

Key Agreement

- We have assumed that Alice and Bob have agreed upon a key known only to themselves
- How did they do that?
- Secret key agreement: Alice and Bob agree upon shared key K , over a public channel, without any eavesdroppers learning K
- How can we achieve secret key agreement?

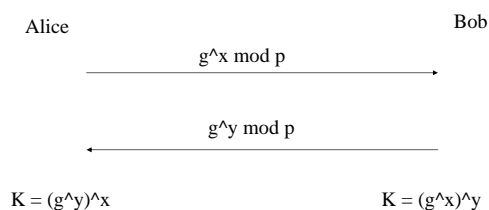
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Diffie-Hellman (1/3)

- Two people can agree over an insecure channel on a secret key in such a way that both of them receive the same key without anyone else knowing it
- Original protocol published in 1976
- p : A prime number being 2000 to 4000 bits long
 - Prime: A number that has exactly two divisors, 1 and itself
- Taking a modulo: Just divide r by p , throw away the quotient and keep the remainder as the answer
 - Example: 25 modulo 7, you divide 25 by 7, which gives a quotient of 3 with a remainder of 4, so $25 \bmod 7 = 4$
- We first choose a large prime p and a primitive element g which generates a finite field

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Diffie-Hellman (2/3)



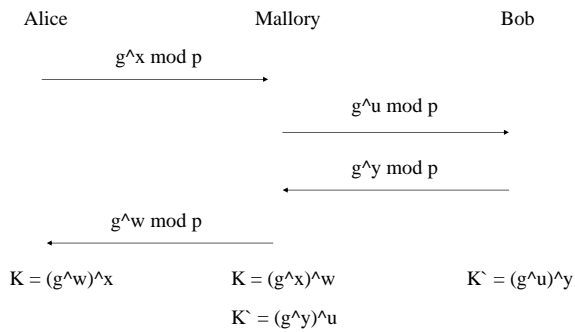
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Diffie-Hellman (3/3)

- The attacker sees g^x and g^y but not x or y
- The problem of computing g^{xy} given g^x and g^y is known as the DH problem
- As long as p and g are chosen correctly there is no way to compute this efficiently
- In the finite field is called discrete logarithm and the problem of computing x from g^x in a finite group is known as the discrete logarithm problem

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An Active Attack



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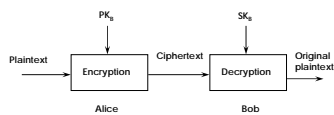
Asymmetric Key Cryptosystems

- In public key cryptography each person has a pair of keys
 - The *public key* and the *private key*
- Public key is published and widely distributed
 - While the private key is kept secret
- Need for exchanging secret keys is eliminated
 - All communications involve only public keys
- Examples of public key cryptographic algorithms are:
 - RSA, ElGamal, Rabin

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Public Key Cryptography

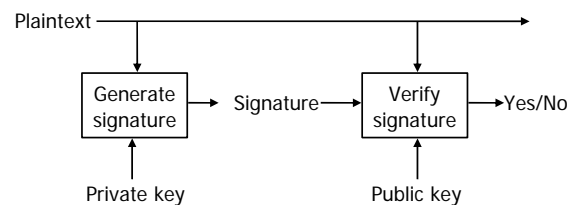
- Each user in a public key system creates his own private key (SK) and his own public key (PK)



- When user Alice wants to send an encrypted message to Bob
 - She looks up his public key (PK_B) in a public directory
 - * Or obtains it by some other means

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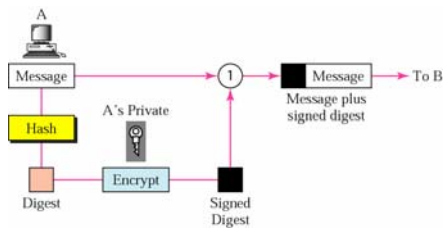
Public Key Integrity Protection



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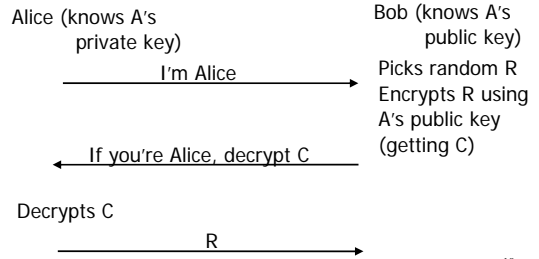
Signatures and Message Digests

- Instead of creating a digital signature on an arbitrarily large document
 - Compute a message digest on the document and then create a digital signature on the digest



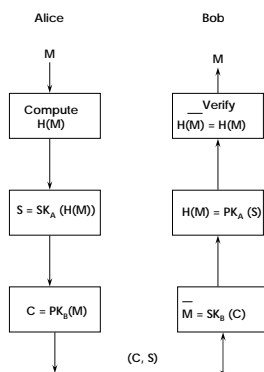
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Public Key Authentication



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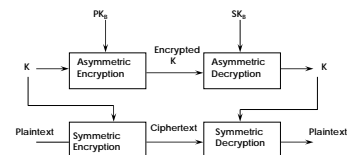
Enveloped and Signed Data



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Hybrid Schemes

- Public key algorithms are not a replacement for secret key algorithms such as AES
 - Rather they supplement AES or any other fast bulk encryption cipher



- The above example shows
 - How we can use a public key algorithm to securely transfer a *session key* (K) and
 - Use the session key for bulk encryption and decryption

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RSA

- Named after its inventors Rivest, Shamir and Adleman who developed it in 1978 while working at MIT
- Algorithm:
 - Randomly choose two different large primes p and q and compute $n = p * q$ (n is known as the *modulus*)
 - Randomly choose an encryption key e such that e and $(p-1) * (q-1)$ are relatively prime
 - To encrypt a message m the sender computes the ciphertext c as $c := m^e \pmod{n}$
 - To decrypt a ciphertext c the receiver computes $c^d \pmod{n}$
 - d is the decryption key: $e * d = 1 \pmod{(p-1) * (q-1)}$
 - The pair (n, e) forms the public key
 - The values (p, q, d) are the private key
- To sign a message m the owner of the private key computes s as $s := m^d \pmod{n}$ the pair (m, s) is now a signed message
- To verify the signature anyone who knows the public key can verify that $s^e = m \pmod{n}$

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RSA Security

- The security of RSA is based on a trapdoor one-way function
- Given the public n and e it is easy to compute $m^e \pmod{n}$ from m but not the other way around
- However, if you know the factorization of n then it is easy to do the inverse computation
- The factorization of n is the trapdoor information
- As with encryption the security of the signature is based on the fact that the e 'th root on m can only be computed by someone who knows the private key
- Just remember that computations of any roots modulo n require knowledge of the private key

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Key Management

- Public key cryptography is based on the idea that
 - An individual will generate a key pair
 - Keep one component secret and publish the other component (public key)
- Other users on the network
 - Must be able to retrieve this public key and associate the user's identity with it
- One way to form this association is
 - To enlist the services of a Trusted Third Party (TTP)

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X.509 Certificates

- The TTP will construct a message referred to as a *certificate*

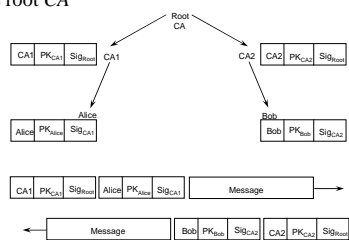
Subject (Identity of User)	Public Key	Validity Period	Issuer (Identity of TTP)	Other fields	Signature of TTP
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- The certificate contains a number of fields
 - Identity of the user
 - Public key of the user
 - Validity period of the certificate
 - Identity of the TTP
 - Miscellaneous fields
 - A digital signature on the above fields with the secret key of the TTP
- It is assumed that every user in the system is equipped with the public key of the TTP
 - This allows one to verify the digital signature on the certificate
 - Thus guaranteeing that the public key is associated with the named user

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Certification Hierarchy

- TTPs that issue certificates are referred to as Certification Authorities (CAs)
- The root CA issues certificates only to other CAs
- Each user of the system need only hold the public key of the root CA



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