Assistant Professor
# place      : University of Colorado, Boulder
# years      : 1989-1995
# [Faculty]
# rank       : Associate Professor
# place      : University of Colorado, Boulder
# years      : 1995-2007
# [Faculty]
# rank       : Full Professor
# place      : University of Colorado, Boulder
# years      : 2007-2011
# recordDate : 7/4/2011
```

[1] CS data from 2011, Business schools from 2012, History from 2013

[2] all data from public sources, mainly faculty CVs and homepages

[3] data collected by a team of 12 students over 3 years, using a random 20% re-collection protocol, with script-based post-processing to detect errors & inconsistencies, which were then corrected by hand

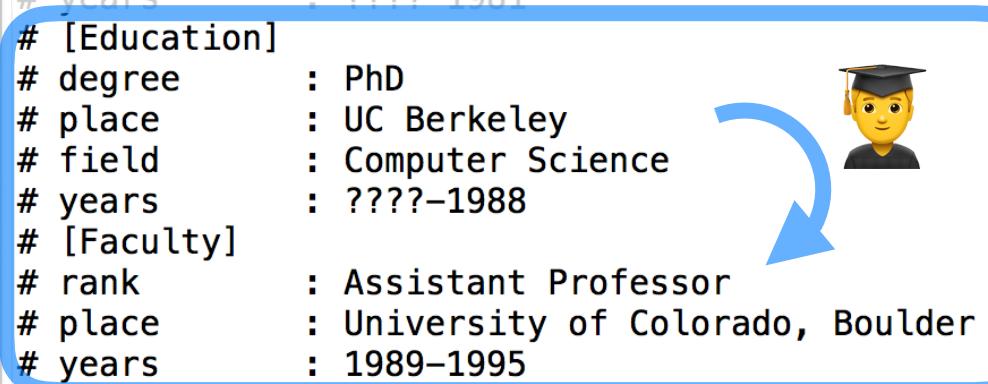
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what's in the data

	Computer Science	Business	History
institutions	205	112	144
tenure-track faculty	5032	9336	4556
mean size	25	83	32

$\sum = 18,924$

what's in the data

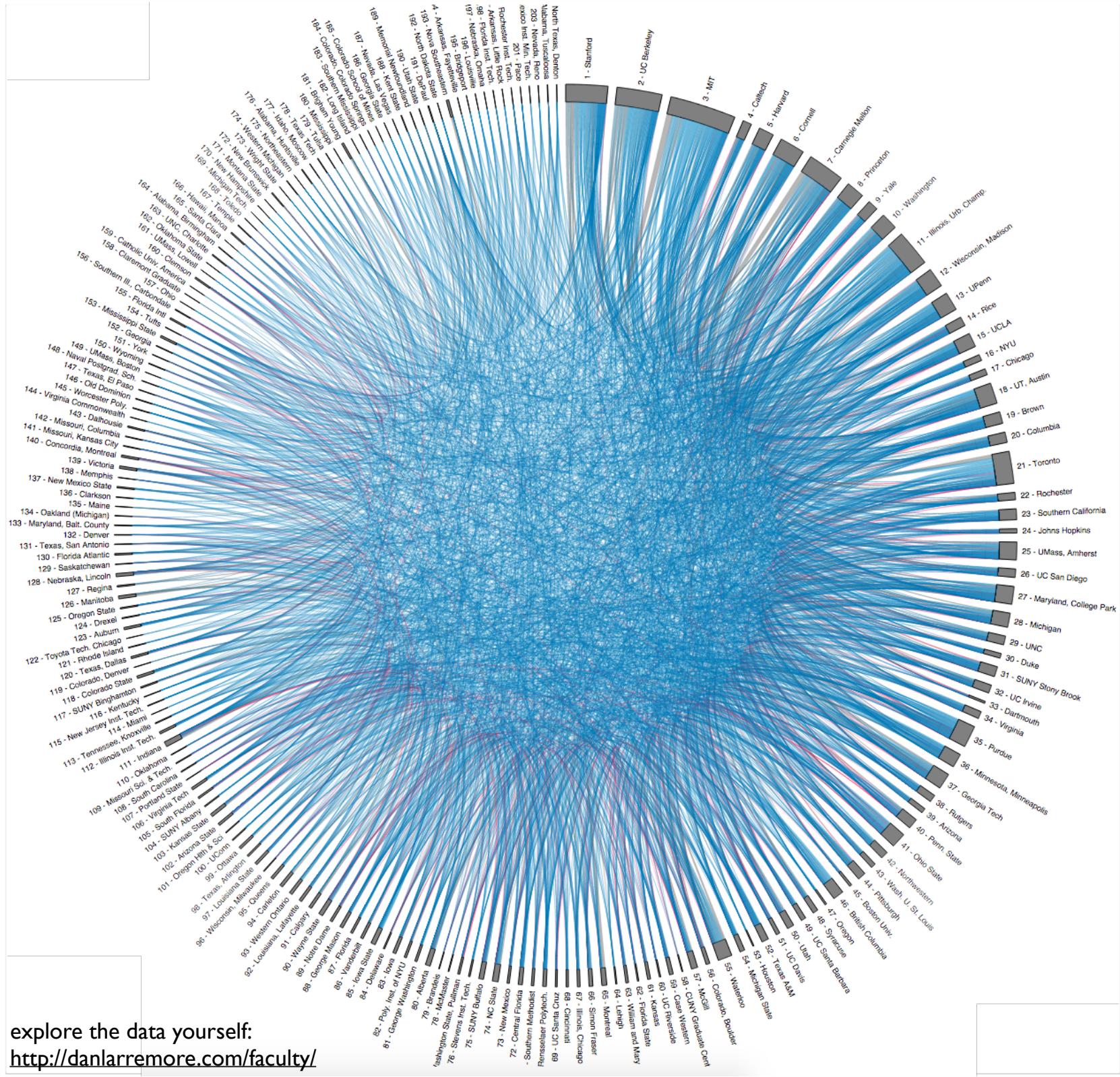
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tenure-track faculty	5032	9336	4556	$\sum = 18,924$
mean size	25	83	32	
Full Professors	2400 (48%)	4294 (46%)	2097 (46%)	
Associate Prof.	1772 (35%)	2521 (27%)	1611 (35%)	
Assistant Prof.	860 (17%)	2521 (27%)	848 (19%)	
female	15%	22%	36%	

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female	15%	22%	36%	
PhDs in-sample	87%	84%	89%	



nearly closed hiring systems



explore the data yourself:
<http://danlarremore.com/faculty/>

huge inequalities in faculty production

huge inequalities in faculty production

Gini coefficients (out-degree)

- 0.69, 0.62, 0.72

50% of faculty from

- 18, 16, 8 universities

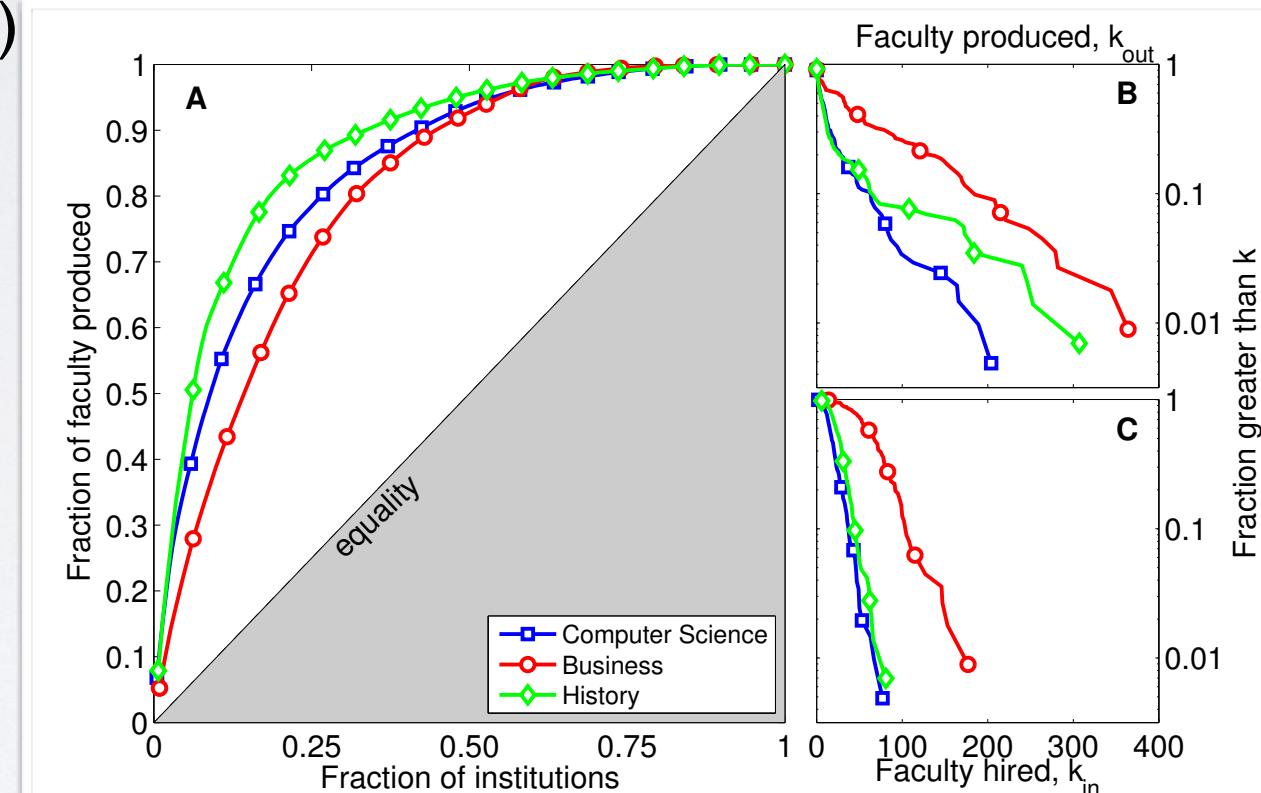
net producers $k_{\text{out}}/k_{\text{in}} > 1$

- 24%, 36%, 18%

I-10 producers vs.

- I-20 : 1.6, 2.1, 3.0x more
- 21-30 : 3.1, 2.3, 5.6x more

CS Business History



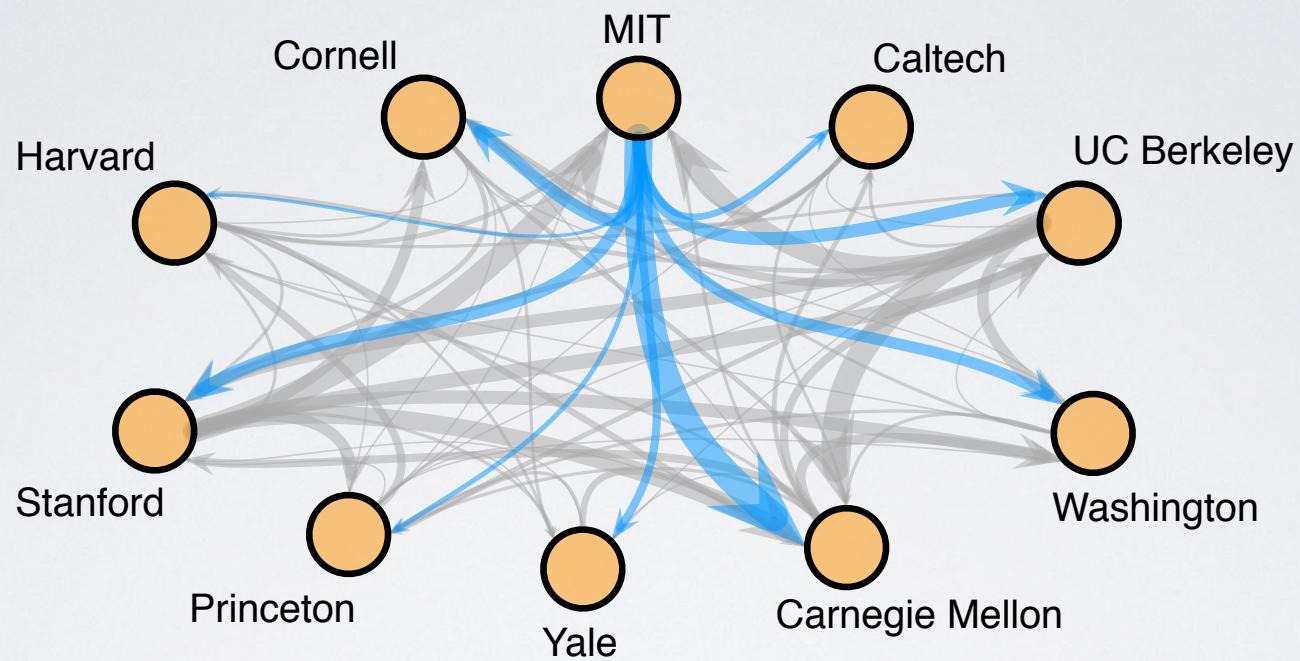
[1] order: CS, Business, History

[2] U.S. Income Gini coefficient = 0.45

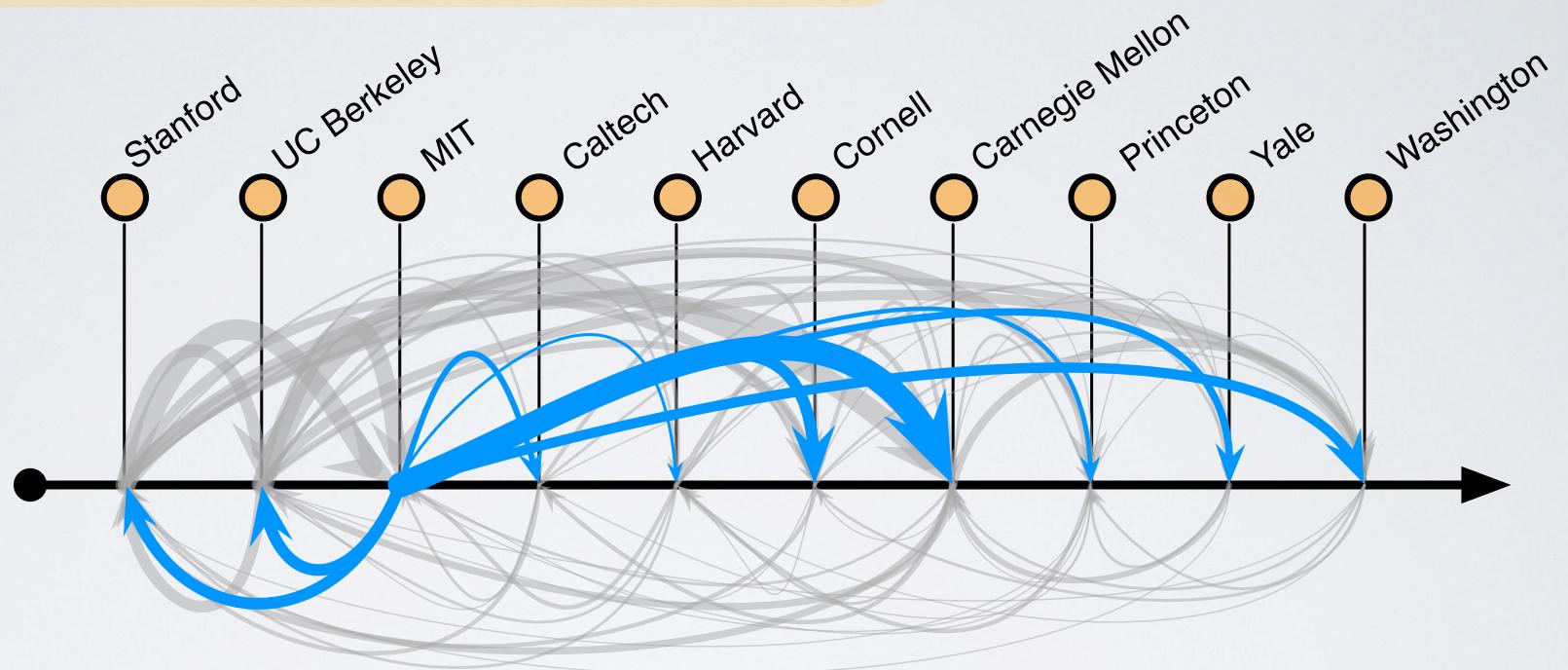
a prestige hierarchy

- difficult to talk about inequalities in academia without talking about rankings (centralities!)
- let's extract a data-driven ranking from the network

a prestige hierarchy



a prestige hierarchy



- select permutation (a ranking) π that minimizes the number of "rank violations" : edges (u, v) where $\pi_v < \pi_u$
- higher-ranked nodes have greater "placement power"
- equivalent to *minimum feedback arc set problem* (NP-hard)

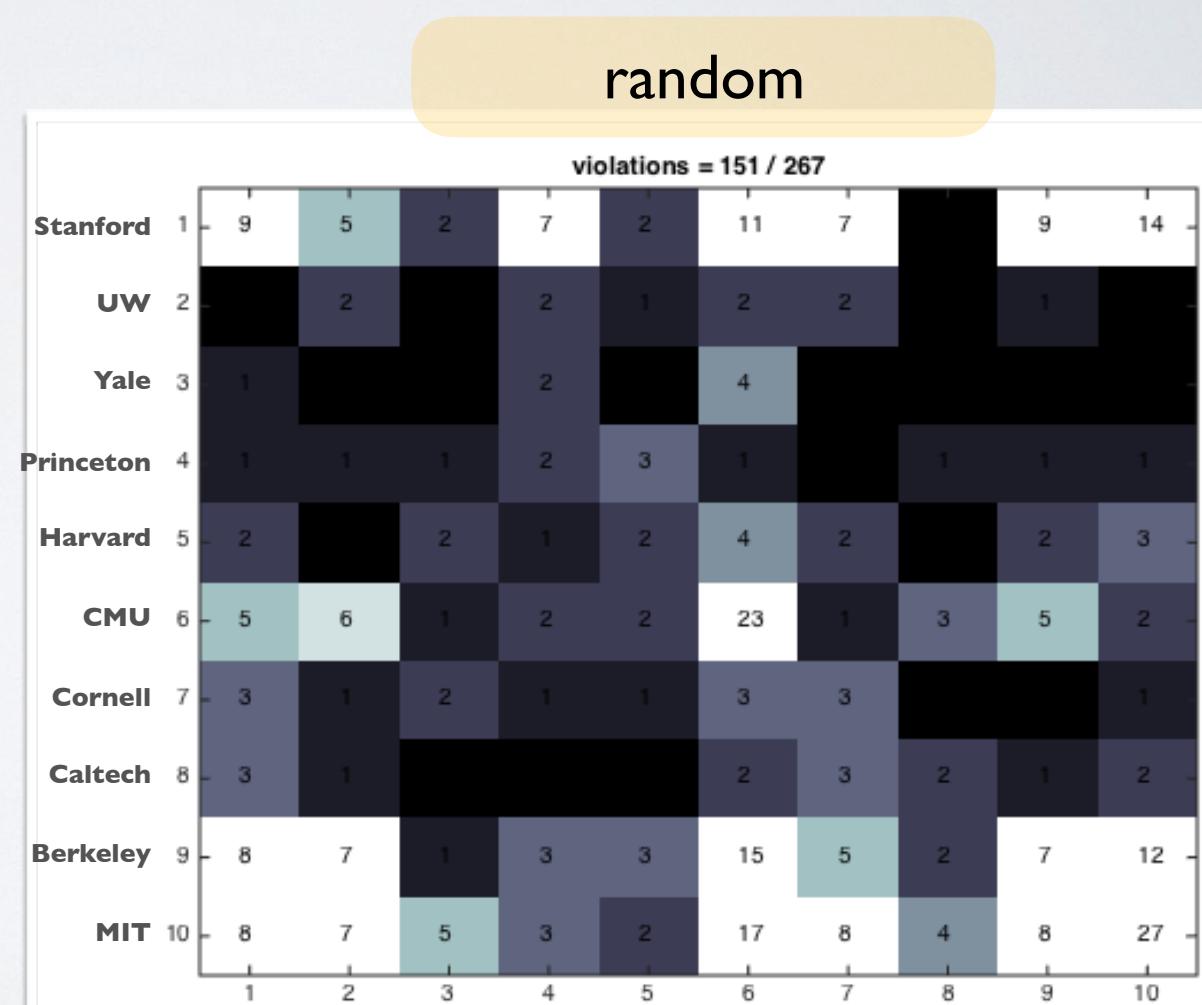
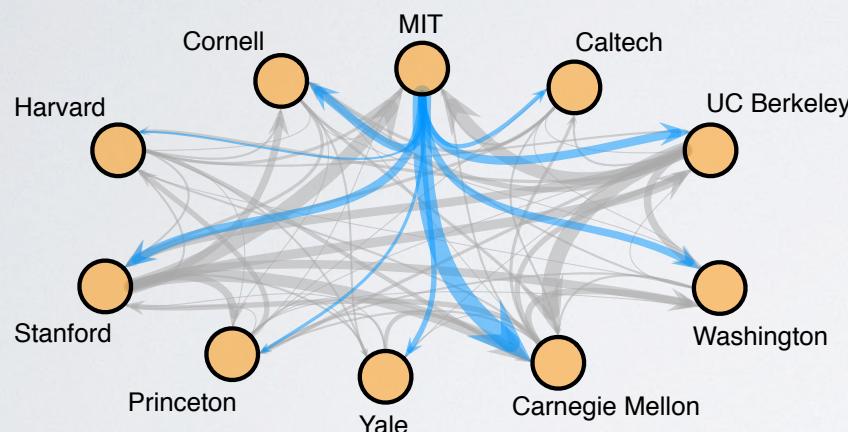
[1] these "MVR"s have a deep history in social theory for extracting dominance or prestige hierarchies from data, especially in animal behavior

[2] MFAS: find the set of arcs of minimum cardinality whose removal converts a directed graph G into a directed acyclic graph

[3] there are many equivalent MVRs for our network. we sample these using a zero-temp MCMC, and average across them to obtain $\langle \pi \rangle$

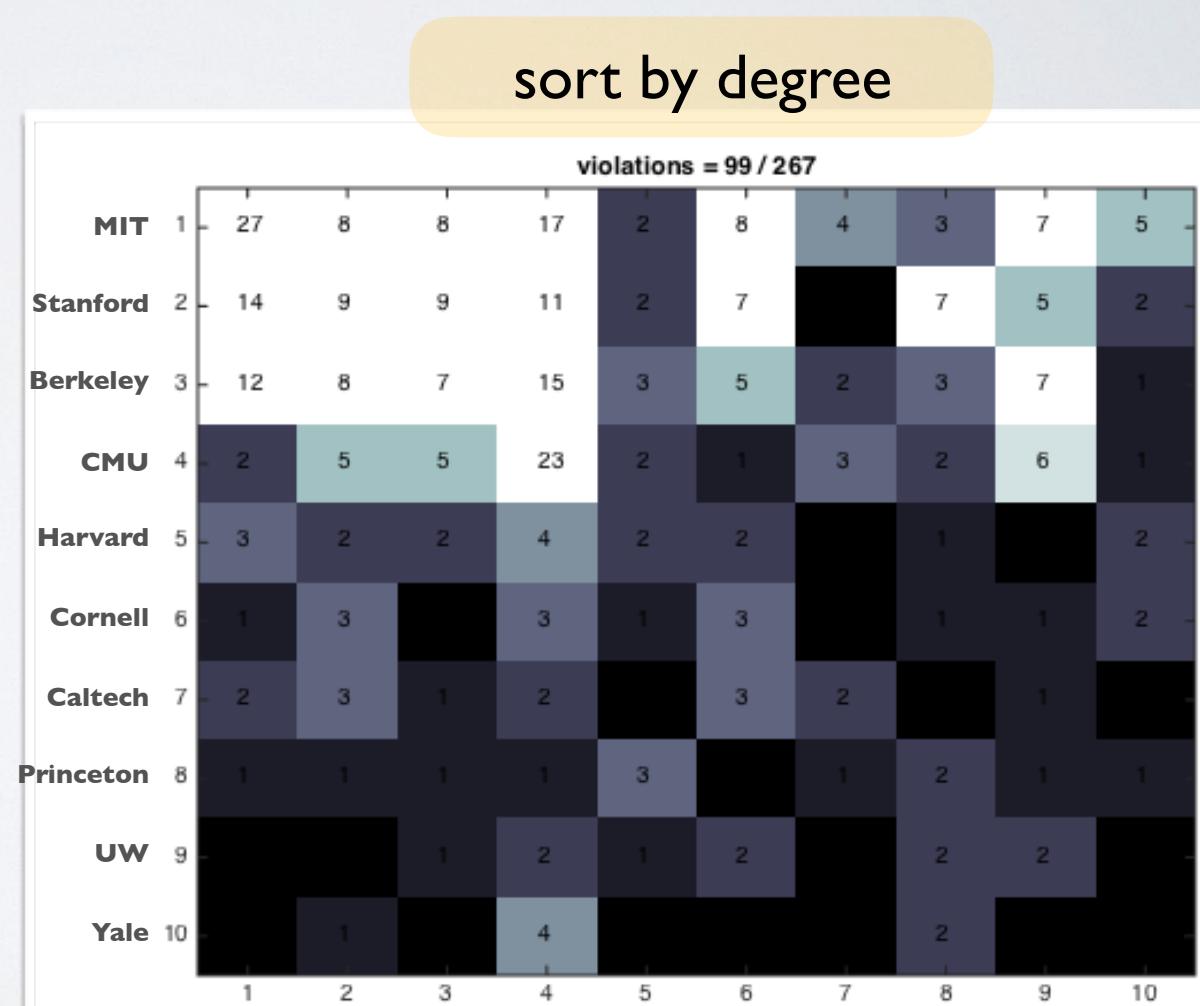
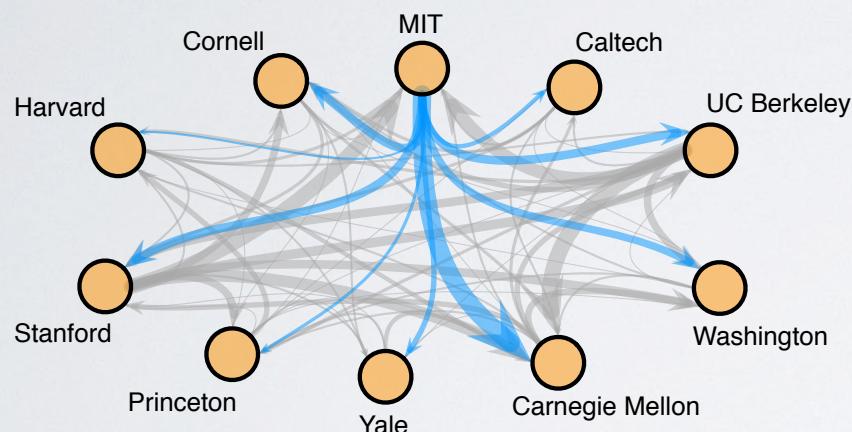
simple zero-temperature MCMC sampler:

- given an ordering π with $\psi(\pi, A)$ rank violations on network A
- repeat *ad infinitum*: choose a pair (u, v) , swap their ranks $\pi_u \leftrightarrow \pi_v$ to obtain π' , compute $\psi(\pi', A)$, accept change if $\psi(\pi', A) \geq \psi(\pi, A)$
- for instance:



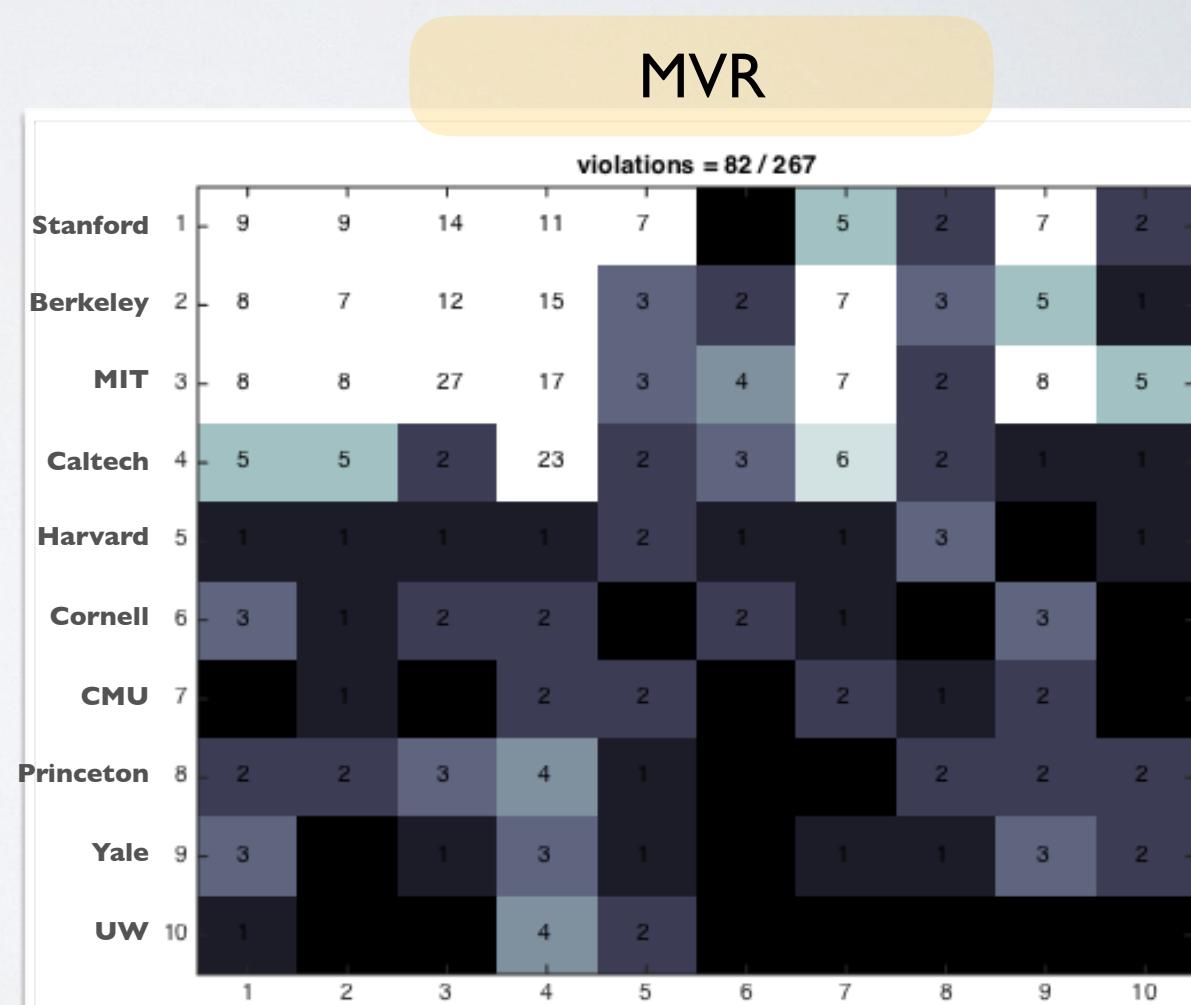
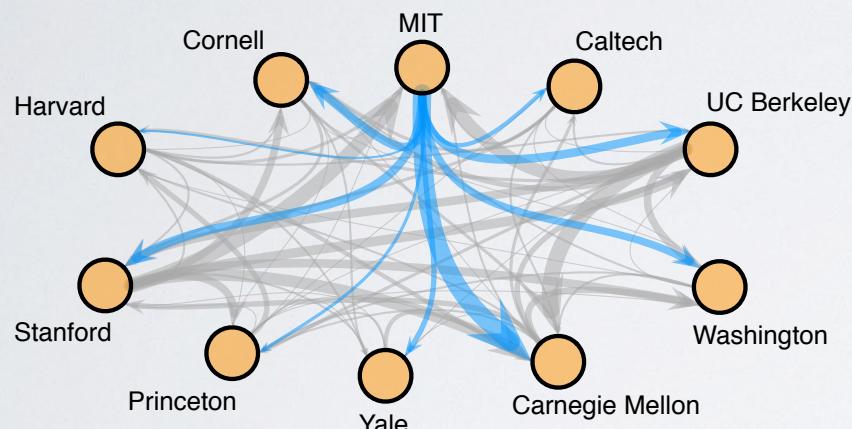
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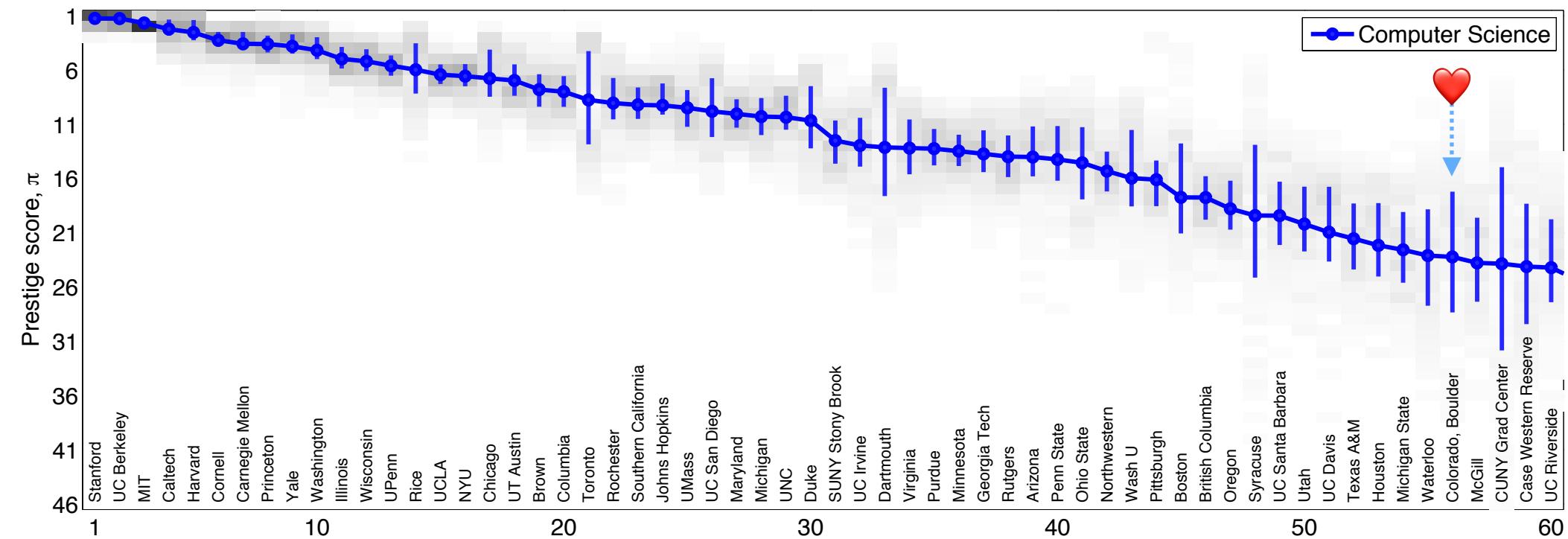
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a prestige hierarchy

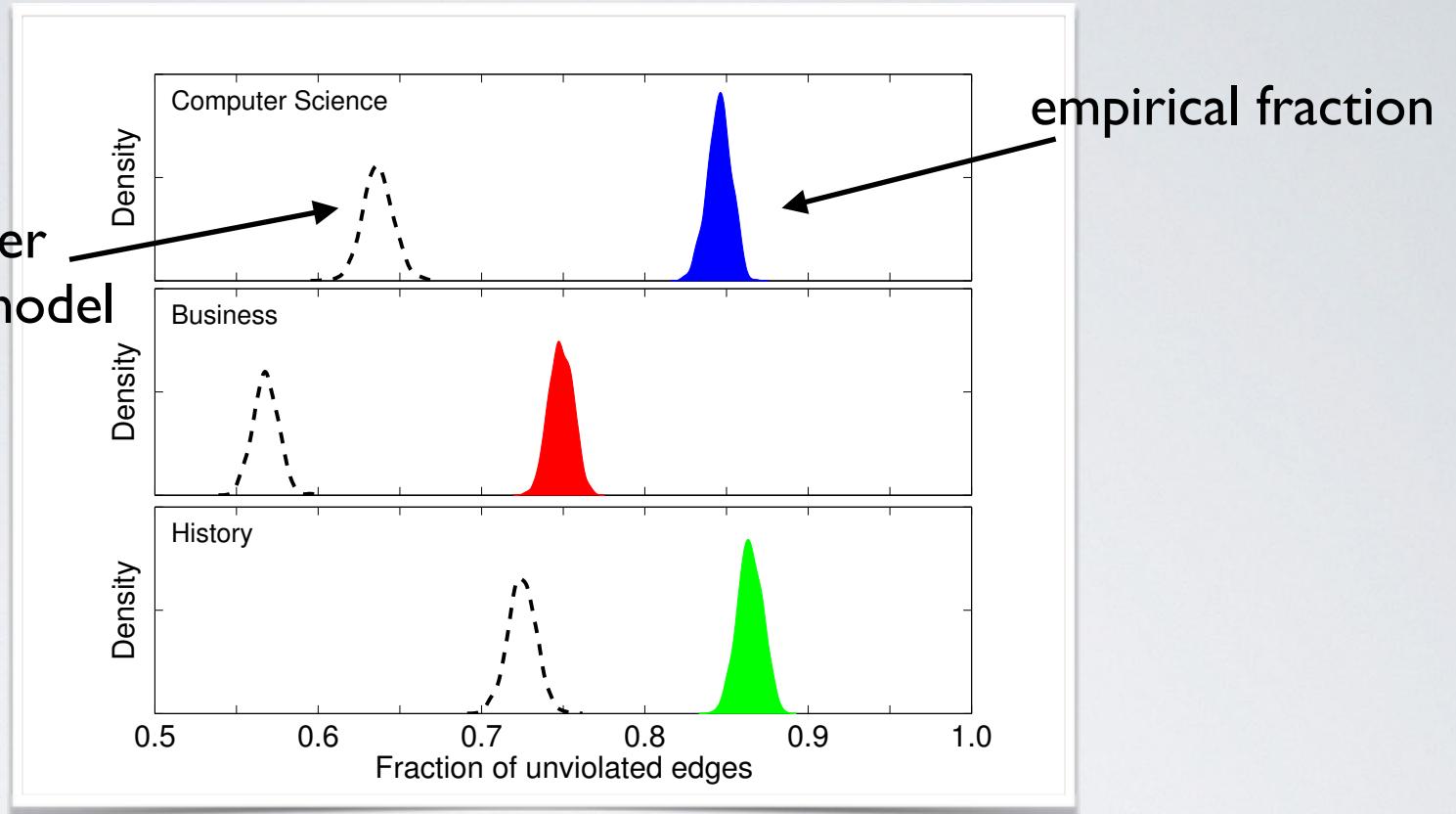
- what do these prestige hierarchies look like?
- what do they tell us about the structure of faculty hiring?
- what predicts placement?



prestige rankings correlate with USNews and NRC

- here, prestige π quantifies *placement power*
- uncertainty increases as prestige decreases
- similar results, but different orderings for Business and History

fraction under
configuration model



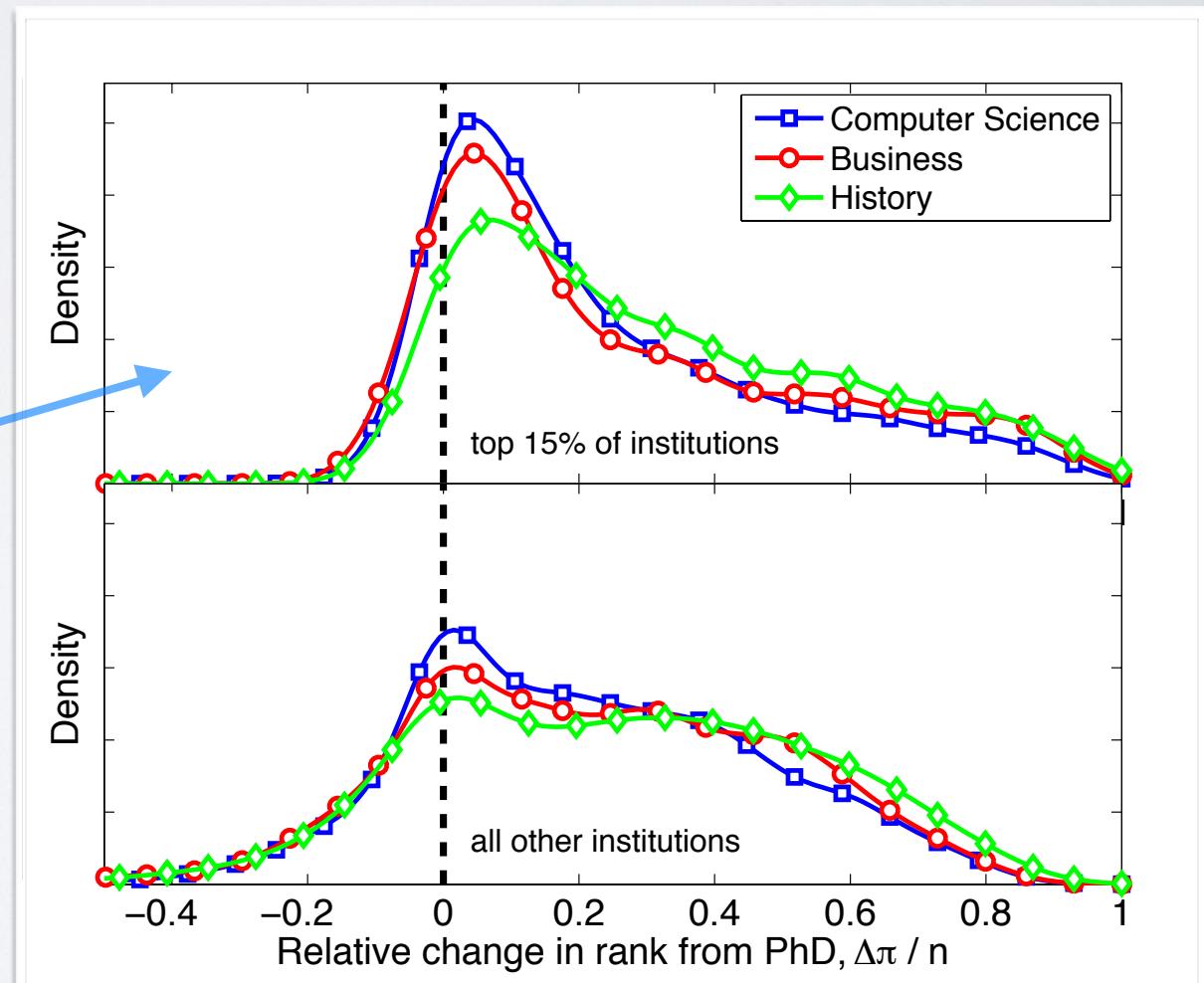
degrees alone do not explain all of the hierarchy

- use configuration model with *observed* degree sequence
- extract MVRs for random graphs & measure fraction of unviolated edges
- compare that null distribution to empirical fraction
- the gap is prestige effect beyond faculty production alone

most placements are down the hierarchy

most placements are down the hierarchy

- down : 88%, 86%, 91%
- up : 12%, 14%, 9%
- $\langle \Delta\pi \rangle = 47, 27, 42$ steps down
- CS: top 15% of departments produce 68% of their own faculty
and hire 7% from outside top 25% of departments



what predicts placement?

- compare 10 node-level features ("importances"):

prestige

US News rank

NRC rank

out-degree

in-degree

out/in degree

eigenvector centrality

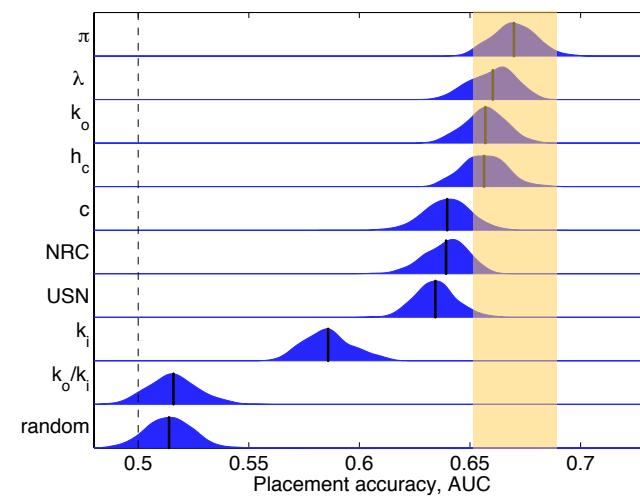
harmonic centrality

closeness centrality

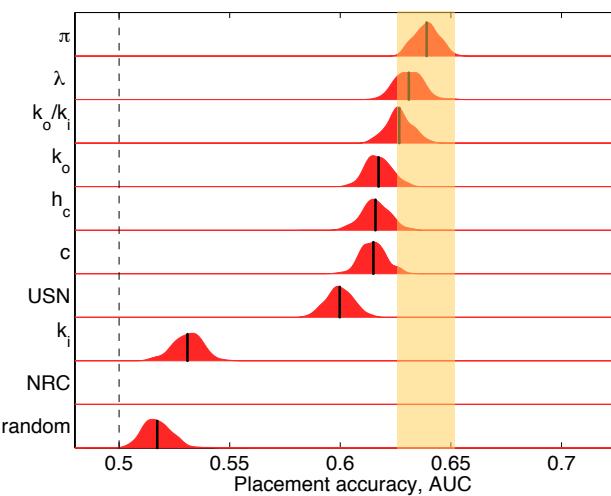
random

what predicts placement?

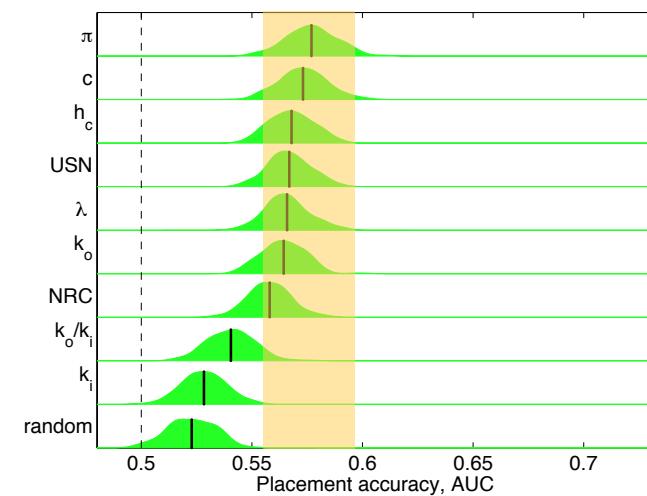
- prestige best *single* predictor in all 3 fields
- order of other features varies by field
- AUCs all below 0.67 = plenty of room for improvement



CS



Business



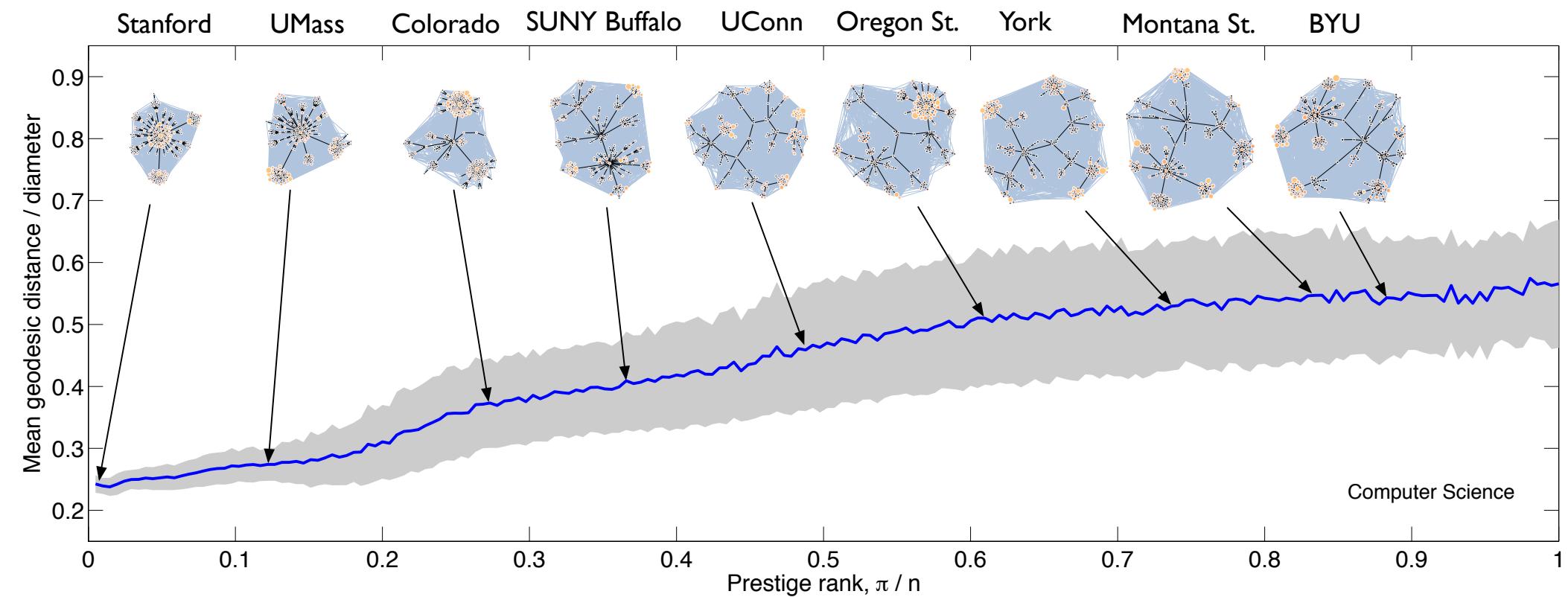
History

prestige correlates with network position

- core and periphery

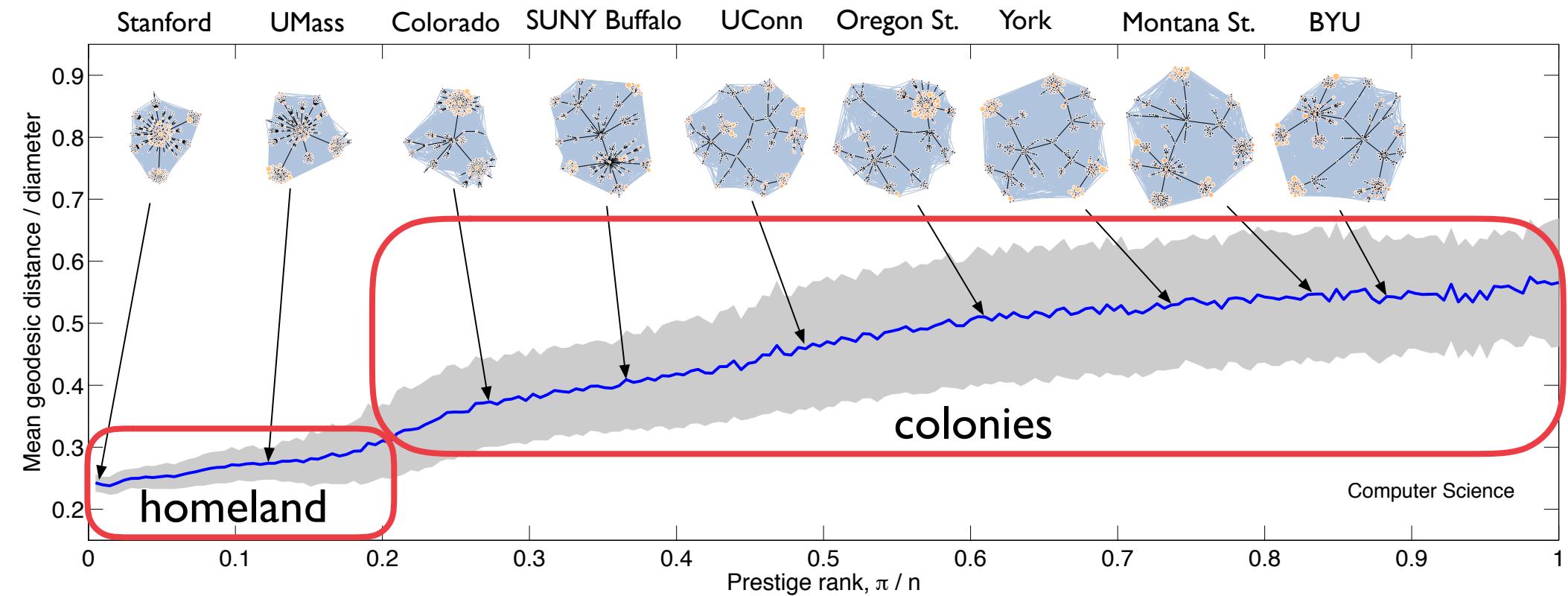
prestige correlates with network position

- core and periphery



prestige correlates with network position

- ~~core and periphery~~ homeland and colonies
- prestige is *influence*, via doctoral placement, over research agendas, research communities, and departmental norms across the discipline



inequality and prestige hierarchies

- prestige is *influence*, encoded in faculty hiring network
- faculty flow out of network core, into periphery ("the colonies")
- small fraction stay inside core
- only ~10% of hires flow "upstream"

future work

- how to measure cultural influence of core departments?
- what is different about "upstream" hires?
- what role for other inequalities : gender, ethnicity/race, SES, neighborhood effects, productivity, etc.?



conclusions and outlook



conclusions and outlook

🎉 networks are cool
[obviously, right?]



conclusions and outlook



networks are cool

[obviously, right?]



powerful window into structure of complex systems

[structure + dynamics = function]



network methods for exploiting rich data

[connectivity + node annotations + edge weights + temporal information | link or label prediction | etc.]



abundance of interesting science applications

[dynamics of social influence | emergence of hierarchy | online social network assembly | etc.]



but be careful: network methods have fundamental limits:

- networks are themselves a *model* of underlying system
- centralities and community detection typically *unsupervised*
- some supervision & auxiliary data = *better* inferences / predictions
- formulate your mechanism in terms of nodes, edges, and attributes
- have fun!



University of Colorado **Boulder**

more material here A yellow hand emoji pointing towards the right side of the slide.

Network Analysis and Modeling

Instructor: Aaron Clauset or Daniel Larremore

This graduate-level course will examine modern techniques for analyzing and modeling the structure and dynamics of complex networks. The focus will be on statistical algorithms and methods, and both lectures and assignments will emphasize model interpretability and understanding the processes that generate real data. Applications will be drawn from computational biology and computational social science. No biological or social science training is required. (Note: this is not a scientific computing course, but there will be plenty of computing for science.)

Full lectures notes online (~150 pages in PDF)

<http://santafe.edu/~aaronc/courses/5352/>