

**COMS30127/COMSM2127**  
*Computational Neuroscience*

**Lecture 19: Ion channels (j)**

**Dr. Cian O'Donnell**

**[cian.odonnell@bristol.ac.uk](mailto:cian.odonnell@bristol.ac.uk)**

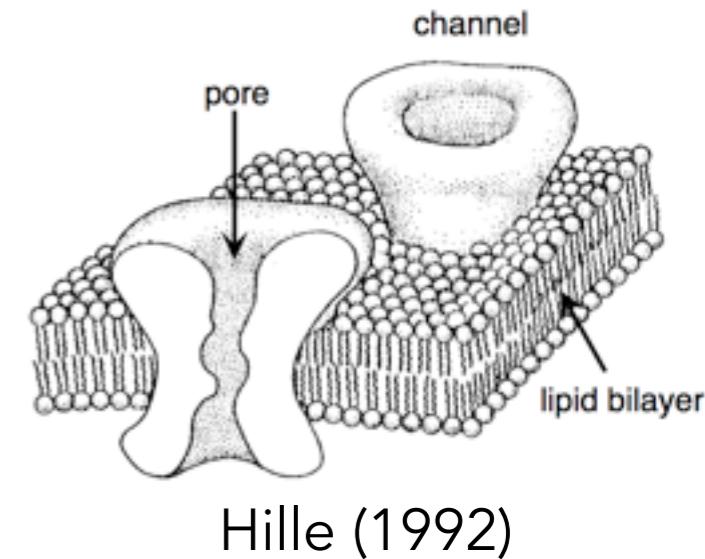


# What we will cover today

- What are ion channels and what do they do?
- The different types of ion channels.
- Modelling ion channels.
- How ion channels make the neuron's input-output function nonlinear.
- Ion channels as an intrinsic source of noise in the brain.

# What are ion channels?

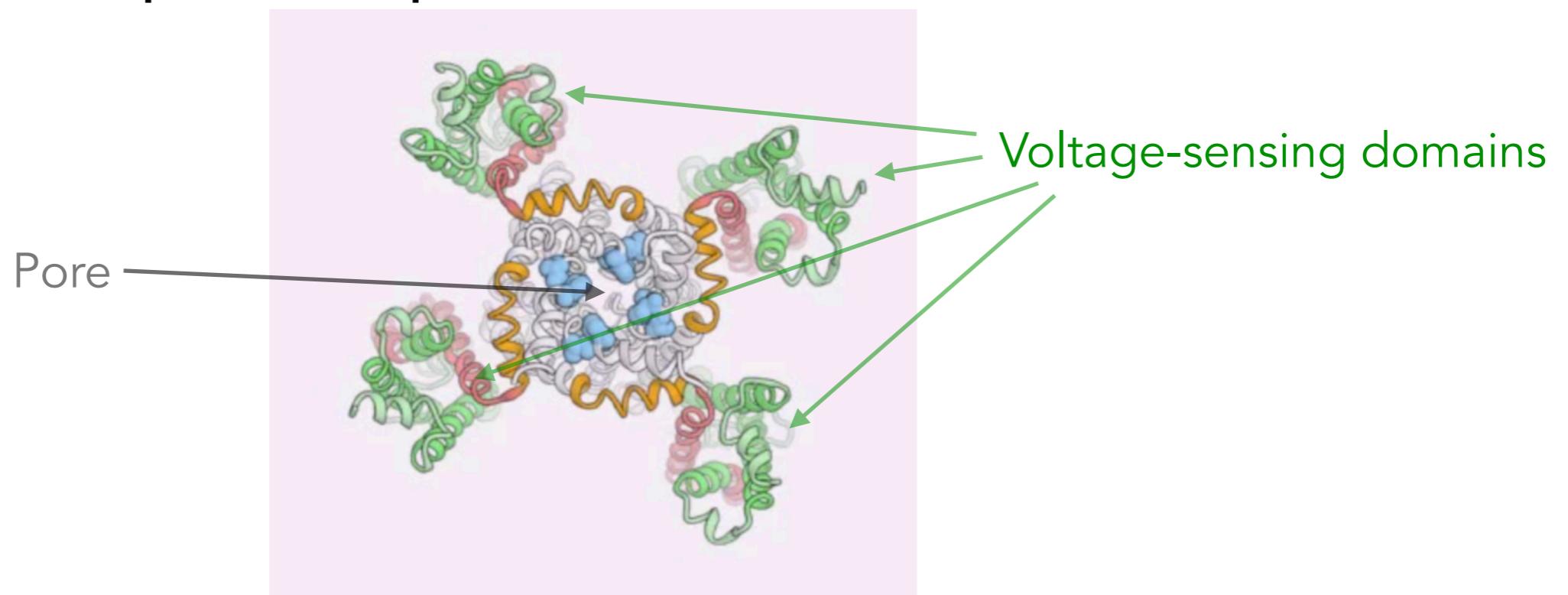
- Ion channels are ion-permeable pores in the lipid membrane of cells.
- A single neuron typically has hundreds of thousands to millions of ion channels embedded in its membrane.
- They open and close in response to stimuli (**voltage**, neurotransmitters, intracellular chemicals, pH, mechanical forces, temperature...), passing ions like  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Ca}^{2+}$ ,  $\text{Cl}^-$ .
- Their currents mediate electrical signalling in the nervous system.
- The conductance of single ion channels vary between ~0.1 and 100 picoSiemens. For most channels it's around 10 pS.
- The flux through a single open channel can be millions of ions per second.



# What are ion channels?

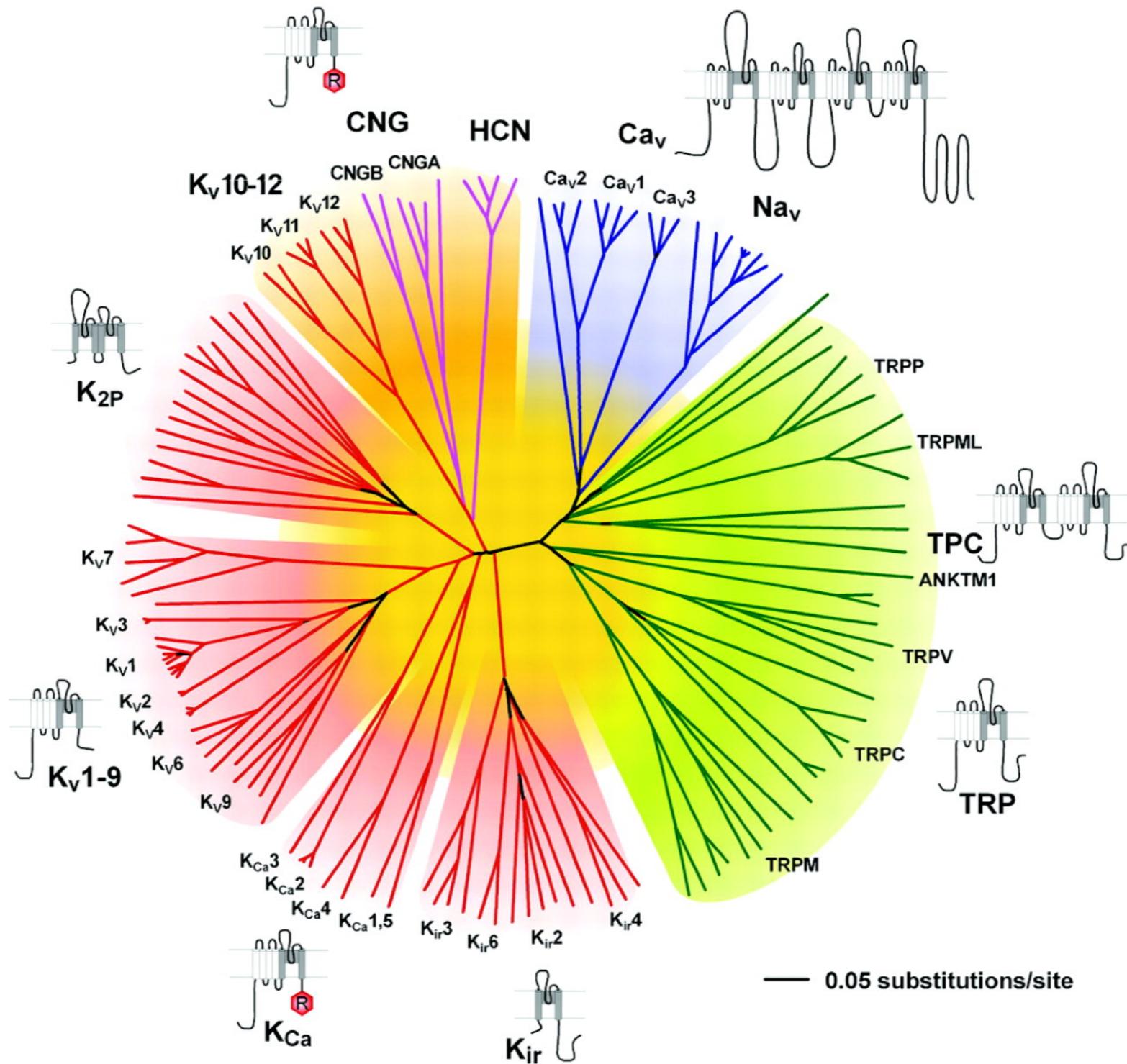
- Voltage-gated ion channels typically have a pore domain made up of four identical, or similar, channel subunits arranged in a ring. The ion pore is made along the axis where they meet.
- The channel also has secondary voltage-sensing domains, that deform in response to changes in the transmembrane voltage. These drag the pore-domain components to switch the channel open or closed.

**Bottom-up view of a potassium channel (from inside the cell)**



# Ion channel types

# The ion channel zoo



# Ion channel types

- Sodium ( $\text{Na}^+$ ) channels mediate inward currents that depolarise the voltage.
  - Fast gating and activated by depolarisation (positive feedback).
  - Responsible for upswing of the action potential, and boosting subthreshold inputs in dendrites.
  - Targets for some anaesthetics (e.g. lidocaine, pufferfish venom)
- Potassium ( $\text{K}^+$ ) channels mediate outward currents that hyperpolarise the voltage.
  - Can be fast or slow gating, activated by depolarisation (negative feedback).
  - Voltage-independent  $\text{K}^+$  channels mediate the 'leak' current.
  - Very genetically diverse (around 50 types in mammals).
- Calcium ( $\text{Ca}^{2+}$ ) channels, like sodium, mediate inward currents that depolarise the voltage.
  - Fast gating, but not as strongly expressed as sodium so have weaker effect on the voltage.
  - Responsible for some forms of dendritic spikes.
  - Generate intracellular calcium signals that the cell uses to monitor its electrical activity.
- Other channels include
  - Chloride ( $\text{Cl}^-$ ) channels: involved in setting resting voltage.
  - HCN channels: mixed sodium/potassium permeability, active at resting voltage, inactivated by depolarisation (negative feedback), heavily expressed in dendrites).

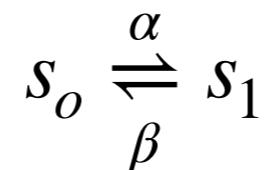
# Modelling ion channels

# Modelling ion channels

- In most neuroscience applications we don't care about all the molecular details of the ion channel, we just want a simple model that captures their dynamics.
- Usually this involves state-based modelling.
- We assume that each channel can be in one of a small number of discrete states. The channel can transition between states, with transition rates that depend on the cell's voltage.

# Modelling ion channels

Consider a 2-state ion channel model with transitions between the closed  $s_0$  and open  $s_1$  states, with transition rates  $\alpha$  and  $\beta$ :



If we imagine a large population of such channels, we could think of  $s_1$  as representing the proportion of the population in the open state.  
Then we can write down a differential equation to describe its dynamics:

$$\frac{ds_1(t)}{dt} = \alpha s_0(t) - \beta s_1(t)$$

The steady state value  $s_\infty$  is found by setting  $ds_1/dt = 0$ :  $s_\infty = \frac{\alpha}{\alpha + \beta}$

Then we can rewrite the right hand side of the dynamics equations as

$$\frac{ds_1(t)}{dt} = \frac{s_\infty - s_1(t)}{\tau}$$

Where we have introduced the time constant  $\tau = \frac{1}{\alpha + \beta}$

# Modelling ion channels

- The previous slide showed a very simple 2-state channel example. Most real channels are too complicated to describe so compactly, so their models often have many more states.
- The voltage dependence is built into these channel models by making the transitions rate ( $\alpha$  and  $\beta$ ) functions of voltage.
- You will go through a famous example of the Hodgkin-Huxley squid axon model in the next lecture.

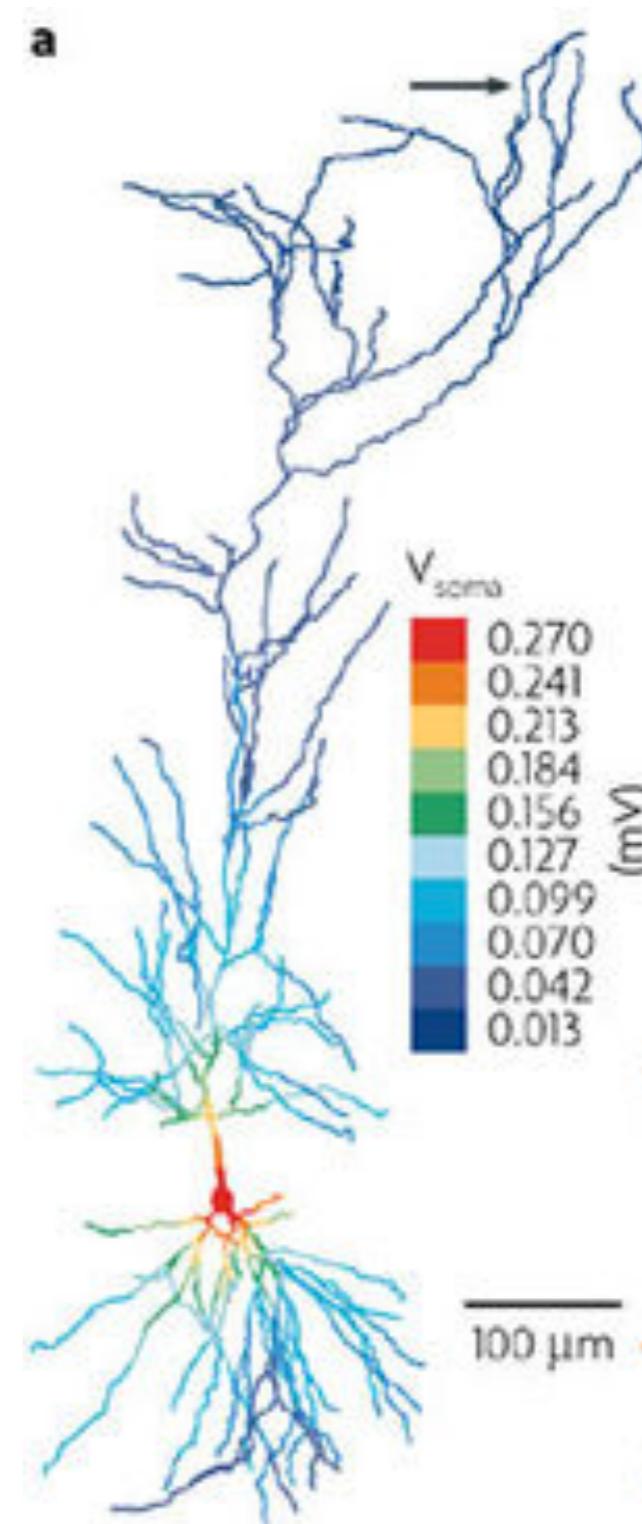
The neuron's input-output function  
a.k.a. synaptic integration

# Non-linear synaptic integration

- Neurons receive multiple temporal patterns of spike trains as input, and produce a single spike train as output.
- “Point” neuron models (like the integrate-and-fire) assume that the soma performs a weighted linear sum of the synaptic currents.
- However, real neurons differ from this idealisation in two key aspects:
  1. Neurons have dendrites, which implies a **spatial layout of synaptic inputs**.
  2. Dendrites have voltage-dependent (active) ion channels which makes **synaptic integration non-linear**.

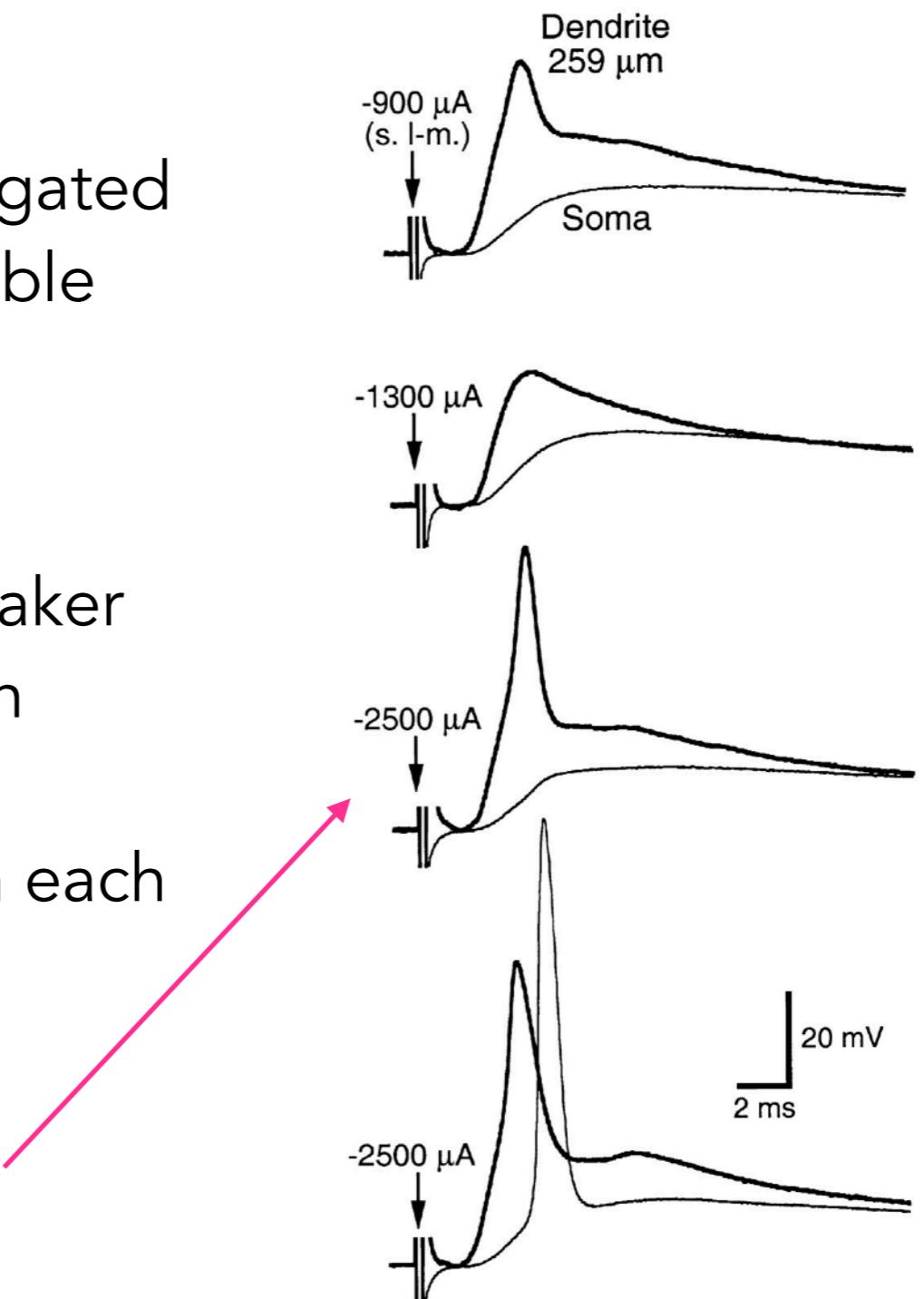
# Synaptic location matters

- The figure on the right is a trace of the dendritic tree of a CA1 pyramidal cell from a rat.
- The colour indicates the amplitude of the voltage response (EPSP) at the soma, when the synapse is placed at the corresponding location on the dendritic tree.
- Without any “boosting”, a synapse would give a smaller somatic response if it was located at a distal dendritic site.
- However it turns out that voltage-dependent ion channels in dendrites can boost synaptic inputs to amplify their effect at the soma.

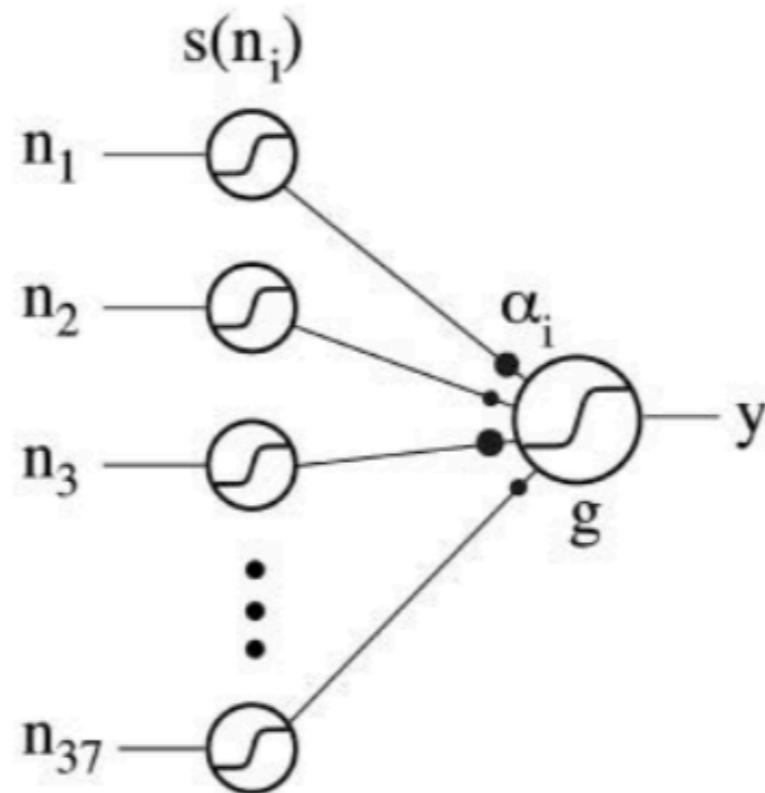
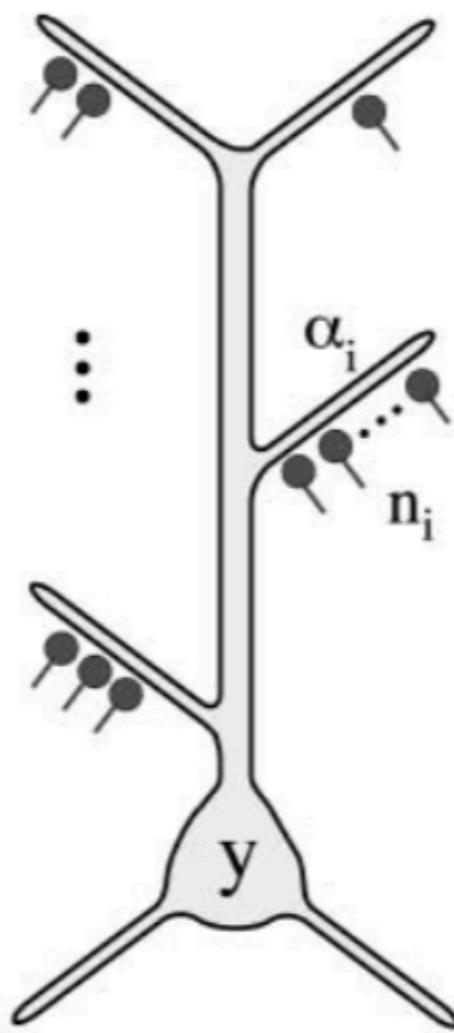


# Dendritic spikes

- Some neurons have enough voltage-gated ion channels in their dendrites to enable purely dendritically-generated action potentials.
- These dendritic spikes tend to be weaker and less all-or-none than axonal action potentials  
(note variable dendritic amplitudes in each plot on right).
- A single dendritic spike is not always sufficient to trigger an axonal spike.



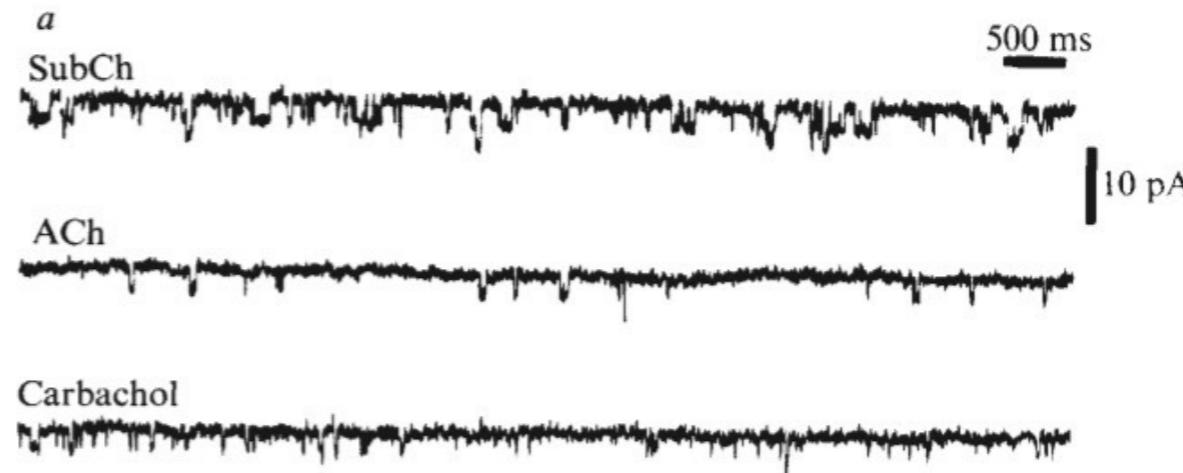
# The single neuron as two-layer neural network



- The existence of dendritic spikes means we can almost think of a single pyramidal neuron as a multi-layer neural network. Each dendritic does a nonlinear operation on its inputs before passing the signal to the soma.
- Voltage-gated ion channels expand the brain's computational power.

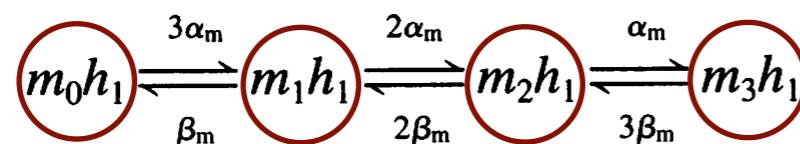
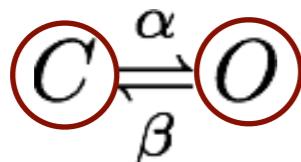
# Stochasticity of ion channels

# Ion channels are discrete and stochastic



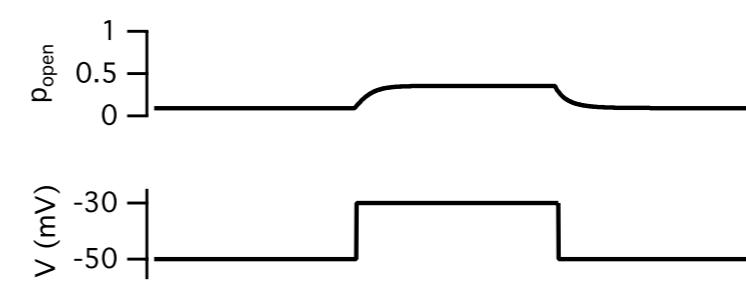
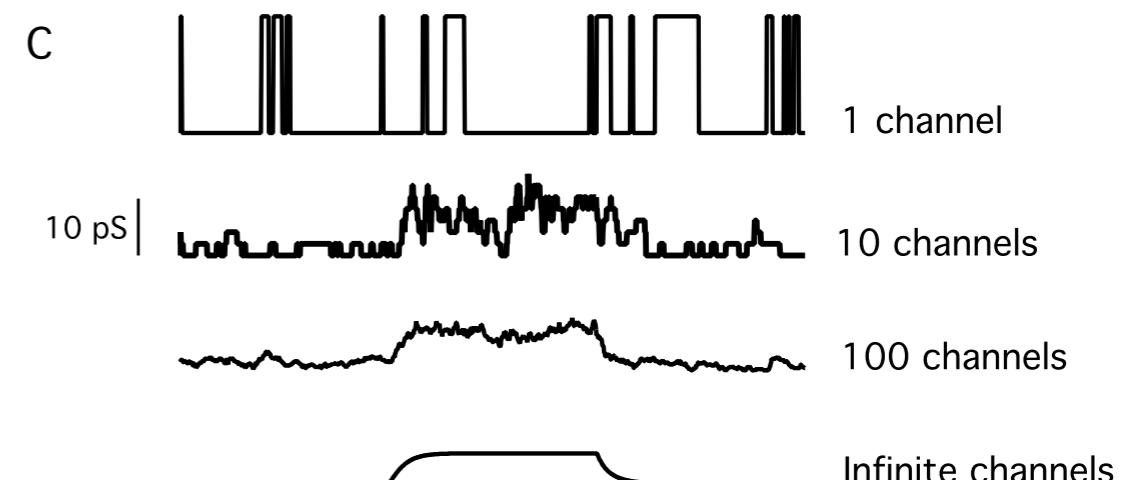
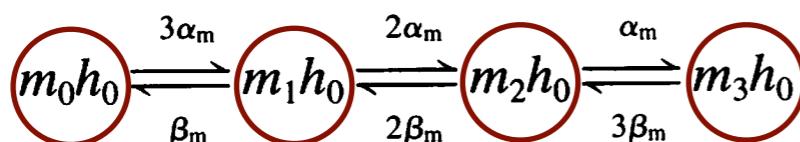
Neher & Sakmann, Nature (1976)

**2-state:**



**8-state:**

$$\alpha_h \uparrow \beta_h \quad \alpha_h \uparrow \beta_h \quad \alpha_h \uparrow \beta_h \quad \alpha_h \uparrow \beta_h$$



O'Donnell & Nolan (2014)

# Ion channel noise

- Ohm's law tells us that the open single-channel current  $i$  can be written as

$$i = \gamma(E_{rev} - V)$$

where  $\gamma$  is the single-channel conductance,  $E_{rev}$  the reversal potential, and  $V$  the membrane voltage.

- If we have  $N$  of these channels, the mean current through the population, for a constant voltage, is  $\bar{I} = Nip$

where  $p$  is the steady-state open probability of the channel (fraction of time it is open).

- The standard deviation of the population current (i.e. "the noise") is given from the binomial distribution as

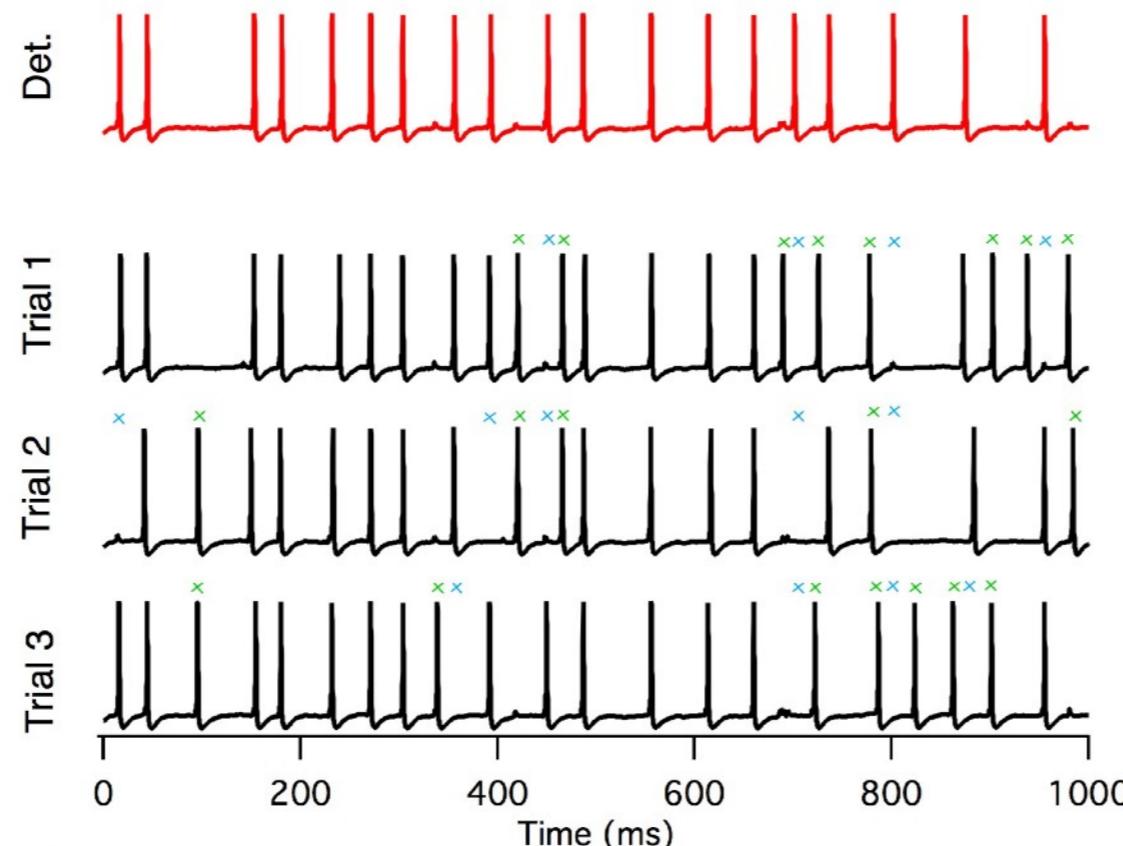
$$\sigma_I = i\sqrt{Np(1-p)}$$

- The coefficient of variation (ratio of the standard deviation to the mean) is:

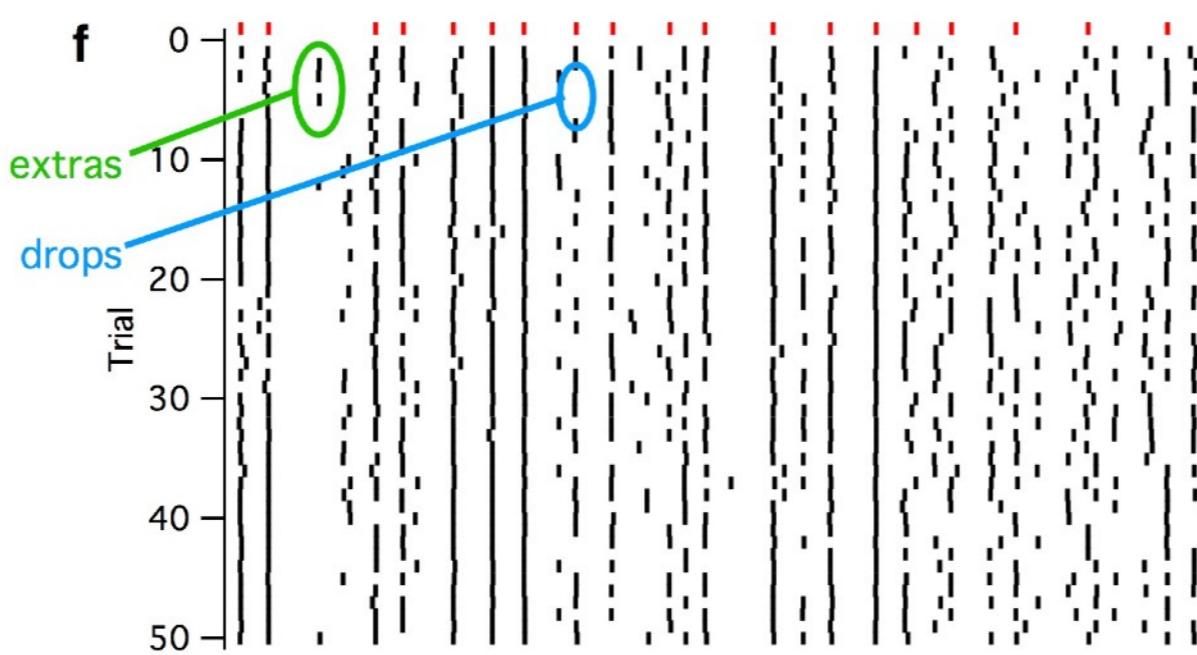
$$\text{C.V.} = \frac{\sigma_I}{\bar{I}} = \sqrt{\frac{1-p}{Np}}$$

# Ion channel noise makes the neuron's input-output function probabilistic

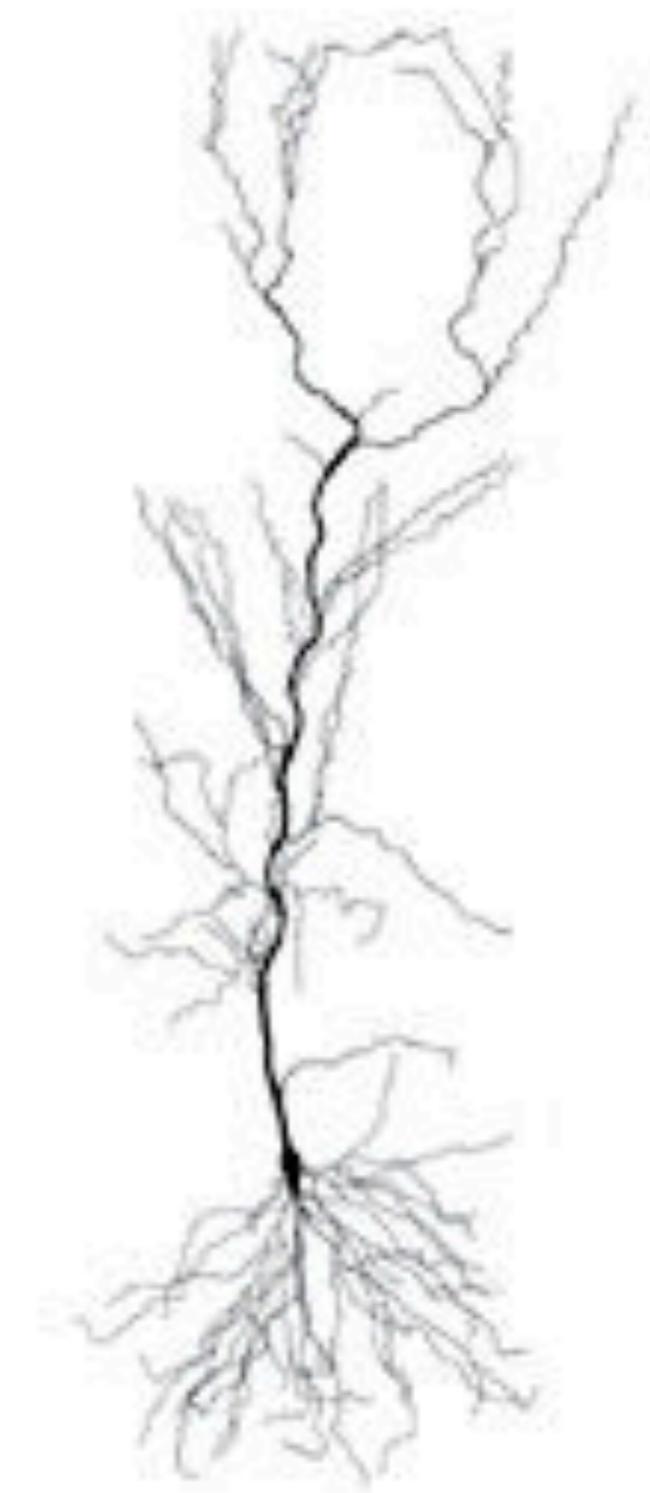
no noise



noise turned on



raster plot of  
many trials



# Optional further reading

- Scholarpedia article by Hille: [http://www.scholarpedia.org/article/Ion\\_channels](http://www.scholarpedia.org/article/Ion_channels)
- Spruston 2008. “Pyramidal Neurons: Dendritic Structure and Synaptic Integration.” *Nature Reviews Neuroscience* 9 (3): 206–21
- O'Donnell, and van Rossum, 2014. “Systematic Analysis of the Contributions of Stochastic Voltage Gated Channels to Neuronal Noise.” *Frontiers in Computational Neuroscience* 8. Frontiers: 105