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Dendritic solutions to the credit assignment problemBlake A Richards^{1,2,3} and Timothy P Lillicrap⁴



Guaranteeing that synaptic plasticity leads to effective learning requires a means for assigning credit to each neuron for its contribution to behavior. The 'credit assignment problem' refers to the fact that credit assignment is non-trivial in hierarchical networks with multiple stages of processing. One difficulty is that if credit signals are integrated with other inputs, then it is hard for synaptic plasticity rules to distinguish creditrelated activity from non-credit-related activity. A potential solution is to use the spatial layout and non-linear properties of dendrites to distinguish credit signals from other inputs. In cortical pyramidal neurons, evidence hints that top-down feedback signals are integrated in the distal apical dendrites and have a distinct impact on spike-firing and synaptic plasticity. This suggests that the distal apical dendrites of pyramidal neurons help the brain to solve the credit assignment problem.

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Introduction: the credit assignment problem

The flexibility of learning in animals indicates that the brain possesses general purpose *learning algorithms*. A learning algorithm is a set of rules for translating the experiences an animal has into changes in their neural circuits (e.g. synaptic changes). The ultimate goal of a learning algorithm is to alter the behavioral phenotype of the animal, helping it to adapt to the environment. Understanding the brain's learning algorithms is key to understanding the biological basis of animal intelligence.

The formal study of learning algorithms often utilizes the concept of a *loss function* (also known as a cost function)

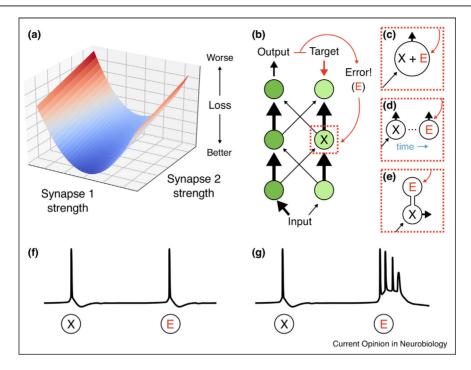
[1,2]. Within neuroscience, a loss function provides a metric for the failure of the current phenotype in achieving an animal's goals (Figure 1a) [3]. For example, a loss function could measure motor slips or sensory prediction errors. Ideally, the brain would have some way of ensuring that changes in a neural circuit reduce a given loss function [3], at least within the environments that the animal is likely to encounter [4]. To do this, it is useful to assign 'credit' (or 'blame') to each neuron or synapse for its contribution to the loss function [5,6]. However, outside of very simple neural circuits, credit assignment calculations are difficult. In a hierarchical sensorimotor circuit with multiple stages of processing, such as the mammalian neocortex, the credit that a neuron in a sensory area deserves for any motor errors depends on that neuron's downstream connections to motor circuits (Figure 1b) [7]. The difficulty of assigning credit in the context of hierarchical circuits is known as the credit assignment problem [8].

Typically, solutions to the credit assignment problem have been explored in neural network models that treat each neuron as a single voltage compartment with a single type of output (e.g. a scalar firing-rate or spike train) $[7,9^{\bullet\bullet},10^{\bullet\bullet},11-14,15^{\bullet}]$. This strategy is reasonable at face value: it fits with the basic properties of neural computation and helps to reduce mathematical complexity. However, there are two reasons that this strategy may have inadvertently made it more difficult to identify the brain's solution to the credit assignment problem. First, if each neuron is calculating everything using a single voltage value, then any incoming signals about credit (e.g. feedback from another cortical area) must be integrated with other signals about sensory data, or they must arrive at a separate time. The result is that any credit related signals must be carefully timed or they risk becoming entangled with other ongoing calculations (Figure 1c,d). There is some evidence of clock-like phasic activity in various parts of the brain [16], but none of these seem to exhibit the clear segregation between feedforward and feedback activity required for credit assignment. Second, if a neuron only has one type of output, for example, a firing rate, then it is not immediately obvious how neural circuits can disambiguate credit related activity from basic information transmission (Figure 1f).

Of course, real neurons are not single compartments—they possess complex dendritic trees that integrate different signals in different locations [17–27], often in nonlinear manners that have important functional implications [28–44]. Moreover, active channels in dendrites can drive spiking behavior that is different from regular

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Figure 1



Loss functions and credit assignment. (a) Illustration of a loss function. A loss function provides a metric for the performance of an agent on some learning task. In a neural circuit, loss functions are functions of synaptic strength. The goal of learning is to find synaptic strengths that minimize the loss function. Here, an arbitrary loss function is plotted for a network with only two synapses. (b) Illustration of the credit assignment problem. A multilayer neural network with two neurons per layer is shown. Circles indicate neurons, with green circles indicating highly active neurons. Arrows indicate synaptic connections and the width of the arrows indicates synaptic strength. If an input arrives at the left-hand neuron, its activity causes strong activation in the downstream left-hand neurons, due to strong synaptic connections. However, if the loss function specifies that the target was to give an output at the right-hand, then an error is generated. To make it more likely that the right-hand output neuron would be activated, it would help to increase the feedforward activity of the right-hand middle neuron, X. In other words, this neuron deserves some 'credit' for the incorrect output. Credit assignment can be achieved if the error signal at the top-level is sent back to the middle-layer. (c) However, if the middle-layer neuron is a single compartment, this error signal, E, would be integrated with the ongoing activity, X, thereby altering the 'forward' computation being performed by this neuron. (d) A possible solution is to have carefully timed phases where feedforward and feedback signals are received at distinct times. (e) An alternative is to integrate the credit assignment signal in a separate dendritic compartment. (f) and (g) Illustration of the use of specialized spike-waveforms for credit assignment. (f) If incoming inputs and credit signals both produce the same type of spiking output in a neuron (indicated by 'X' and 'E', respectively), it is difficult to differentiate credit assignment from ongoing processing. (g) In contrast, if credit signals drive dendritic non-linearities that produce unique spike-waveforms (e.g. a complex spike or high-frequency burst), then it is easy to differentiate credit assignment from other processes.

spiking [45,46]. One possibility, then, is to segregate credit signals into dendritic compartments, where (i) they can be kept separate from other ongoing calculations (Figure 1e), and (ii) they can drive unique spike-waveforms that signal credit information (Figure 1g). Thus, there has been a growing interest in understanding whether one of the solutions to the credit assignment problem lies in dendritic computation [47,48°,49°,50°] (and see also IMN Sacramento et al. arXiv: 1801.00062).

What counts as evidence for credit assignment?

The ideal experiment for understanding credit assignment in the brain would be to measure a loss function explicitly, then demonstrate that a given synaptic plasticity mechanism was responsible for ensuring reductions in that loss function during learning. Such experiments are currently outside of our technical reach, though, because it is often unclear how we can identify a loss function in the brain and track its progress over time [3]. Furthermore, there is no reason to assume that the brain explicitly represents any of the loss functions it may be reducing. Indeed, at the neural level, it is possible to reduce a loss function without there being any direct neural correlate of said loss function to find [51,52].

Given these realities, the best strategy for scientists to study credit assignment depends on the level of analysis. For example, if the desire is to examine whether credit assignment actually shapes activity in the brain based on the extent to which different neurons contribute to a task [53], then it is possible to use tetrode recordings and similar approaches [54]. In contrast, if the desire is to understand the cellular mechanisms by which credit is assigned in a hierarchy, then studies of synaptic plasticity are key. Historically, the study of plasticity rules has focused on two-factor Hebbian updates [55-57], which emphasize correlations in pre and postsynaptic activity [58]. However, the cumulative evidence from computational modeling and machine learning suggests that a simple Hebbian learning algorithm based solely on two factors — pre and postsynaptic activity — is insufficient for credit assignment in difficult tasks where the loss function depends on downstream circuits and delayed outcomes [55–57]. A starting place for coming to grips with this issue is to consider learning rules wherein pre and postsynaptic activity determine an 'eligibility trace' that indicates which synapses are eligible for updates, but a third (or possibly fourth) factor that depends on feedback or neuromodulation determines whether long-term potentiation (LTP) or long-term depression (LTD) occur [7,14,47,48°,59–62,63°,64]. Accordingly, these models predict that LTP/LTD should depend not only on pre and postsynaptic activity, but also on additional 'credit signals' carrying information about things like action outcomes, prediction errors, rewards/punishments, and attention [55-57,65]. Thus, a practical, experimental framework for studying credit assignment is to examine Hebbian synaptic plasticity rules in a circuit and determine whether additional feedback signals carrying creditrelated information can regulate the synaptic changes that occur.

There are several lines of experimental evidence supporting a role for neuromodulators in credit assignment in various neural circuits, including the hippocampus, neocortex and striatum [66-69]. Indeed, neuromodulators have been shown to have modulating effects on Hebbian-like synaptic plasticity in these circuits [66–68]. However, we also know that neuromodulator systems tend to transmit widely to a volume of tissue, and thus are not usually neuron specific, let alone dendrite specific. The most interesting role that dendrites could play in credit assignment would be to provide a site for finegrained credit assignment calculations, since effective credit assignment in deep networks typically requires some form of neuron-by-neuron credit signal [10°,57]. Thus, while neuromodulators undoubtedly play a crucial role in credit assignment systems, we here focus on neuron-by-neuron credit assignment mechanisms, which are more likely to be linked to dendritic processing.

Perhaps the clearest example of experimental evidence for neuron-by-neuron credit assignment is provided by learning in the cerebellum. In the cerebellum, granule cells project to Purkinje cells via parallel fibers, carrying information about input from the spinal cord, the cortex, and the vestibular system. The Purkinje cells carry signals that are considered the output of the cerebellum [70]. Various forms of motor learning may rely on the plasticity of parallel fiber synapses onto Purkinje cells [71–74]

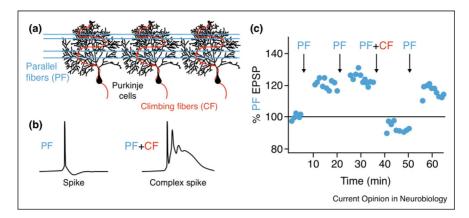
(though see [75]). However, this plasticity depends not only on parallel fiber and Purkinje cell activity, but a third term delivered via climbing fibers from the inferior olivary nucleus [70]. Evidence suggests that diverse error signals from downstream motor systems are communicated by the climbing fibers [76,77], and interestingly. climbing fibers synapse onto Purkinje cells in a one-toone correspondence. This makes one-to-one mapping of error signals possible (Figure 2a). Plasticity at the parallel fiber -> Purkinje cell synapses is mediated by a distinct spike-waveform generated by climbing fiber activity and the calcium currents they control, referred to as a 'complex spike' (Figure 2b) [45,78,79]. This allows the climbing fibers to control whether positive (LTP) or negative (LTD) changes in the parallel fiber → Purkinje cell connections occur [80–83] (Figure 2c). Moreover, the specific timing of climbing fiber activation controls parallel fiber -> Purkinje cell plasticity in a manner that matches the temporal delay between cerebellar activity and error signal receipt [84°]. Thus, this can be modeled as a three-factor learning rule, where pre and/or postsynaptic activities interact with a credit assignment factor provided by the climbing fibers [70,85].

There is a potentially important difference between Purkinje cell credit assignment and credit assignment in other neurons/circuits, though: because Purkinje cells represent the output of the cerebellum, and because there appears to be a one-to-one mapping between climbing fibers and Purkinje cells [45], the credit assignment problem in Purkinje cells is much less difficult. That is, credit assignment in Purkinje cells may be relatively straightforward, since error signals are not being integrated backwards through a complex hierarchy, but instead are directly communicated to each neuron on a one-to-one basis. Therefore, credit calculations in Purkinje cells may not require a dendritic compartment that is segregated from the parallel fiber inputs. In contrast, in pyramidal neurons buried deep in a cortical network in the forebrain, the credit assignment problem is much more daunting and dendritic segregation may be crucial for enabling detailed credit assignment.

Credit assignment in cortical pyramidal neurons

In the neocortex and hippocampus, pyramidal neurons are part of a hierarchical pathway with multiple sources of potential credit-related feedback. Thus, assigning credit in cortical pyramidal neurons may require more involved calculations than in the output layer of the cerebellum with one-to-one climbing fiber → Purkinje cell error signals. Where might these credit calculations take place? To date, direct experimental evidence for credit assignment calculations in neocortical neurons is limited. But, there are converging lines of evidence that led us to propose in a recent computational modeling study that

Figure 2



Credit assignment in the cerebellum. (a) Purkinje cells receive parallel fiber (PF) inputs from granule cells, as well as climbing fiber (CF) inputs in a one-CF-to-one-Purkinje manner. (b) When PF inputs are stimulated in isolation, regular spiking results. When PF inputs are paired with CF inputs, a complex spike is produced. (c) Climbing fiber inputs enable bidirectional regulation of PF \rightarrow Purkinje synaptic plasticity. PF input by itself can induce a saturating LTP that can be reversed by LTD when the same PF input patterns are paired with credit signals from CFs. Excitatory postsynaptic potential (EPSP) data shown is a reproduction by hand from Figure 3 of Ref. [82].

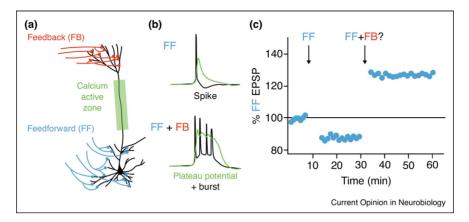
the distal apical dendrites of pyramidal neurons are involved in credit assignment [48**].

We begin by highlighting the properties of distal apical dendrites that make them suitable for credit assignment calculations. First, the distal apical dendrites in neocortex are a major recipient of higher-order cortico-cortical and thalamo-cortical feedback signals [21,86,18–20,86], and in the CA1 region of the hippocampus they receive longrange information back from entorhinal cortex [26,25]. This is notable because one of the key features of credit assignment in a number of computational models is the use of downstream feedback to control upstream synaptic plasticity [7,9**,10**,14,15*,48**]. Second, distal apical dendrites are electrotonically distant from the soma and the basal and oblique dendrites [34,37,87,88], which receive much of the local feedforward and recurrent inputs to pyramidal neurons [22,23]. As such, distal apical dendrites both receive feedback signals that are required for credit assignment, and they are sufficiently segregated to permit credit assignment calculations in isolation from ongoing sensory integration (Figure 3a).

If distal apical dendrites are electrotonically distant, though, how could their computations act as a third-factor to control plasticity in oblique and/or basal dendrites? Synaptic plasticity in pyramidal neurons ultimately depends on local depolarization and non-linear active potentials driven by N-methyl-D-aspartate (NMDA) receptors ('NMDA spikes') [49**,89-94]. Thus, what matters for the induction of synaptic plasticity is not postsynaptic action potential firing, per se, but the manner in which postsynaptic activity affects local depolarization in dendritic compartments [95,96]. Interestingly, distal apical dendrites may actually be well-placed to control depolarization in the basal/oblique dendrites. High-frequency burst-firing is a well established mechanism for inducing dendritic depolarization, NMDA spikes and synaptic plasticity [97,35,98], and burst-firing can alter the sign of synaptic plasticity in proximal synapses in cortical pyramidal neurons [99]. It is notable, then, that the distal apical dendrites are well-placed to drive burstfiring [46]. Specifically, the apical dendrites of pyramidal neurons have a region that is rich in voltage-gated calcium channels [31,33,100,101,43,36], which can induce 'plateau potentials' when the apical dendrites are sufficiently depolarized, or if there is coincident activation of distal apical inputs and somatic spiking (Figure 3b) [34,37,102,43]. These plateau potentials induce high-frequency (>100 Hz) bursts of action potentials [34,37,102]. As such, a switch from regular spiking to burst-firing in pyramidal neurons carries a signal indicating that inputs were received at the distal apical dendrites [102,46,103]. Given that burst-firing can regulate local depolarization in the basal/oblique dendrites, it has been proposed that bursts driven by distal apical inputs provide a third-factor that regulates plasticity in other dendrites based on current higher-order feedback [48**,104]. This proposed role for apical dendrites in synaptic plasticity has been used by computational modelers to implement creditassignment calculations in simulated pyramidal neurons [48°°,104] (IMN Sacramento et al. arXiv: 1801.00062), and thereby reduce high-level loss functions with local synaptic plasticity rules.

As stated above, the properties of apical dendrites make them suitable for credit assignment calculations, but experimental evidence for this proposal is limited. Nonetheless, recent findings support the conclusion that apical dendrites control plasticity in pyramidal neurons. In layer

Figure 3



Credit assignment in pyramidal neuron apical dendrites. (a) There is spatial segregation of the inputs to pyramidal neurons, with local feedforward (FF) inputs largely arriving at basal/oblique dendrites, and feedback (FB) inputs arriving largely at distal apical dendrites. These dendrites are electrotonically distant from each other. As well, the apical dendrites have a zone rich in active calcium conductances that can generate plateau potentials. The image shown here is a recreation of a layer 5 neocortical pyramidal neuron. (b) When FF inputs arrive they trigger regular spiking, which can backpropagate into the apical dendrite (green traces) but does not trigger a plateau potential. In contrast, when FF and FB inputs arrive together a plateau potential is generated, driving burst-firing. (c) The impact of FB inputs on FF synaptic plasticity is not well-understood. For example, one possibility (illustrated here with fake data) is that a protocol that normally generates LTD on FF pathways may be converted into a protocol that generates LTP when FF inputs are paired with FB inputs.

2/3 pyramidal neurons in somatosensory cortex, apical dendrites receiving associative thalamic input can induce synaptic plasticity of sensory inputs without spiking [105], and these same inputs gate synaptic plasticity when spiking does occur (IMN Williams & Holtmaat bioRxiv: 10.1101/281477). In the CA1 region of the hippocampus, two important studies recently demonstrated that apicaldriven plateau potentials control the formation of placecells and determine whether synaptic plasticity in basal dendrites occurs, even with seconds between the occurrence of basal synaptic input and plateau potentials [43°,106°]. Moreover, a series of studies examining visual cortex in the last few years have provided convincing demonstrations that layer 1 inputs from both higherorder cortex and associative thalamus can carry predictive and error feedback signals [107**,108,109*,110,111], which could be used to calculate prediction errors for credit assignment [9°,63°]. Altogether, the new data coming out in the field of dendritic processing, synaptic plasticity, and cortical coding is consistent with the hypothesized role for apical dendrites in credit assignment. This may help to explain the mysterious architecture of pyramidal neurons, wherein a substantial proportion of long-range inputs arrive at an electronically distant site [46]. However, much more experimental data needs to be collected to understand how apical dendrites might be involved in credit assignment calculations in pyramidal neurons. Specifically, more studies are required to determine: first, how apical inputs modify basal/oblique plasticity rules (Figure 3c), similar to how we know the manner in which climbing fiber inputs modulate parallel fiber inputs to Purkinje neurons [82], and second,

whether different pyramidal neurons in different regions use apical signals for credit assignment in different ways (e.g. are there differences in apical credit assignment between hippocampal versus neocortical, or layer 2/3 versus layer 5 pyramidal neurons?). Furthermore, it is possible that the distal compartments of basal dendrites provide another site for credit assignment calculations in cortical pyramidal neurons [49°°,112].

Conclusion

A major goal for researchers in coming years should be a better link between the theory of credit assignment in neural networks [7,9°,10°,11–14], and our growing knowledge of the biophysics of dendrites and dendritic computation [28-44]. Clearly, there is much more to understand about dendritic computations in pyramidal neurons, how they may signal credit information, and how they contribute to learning, in-turn. Three issues that deserve focused attention in our opinion are: first, how do dendritic mechanisms map onto three-factor synaptic update rules [55–57]? Second, what is the role of inhibitory interneuron microcircuits in credit assignment [27,50°,113–115]? Third, how does plasticity of feedback inputs to distal apical dendrites factor into credit assignment $[9^{\bullet\bullet},94,99,116-118]$? Each of these questions are ripe for extensive investigations.

The credit assignment problem has rarely been an explicit focus in experimental studies of synaptic plasticity. But, arguably, that was for two good reasons. First, the major theoretical advances in credit assignment were developed for artificial neural networks that made few

concrete experimental predictions [6,12,13]. Second, it is difficult/impossible to experimentally explore all of the potential input patterns that may drive synaptic plasticity. For example, spike-timing-dependent plasticity may not actually be the true synaptic update rule, but may instead be what emerges from a learning algorithm that uses feedback for credit assignment when studied with highly constrained spike-timing patterns [119°]. Thus, theoretical insights are required to guide synaptic plasticity experiments and provide practical limits on the inputs and spike patterns that need to be tested. One aspect of the current lack of predictions from neural network models is an absence of dendrites and their active properties. The assumption that all neurons are single, linear compartments with just one form of non-linear spiking output has made some mathematical analyses easier. However, whereas in machine learning the circuitry required for learning can be built outside the network being trained and dispensed with when it is not needed, in the real brain the circuitry for learning must fit into existing pathways and is always present. Recent computational work has highlighted the potential importance of dendrites with separate compartments and non-linear properties for solving the credit assignment problem in a biologically realistic manner [47,48°,49°]. Given the success of deep learning in artificial intelligence [2], and the emergence of sophisticated optical tools for studying dendritic computation [120], now is the ideal time for modelers and experimentalists to work together, and unify our understanding of dendritic computation with our theories of learning in hierarchical neural networks.

Conflict of interest statement

Nothing declared.

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References and recommended reading

Papers of particular interest, published within the period of review, have been highlighted as:

- · of special interest
- of outstanding interest
- MacKay DJ: Information Theory, Inference and Learning Algorithms. Cambridge University Press; 2003.
- LeCun Y, Bengio Y, Hinton G: Deep learning. Nature 2015, 521:436-444 http://dx.doi.org/10.1038/nature14539
- Marblestone AH, Wayne G, Kording KP: Toward an integration of deep learning and neuroscience. Front Comput Neurosci 2016, 10 http://dx.doi.org/10.3389/fncom.2016.00094.
- Wolpert DH, Macready WG: No free lunch theorems for optimization. IEEE Trans Evol Comput 1997, 1:67-82
- Schmidhuber J: Deep learning in neural networks: an overview. Neural Netw 2015, 61:85-117 URL http://www.sciencedirect.com/ science/article/pii/S0893608014002135

- Rumelhart DE, Hinton GE, Williams RJ: Learning representations by back-propagating errors. Nature 1986, 323:5
- Roelfsema PR, Ooyen AV: Attention-gated reinforcement learning of internal representations for classification. Neural Comput 2005, 17:2176-2214 http://dx.doi.org/10.1162/ 0899766054615699.
- Minsky M: Steps toward artificial intelligence. Proc IRE 1961.
- Lee D-H, Zhang S, Fischer A, Bengio Y: This paper introduces difference target propagation, an alternative to the backpropagation-of-error algorithm that avoids the requirement for symmetric feedback weights. The authors demonstrate that the algorithm can engage in efficient credit assignment in multilayer networks.. Difference target propagation. Springer; 2015:498-515.
- 10. Lillicrap TP, Cownden D, Tweed DB, Akerman CJ; Random synaptic feedback weights support error backpropagation for deep learning. Nat Commun 2016, 7:13276 http://dx.doi.org/ 10 1038/ncomms13276

This paper demonstrates that feedback pathways need not be symmetric to feedforward pathways for credit assignment to work. It provided one of the first possible solutions to the weight symmetry problem faced by backpropagation.

- Scellier B, Bengio Y: Equilibrium propagation: bridging the gap between energy-based models and backpropagation. Front Comput Neurosci 2017, 11:24 http://dx.doi.org/10.3389/
- 12. Hinton GE, Dayan P, Frey BJ, Neal RM: The 'wake-sleep' algorithm for unsupervised neural networks. Science 1995, 268:1158-1161 http://dx.doi.org/10.1126/science.7761831.
- 13. Hinton GE, Osindero S, Teh Y-W: A fast learning algorithm for deep belief nets. Neural Comput 2006, 18:1527-15
- 14. Rombouts JO, Bohte SM, Roelfsema PR: How attention can create synaptic tags for the learning of working memories in sequential tasks. PLOS Comput Biol 2015, 11:e1004060 http:// dx.doi.org/10.1371/journal.pcbi.1004060.
- 15. Zenke F, Ganguli S: SuperSpike: supervised learning in multilayer spiking neural networks. Neural Comput 2018, 30:1514-1541 http://dx.doi.org/10.1162/neco a 01086.

This paper provides a learning algorithm for credit assignment with precisely timed spike trains. The authors demonstrate that the algorithm can be used to solve the credit assignment problem in multilayer networks.

- 16. Buzsáki G, Draguhn A: Neuronal oscillations in cortical networks. Science 2004, 304:1926-1929 http://dx.doi.org/ 10.1126/science.1099745.
- 17. Cauller L, Connors B: Synaptic physiology of horizontal afferents to layer i in slices of rat SI neocortex. J Neurosci 1994, 14:751 http://dx.doi.org/10.1523/JNEUROSCI.14-02-00751
- Lu S-M, Lin RC-S: Thalamic afferents of the rat barrel cortex: a light- and electron-microscopic study using Phaseolus vulgaris leucoagglutinin as an anterograde tracer. Somatosens Motor Res 1993, 10:1-16 http://dx.doi.org/10.3109/ 08990229309028819.
- 19. Ohno S, Kuramoto E, Furuta T, Hioki H, Tanaka YR, Fujiyama F, Sonomura T, Uemura M, Sugiyama K, Kaneko T: A morphological analysis of thalamocortical axon fibers of rat posterior thalamic nuclei: a single neuron tracing study with viral vectors. Cereb Cortex 2012, 22:2840-2857 http://dx.doi.org/ 10.1093/cercor/bhr356.
- 20. Meyer HS, Wimmer VC, Hemberger M, Bruno RM, de Kock CP, Frick A, Sakmann B, Helmstaedter M: Cell type-specific thalamic innervation in a column of rat vibrissal cortex. Cereb Cortex 2010, 20:2287-2303 http://dx.doi.org/10.1093/cercor/bhq069.
- 21. Rockland KS, Virga A: Terminal arbors of individual 'feedback axons projecting from area v2 to v1 in the macaque monkey: a study using immunohistochemistry of anterogradely transported Phaseolus vulgaris-leucoagglutinin. J Comp Neurol 2004, 285:54-72 http://dx.doi.org/10.1002/ cne.902850106.

- Feldmeyer D, Lübke J, Silver RA, Sakmann B: Synaptic connections between layer 4 spiny neurone-layer 2/3 pyramidal cell pairs in juvenile rat barrel cortex: physiology and anatomy of interlaminar signalling within a cortical column. J Physiol 2004, 538:803-822 http://dx.doi.org/10.1113/jphysiol.2001.012959.
- Markram H, Lübke J, Frotscher M, Roth A, Sakmann B: Physiology and anatomy of synaptic connections between thick tufted pyramidal neurones in the developing rat neocortex. J Physiol 1997, 500:409-440 http://dx.doi.org/ 10.1113/jphysiol.1997.sp022031.
- Suh J, Rivest AJ, Nakashiba T, Tominaga T, Tonegawa S: Entorhinal cortex layer III input to the hippocampus is crucial for temporal association memory. Science 2011, 334:1415 http://dx.doi.org/10.1126/science.1210125.
- Megías M, Emri Z, Freund T, Gulyás A: Total number and distribution of inhibitory and excitatory synapses on hippocampal CA1 pyramidal cells. Neuroscience 2001, 102:527-540 http://dx.doi.org/10.1016/S0306-4522(00)00496-6.
- Steward O, Scoville Sheila A: Cells of origin of entorhinal cortical afferents to the hippocampus and fascia dentata of the rat. J Comp Neurol 2004, 169:347-370 http://dx.doi.org/10.1002/ cne.901690306.
- Muñoz W, Tremblay R, Levenstein D, Rudy B: Layer-specific modulation of neocortical dendritic inhibition during active wakefulness. Science 2017, 355:954 http://dx.doi.org/10.1126/ science.aag2599.
- Poirazi P, Brannon T, Mel BW: Arithmetic of subthreshold synaptic summation in a model CA1 pyramidal cell. Neuron 2003, 37:977-987 http://dx.doi.org/10.1016/S0896-6273(03) 00148-X.
- Poirazi P, Brannon T, Mel BW: Pyramidal neuron as two-layer neural network. Neuron 2003, 37:989-999 http://dx.doi.org/ 10.1016/S0896-6273(03)00149-1.
- Takahashi H, Magee JC: Pathway interactions and synaptic plasticity in the dendritic tuft regions of CA1 pyramidal neurons. Neuron 2009, 62:102-111 http://dx.doi.org/10.1016/j. neuron.2009.03.007.
- Yuste R, Gutnick MJ, Saar D, Delaney KR, Tank DW: Ca2+ accumulations in dendrites of neocortical pyramidal neurons: an apical band and evidence for two functional compartments. Neuron 1994, 13:23-43 http://dx.doi.org/10.1016/0896-6273(94) 90457-X.
- Hirsch JA, Alonso J-M, Reid RC: Visually evoked calcium action potentials in cat striate cortex. Nature 1995, 378:612 http://dx. doi.org/10.1038/378612a0.
- Schiller J, Schiller Y, Stuart G, Sakmann B: Calcium action potentials restricted to distal apical dendrites of rat neocortical pyramidal neurons. J Physiol 2004, 505:605-616 http://dx.doi.org/10.1111/j.1469-7793.1997.605ba.x.
- Larkum ME, Zhu JJ, Sakmann B: A new cellular mechanism for coupling inputs arriving at different cortical layers. *Nature* 1999, 398:338-341 http://dx.doi.org/10.1038/18686.
- Larkum ME, Kaiser KMM, Sakmann B: Calcium electrogenesis in distal apical dendrites of layer 5 pyramidal cells at a critical frequency of back-propagating action potentials. Proc Natl Acad Sci U S A 1999, 96:14600 http://dx.doi.org/10.1073/ pnas.96.25.14600.
- Larkum ME, Waters J, Sakmann B, Helmchen F: Dendritic spikes in apical dendrites of neocortical layer 2/3 pyramidal neurons. J Neurosci 2007, 27:8999-9008 http://dx.doi.org/10.1523/ JNEUROSCI.1717-07.2007.
- Larkum ME, Nevian T, Sandler M, Polsky A, Schiller J: Synaptic integration in tuft dendrites of layer 5 pyramidal neurons: a new unifying principle. Science 2009, 325:756-760 http://dx.doi. org/10.1126/science.1171958.
- Branco T, Clark BA, Häusser M: Dendritic discrimination of temporal input sequences in cortical neurons. Science 2010, 329:1671-1675.

- Schmidt-Hieber C, Toleikyte G, Aitchison L, Roth A, Clark BA, Branco T, Hausser M: Active dendritic integration as a mechanism for robust and precise grid cell firing. Nat Neurosci 2017, 20:1114-1121 http://dx.doi.org/10.1038/nn.4582.
- Waters J, Larkum M, Sakmann B, Helmchen F: Supralinear Ca2+ influx into dendritic tufts of layer 2/3 neocortical pyramidal neurons in vitro and in vivo. J Neurosci 2003, 23:8558 http://dx. doi.org/10.1523/JNEUROSCI.23-24-08558.2003.
- Takahashi N, Oertner TG, Hegemann P, Larkum ME: Active cortical dendrites modulate perception. Science 2016, 354:1587 http://dx.doi.org/10.1126/science.aah6066.
- Suzuki M, Larkum ME: Dendritic calcium spikes are clearly detectable at the cortical surface. Nat Commun 2017, 8 http:// dx.doi.org/10.1038/s41467-017-00282-4.
- 43. Bittner KC, Grienberger C, Vaidya SP, Milstein AD, Macklin JJ, Suh J, Tonegawa S, Magee JC: Conjunctive input processing drives feature selectivity in hippocampal CA1 neurons. *Nat Neurosci* 2015, **18**:1133-1142 http://dx.doi.org/10.1038/nn.4062.
- Palmer LM, Shai AS, Reeve JE, Anderson HL, Paulsen O, Larkum ME: NMDA spikes enhance action potential generation during sensory input. Nat Neurosci 2014, 17:383-390 http://dx. doi.org/10.1038/nn.3646.
- Schmolesky M, Weber John T, Zeeuw Chris I, Christian H: The making of a complex spike: ionic composition and plasticity. Ann N Y Acad Sci 2006, 978:359-390 http://dx.doi.org/10.1111/ j.1749-6632.2002.tb07581.x.
- Larkum M: A cellular mechanism for cortical associations: an organizing principle for the cerebral cortex. *Trends Neurosci* 2013, 36:141-151 http://dx.doi.org/10.1016/j.tins.2012.11.006.
- Urbanczik R, Senn W: Learning by the dendritic prediction of somatic spiking. Neuron 2014, 81:521-528 http://dx.doi.org/ 10.1016/j.neuron.2013.11.030.
- 48. Guerguiev J, Lillicrap TP, Richards BA: Towards deep learning
 with segregated dendrites. eLife 2017, 6:e22901 http://dx.doi.org/10.7554/eLife.22901.

This paper provides a computational model of credit assignment with electronically segregated dendrites. It illustrates how the electronic segregation of credit signals can be used to make credit calculations easier in a biologically realistic framework.

 49. Bono J, Clopath C: Modeling somatic and dendritic spike
 mediated plasticity at the single neuron and network level. Nat Commun 2017, 8:706 http://dx.doi.org/10.1038/s41467-017-00740-z.

This paper uses computational modeling to explore synaptic plasticity mediated by dendritic mechanisms. It finds that dendrites permit multiple plasticity rules to co-exist in the same cell. One notable finding is that inputs to the distal basal dendrites can be used to switch the sign of synaptic plasticity in other basal compartments.

 Wilmes KA, Sprekeler H, Schreiber S: Inhibition as a binary switch for excitatory plasticity in pyramidal neurons. PLOS Comput Biol 2016, 12:e1004768 http://dx.doi.org/10.1371/journal. pcbi.1004768.

This paper uses multi-compartment modeling of pyramidal neurons to examine the potential for inhibition to gate synaptic plasticity in dendrites. The authors find that with precisely timed inhibition it is possible to gate synaptic plasticity in an all-or-none manner in the dendrites without impacting information processing in the soma.

- Hinton GE: Training products of experts by minimizing contrastive divergence. Neural Comput 2002, 14:1771-1800 http://dx.doi.org/10.1162/089976602760128018.
- Hinton GE, Sejnowski TJ: Learning and relearning in Boltzmann machines. Parallel Distributed Processing: Explorations in the Microstructure of Cognition. MIT Press; 1986:282-317.
- Abbott LF, DePasquale B, Memmesheimer R-M: Building functional networks of spiking model neurons. Nat Neurosci 2016, 19:350 http://dx.doi.org/10.1038/nn.4241.
- Gulati T, Guo L, Ramanathan DS, Bodepudi A, Ganguly K: Neural reactivations during sleep determine network credit assignment. Nat Neurosci 2017, 20:1277-1284 http://dx.doi.org/ 10.1038/nn.4601.

- 55. Frémaux N, Gerstner W: Neuromodulated spike-timingdependent plasticity, and theory of three factor learning rules. Front Neural Circuits 2016, 9:85 http://dx.doi.org/10.3389/ fncir.2015.00085
- 56. Kuśmierz L, Isomura T, Toyoizumi T: Learning with three factors: modulating Hebbian plasticity with errors. Comput Neurosci 2017, 46:170-177 http://dx.doi.org/10.1016/j.conb.2017.08.020.
- 57. Roelfsema PR, Holtmaat A: Control of synaptic plasticity in deep cortical networks. Nat Rev Neurosci 2018, 19:166 http://dx.doi. org/10.1038/nrn.2018.6.
- 58. Bi G, Poo M: Synaptic modification by correlated activity: Hebb's postulate revisited. Annu Rev Neurosci 2001, 24:139-166 http://dx.doi.org/10.1146/annurev.neuro.24.1.139.
- 59. Xie X, Seung HS: Learning in neural networks by reinforcement of irregular spiking. *Phys Rev E* 2004, **69**:041909 http://dx.doi.org/10.1103/PhysRevE.69.041909.
- Vasilaki E, Frémaux N, Urbanczik R, Senn W, Gerstner W: Spikebased reinforcement learning in continuous state and action space: when policy gradient methods fail. PLoS Comput Biol 2009, 5:e1000586 http://dx.doi.org/10.1371/journal. pcbi.1000586.
- 61. Legenstein R, Pecevski D, Maass W: A learning theory for reward-modulated spike-timing-dependent plasticity with application to biofeedback. PLoS Comput Biol 2008, 4: e1000180 http://dx.doi.org/10.1371/journal.pcbi.1000180.
- Brzosko Z, Zannone S, Schultz W, Clopath C, Paulsen O: Sequential neuromodulation of Hebbian plasticity offers mechanism for effective reward-based navigation. eLife 2017, 6:e27756 http://dx.doi.org/10.7554/eLife.27756
- Whittington JC, Bogacz R: An approximation of the error backpropagation algorithm in a predictive coding network with local Hebbian synaptic plasticity. Neural Comput 2017. 29:1229-1262

This paper demonstrates that the popular predictive coding framework is functionally equivalent to the backpropagation-of-error algorithm and can be used for credit assignment in hierarchical networks.

- Urbanczik R, Senn W: Reinforcement learning in populations of spiking neurons. Nat Neurosci 2009, 12:250.
- Lisman J, Grace AA, Duzel E: A neo Hebbian framework for episodic memory; role of dopamine-dependent late LTP Hippocampus Mem 2011, 34:536-547 http://dx.doi.org/10.1016/j. tins.2011.07.006.
- He K, Huertas M, Hong SZ, Tie X, Hell JW, Shouval H, Kirkwood A: Distinct eligibility traces for LTP and LTD in cortical synapses. Neuron 2015, 88:528-538.
- Brzosko Z, Schultz W, Paulsen O: Retroactive modulation of spike timing-dependent plasticity by dopamine. eLife 2015, 4 http://dx.doi.org/10.7554/eLife.09685
- Yagishita S, Hayashi-Takagi A, Ellis-Davies GC, Urakubo H, Ishii S, Kasai H: A critical time window for dopamine actions on the structural plasticity of dendritic spines. Science 2014, **345**:1616-1620.
- 69. Schultz W, Dayan P, Montague PR: A neural substrate of prediction and reward. Science 1997, 275:1593-1599 http://dx. doi.org/10.1126/science.275.5306.1593
- 70. Ito M: Control of mental activities by internal models in the cerebellum. Nat Rev Neurosci 2008, 9:304 http://dx.doi.org/
- Koekkoek SKE, Hulscher HC, Dortland BR, Hensbroek RA, Elgersma Y, Ruigrok TJH, De Zeeuw Cl: Cerebellar LTD and learning-dependent timing of conditioned eyelid responses. Science 2003, 301:1736 http://dx.doi.org/10.1126/ science.1088383
- 72. Boyden ES, Katoh A, Pyle JL, Chatila TA, Tsien RW, Raymond J: Selective engagement of plasticity mechanisms for motor memory storage. Neuron 2006, 51:823-834 http://dx.doi.org/ 10.1016/j.neuron.2006.08.026.
- De Zeeuw Cl, Hansel C, Bian F, Koekkoek SK, van Alphen AM, Linden DJ, Oberdick J: Expression of a protein kinase c inhibitor

- in Purkinje cells blocks cerebellar LTD and adaptation of the vestibulo-ocular reflex. Neuron 1998, 20:495-508 http://dx.doi. org/10.1016/S0896-6273(00)80990-3.
- Hansel C, de Jeu M, Belmeguenai A, Houtman SH, Buitendijk G, Andreev D, DeZeeuw C, Elgersma Y: alpha-CaMKII is essential for cerebellar LTD and motor learning. Neuron 2006, 51:835-843 http://dx.doi.org/10.1016/j.neuron.2006.08.013.
- Schonewille M, Gao Z, Boele H-J, VinuezaVeloz M, Amerika W, imek A, DeJeu M, Steinberg J, Takamiya K, Hoebeek F, Linden D, Huganir R, DeZeeuw C: Reevaluating the role of LTD in cerebellar motor learning. Neuron 2011, 70:43-50 http://dx.doi. org/10.1016/j.neuron.2011.02.044.
- 76. Guo CC, Ke MC, Raymond JL: Cerebellar encoding of multiple candidate error cues in the service of motor learning. JNeurosci 2014, 34:9880 http://dx.doi.org/10.1523/ JNEUROSCI.5114-13.2014.
- 77. Kimpo RR, Rinaldi JM, Kim CK, Payne HL, Raymond JL: Gating of neural error signals during motor learning. eLife 2014:3.
- 78. Llinas R, Sugimori M: Electrophysiological properties of in vitro Purkinje cell dendrites in mammalian cerebellar slices. JPhysiol 1980, 305:197-213.
- 79. Llinas R, Sugimori M: Electrophysiological properties of in vitro Purkinje cell somata in mammalian cerebellar slices. J Physiol 1980, **305**:171-195.
- 80. Lev-Ram V, Wong ST, Storm DR, Tsien RY: A new form of cerebellar long-term potentiation is postsynaptic and depends on nitric oxide but not cAMP. Proc Natl Acad Sci U S A 2002, 99:8389 http://dx.doi.org/10.1073/pnas.122206399.
- 81. Lev-Ram V, Mehta SB, Kleinfeld D, Tsien RY: Reversing cerebellar long-term depression. Proc Natl Acad Sci USA 2003, 100:15989 http://dx.doi.org/10.1073/pnas.2636935100.
- 82. Coesmans M, Weber JT, De Zeeuw Cl, Hansel C: Bidirectional parallel fiber plasticity in the cerebellum under climbing fiber control. *Neuron* 2004, **44**:691-700.
- 83. Yang Y, Lisberger SG: Purkinje-cell plasticity and cerebellar motor learning are graded by complex-spike duration. Nature 2014, **510**:529-532
- 84. Suvrathan A, Payne HL, Raymond JL: Timing rules for synaptic plasticity matched to behavioral function. *Neuron* 2016, **92**:959 967 http://dx.doi.org/10.1016/j.neuron.2016.10.022.

This paper demonstrates that the spike-timing-dependent plasticity rules in different regions of the cerebellum are adapted to the specific delay at which error signals from the climbing fibers would normally arrive during motor learning.

- 85. Kawato M, Furukawa K, Suzuki R: A hierarchical neural-network model for control and learning of voluntary movement. Biol Cybern 1987, 57:169-185 http://dx.doi.org/10.1007/BF00364149.
- 86. Kwon SE, Yang H, Minamisawa G, O'Connor DH: Sensory and decision-related activity propagate in a cortical feedback loop during touch perception. Nat Neurosci 2016, 19:1243 http://dx. doi.org/10.1038/nn.4356.
- 87. Stuart G, Spruston N: Determinants of voltage attenuation in neocortical pyramidal neuron dendrites. J Neurosci 1998, 18:3501 http://dx.doi.org/10.1523/JNEUROSCI.18-10-03501
- 88. Williams SR, Stuart GJ: Dependence of EPSP efficacy on synapse location in neocortical pyramidal neurons. Science 2002, 295:1907 http://dx.doi.org/10.1126/science.1067903.
- 89. Kampa BM, Letzkus JJ, Stuart GJ: Requirement of dendritic calcium spikes for induction of spike-timing-dependent synaptic plasticity. J Physiol 2006, 574:283-290 http://dx.doi. org/10.1113/jphysiol.2006.111062.
- 90. Sjöström PJ, Turrigiano GG, Nelson SB: Rate, timing, and cooperativity jointly determine cortical synaptic plasticity. Neuron 2001, 32:1149-1164 http://dx.doi.org/10.1016/S0896-6273(01)00542-6.
- 91. Golding NL, Staff NP, Spruston N: Dendritic spikes as a mechanism for cooperative long-term potentiation. Nature 2002, 418:326 http://dx.doi.org/10.1038/nature00854.

- 92. Feldman DE: Timing-based LTP and LTD at vertical inputs to layer II/III pyramidal cells in rat barrel cortex. Neuron 2000, 27:45-56 http://dx.doi.org/10.1016/S0896-6273(00)00008-8.
- 93. Clopath C, Büsing L, Vasilaki E, Gerstner W: Connectivity reflects coding: a model of voltage-based STDP with homeostasis. Nat Neurosci 2010, 13:344-352.
- 94. Sjöström PJ, Häusser M: A cooperative switch determines the sign of synaptic plasticity in distal dendrites of neocortical pyramidal neurons. Neuron 2006, 51:227-238 http://dx.doi.org/ 10.1016/j.neuron.2006.06.017.
- 95. Kampa BM, Letzkus JJ, Stuart GJ: Dendritic mechanisms controlling spike-timing-dependent synaptic plasticity. Trends Neurosci 2007, 30:456-463 http://dx.doi.org/10.1016/j. tins 2007 06 010
- 96. Lisman J, Spruston N: Questions about STDP as a general model of synaptic plasticity. Front Synaptic Neurosci 2010,
- Kampa BM, Stuart GJ: Calcium spikes in basal dendrites of layer 5 pyramidal neurons during action potential bursts. J Neurosci 2006, 26:7424 http://dx.doi.org/10.1523/ JNEUROSCI.3062-05.2006.
- 98. Pike FG, Meredith RM, Olding AWA, Paulsen O: Postsynaptic bursting is essential for 'Hebbian' induction of associative long-term potentiation at excitatory synapses in rat hippocampus. *J Physiol* 1999, **518**:571-576 http://dx.doi.org/ 10.1111/i.1469-7793.1999.0571p.x.
- 99. Letzkus JJ, Kampa BM, Stuart GJ: Learning rules for spike timing-dependent plasticity depend on dendritic synapse location. *J Neurosci* 2006, **26**:10420-10429 URL http://www. jneurosci.org/content/26/41/10420.short.
- 100. Larkum ME, Zhu JJ: Signaling of layer 1 and whisker-evoked Ca2+ and Na+ action potentials in distal and terminal dendrites of rat neocortical pyramidal neurons in vitro and in vivo. J Neurosci 2002, 22:6991 http://dx.doi.org/10.1523 JNEUROSCI.22-16-06991.2002.
- 101. Amitai Y, Friedman A, Connors BW, Gutnick MJ: Regenerative activity in apical dendrites of pyramidal cells in neocortex. Cereb Cortex 1993, 3:26-38 http://dx.doi.org/10.1093/cercor/
- 102. Shai AS, Anastassiou CA, Larkum ME, Koch C: Physiology of layer 5 pyramidal neurons in mouse primary visual cortex: coincidence detection through bursting. PLoS Comput Biol 2015, 11:e1004090 http://dx.doi.org/10.1371/journal. pcbi.1004090.
- 103. Naud R, Sprekeler H: Sparse bursts optimize information transmission in a multiplexed neural code. Proc Natl Acad Sci U S A 2018, 201720995.
- 104. Körding KP, König P: Supervised and unsupervised learning with two sites of synaptic integration. J Comput Neurosci 2001, 11:207-215 http://dx.doi.org/10.1023/A:1013776130161
- 105. Gambino F, Pages S, Kehayas V, Baptista D, Tatti R, Carleton A, Holtmaat A: Sensory-evoked LTP driven by dendritic plateau potentials in vivo. Nature 2014, 515:116-119 http://dx.doi.org/ 10.1038/nature13664
- 106. Bittner KC, Milstein AD, Grienberger C, Romani S, Magee JC: Behavioral time scale synaptic plasticity underlies CA1 place
- fields. Science 2017, 357:1033 http://dx.doi.org/10.1126/science.

This paper demonstrates that place-field formation in CA1 of the hippocampus depends on a synaptic plasticity rule that depends on plateau potentials. The timing-rules are such that inputs that occur seconds before or after a plateau potential are potentiated.

- 107. Leinweber M, Ward DR, Sobczak JM, Attinger A, Keller GB: A sensorimotor circuit in mouse cortex for visual flow
- predictions. Neuron 2017, 95:1420-1432.e5 http://dx.doi.org/ 10.1016/j.neuron.2017.08.036.

This paper demonstrated the existence of a feedback pathway from premotor cortex to primary visual cortex in mice. The signals communicated by this pathway could potentially be used to solve the credit assignment problem.

- 108. Keller GB, Bonhoeffer T, Hübener M: Sensorimotor mismatch signals in primary visual cortex of the behaving mouse. *Neuron* 2012, **74**:809-815 http://dx.doi.org/10.1016/j. neuron.2012.03.040.
- 109. Roth MM, Dahmen JC, Muir DR, Imhof F, Martini FJ, Hofer SB: Thalamic nuclei convey diverse contextual information to layer 1 of visual cortex. Nat Neurosci 2016, 19:299-307 http://dx. doi.org/10.1038/nn.4197

This paper explores thalamic inputs to layer 1 of primary visual cortex. One notable finding in the paper is the observation that feedback from associative thalamus contains information about visuomotor mismatches, which are the type of error signal used for credit assignment in some computational models.

- 110. Zmarz P, Keller G: Mismatch receptive fields in mouse visual cortex. Neuron 2016, 92:766-772 http://dx.doi.org/10.1016/j. neuron.2016.09.057.
- 111. Fiser A, Mahringer D, Oyibo HK, Petersen AV, Leinweber M, Keller GB: Experience-dependent spatial expectations in mouse visual cortex. Nat Neurosci 2016 http://dx.doi.org/
- 112. Gordon U, Polsky A, Schiller J: Plasticity compartments in basal dendrites of neocortical pyramidal neurons. J Neurosci 2006, 26:12717 http://dx.doi.org/10.1523/JNEUROSCI.3502-06.2006.
- 113. Groen MR, Paulsen O, Pérez-Garci E, Nevian T, Wortel J, Dekker MP, Mansvelder HD, van Ooyen A, Meredith RM: Development of dendritic tonic GABAergic inhibition regulates excitability and plasticity in CA1 pyramidal neurons. Neurophysiol 2014, 112:287-299 http://dx.doi.org/10.1152/ jn.00066.2014
- 114. Meredith RM, Floyer-Lea AM, Paulsen O: Maturation of longterm potentiation induction rules in rodent hippocampus: role of GABAergic inhibition. J Neurosci 2003, 23:11142-11146 URL http://view.ncbi.nlm.nih.gov/pubmed/14657173.
- 115. Fagiolini M, Hensch TK: Inhibitory threshold for critical-period activation in primary visual cortex. Nature 2000, 404:183-186 http://dx.doi.org/10.1038/35004582.
- 116. Froemke RC, Poo MM, Dan Y: Spike-timing-dependent synaptic plasticity depends on dendritic location. Nature 2005, 434:221-25 http://dx.doi.org/10.1038/nature03366
- 117. Burbank KS: Mirrored STDP implements autoencoder learning in a network of spiking neurons. PLoS Comput Biol 2015, 11 http://dx.doi.org/10.1371/journal.pcbi.1004566.
- 118. Burbank KS, Kreiman G: Depression-biased reverse plasticity rule is required for stable learning at top-down connections. PLOS Comput Biol 2012, 8:e1002393 http://dx.doi.org/10.1371/ journal.pcbi.1002393.
- 119. Bengio Y, Mesnard T, Fischer A, Zhang S, Wu Y: STDPcompatible approximation of backpropagation in an energybased model. Neural Comput 2017, 29:555-577.

This paper demonstrates that a spike-timing-dependent plasticity rule can emerge from a rate-based synaptic plasticity rule that solves the credit assignment problem. The algorithm uses backpropagated gradients contained in the temporal derivatives of the firing rates.

120. Scanziani M, Hausser M: Electrophysiology in the age of light. Nature 2009, 461:930-939 http://dx.doi.org/10.1038/nature08540.