## Solution 1:

- The inner loss is the loss that is optimized directly by the machine learning model. The outer loss is the loss (or performance measurement) used to evaluate the model.
- Which model is more likely to overfit the training data:
  - k-NN with 1 or with 10 neighbors? 1 neighbor, because it's an exact memorization of training data.
  - Logistic regression with 10 or 20 features? 20 features, because the more features, the more coefficients
    the learner estimates. More coefficients mean more degrees of freedom, which make overfitting more
    likely.
  - LDA or QDA? QDA, because it has more parameters to possibly overfit the data. LDA is more likely
    to underfit more complex relationships.
- Which of the following methods yield an unbiased generalization error estimate? Performance estimation ...
  - on training data: Biased, too optimistic
  - on test data: Unbiased / Biased, too pessimistic (Test data is not included / included in the final model)
  - on training and test data combined: **Biased, too optimistic** (But a little bit less than only using training data).
  - using cross validation: **Biased, too pessimistic** (The higher the ratio of folds / number of observation, the smaller the pessimistic bias)
  - using subsampling: **Biased, too pessimistic** (The smaller the subsampling rate, the larger the pessimistic bias)
- Resampling strategies solve the problem that comes from the randomness of the training and test data split: Error estimation using a single split has a high variance. Resampling estimates are more robust because they average over different splits.
- Nested resampling solves the problem of simultaneously conducting tuning/model selection and performance estimation. When we use the performance estimates from the same data that were used for model selection (as done in simple, not-nested resampling), the final error estimate is too optimistic.

## Solution 2:

- The training performance is too optimistic (mmce of 0), because the mmce is higher on new data.
- The test performance is unbiased (if the final model is only trained on the training data), but it depends on the split, as can be seen in the CV folds: Each CV fold represents a training test split and the mmce measure varies between folds.
- The CV estimate averages over the different splits and gives an slightly pessimistic, more robust estimate.
- The CV estimate is preferable over the other two, but more computationally expensive.

## Solution 3:

a) Each loss function we have learned so far to fit the model (inner loss) can also be used as performance measure (outer loss).

For classification:

- 0-1 loss (= mean misclassification error),
- Logistic loss (bernoulli loss), ...

For regression:

- $L_2$ -loss (= mean squared error),
- $L_1$ -loss (= mean absolute error), ...

To get a list of all measures you can use mlr\_measures.

```
b) # look at the task
  task <- tsk("boston_housing")</pre>
  task
  ## <TaskRegr:boston_housing> (506 x 19)
  ## * Target: medv
  ## * Properties: -
  ## * Features (18):
       - dbl (13): age, b, cmedv, crim, dis, indus, lat, lon, lstat, nox,
       ptratio, rm, zn
  ## - int (3): rad, tax, tract
      - fct (2): chas, town
  n <- task$nrow
  # select index vectors to subset the data randomly
  set.seed(123)
  train_ind <- sample(seq_len(n), 0.5*n)
  test_ind <- setdiff(seq_len(n), train_ind)</pre>
  # specify learner
  learner <- lrn("regr.kknn", k = 3)</pre>
  # train model to the training set
  learner$train(task, row_ids = train_ind)
  # predict on the test set
  pred <- learner$predict(task, row_ids = test_ind)</pre>
  pred
  ## <PredictionRegr> for 253 observations:
        row_ids truth response
              1 24.0 23.22445
  ##
               2 21.6 19.98830
  ##
               3 34.7 34.97419
  ##
  ## ---
             504 23.9 22.22775
  ##
             505 22.0 21.76531
          506 11.9 20.88958
```

```
c) # predict on the train set
    pred_train <- learner$predict(task, row_ids = train_ind)
    pred_train$score(list(msr("regr.mse"), msr("regr.mae")))

## regr.mse regr.mae
## 1.2322560 0.7564092

# predict on the test set
    pred_test <- learner$predict(task, row_ids = test_ind)
    pred_test$score(list(msr("regr.mse"), msr("regr.mae")))

## regr.mse regr.mae
## 12.424958 2.596332</pre>
```

Unsurprisingly the model performs better on the training data (smaller loss) then on the test data.

```
d) # select different index vectors to subset the data randomly
  set.seed(321)
  train_ind <- sample(seq_len(n), 0.5*n)</pre>
  test_ind <- setdiff(seq_len(n), train_ind)</pre>
  # specify learner
  learner <- lrn("regr.kknn", k = 3)</pre>
  # train model to the training set
  learner$train(task, row_ids = train_ind)
  # predict on the test set
  pred_test <- learner$predict(task, row_ids = test_ind)</pre>
  pred_test
  ## <PredictionRegr> for 253 observations:
  ##
         row_ids truth response
               2 21.6 29.45474
  ##
               5 36.2 33.14900
  ##
  ##
               6 28.7 32.95574
  ## ---
  ##
             501 16.8 19.61312
              505 22.0 23.29286
             506 11.9 21.28301
  ##
  pred_test$score(list(msr("regr.mse"), msr("regr.mae")))
  ## regr.mse regr.mae
  ## 12.507468 2.458798
```

Effect: We will predict different observations since the test set is different. The same observations get a slightly different prediction (e.g. observation with id 2). This affects the final error estimation.

```
e) rdesc <- rsmp("cv", folds = 10)
r <- resample(task, learner, rdesc)

## INFO [17:26:43.566] [mlr3] Applying learner 'regr.kknn' on task 'boston_housing' (iter 9/10)
## INFO [17:26:43.616] [mlr3] Applying learner 'regr.kknn' on task 'boston_housing' (iter 10/10)
## INFO [17:26:43.643] [mlr3] Applying learner 'regr.kknn' on task 'boston_housing' (iter 7/10)
## INFO [17:26:43.662] [mlr3] Applying learner 'regr.kknn' on task 'boston_housing' (iter 6/10)
```

```
## INFO [17:26:43.683] [mlr3] Applying learner 'regr.kknn' on task 'boston_housing' (iter 4/10)
## INFO [17:26:43.705] [mlr3] Applying learner 'regr.kknn' on task 'boston_housing' (iter 8/10)
## INFO [17:26:43.726] [mlr3] Applying learner 'regr.kknn' on task 'boston_housing' (iter 1/10)
## INFO [17:26:43.749] [mlr3] Applying learner 'regr.kknn' on task 'boston_housing' (iter 5/10)
## INFO [17:26:43.770] [mlr3] Applying learner 'regr.kknn' on task 'boston_housing' (iter 3/10)
## INFO [17:26:43.790] [mlr3] Applying learner 'regr.kknn' on task 'boston_housing' (iter 2/10)

r$aggregate(list(msr("regr.mse"), msr("regr.mae")))

## regr.mse regr.mae
## 10.045363 2.229458
```