

DCM for EEG

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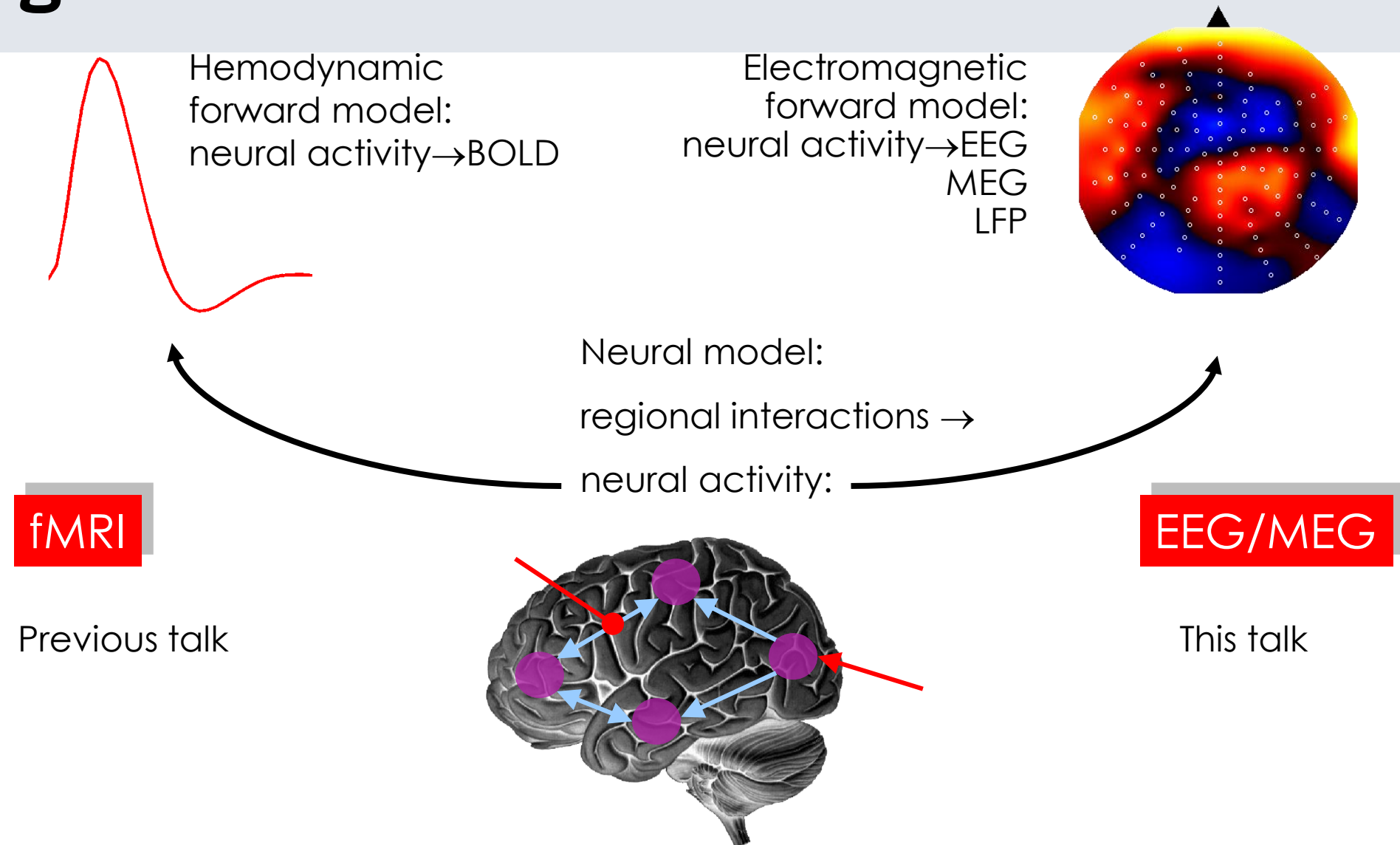
University of
Zurich^{UZH}

ETH zürich



Translational Neuromodeling Unit

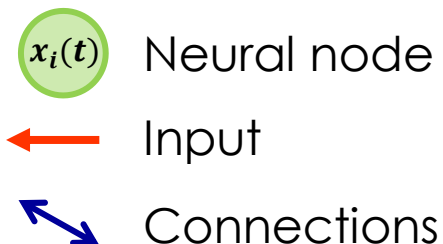
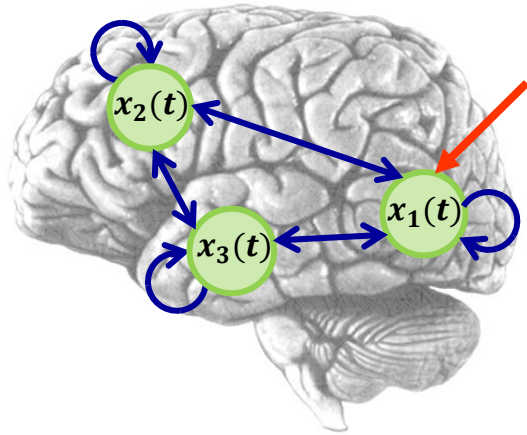
Recap: Dynamic Causal Modeling (DCM)



Recap: DCM approach to effective connectivity

A simple model of
a neural network

...



... described as a
dynamical system

...

$$\dot{x} = f(x, u, \theta_x)$$

... causes the data
(BOLD signal).

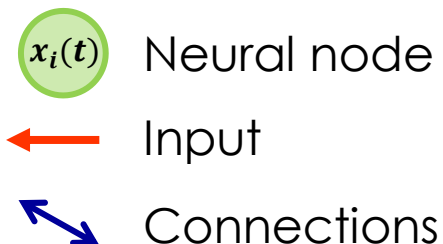
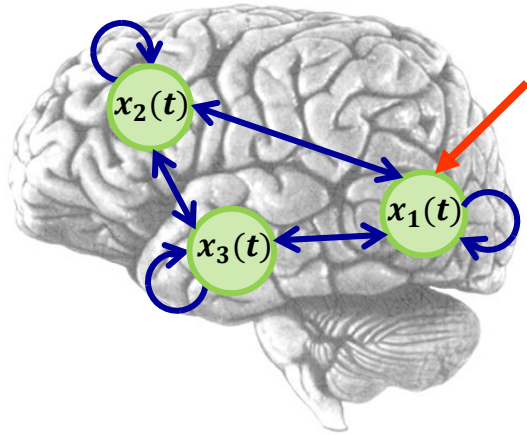
$$y = g(x, \theta_y) + \varepsilon$$

Let the system run with input (u) and parameters (θ_x, θ_y), and you will get a BOLD signal time course y that you can compare to the measured data.

Recap: DCM approach to effective connectivity

A simple model of
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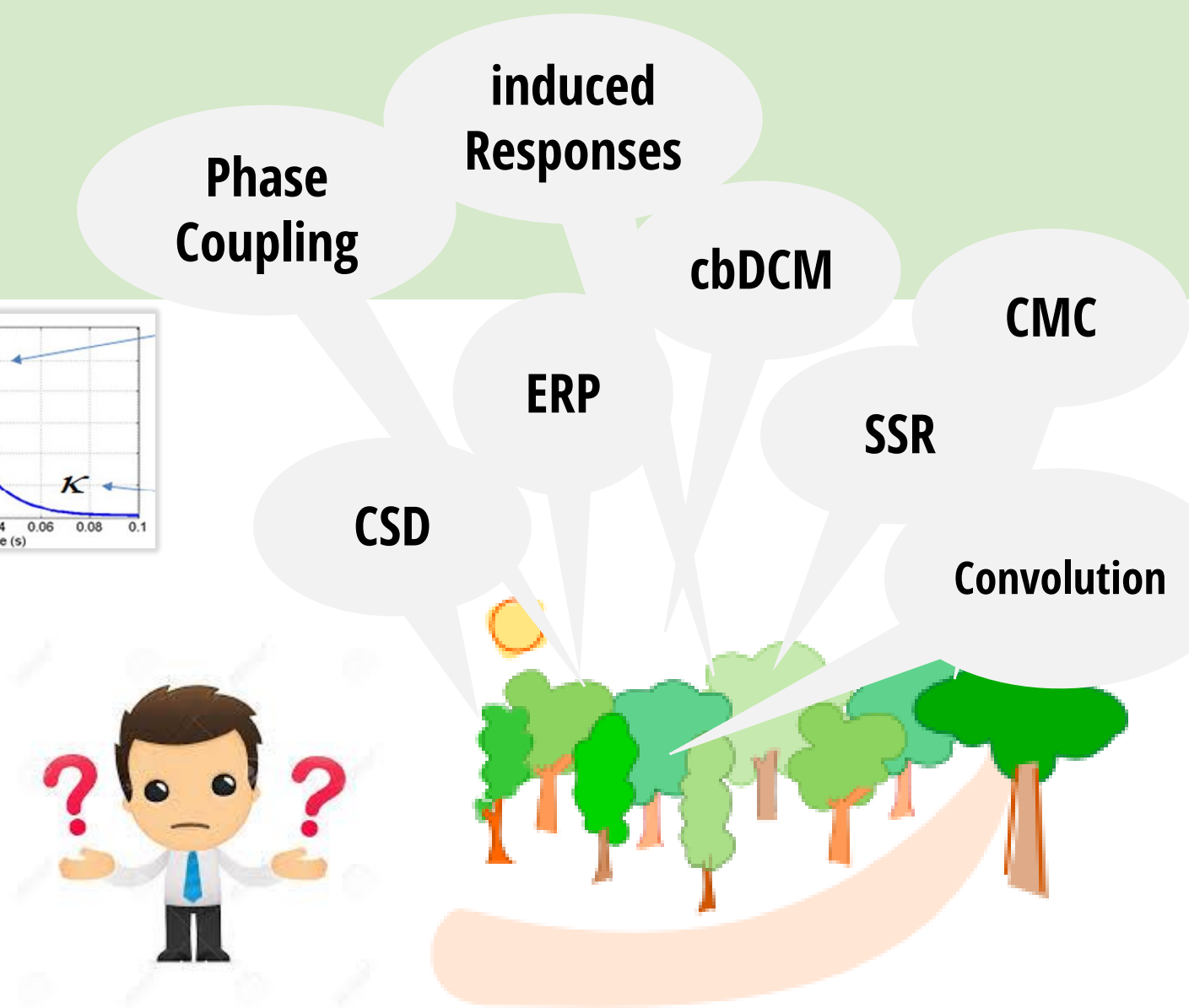
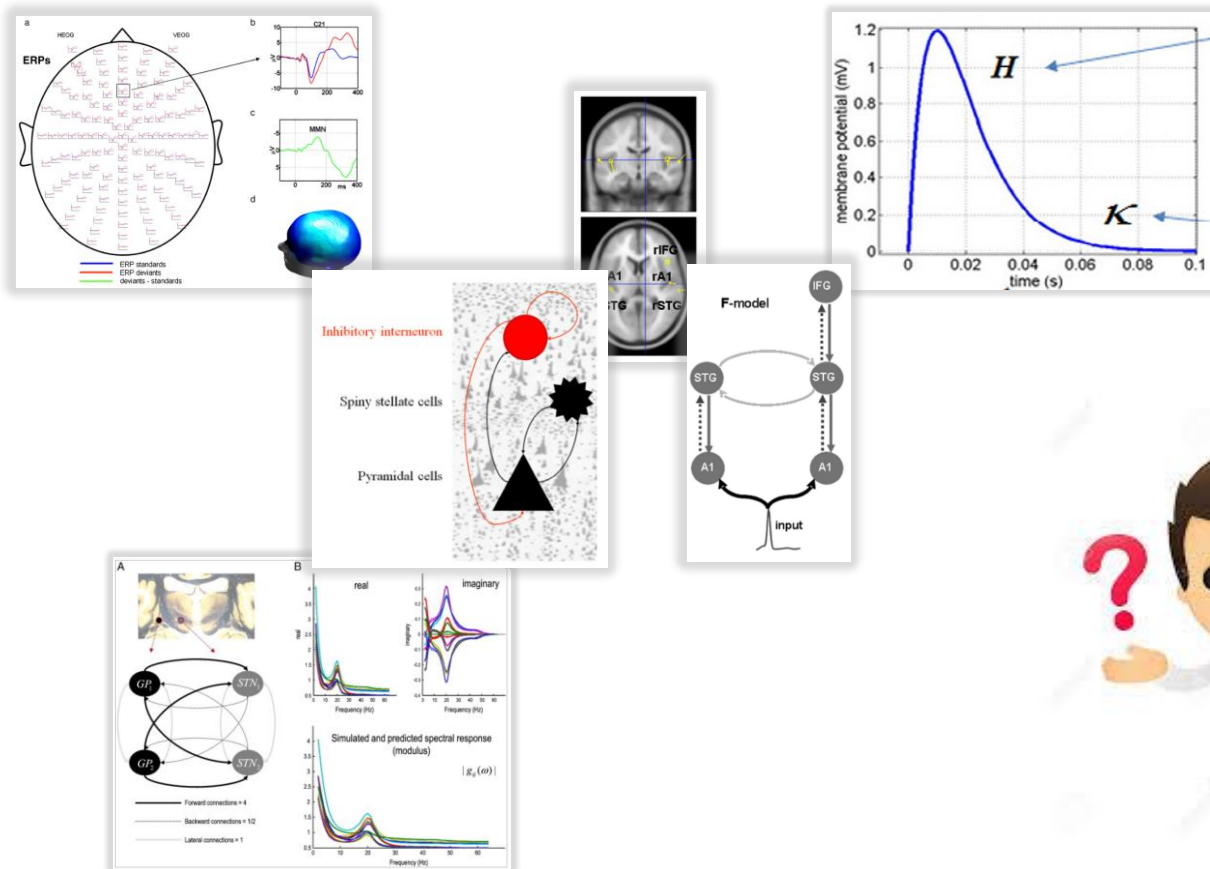
EEG

$$y = g(x, \theta_y) + \varepsilon$$

EEG

Let the system run with input (u) and parameters (θ_x, θ_y), and you will get a **BOLD** signal time course y that you can compare to the measured data.

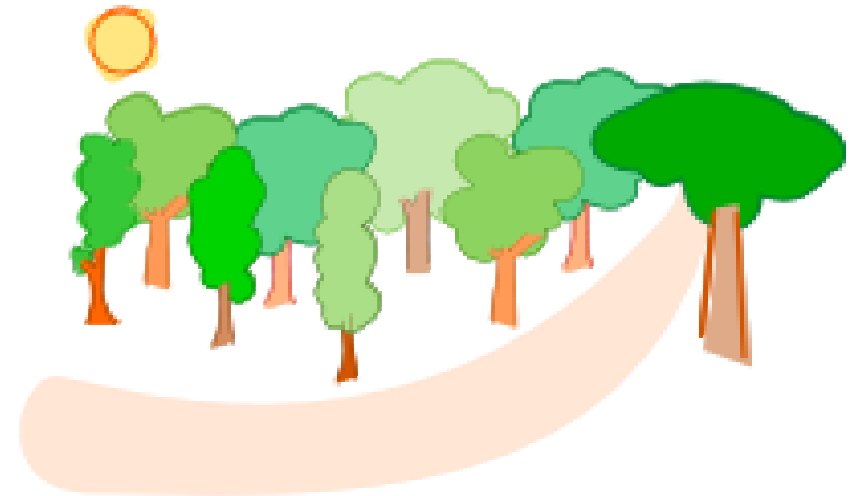
The variety of DCM for EEG

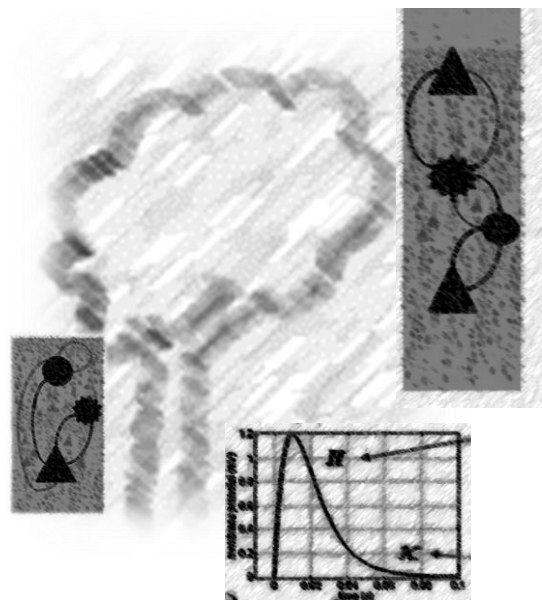


Garrido, Neuroimage, 2007; Moran, frontiers in Comp. Neuroscience, 2013; Friston, Neuroimage, 2012

“ ... important distinction between different models and different data features ...”

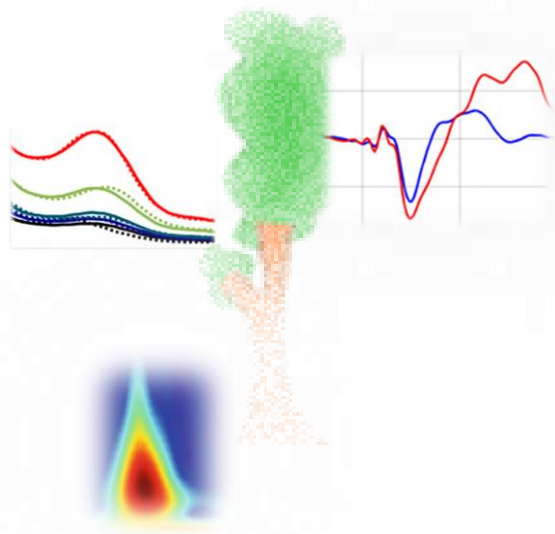
Moran, frontiers in Comp. Neuroscience, 2013



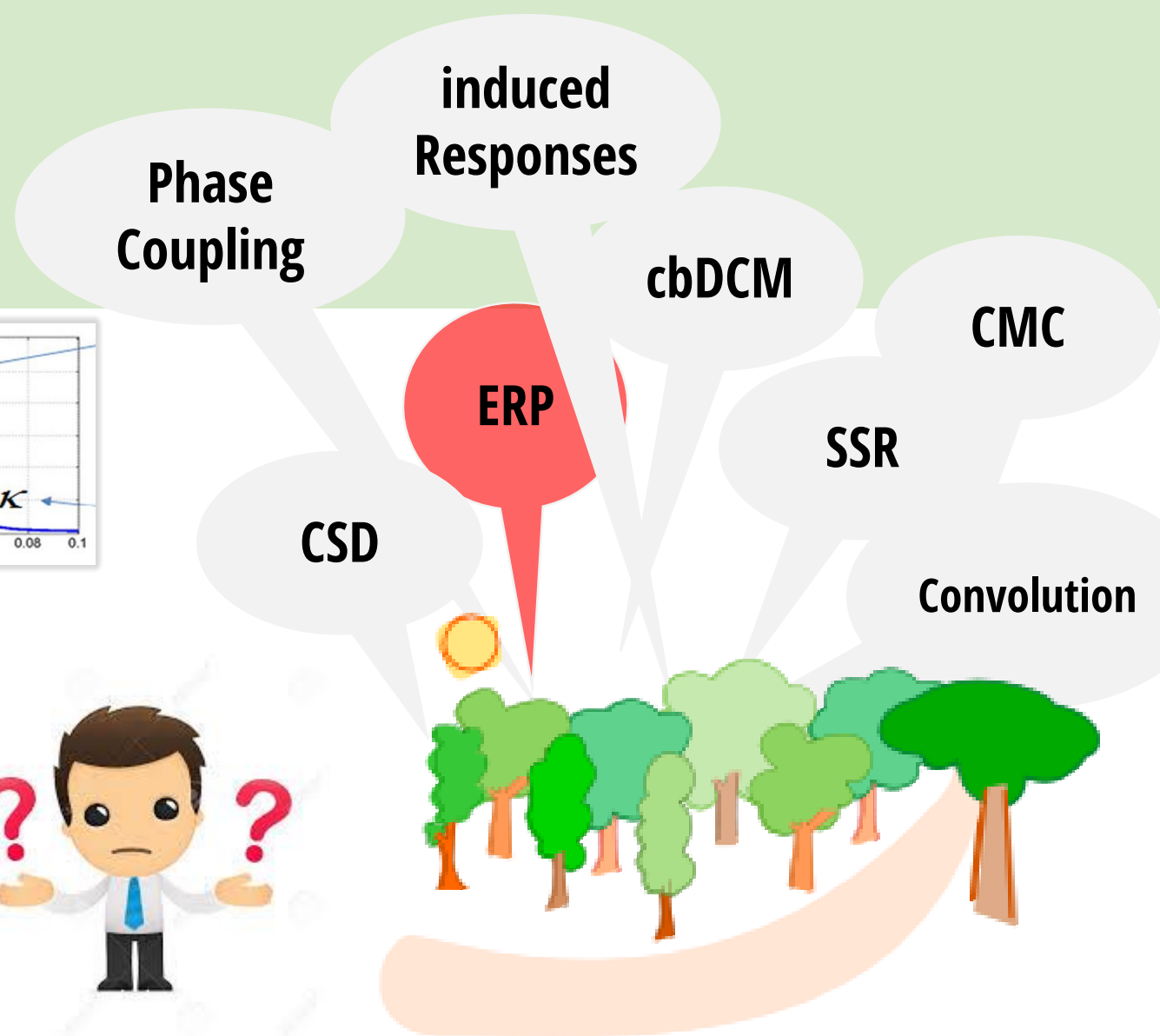
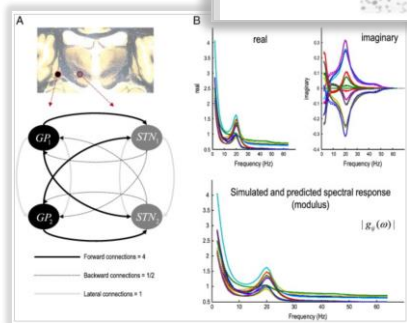
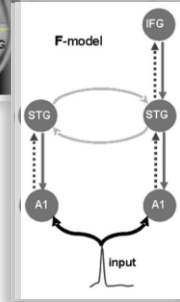
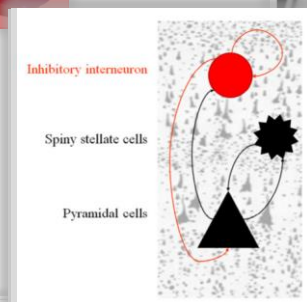
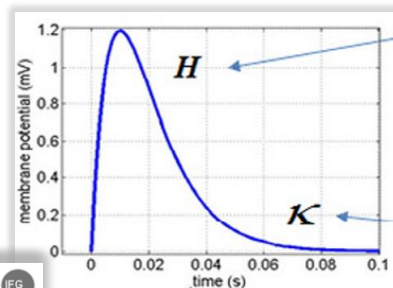
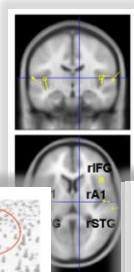
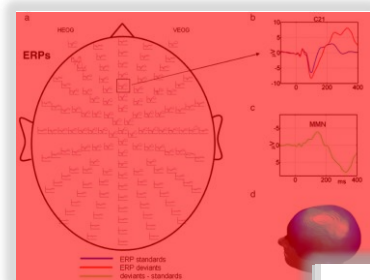


The naming refers to either data feature, within source connectivity, or dynamics.

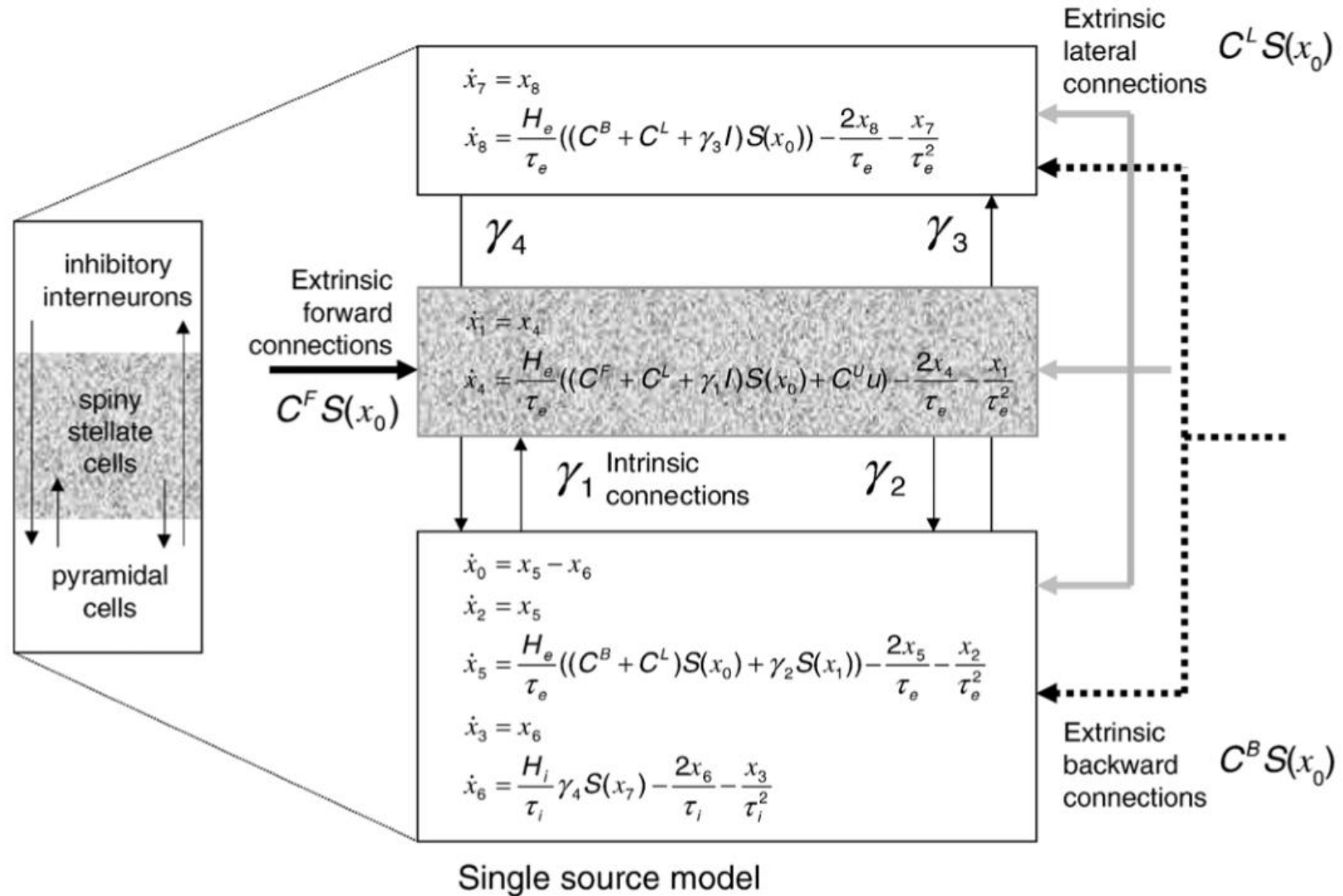
There is usually not a unique model to model a data feature, but some might be more suited than others.



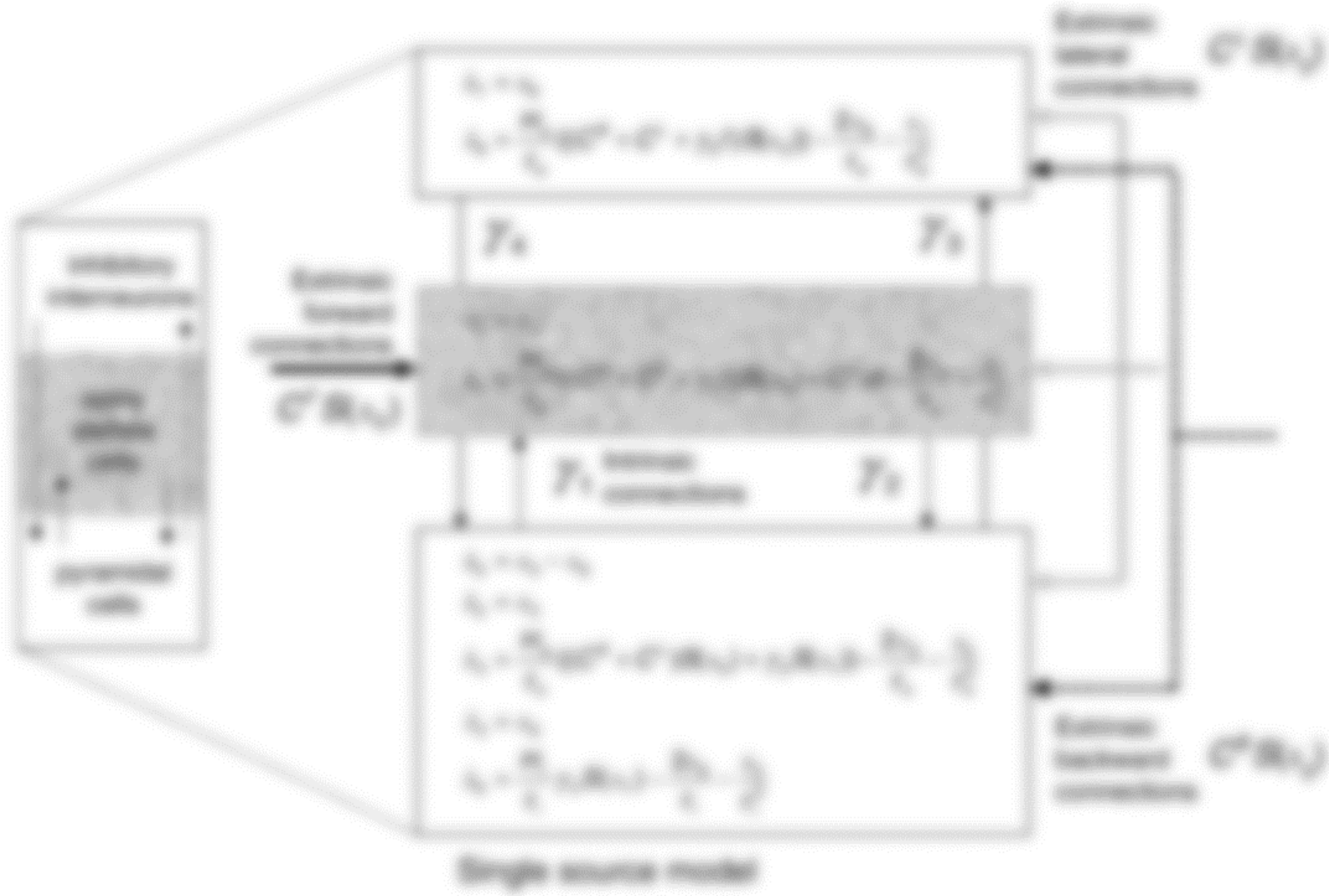
The variety of DCM for EEG



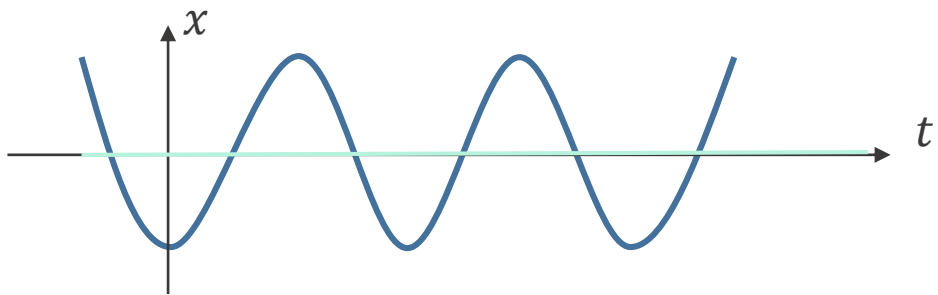
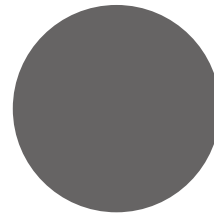
Models



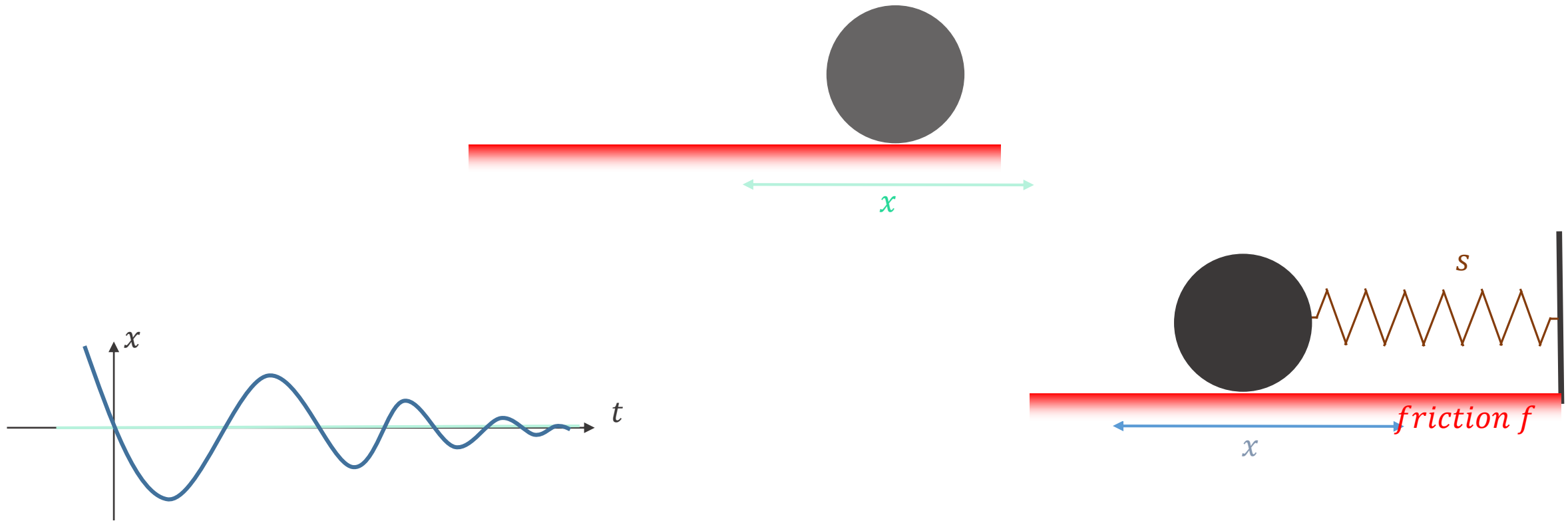
Models



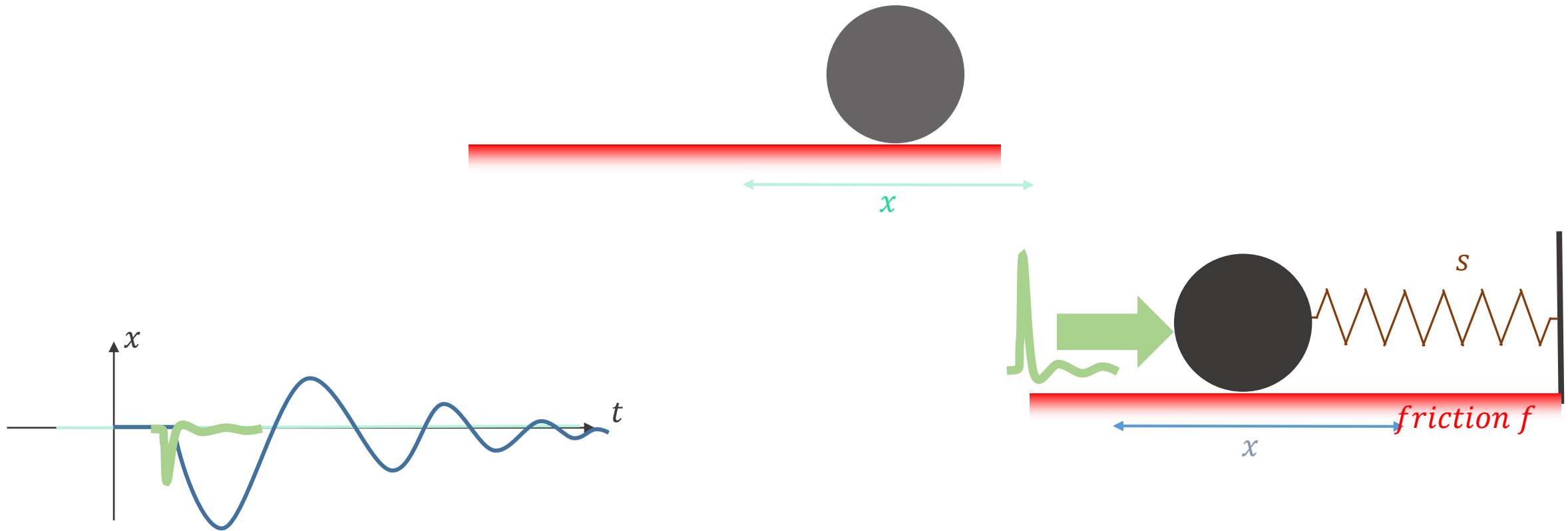
Thought Experiment



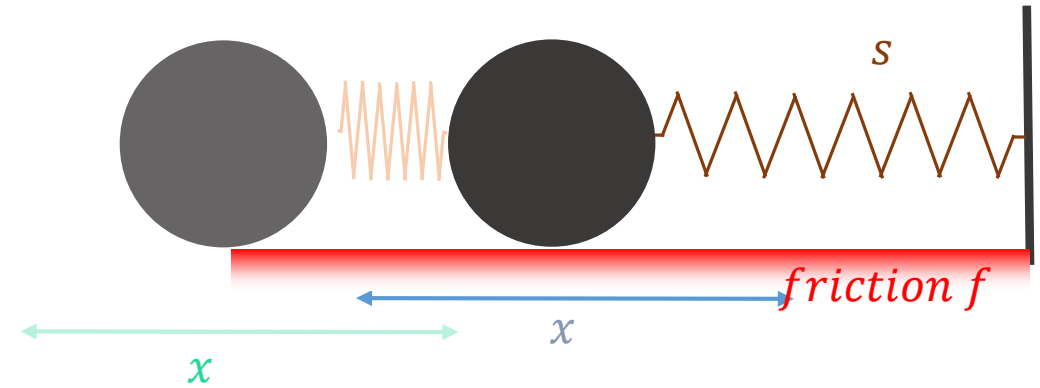
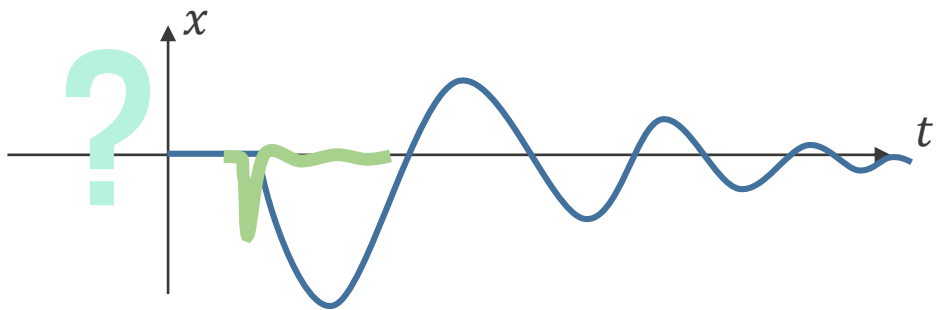
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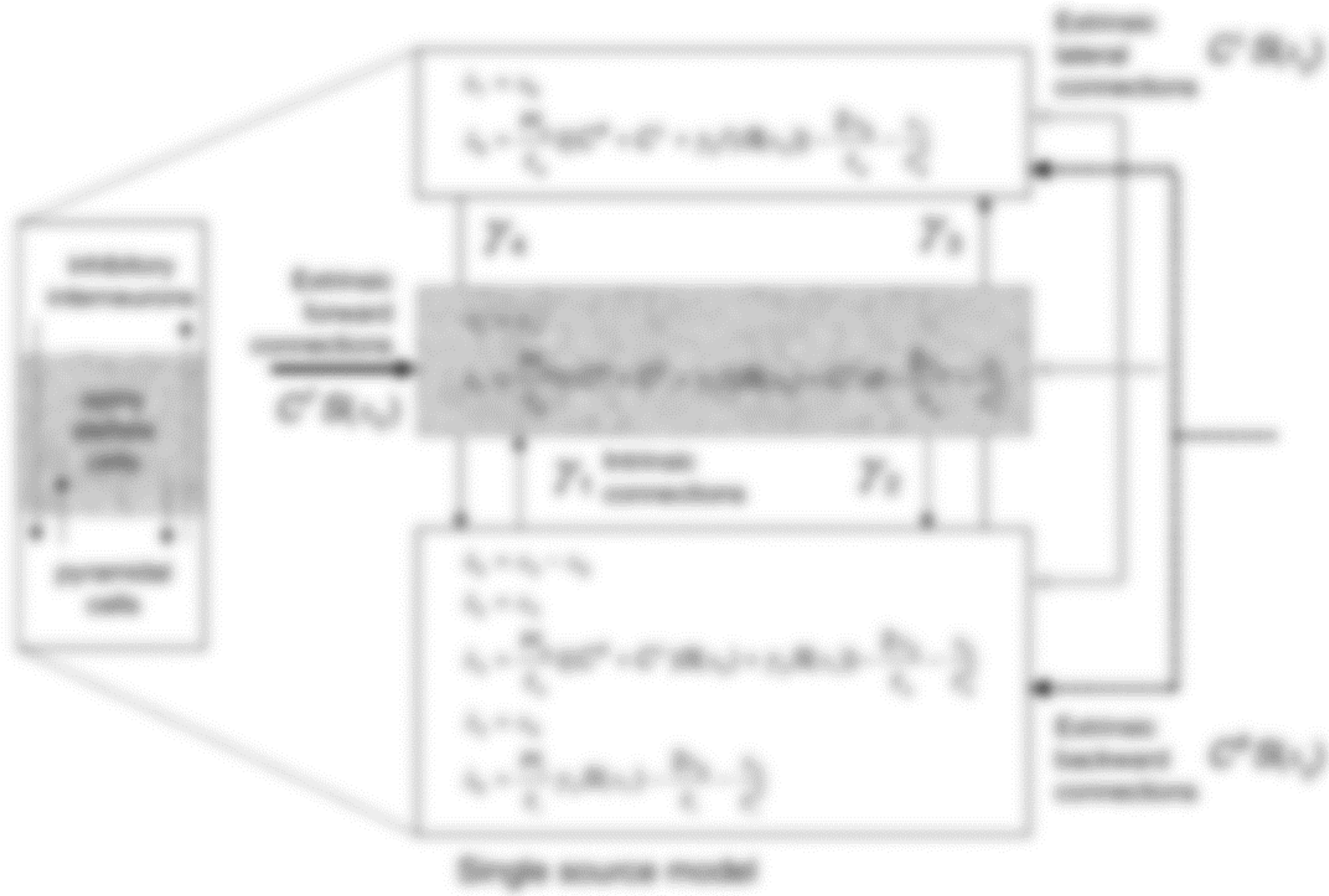
Thought Experiment



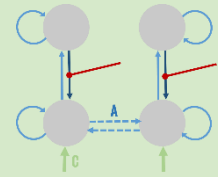
Thought Experiment



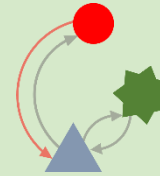
Models



Models



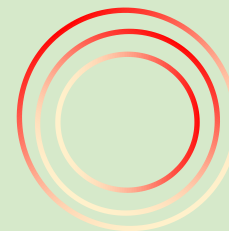
Between Source Connectivity



Within Source Connectivity



Dynamics



Forward Model

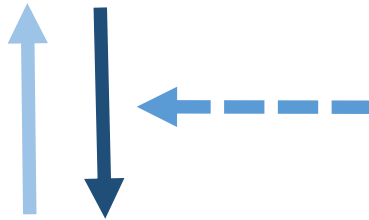
Between Source Connectivity

Sources / Regions



Three types of connections:

Forward, Backward, Lateral



Between condition effects



Input



SPM Variable

X

A

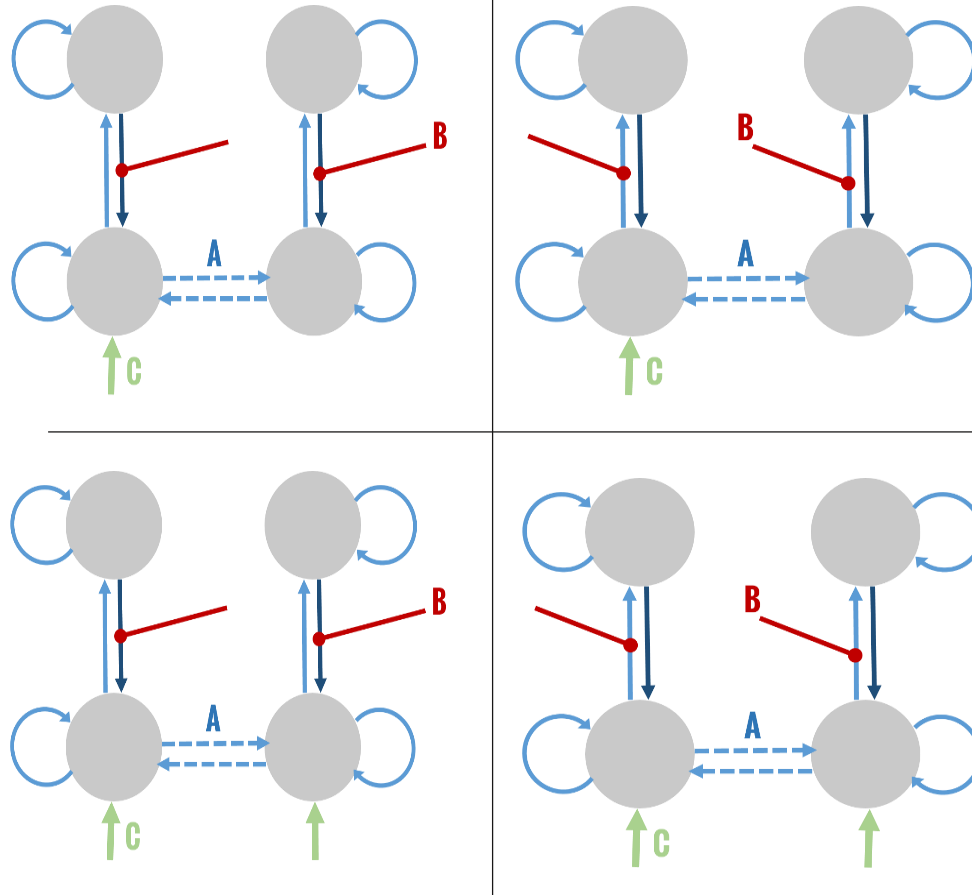
B

C

Hypotheses

Hypotheses should be based on classical finding.

Once again, you try to explain a difference that is in the data.

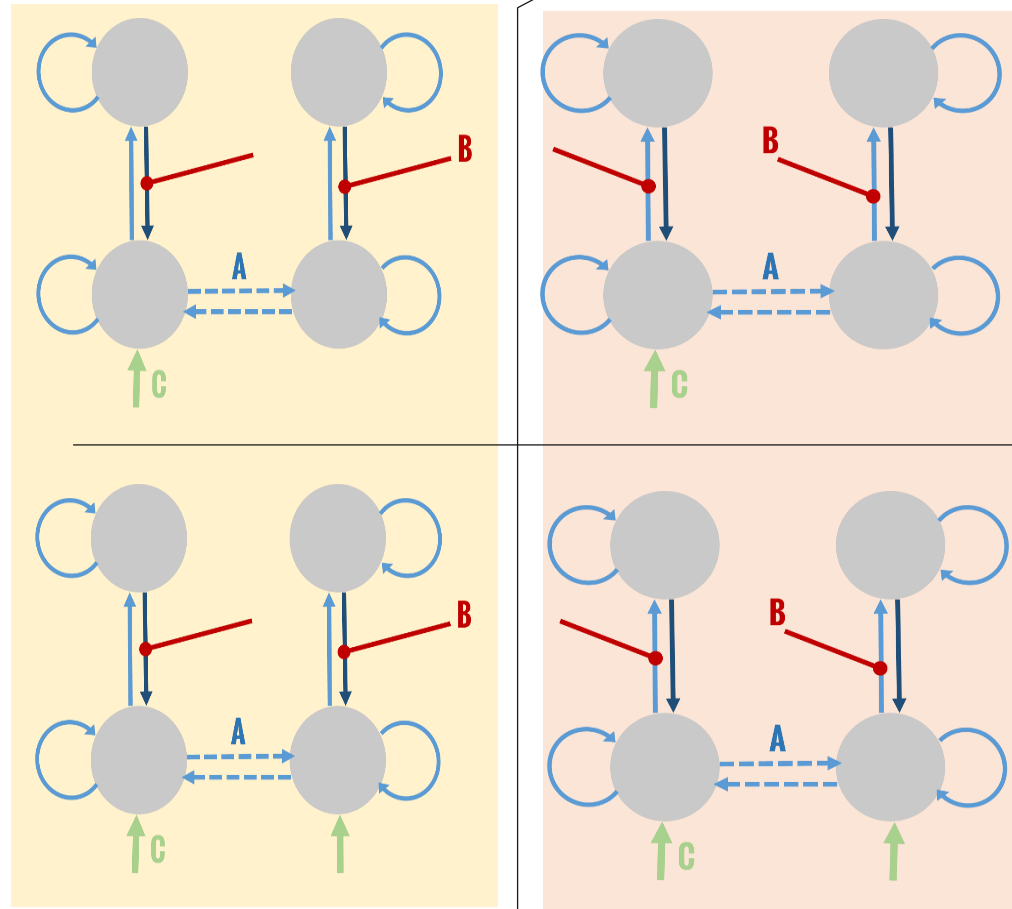


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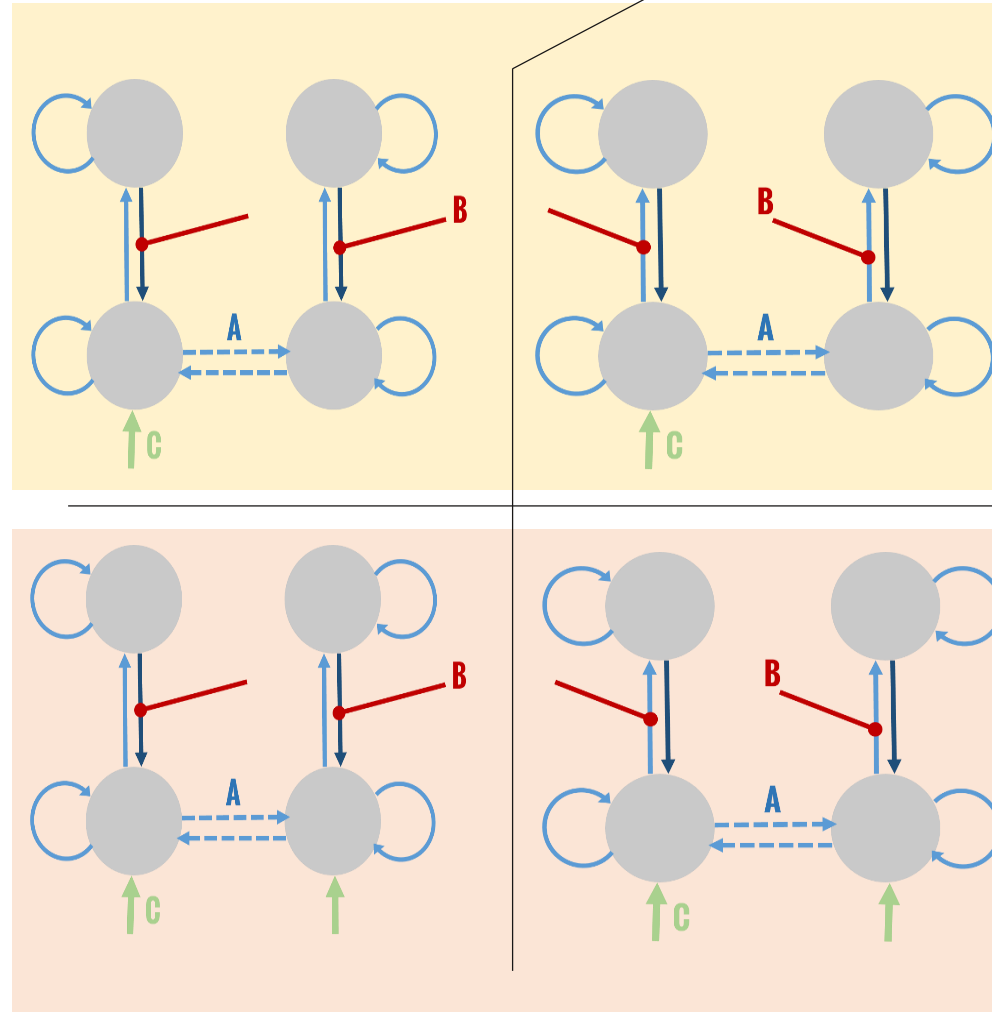
Is there a condition specific forward vs. backward modulation?



Hypotheses

Hypotheses should be based on classical finding.

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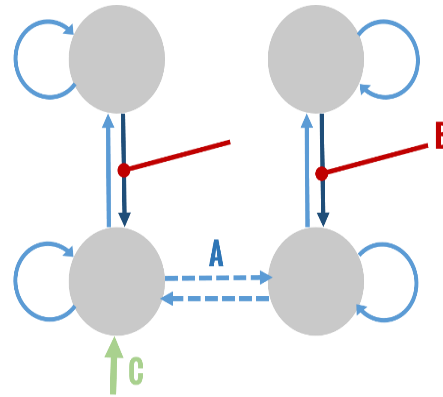
Is the effect of exogenous input bilateral?

Hypotheses

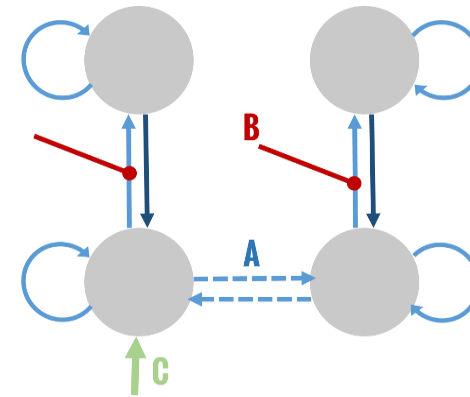
Computation of
parameter estimates.

Model Comparisons

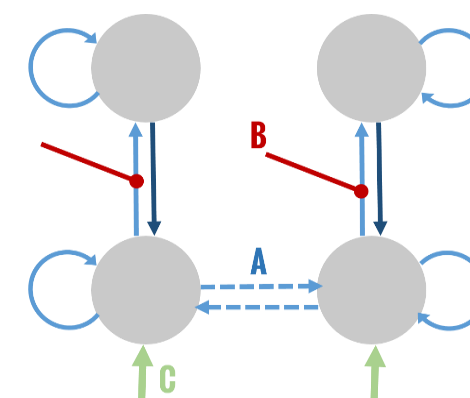
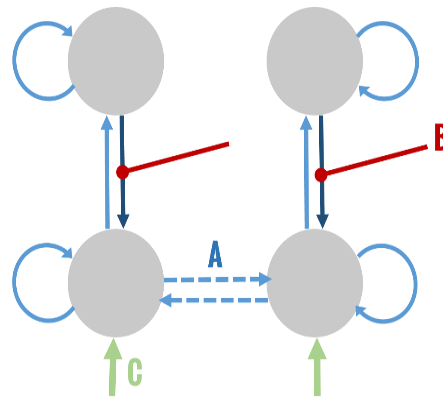
*Which one of competing
Hypotheses describes the
data best.*



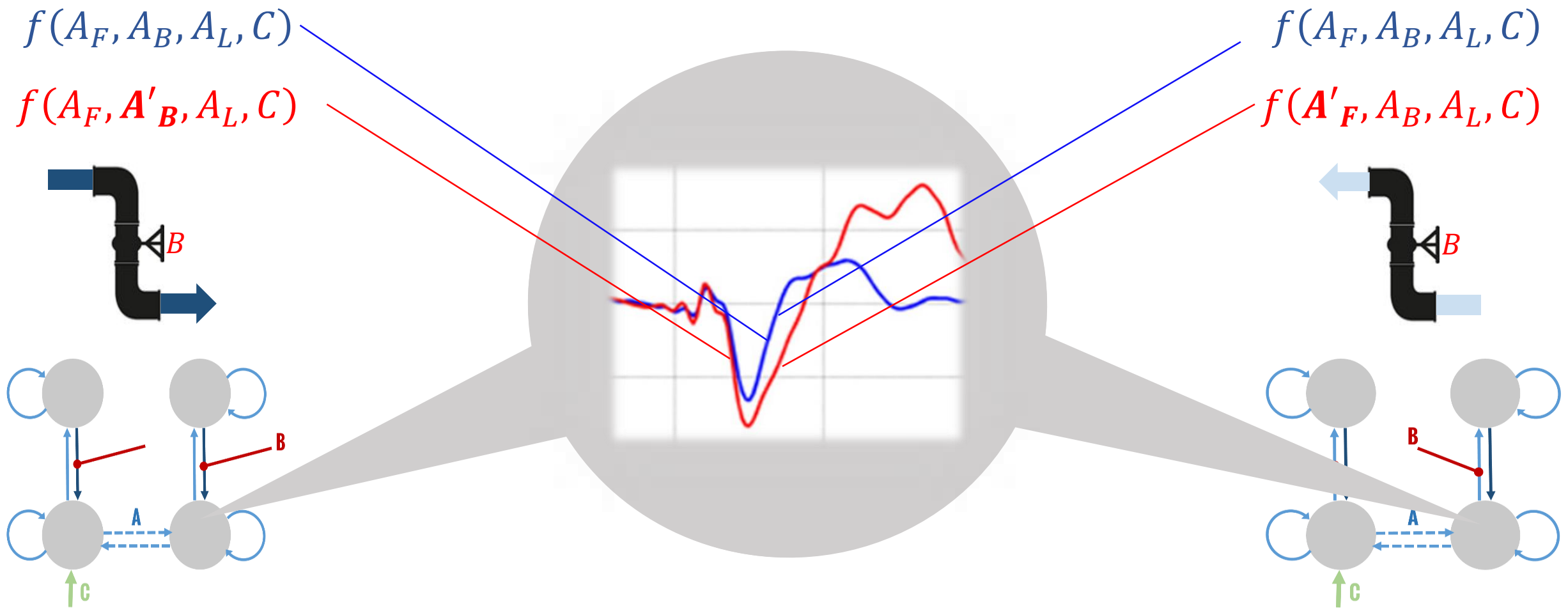
Is there a condition specific
forward vs. backward
modulation?



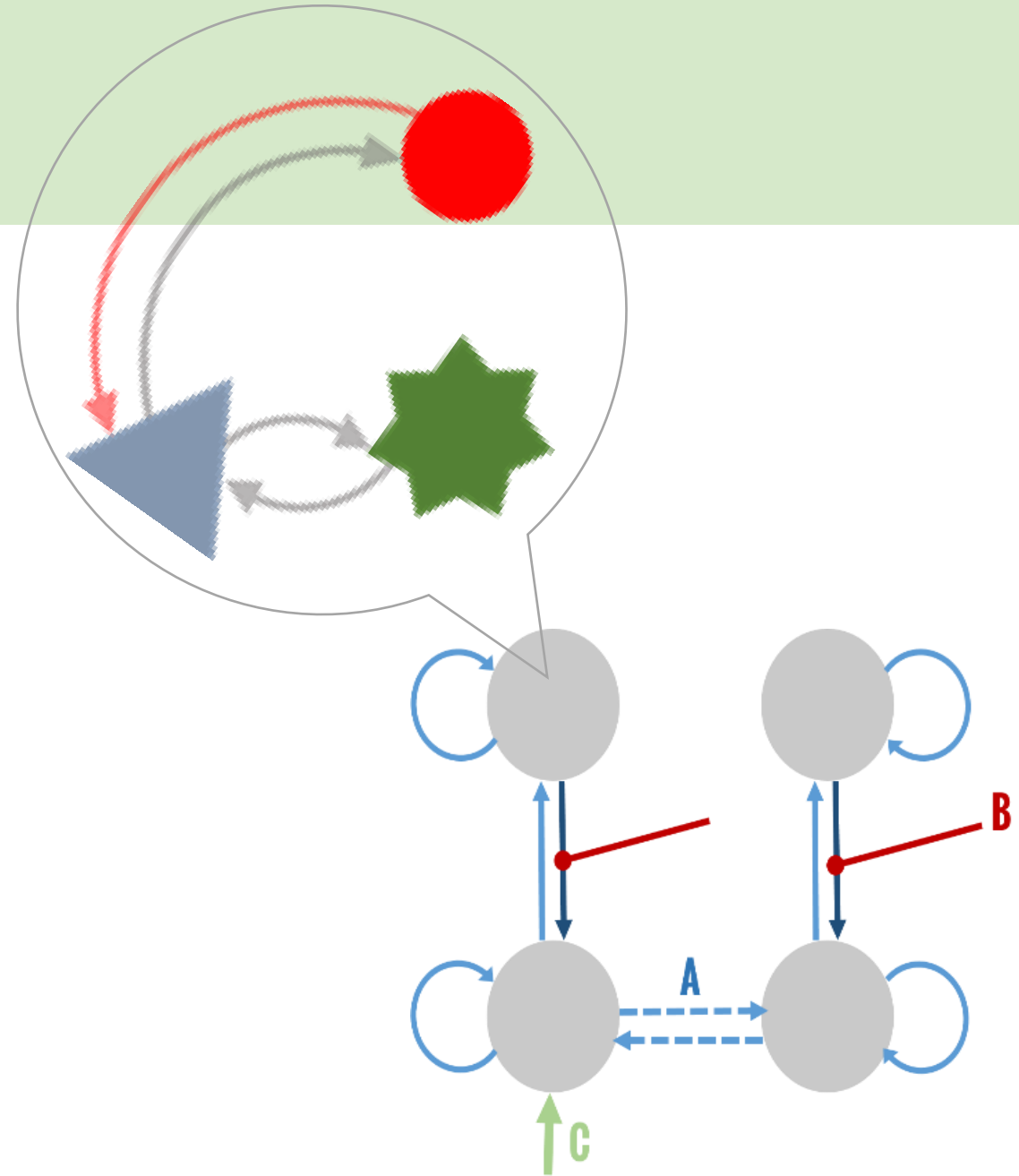
Is the effect of exogenous
input bilateral?



What it means to have a condition specific effect



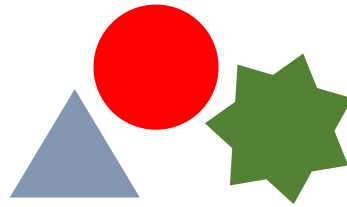
Within Source Connectivity



Within Source Connectivity

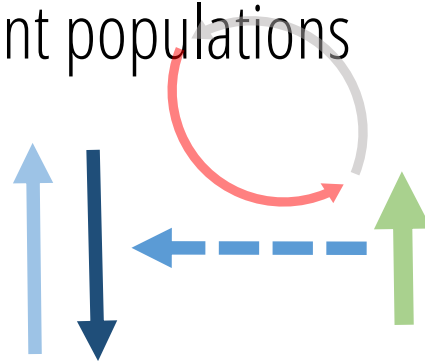
Three types of Cell Populations:

Pyramidal, Inhibitory, Stellate



Inhibitory / Excitatory effects on different populations

Dependence on Extrinsic Connectivity



SPM Variable

X

G

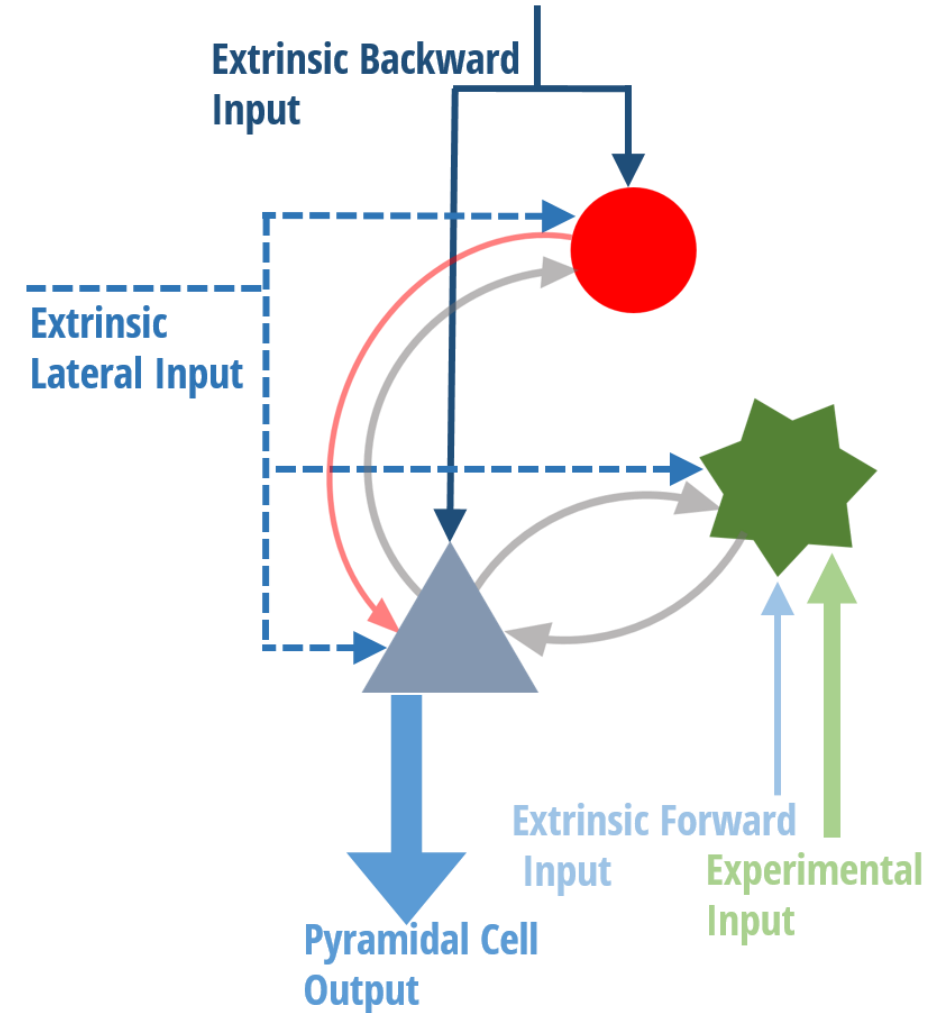
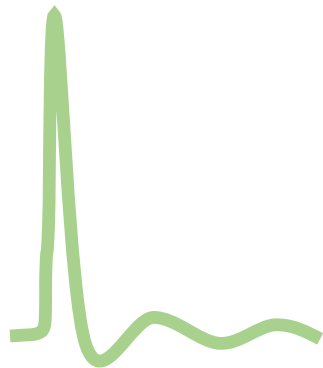
A, C

ERP Model

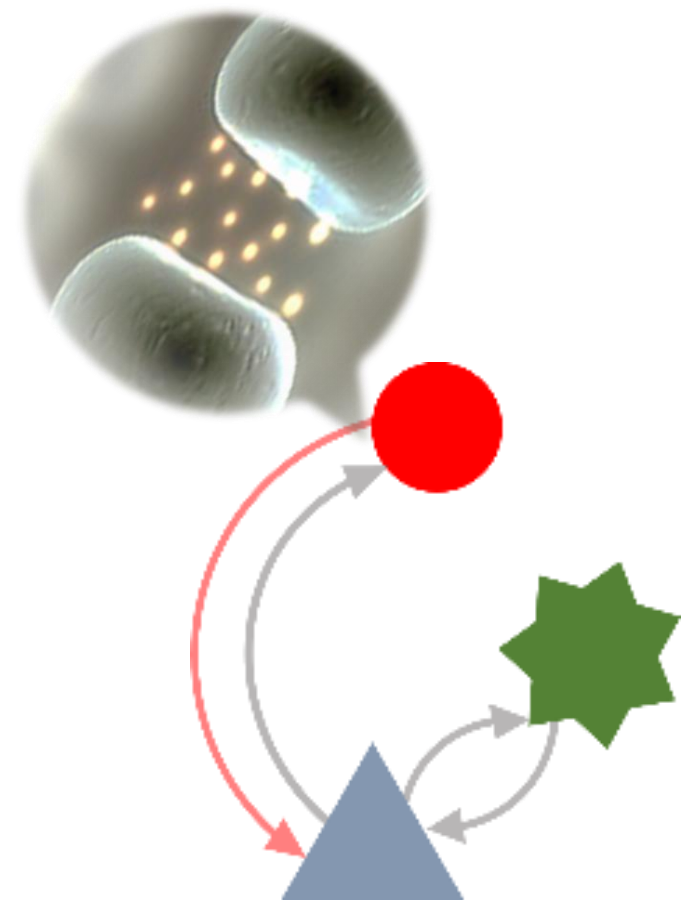
Name of a Between Source Connection refers to the cell population that is being targeted.

Output from the Pyramidal Cell

Experimental Input



Dynamics



Convolution Based Models

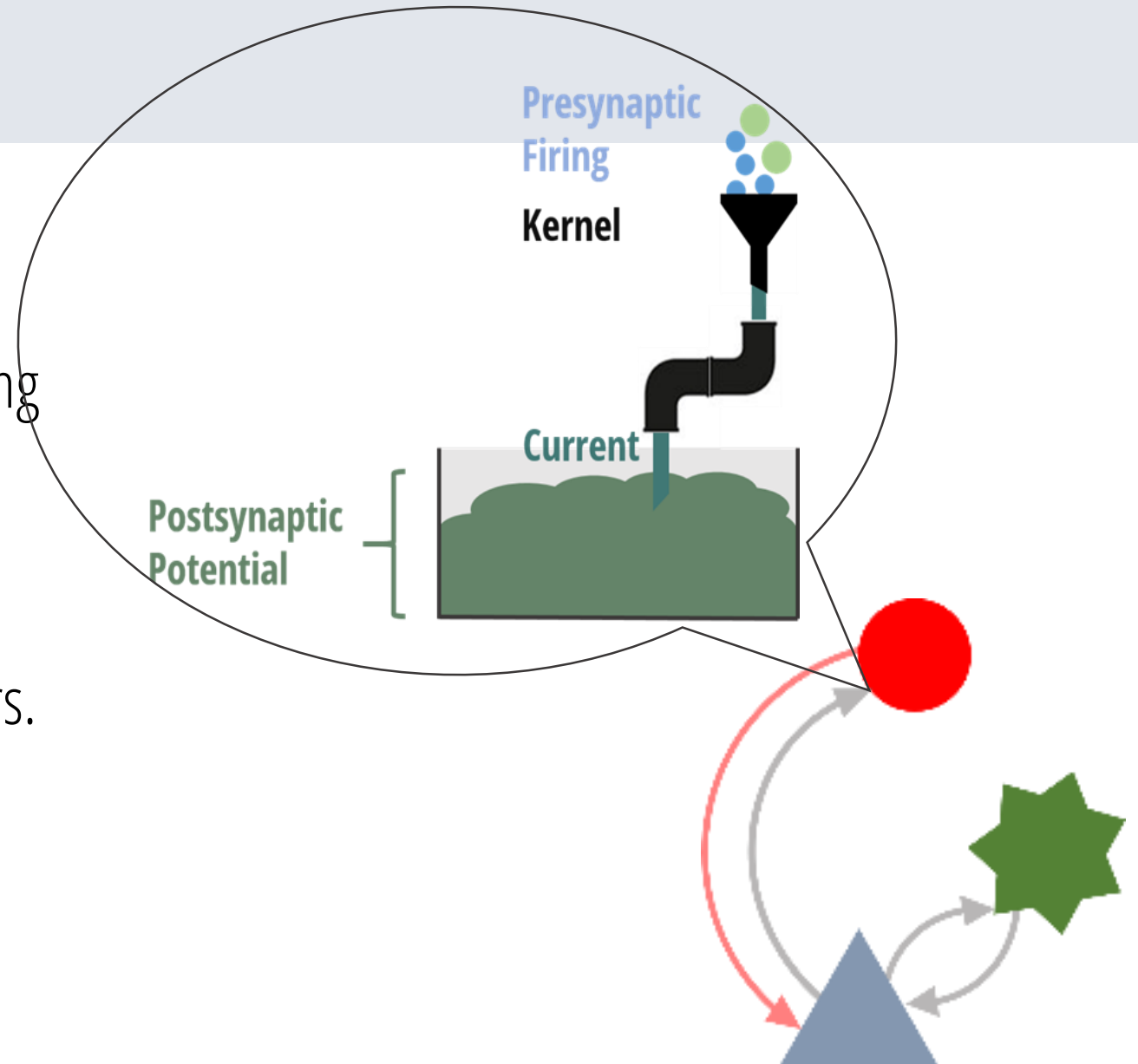
Jansen and Rit (1995)

The Kernel transforms the presynaptic firing rate into a postsynaptic potential.

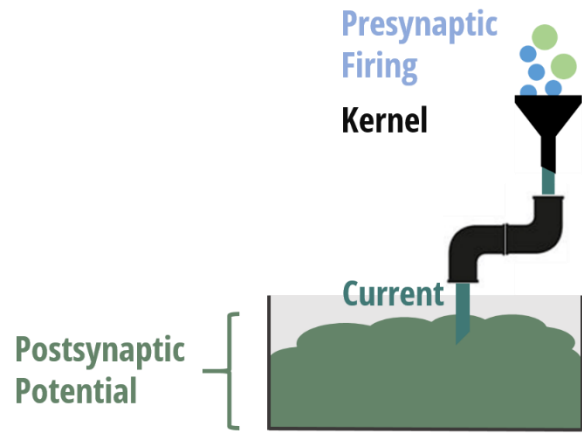
Transformation is a convolution.

Kernel is parameterized by two parameters.

Voltage over time shows similarities with Harmonic Oscillator.

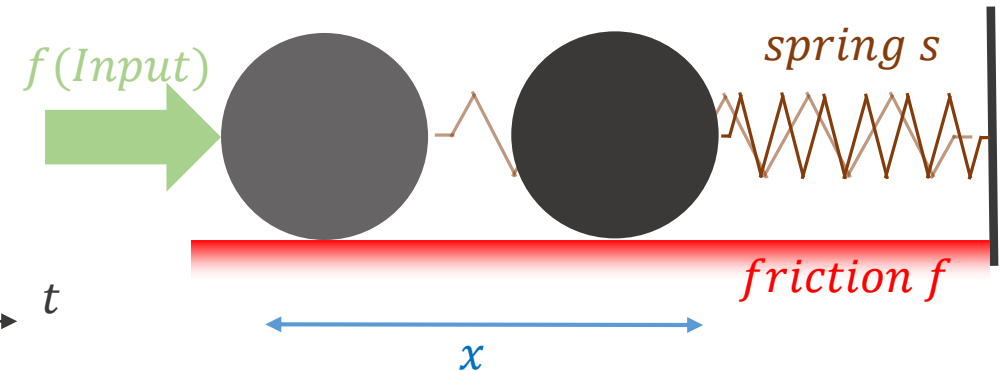
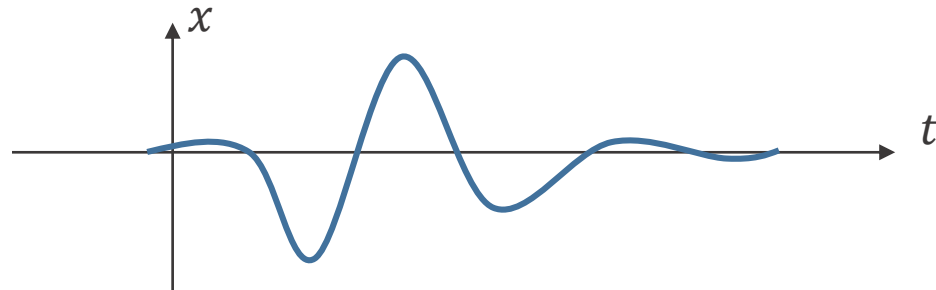


Convolution Based Models



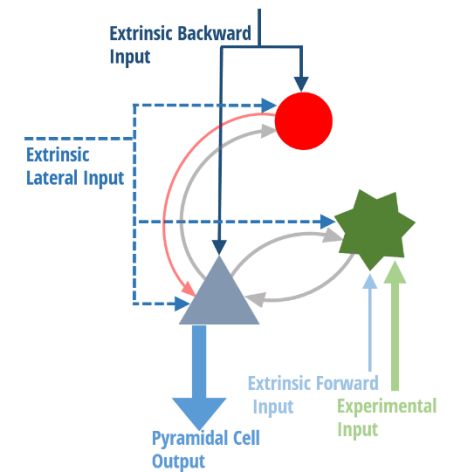
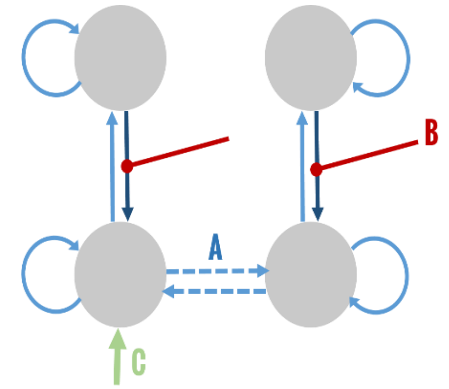
$$\ddot{v} = f(\text{Input}) - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$

$$\ddot{x} = f(\text{Input}) - f\dot{x} - sx$$



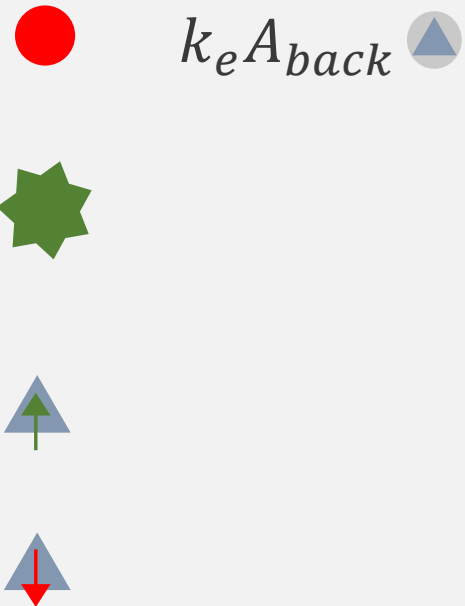
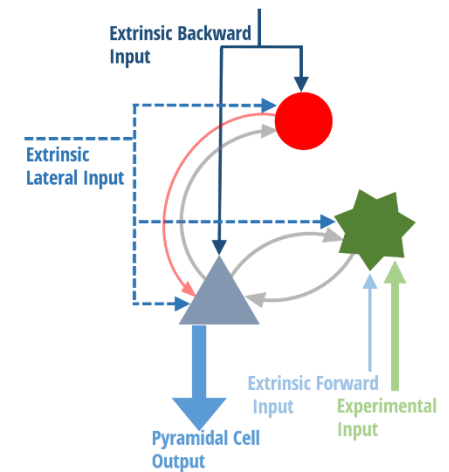
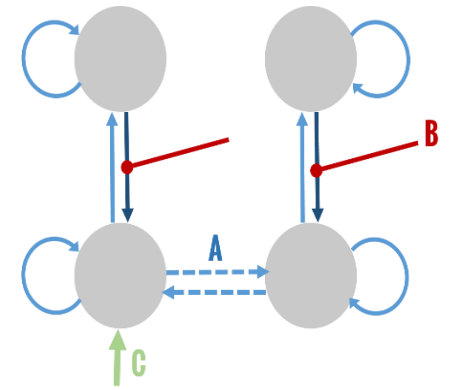
Dynamics

$$\ddot{v} = f(\text{Input}) - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$



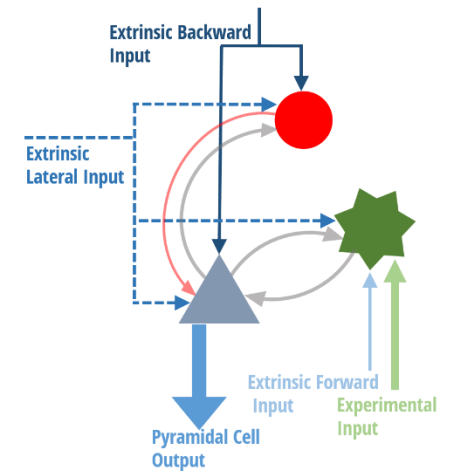
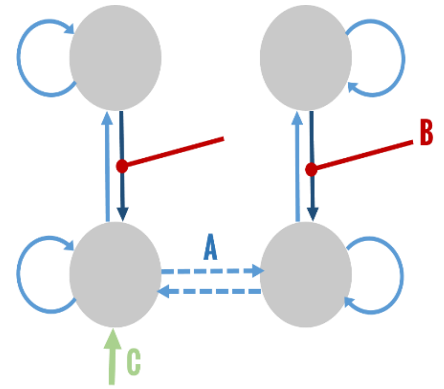
Dynamics




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Dynamics

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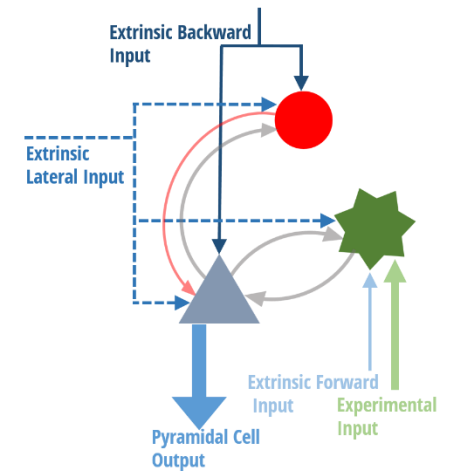
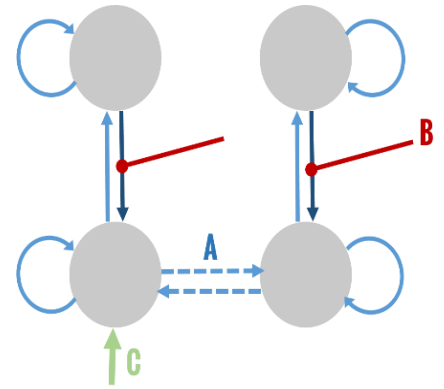



 $k_e A_{back}$

 $+ k_e A_{lateral}$


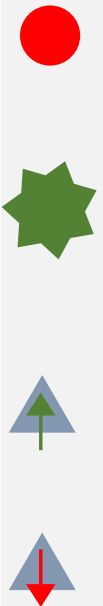


Dynamics

$$\ddot{v} = f(\text{Input}) - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$



● $k_e A_{back}$ ▲ + $k_e A_{lateral}$ ▲ + $k_e G$ ● ▲

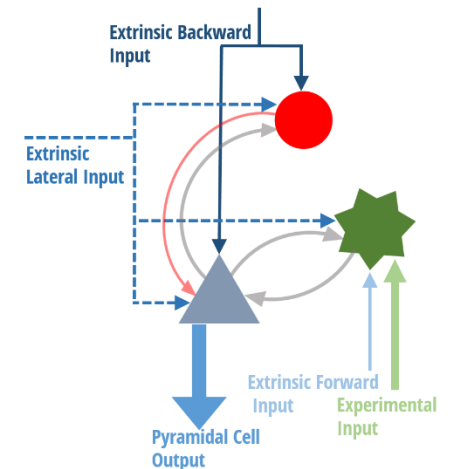
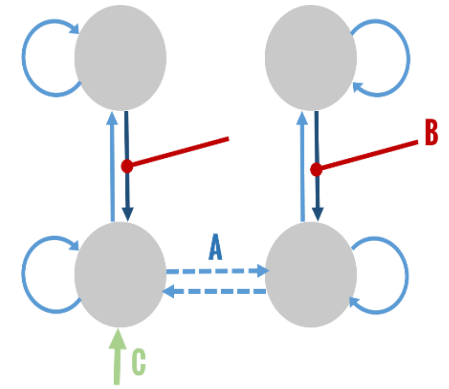


Dynamics

$$\ddot{v} = f(\text{Input}) - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$

● $k_e A_{back} \triangle + k_e A_{lateral} \triangle + k_e G_{\bullet} \triangle$

★ $k_e A_{Forward} \triangle + k_e A_{lateral} \triangle + k_e G_{\star} \triangle + C \text{ (waveform)}$



Dynamics

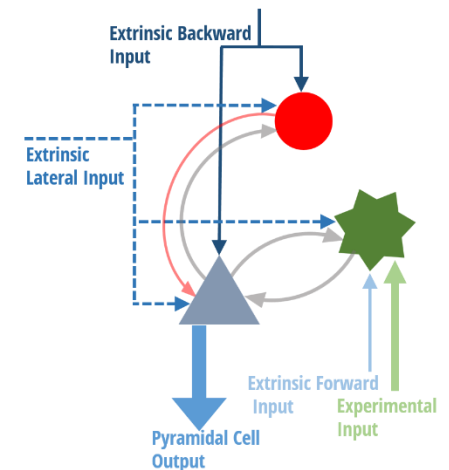
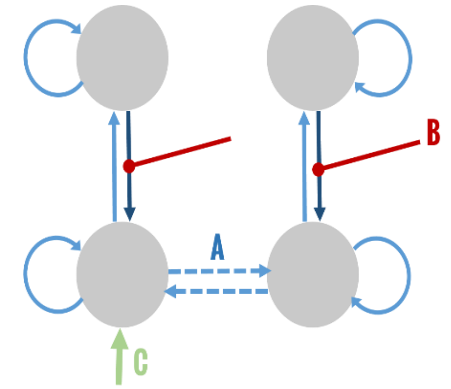
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★ $k_e A_{Forward} \triangle + k_e A_{lateral} \triangle + k_e G_{\star} \triangle + C \text{ [waveform]}$

↑ $k_e A_{back} \triangle + k_e A_{lateral} \triangle + k_e G_{\triangle} \star$

↓



Dynamics

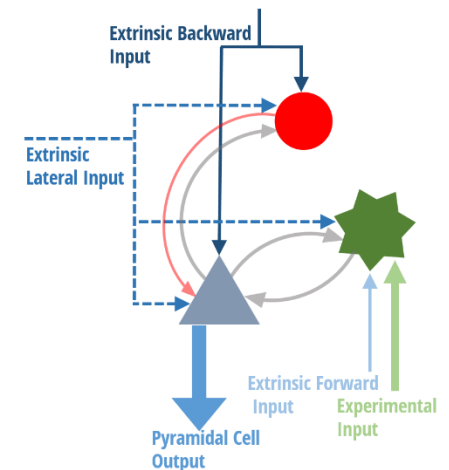
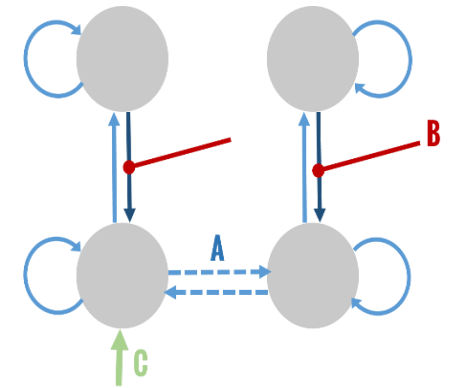
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★ $k_e A_{Forward} \triangle + k_e A_{lateral} \triangle + k_e G_{\star} \triangle + C$

▲ $k_e A_{back} \triangle + k_e A_{lateral} \triangle + k_e G_{\star} \star$

▲ $k_i G_{\bullet} \bullet$



Dynamics

$$\ddot{v} = f(\text{Input}) - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$



$$\ddot{v} = k_e((A_{back} + A_{lateral}) \text{triangle} + G_{\text{red dot}} \text{triangle}) - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$



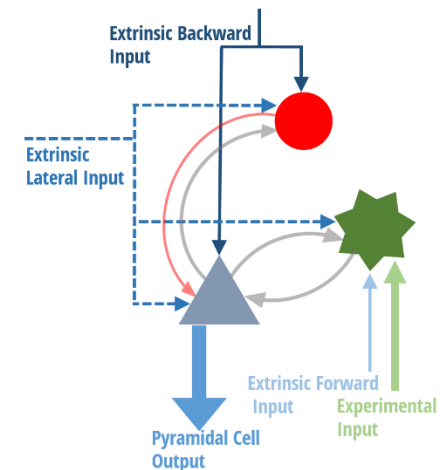
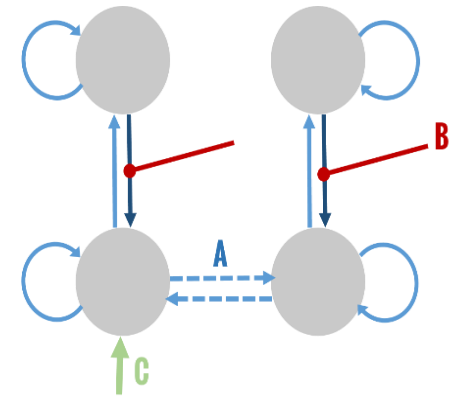
$$\ddot{v} = k_e((A_{Forward} + A_{lateral}) \text{triangle} + G_{\text{green star}} \text{triangle}) + C \text{ pulse} - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$



$$\ddot{v} = k_e((A_{back} + A_{lateral}) \text{triangle} + G_{\text{blue triangle with green star}} \text{star}) - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$



$$\ddot{v} = k_i G_{\text{blue triangle with red dot}} \text{red dot} - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$



Dynamics

$$\ddot{v} = f(\text{Input}) - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$



$$\ddot{v} = k_e((A_{back} + A_{lateral}) \text{ (triangle icon)} + G_{\text{ (red circle icon) }} \text{ (triangle icon)}) - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$

```
f(:,8) = (He.*((A{2} + A{3}))*S(:,9) + G(:,3).*S(:,9)) - 2*x(:,8) - x(:,7)./Te)./Te;
```



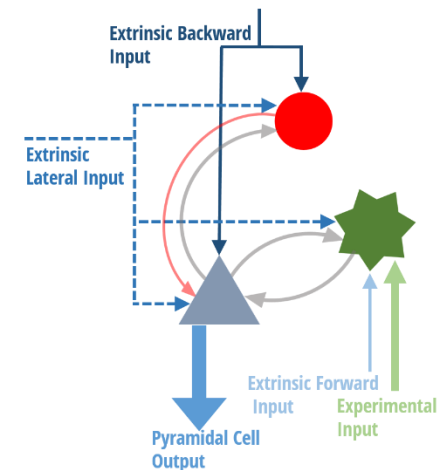
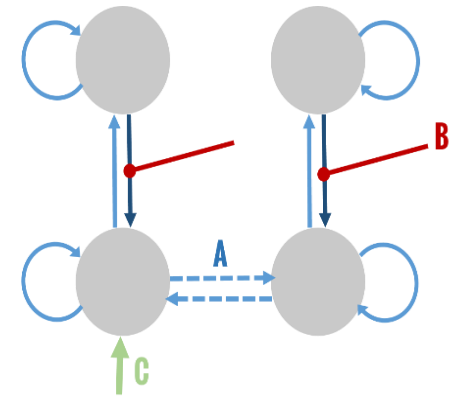
$$\ddot{v} = k_e((A_{forward} + A_{lateral}) \text{ (triangle icon)} + G_{\text{ (green star icon) }} \text{ (triangle icon)}) + C_{\text{ (green waveform icon) }} - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$



$$\ddot{v} = k_e((A_{back} + A_{lateral}) \text{ (triangle icon)} + G_{\text{ (blue triangle icon) }} \text{ (green star icon)}) - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$



$$\ddot{v} = k_i G_{\text{ (blue triangle icon) }} \text{ (red circle icon)} - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$



Dynamics

$$\ddot{v} = f(\text{Input}) - \frac{2}{\tau} \dot{v} - \frac{1}{\tau^2} v$$

% Supragranular layer (inhibitory interneurons): Voltage & depolarizing current

%-----

f(:,7) = x(:,8);

f(:,8) = (He.*(A{2} + A{3})*S(:,9) + G(:,3).*S(:,9)) - 2*x(:,8) - x(:,7)./Te)./Te;

% Granular layer (spiny stellate cells): Voltage & depolarizing current

%-----

f(:,1) = x(:,4);

f(:,4) = (He.*(A{1} + A{3})*S(:,9) + G(:,1).*S(:,9) + U) - 2*x(:,4) - x(:,1)./Te)./Te;

% Infra-granular layer (pyramidal cells): depolarizing current

%-----

f(:,2) = x(:,5);

f(:,5) = (He.*(A{2} + A{3})*S(:,9) + G(:,2).*S(:,1)) - 2*x(:,5) - x(:,2)./Te)./Te;

% Infra-granular layer (pyramidal cells): hyperpolarizing current

%-----

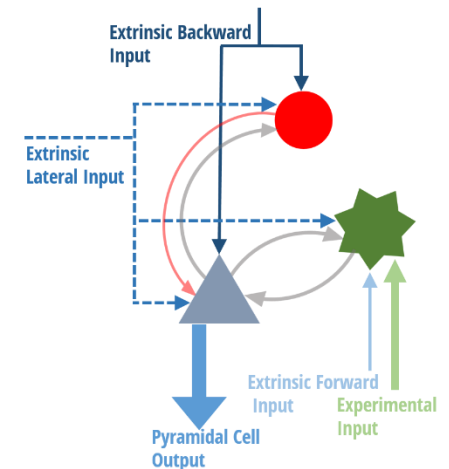
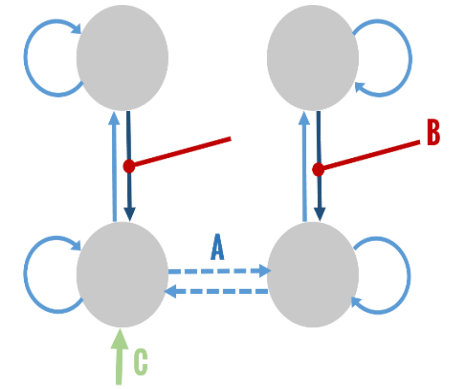
f(:,3) = x(:,6);

f(:,6) = (Hi.*G(:,4).*S(:,7) - 2*x(:,6) - x(:,3)./Ti)./Ti;

% Infra-granular layer (pyramidal cells): Voltage

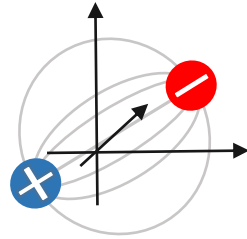
%-----

f(:,9) = x(:,5) - x(:,6);



Forward Model

Equivalent Current Dipoles



Leadfield matrix



Measured Data

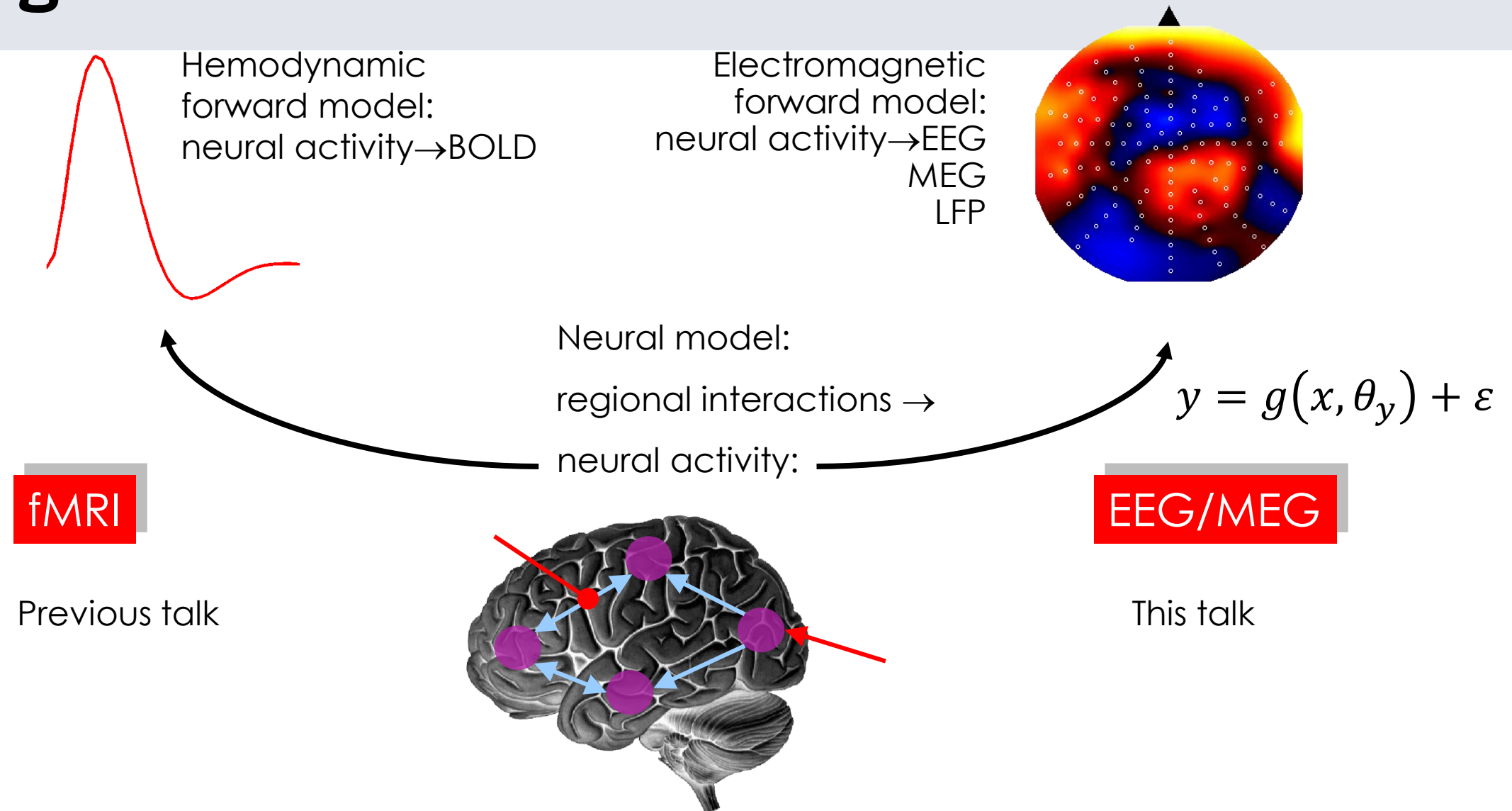
SPM Variable

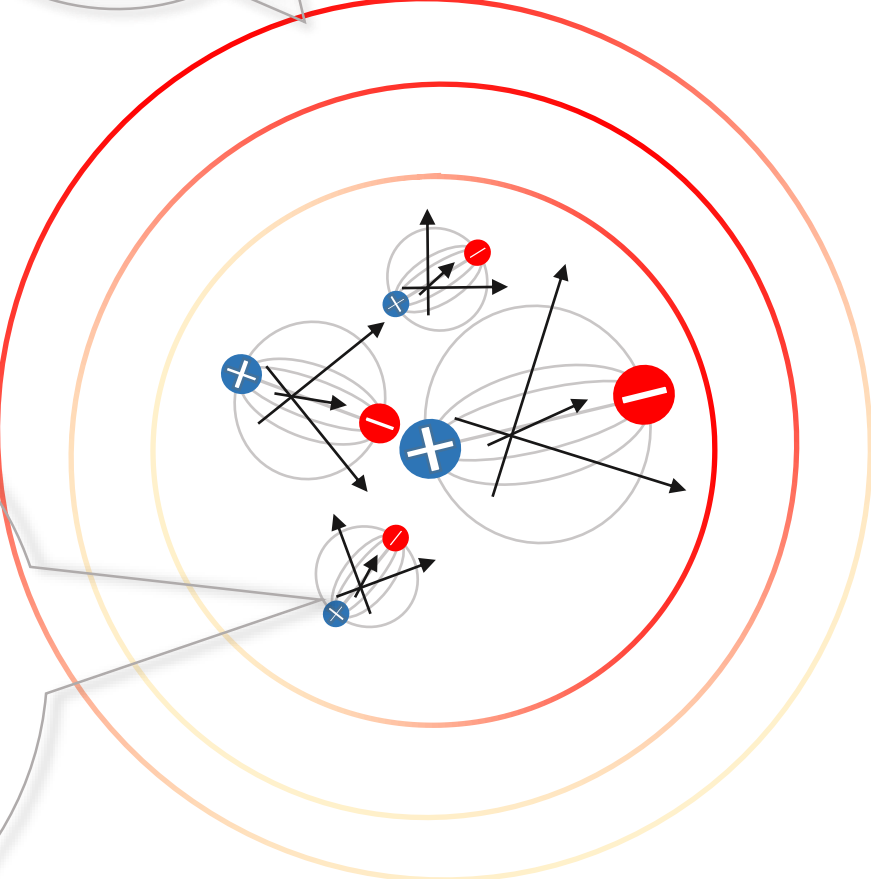
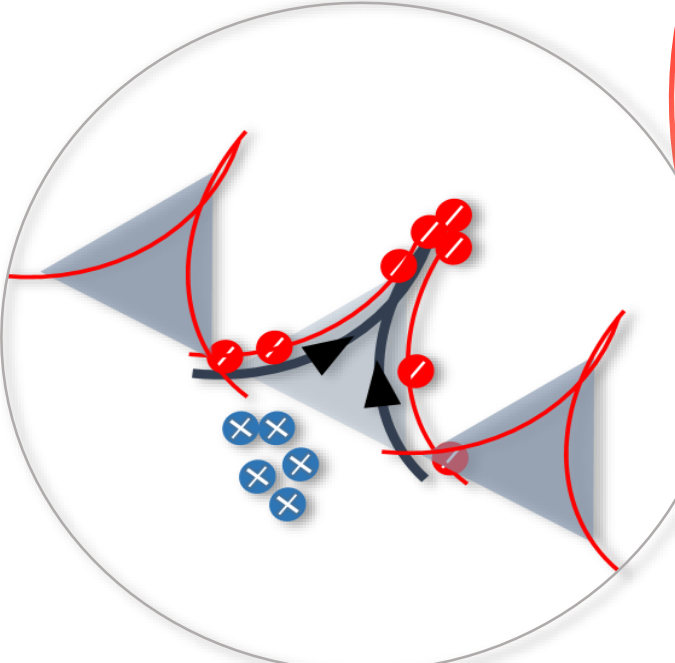
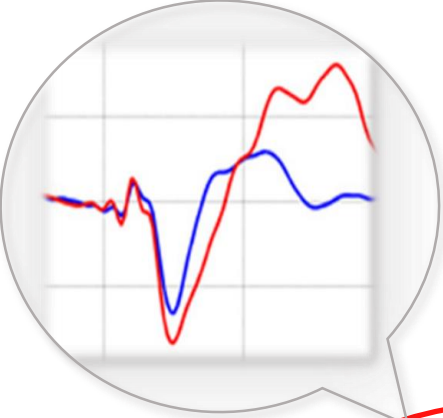
X

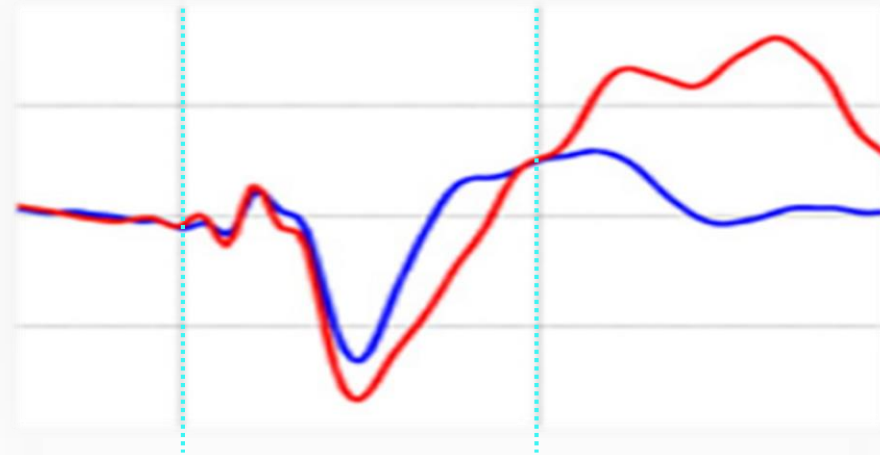
L

Y

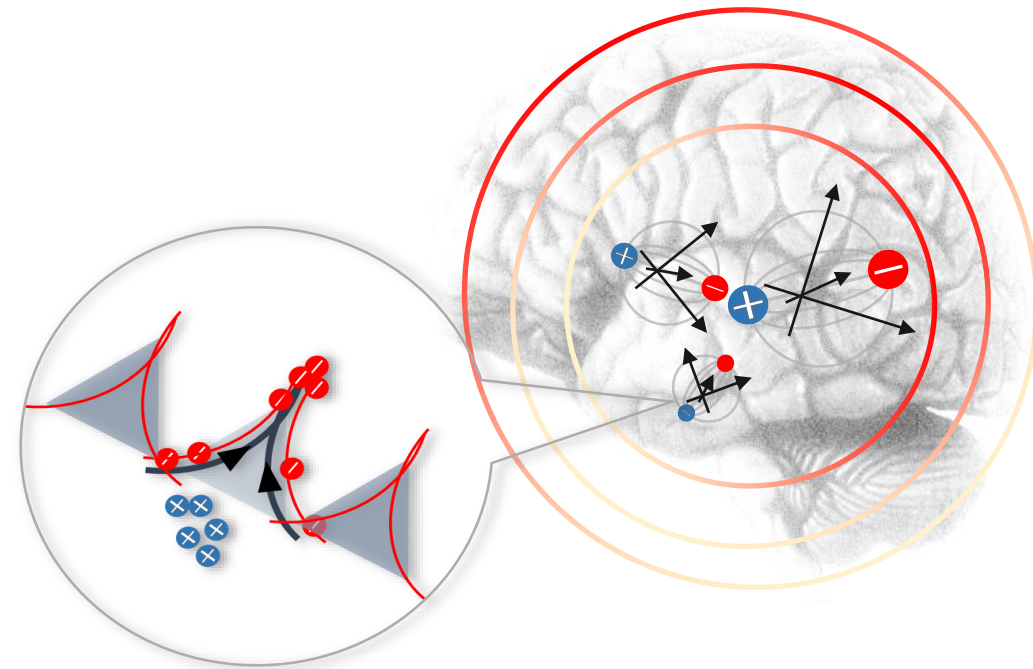
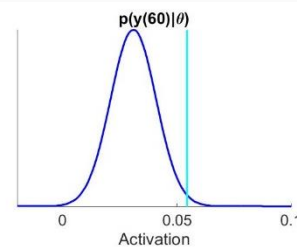
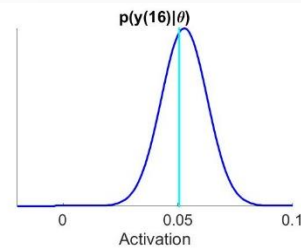
Recap: Dynamic Causal Modeling (DCM)







$$y = Lx + \varepsilon$$

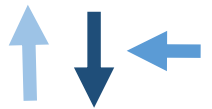


Forward Model

Reminder before SPM



Sources / Regions



Three types of connections



Between conditions effects



Input



Three types of cell populations



Inhibitory / Excitatory effects on different populations

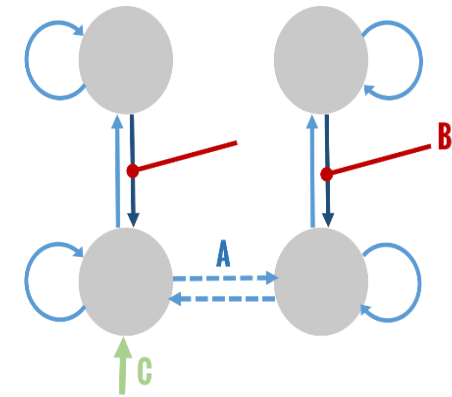
SPM Variable

X

A

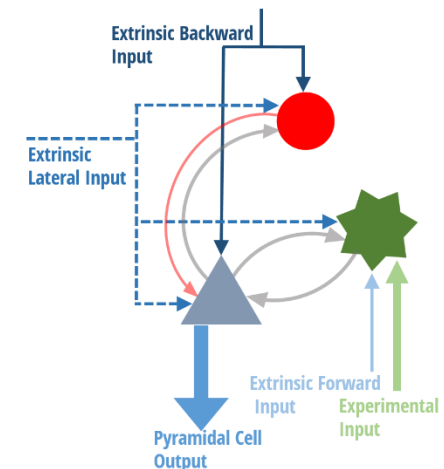
B

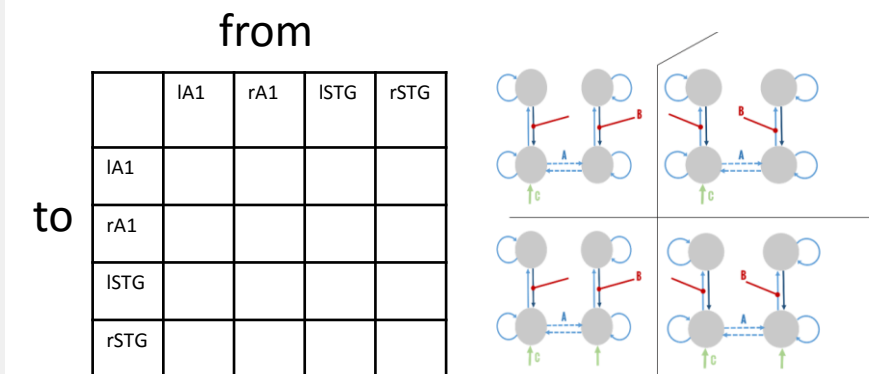
C



X

G





**Some weirdly
unsorted appendix**

Thank you

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University of
Zurich^{UZH}

ETH zürich



Translational Neuromodeling Unit