3ba2 Artificial Intelligence

Non-deterministic Turing machines in Prolog

Marks will be awarded for this exercise. Due by Th, Dec 9, 2004 (at lab).[1]

A *non-deterministic Turing machine (nTm) M* is specified by four finite lists, `move-right, move-left, write-list, halt-list` where

- `move-right` is a list of triples `[Q0,X,Q]` saying:

  from state `Q0`, reading symbol `X`, move one square right, and go to state `Q`

- `move-left` is a list of triples `[Q0,X,Q]` saying:

  from state `Q0`, reading symbol `X`, move one square left, and go to state `Q`

- `write-list` is a list of quadruples `[Q0,X,Y,Q]` saying:

  from state `Q0`, reading symbol `X`, write symbol `Y` and go to state `Q` (keeping the head still)

and

- `halt-list` is a list of pairs `[Q0,X]` saying:

  from state `Q0`, reading symbol `X`, halt.

Let us assume that every nTm M has initial state `q0`, and let us write `b-k` for blank (a symbol indicating an empty tape cell). Let us agree that M falls into a loop from which it can never halt, if it should ever be at a state `Q0` reading symbol `X` such that none of its four lists specifies a next step.

Your task is to define a predicate

`nTm(+move-right,+move-left,+write-list,+halt-list,+input,?output)`

such that the nTm specified by `move-right`, `move-left`, `write-list` and `halt-list` may halt with tape content `output`, given tape content `input` (and initial state `q0` with the head at the leftmost symbol of `input`). Let us assume without loss of generality that `input` is a non-empty list, using the list `[b-k]`, if necessary, to represent the empty string. As for the output string, on the other hand, let us arrange that it never begins or ends with a blank (so that for example the list `[b-k]` is rewritten as `[]`, and `[b-k,a,b-k,b,b-k]` as `[a,b-k,b]`).

Hint

Take "snapshots" `[L,R,Q]` of a run of a nTm, where

- `L` lists the non-blank tape contents to the left of the nTm head (in reverse)

- `R` lists the non-blank tape contents to the right of the nTm head, including the currently scanned cell (the head of `R`)

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[1] You are strongly encouraged to have your solution marked before then. Email submissions to Tim Fernando will receive an F3.

- `Q` is the current nTm state.

Search through a graph with nodes `[L,R,Q]`, the children of which arise from a single nTm step.

A query

```
nTm(MR,ML,WL,HL,Input,Output)
```

sets the **start node** (the root of the computation tree) to `[[],Input,q0]`.

Sample runs

```
| ?- nTm([],[],[],[[q0,X]],[b-k,i,n,b-k,p,u,t,b-k,b-k],Out).
X = b-k,
Out = [i,n,b-k,p,u,t] ? ;
no


| ?- nTm([[q1,1,q2],[q1,0,q2],[q1,b-k,q2]],[],
          [[q0,0,1,q1], [q2,0,b-k,q1]],
          [[q1,b-k]],
          [0,0,0,0,0],
          Out).
Out = [1,b-k,0,0,0] ? ;
Out = [1,b-k,b-k,0,0] ? ;
Out = [1,b-k,b-k,b-k,0] ? ;
Out = [1] ? ;
no


| ?- nTm([[mr1,h,we],[mr1,e,wl],[mr1,l,wp],[mr1,p,hbk],
           [mr,l,wo],[mr,o,wo],[mp,o,wp]],
          [[q0,0,lbk],[lbk,b-k,lbk]],
          [[q0,0,h,mr1],[we,1,e,mr1],[wl,0,l,mr1],[wp,1,p,mr1],
           [q0,0,l,mr],[wo,1,o,mr],[wo,0,o,mp]],
          [[hbk,b-k]],
          [0,1,0,1],
          Output).
Output = [h,e,l,p] ? ;
Output = [l,o,o,p] ? ;

<loops>
```