

Computational Neuroscience 03 hippocampus

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October 2023

Modelling

This is an example of a model that explains what might be happening without giving a detailed simulation of the individual components involved.

Recap - McCulloch-Pitts neurons

$$x_i = \phi \left(\sum_j w_{ij} x_j \right)$$

where in classic applications

$$x_i = \begin{cases} +1 & \sum_j w_{ij} x_j > \theta \\ -1 & \text{otherwise} \end{cases}$$

and here we simplify further by setting $\theta = 0$.

Modelling

Here we look at the hippocampus and introduce a more top down style of modelling.

The hippocampus

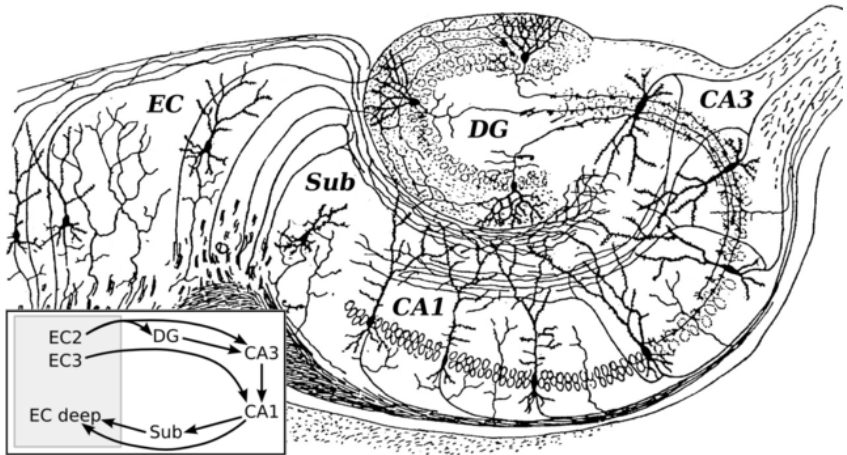


image from wikipedia, originally due to Cajal

The role of the hippocampus



The role of the hippocampus



image of Rodin's *The Thinker* from wikipedia

The hippocampus

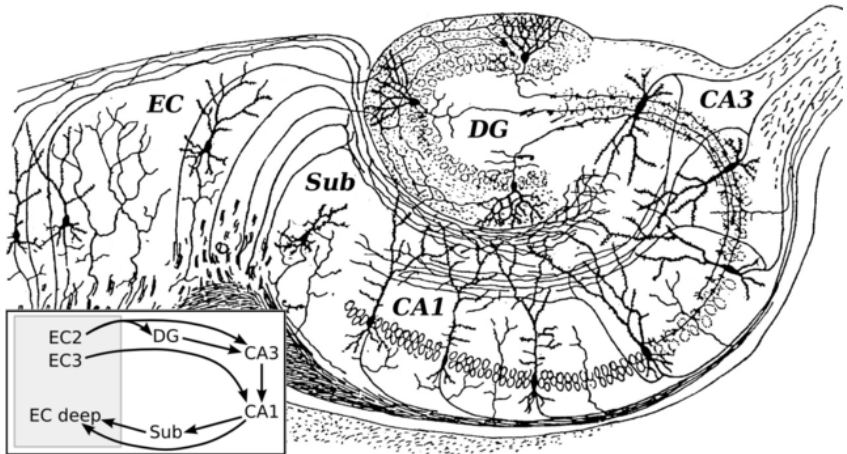
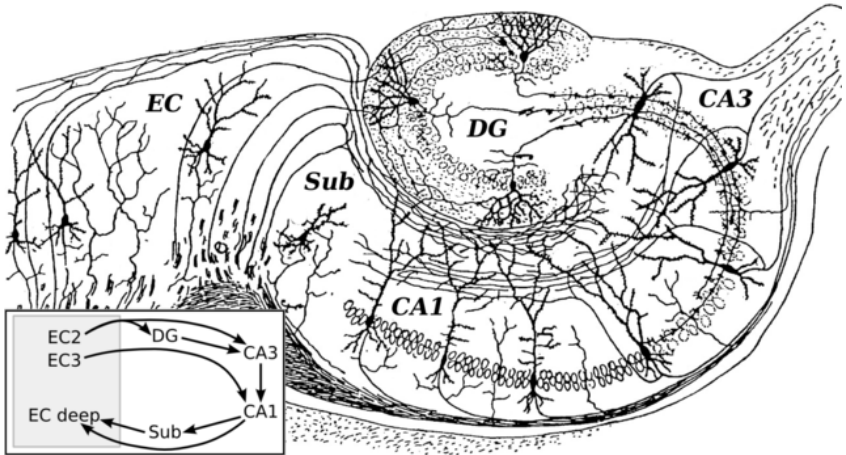


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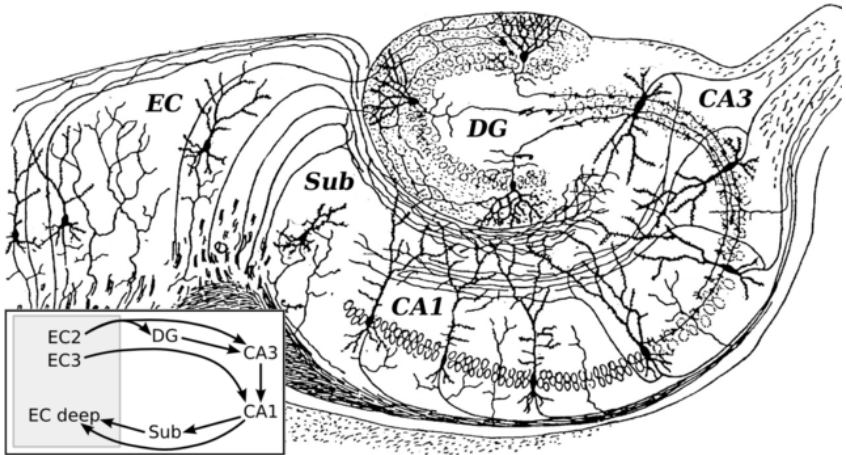
The hippocampus

Cornu Ammonis (CA) - meaning the *horn of Ammon*. The CA is usually divided into four regions, labelled CA1 through to CA4.



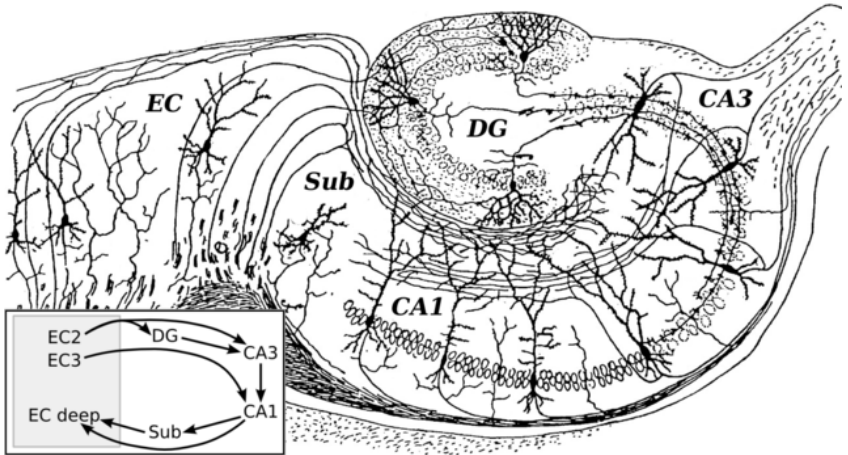
The hippocampus

Cornu Ammonis (CA) - meaning the *horn of Ammon*. The CA is usually divided into four regions, labelled CA1 through to CA4 - sort of.



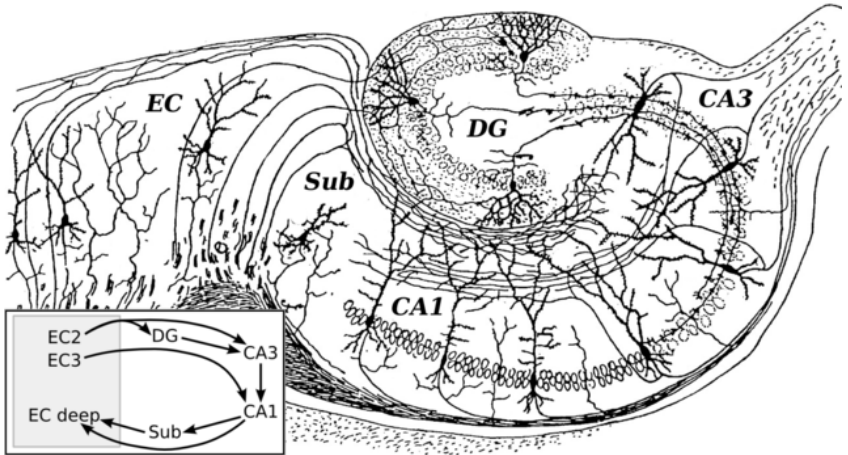
The hippocampus

Dentate Gyrus (DG)- gyrus is the name given to the ridges in the cortex, dentate means *with teeth*.

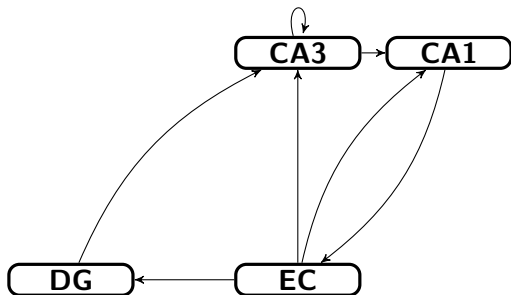


The hippocampus

Entorhinal Cortex (EC) - entorhinal means *near the smell processing area* - an honorary part of the hippocampus.

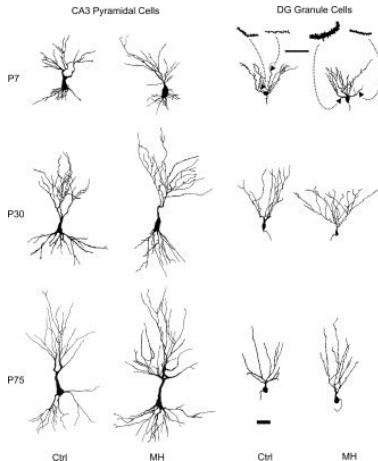


How the hippocampus is connected



Cells

The dentate gyrus is composed of granule cells, CA3 of pyramidal cells. DG is thought of a *feed-forward* whereas CA3 is highly *recurrent*.



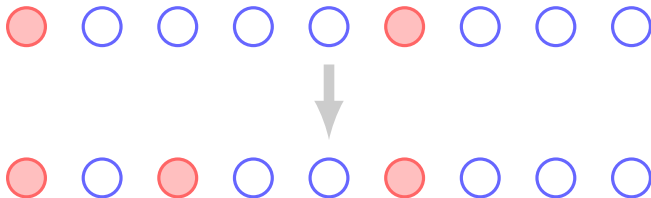
Auto-associative memory

A memory is a pattern of active neurons!



Auto-associative memory

The dynamics of the network complete partial patterns.



McCulloch-Pitts neurons

ON!

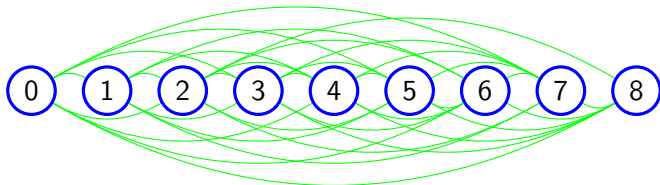


McCulloch-Pitts neurons

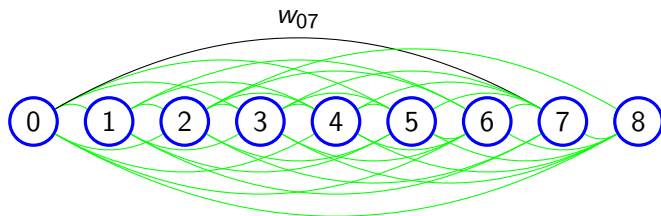
OFF!



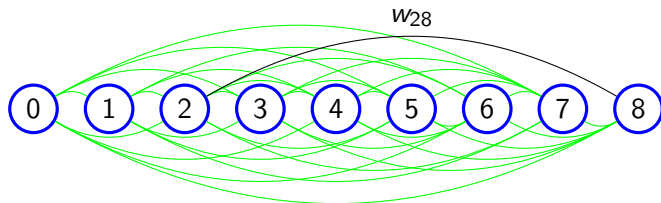
All-to-all network



All-to-all network



All-to-all network



Hebbian learning

$$\Delta w_{ij} = \eta(x_i - a)(x_j - a)$$

where a is the average number of ON nodes.

Hebbian learning

$$\Delta w_{ij} = \eta(x_i - a)(x_j - a)$$

OFF-OFF causes a small increase

$$\Delta w_{01} = \eta a^2$$



Hebbian learning

$$\Delta w_{ij} = \eta(x_i - a)(x_j - a)$$

OFF-ON causes a medium decrease

$$\Delta w_{01} = -\eta a(1 - a)$$

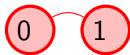


Hebbian learning

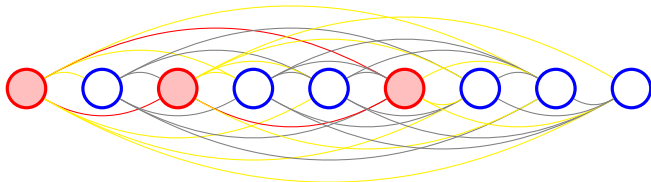
$$\Delta w_{ij} = \eta(x_i - a)(x_j - a)$$

ON-ON causes a big increase

$$\Delta w_{01} = \eta(1 - a)^2$$



Learning a pattern

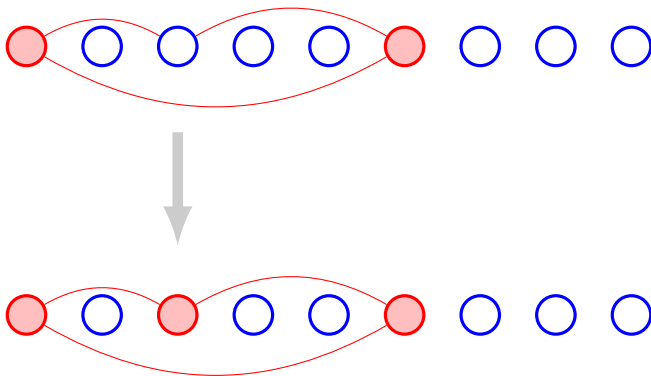


Activation

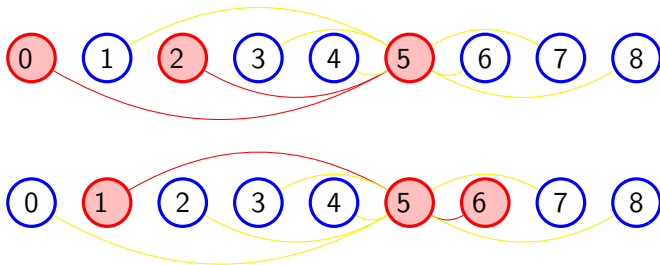
$$h_i = \sum w_{ij}x_j = w_{i0}x_0 + w_{i1}x_1 + w_{i2}x_2 + \dots$$

and if $h_i > \theta$ set x_i to one, otherwise set it to zero.

Auto-associative memory



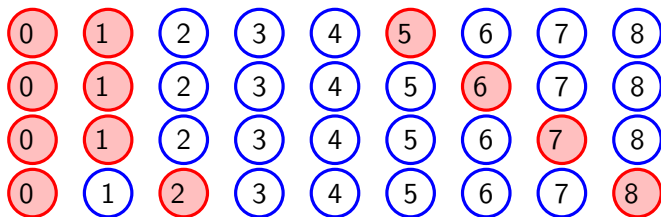
Capacity



Capacity

- ▶ N^2 connections.
- ▶ N neurons in a pattern.
- ▶ Can store something proportional to $N^2/N = N$ patterns.

Correlated patterns



Erroneous completion



or even



Patterns separation

Maybe the Dentate Gyrus fixes this problem!

Summary

1. CA3 - many recurrent connections, that is excitatory neurons connected to each other.
2. CA3 - an auto-associative memory store - patterns are completed.
3. CA3 - capacity proportional to N .
4. DG - feedforward, that is few, or even no, lateral connections between the excitatory neurons.
5. DG - separates patterns ready for EC to store them by randomizing them.