

$$N=2$$

$$I = \int_{-1}^1 f(x) dx = \sum_{i=1}^n \frac{2}{n} f(t_i)$$

$$\int_a^b f(x) dx = \frac{b-a}{n} \sum_{i=1}^n f\left(\frac{b+a}{2} + \frac{b-a}{2} t_i\right)$$

$$\begin{cases} t_1 + t_2 + t_3 = 0 \\ t_1^2 + t_2^2 + t_3^2 = 1 \\ t_1^3 + t_2^3 + t_3^3 = 0 \end{cases} \Rightarrow t_1 = -0.707207, t_2 = 0, t_3 = 0.70707$$

$$\int_0^{\pi/4} f(x) \sin(2x) dx = \frac{\pi}{12} \sum_{i=1}^3 \sin 2t_i f(t_i)$$

$$t'_1 = \frac{\pi}{8} - \frac{\pi}{8} \cdot 0.707207 \approx 0.114379,$$

$$t'_2 = \frac{\pi}{8} \approx 0.392699$$

$$t'_3 = \frac{\pi}{8} + \frac{\pi}{8} \cdot 0.707207 \approx 0.670418$$

$$I = \frac{\pi}{8} \left(\frac{2}{3} \sin 2t'_1 f(t'_1) + \frac{2}{3} \sin 2t'_2 f(t'_2) + \frac{2}{3} \sin 2t'_3 f(t'_3) \right) =$$

$$= \frac{\pi}{8} (0.151358 \cdot f(0.114379) + 0.471404 \cdot f(0.392699) + 0.643116 f(0.670418))$$