

UNIVERSITY OF DUBLIN

TRINITY COLLEGE

Faculty of Engineering and Systems Science
Department of Computer Science

B.A.(Mod.) Computer Science
Senior Freshman Examination

Trinity Term 2001

2BA2 - Programming Techniques

Saturday 26th May

Regent House

14.00 –17.00

Dr. Hugh Gibbons

Attempt **FOUR** questions
(in presenting programs explain clearly the design of the Eiffel code)

Qs 1

- i) Implement an Eiffel function that will find the square root of a number using the technique of binary search.

```

bin_sqrt(low, high, eps, x : REAL) : REAL is
  require
    low^2 <= x and x < high^2
  ensure
    Result^2 <= x and x < (Result + eps)^2

```

- ii) Present an Eiffel routine that will search an array of unordered items. This can be achieved by searching in a linear way from the start of the array.

Assume an array, *a*, has *N* items with bounds such that

a.lower = 0 and *a.upper* = *N*-1.

If the item, *x*, is in the array then the index of the item should be returned, i.e. *x* = *a.item*(*Result*). The item may occur more than once in the array and if so then any index can be returned such that *x* = *a.item*(*Result*). But the item looked for may not occur at all in the array and in this case the index *N* should be returned.

```

linear_search(a:ARRAY[G]; x:G) : INTEGER is
  require
    a /= void
  ensure
    Result = N or else x = a.item(Result)

```

If it is known in advance that the item looked for is somewhere in the array, how would this simplify the *linear_search* program.

- iii) Implement a routine, *is_in*, that checks if an item, *x*, is in the unordered array, *a*.

```

is_in(x : G; a:ARRAY[G]) : BOOLEAN is
  require
    a /= void
  ensure
    — Result = x ∈ a[0 .. n-1]

```

Qs 2

Assume we have an array, *a*, indexed from 1 to *N* with integer values.

- a) Implement a boolean function,

isa_combination(*a*:ARRAY[INTEGER]; *k*, *N*: INTEGER) : BOOLEAN

that will determine if a sub-array indexed from 1 to *k* ($1 \leq k \leq N$) is a combination of *k* numbers from 1 to *N*.

For example:

The sequence of values [4,2,9,5] is a combination of 4 numbers from 1 to 10.

The sequences [0,9,4,6] and [4,7,7,1] are not valid combinations from 1 to 10.

- b) Present an Eiffel class that will provide a routine that will generate all the combinations of choosing *k* numbers from 1 to *N*.

Qs 3

- a) Present an Eiffel class that will provide a routine that will Heapsort an array.

- b) Given an array, present a Boolean function

isa_heap(*a*:ARRAY[STRING]) : BOOLEAN

that will determine if the array, *a*, satisfies the *heap property* that for each index, *k*,

$a.item(k) \geq a.item(2k)$ and $a.item(k) \geq a.item(2k+1)$,

given that these items are within bounds.

Qs 4

Assume we have classes, LIST_BAG and NODE with short forms

class interface LIST_BAG [G]

add(*x* : G)

-- Add *x*, maybe again

count : INTEGER

empty : BOOLEAN

has (*x* : G) : BOOLEAN

remove (*x* : G)

is_equal(*s* : LIST_BAG[G])

end -- class LIST_BAG

class interface NODE[G]

item : G;

next : NODE[G];

set_item(*x* :G)

set_next(*n* : NODE[G])

end -- NODE

Implement the routines in the class, LIST_BAG, using linked nodes. Use linked list diagrams in explaining the routines.

Qs 5

- a) Explain why there is no Knight's tour (cyclic journey) on an $N \times N$ board when N is odd.
- b) If N is odd, it may be possible to find a Knight's tour on an $N \times N$ board if one square is not used. Present an Eiffel class that will provide a routine that will find a Knight's tour, if any, on $N \times N$ board when the bottom right square is not used.
For example: if $N = 7$ and the top left square is $(1,1)$, then the bottom right square at $(7, 7)$ is not used.

Qs 6

Present an Eiffel class that will provide:

- a) A *non-recursive* Eiffel routine using an *explicit stack* that will inorder traverse a binary tree.
- b) A *non-recursive* Eiffel routine *without* using an explicit stack that will inorder traverse a binary tree.