

Pytorch and Titanic: Connecting the Math to Coding

Now that you've seen the very basics of how to use `pytorch`, we're going to see how to apply it to a machine learning problem. Along the way we'll make connections back to the Titanic dataset and help solidify your understanding of the connection between the math we've been learning and the code we'll be writing using `pytorch`.

To get started, let's load our trusty Titanic dataset.

In [1]:

```
import gdown
import numpy as np
import pandas as pd
```

```
gdown.download('https://drive.google.com/uc?authuser=0&id=1XIFiL3WxxR6M2nWgADi3xWvuRO6A-Ov8&export=download', 'titanic_train.csv', False)
df = pd.read_csv('titanic_train.csv')
df
```

```
Downloading...
From: https://drive.google.com/uc?authuser=0&id=1XIFiL3WxxR6M2nWgADi3xWvuRO6A-Ov8&export=download
To: /Users/pruvolo/Documents/assignments/Module 1/07/titanic_train.csv
100%|██████████| 61.2k/61.2k [00:00<00:00, 1.95MB/s]
```

Out[1]:

| | PassengerId | Survived | Pclass | Name | Sex | Age | SibSp | Parch | Ticket | Fare | Cabin | Embarked |
|----|-------------|----------|--------|--|--------|------|-------|-------|---------------------|---------|-------|----------|
| 0 | 1 | 0 | 3 | Braund, Mr. Owen Harris | male | 22.0 | 1 | 0 | A/5 21171 | 7.2500 | NaN | S |
| 1 | 2 | 1 | 1 | Cumings, Mrs. John Bradley (Florence Briggs Th... | female | 38.0 | 1 | 0 | PC 17599 | 71.2833 | C85 | C |
| 2 | 3 | 1 | 3 | Heikkinen, Miss. Laina | female | 26.0 | 0 | 0 | STON/O2. 3101282 | 7.9250 | NaN | S |
| 3 | 4 | 1 | 1 | Futrelle, Mrs. Jacques Heath (Lily May Peel) | female | 35.0 | 1 | 0 | 113803 | 53.1000 | C123 | S |
| 4 | 5 | 0 | 3 | Allen, Mr. William Henry | male | 35.0 | 0 | 0 | 373450 | 8.0500 | NaN | S |
| 5 | 6 | 0 | 3 | Moran, Mr. James | male | NaN | 0 | 0 | 330877 | 8.4583 | NaN | Q |
| 6 | 7 | 0 | 1 | McCarthy, Mr. Timothy J | male | 54.0 | 0 | 0 | 17463 | 51.8625 | E46 | S |
| 7 | 8 | 0 | 3 | Palsson, Master. Gosta Leonard | male | 2.0 | 3 | 1 | 349909 | 21.0750 | NaN | S |
| 8 | 9 | 1 | 3 | Johnson, Mrs. Oscar W (Elisabeth Vilhelmina Berg) | female | 27.0 | 0 | 2 | 347742 | 11.1333 | NaN | S |
| 9 | 10 | 1 | 2 | Nasser, Mrs. Nicholas (Adele Achem) | female | 14.0 | 1 | 0 | 237736 | 30.0708 | NaN | C |
| 10 | 11 | 1 | 3 | Sandstrom, Miss. Marguerite Rut | female | 4.0 | 1 | 1 | PP 9549 | 16.7000 | G6 | S |
| 11 | 12 | 1 | 1 | Bonnell, Miss. Elizabeth | female | 58.0 | 0 | 0 | 113783 | 26.5500 | C103 | S |
| 12 | 13 | 0 | 3 | Saunderscock, Mr. William Henry | male | 20.0 | 0 | 0 | A/5. 2151 | 8.0500 | NaN | S |
| 13 | 14 | 0 | 3 | Andersson, Mr. Anders Johan | male | 39.0 | 1 | 5 | 347082 | 31.2750 | NaN | S |
| 14 | 15 | 0 | 3 | Vestrom, Miss. Hulda Amanda Adolfina | female | 14.0 | 0 | 0 | 350406 | 7.8542 | NaN | S |
| 15 | 16 | 1 | 2 | Hewlett, Mrs. (Mary D Kingcome) | female | 55.0 | 0 | 0 | 248706 | 16.0000 | NaN | S |
| 16 | 17 | 0 | 3 | Rice, Master. Eugene | male | 2.0 | 4 | 1 | 382652 | 29.1250 | NaN | Q |
| 17 | 18 | 1 | 2 | Williams, Mr. Charles Eugene | male | NaN | 0 | 0 | 244373 | 13.0000 | NaN | S |
| 18 | 19 | 0 | 3 | Vander Planke, Mrs. Julius | female | 31.0 | 1 | 0 | 345763 | 18.0000 | NaN | S |

| PassengerId | Survived | Pclass | Name | Sex | Age | SibSp | Parch | Ticket | Fare | Cabin | Embarked |
|-------------|----------|--------|---|--------|------|-------|-------|---------------------|----------|-------------------|----------|
| 19 | 0 | 3 | (Emelia Maria Vande... Masseimani, Mrs. Fatima | female | NaN | 0 | 0 | 2649 | 7.2250 | NaN | C |
| 20 | 0 | 2 | Fynney, Mr. Joseph J | male | 35.0 | 0 | 0 | 239865 | 26.0000 | NaN | S |
| 21 | 1 | 2 | Beesley, Mr. Lawrence | male | 34.0 | 0 | 0 | 248698 | 13.0000 | D56 | S |
| 22 | 1 | 3 | McGowan, Miss. Anna "Annie" | female | 15.0 | 0 | 0 | 330923 | 8.0292 | NaN | Q |
| 23 | 1 | 1 | Sloper, Mr. William Thompson | male | 28.0 | 0 | 0 | 113788 | 35.5000 | A6 | S |
| 24 | 0 | 3 | Palsson, Miss. Torborg Danira | female | 8.0 | 3 | 1 | 349909 | 21.0750 | NaN | S |
| 25 | 1 | 3 | Asplund, Mrs. Carl Oscar (Selma Augusta Emilia...) | female | 38.0 | 1 | 5 | 347077 | 31.3875 | NaN | S |
| 26 | 0 | 3 | Emir, Mr. Farred Chehab | male | NaN | 0 | 0 | 2631 | 7.2250 | NaN | C |
| 27 | 0 | 1 | Fortune, Mr. Charles Alexander | male | 19.0 | 3 | 2 | 19950 | 263.0000 | C23 C25 C27 | S |
| 28 | 1 | 3 | O'Dwyer, Miss. Ellen "Nellie" | female | NaN | 0 | 0 | 330959 | 7.8792 | NaN | Q |
| 29 | 0 | 3 | Todoroff, Mr. Lalio | male | NaN | 0 | 0 | 349216 | 7.8958 | NaN | S |
| ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... |
| 861 | 0 | 2 | Giles, Mr. Frederick Edward | male | 21.0 | 1 | 0 | 28134 | 11.5000 | NaN | S |
| 862 | 1 | 1 | Swift, Mrs. Frederick Joel (Margaret Welles Ba...) | female | 48.0 | 0 | 0 | 17466 | 25.9292 | D17 | S |
| 863 | 0 | 3 | Sage, Miss. Dorothy Edith "Dolly" | female | NaN | 8 | 2 | CA. 2343 | 69.5500 | NaN | S |
| 864 | 0 | 2 | Gill, Mr. John William | male | 24.0 | 0 | 0 | 233866 | 13.0000 | NaN | S |
| 865 | 1 | 2 | Bystrom, Mrs. (Karolina) | female | 42.0 | 0 | 0 | 236852 | 13.0000 | NaN | S |
| 866 | 1 | 2 | Duran y More, Miss. Asuncion | female | 27.0 | 1 | 0 | SC/PARIS 2149 | 13.8583 | NaN | C |
| 867 | 0 | 1 | Roebing, Mr. Washington Augustus II | male | 31.0 | 0 | 0 | PC 17590 | 50.4958 | A24 | S |
| 868 | 0 | 3 | van Melkebeke, Mr. Philemon | male | NaN | 0 | 0 | 345777 | 9.5000 | NaN | S |
| 869 | 1 | 3 | Johnson, Master. Harold Theodor | male | 4.0 | 1 | 1 | 347742 | 11.1333 | NaN | S |
| 870 | 0 | 3 | Balkic, Mr. Cerin | male | 26.0 | 0 | 0 | 349248 | 7.8958 | NaN | S |
| 871 | 1 | 1 | Beckwith, Mrs. Richard Leonard (Sallie Monypeny) | female | 47.0 | 1 | 1 | 11751 | 52.5542 | D35 | S |
| 872 | 0 | 1 | Carlsson, Mr. Frans Olof | male | 33.0 | 0 | 0 | 695 | 5.0000 | B51 B53 B55 | S |
| 873 | 0 | 3 | Vander Cruyssen, Mr. Victor | male | 47.0 | 0 | 0 | 345765 | 9.0000 | NaN | S |
| 874 | 1 | 2 | Abelson, Mrs. Samuel (Hannah Wizosky) | female | 28.0 | 1 | 0 | P/PP 3381 | 24.0000 | NaN | C |
| 875 | 1 | 3 | Najib, Miss. Adele Kiamie "Jane" | female | 15.0 | 0 | 0 | 2667 | 7.2250 | NaN | C |
| 876 | 0 | 3 | Gustafsson, Mr. Alfred Ossian | male | 20.0 | 0 | 0 | 7534 | 9.8458 | NaN | S |
| 877 | 0 | 3 | Petroff, Mr. Nedelio | male | 19.0 | 0 | 0 | 349212 | 7.8958 | NaN | S |
| 878 | 0 | 3 | Laleff, Mr. Kristo | male | NaN | 0 | 0 | 349217 | 7.8958 | NaN | S |
| 879 | 1 | 1 | Potter, Mrs. Thomas Jr (Lily Alexenia Wilson) | female | 56.0 | 0 | 1 | 11767 | 83.1583 | C50 | C |
| 880 | 1 | 2 | Shelley, Mrs. William (Imanita Parrish Hall) | female | 25.0 | 0 | 1 | 230433 | 26.0000 | NaN | S |
| 881 | 0 | 3 | Markun, Mr. Johann | male | 33.0 | 0 | 0 | 349257 | 7.8958 | NaN | S |
| 882 | 0 | 3 | Dahlberg, Miss. Gerda Ulrika | female | 22.0 | 0 | 0 | 7552 | 10.5167 | NaN | S |
| 883 | 0 | 2 | Banfield, Mr. Frederick James | male | 28.0 | 0 | 0 | C.A./SOTON 34068 | 10.5000 | NaN | S |
| 884 | 0 | 3 | Sutehall, Mr. Henry Jr | male | 25.0 | 0 | 0 | SOTON/OQ 392076 | 7.0500 | NaN | S |
| 885 | 0 | 3 | Rice, Mrs. William (Margaret Norton) | female | 39.0 | 0 | 5 | 382652 | 29.1250 | NaN | Q |

| PassengerId | Survived | Pclass | Name | Sex | Age | SibSp | Parch | Ticket | Fare | Cabin | Embarked |
|-------------|----------|--------|--|--------|------|-------|-------|------------|---------|-------|----------|
| 886 | 0 | 2 | Montvila, Rev. Juozas | male | 27.0 | 0 | 0 | 211536 | 13.0000 | NaN | S |
| 887 | 1 | 1 | Graham, Miss. Margaret Edith | female | 19.0 | 0 | 0 | 112053 | 30.0000 | B42 | S |
| 888 | 0 | 3 | Johnston, Miss. Catherine Helen "Carrie" | female | NaN | 1 | 2 | W./C. 6607 | 23.4500 | NaN | S |
| 889 | 1 | 1 | Behr, Mr. Karl Howell | male | 26.0 | 0 | 0 | 111369 | 30.0000 | C148 | C |
| 890 | 0 | 3 | Dooley, Mr. Patrick | male | 32.0 | 0 | 0 | 370376 | 7.7500 | NaN | Q |

891 rows × 12 columns

In the Assignment 6 companion notebook we fit two models:

1. We used the `Age` and `Sex` columns along with a synthetic feature called `is_young_male` as inputs to a logistic regression model in order to predict whether someone survived.
2. We used just the `Age` and `Sex` as inputs to a multilayer perceptron model in order to predict whether someone survived.

In this notebook we'll be implementing both of these models in `pytorch`. To get started, let's perform the following data processing / cleaning steps.

1. Get rid of any passengers where we don't know their age (don't do this in a real machine learning application as it will skew your results).
2. Convert the `Sex` column to a dummy variable called `male` that will take on value 1 if the passenger is male and 0 otherwise.
3. Create the `is_young_male` column that will be 1 for males under the age of 5 and 0 for everyone else.

In [2]:

```
# get rid of null values for age since this is just an illustrative example.
# this would not be a good thing to do if we were trying to evaluate the
# performance of a model.
df_filtered = df[['Age', 'Sex', 'Survived']].dropna()
is_young_male = ((df_filtered['Sex'] == 'male') & (df_filtered['Age'] < 5)).astype(int)
is_young_male.name = 'is_young_male'
experiment_1_data = pd.concat((pd.get_dummies(df_filtered['Sex'], drop_first=True),
df_filtered['Age'], is_young_male), axis=1)
experiment_1_outputs = df_filtered['Survived']
experiment_1_data
```

Out[2]:

| | male | Age | is_young_male |
|----|------|------|---------------|
| 0 | 1 | 22.0 | 0 |
| 1 | 0 | 38.0 | 0 |
| 2 | 0 | 26.0 | 0 |
| 3 | 0 | 35.0 | 0 |
| 4 | 1 | 35.0 | 0 |
| 6 | 1 | 54.0 | 0 |
| 7 | 1 | 2.0 | 1 |
| 8 | 0 | 27.0 | 0 |
| 9 | 0 | 14.0 | 0 |
| 10 | 0 | 4.0 | 0 |
| 11 | 0 | 58.0 | 0 |
| 12 | 1 | 20.0 | 0 |
| 13 | 1 | 39.0 | 0 |
| 14 | 0 | 14.0 | 0 |
| 15 | 0 | 55.0 | 0 |
| 16 | 1 | 2.0 | 1 |
| 18 | 0 | 31.0 | 0 |
| 20 | 1 | 35.0 | 0 |

| 21 | 1 | 34.0 | 0 |
|------|-----|---------------|-----|
| male | Age | is_young_male | |
| 22 | 0 | 15.0 | 0 |
| 23 | 1 | 28.0 | 0 |
| 24 | 0 | 8.0 | 0 |
| 25 | 0 | 38.0 | 0 |
| 27 | 1 | 19.0 | 0 |
| 30 | 1 | 40.0 | 0 |
| 33 | 1 | 66.0 | 0 |
| 34 | 1 | 28.0 | 0 |
| 35 | 1 | 42.0 | 0 |
| 37 | 1 | 21.0 | 0 |
| 38 | 0 | 18.0 | 0 |
| ... | ... | ... | ... |
| 856 | 0 | 45.0 | 0 |
| 857 | 1 | 51.0 | 0 |
| 858 | 0 | 24.0 | 0 |
| 860 | 1 | 41.0 | 0 |
| 861 | 1 | 21.0 | 0 |
| 862 | 0 | 48.0 | 0 |
| 864 | 1 | 24.0 | 0 |
| 865 | 0 | 42.0 | 0 |
| 866 | 0 | 27.0 | 0 |
| 867 | 1 | 31.0 | 0 |
| 869 | 1 | 4.0 | 1 |
| 870 | 1 | 26.0 | 0 |
| 871 | 0 | 47.0 | 0 |
| 872 | 1 | 33.0 | 0 |
| 873 | 1 | 47.0 | 0 |
| 874 | 0 | 28.0 | 0 |
| 875 | 0 | 15.0 | 0 |
| 876 | 1 | 20.0 | 0 |
| 877 | 1 | 19.0 | 0 |
| 879 | 0 | 56.0 | 0 |
| 880 | 0 | 25.0 | 0 |
| 881 | 1 | 33.0 | 0 |
| 882 | 0 | 22.0 | 0 |
| 883 | 1 | 28.0 | 0 |
| 884 | 1 | 25.0 | 0 |
| 885 | 0 | 39.0 | 0 |
| 886 | 1 | 27.0 | 0 |
| 887 | 0 | 19.0 | 0 |
| 889 | 1 | 26.0 | 0 |
| 890 | 1 | 32.0 | 0 |

714 rows × 3 columns

Next, we'll go ahead and build our logistic regression model just as we did in the assignment 6 companion notebook. The only small twist we will introduce is turning off the ridge term of the model so that it will make comparing the results from this analysis to what we do in pytorch easier.

In [3]:

```
from sklearn.linear_model import LogisticRegression

model = LogisticRegression(solver='lbfgs', penalty='none') # setting solve silences annoying
warning
model.fit(experiment_1_data, experiment_1_outputs)
print("coefs", model.coef_)
print("intercept", model.intercept_)

coefs [[-2.67342472  0.00808732  2.38307187]]
intercept [0.9018627]
```

Notebook Exercise 1 (10 minutes)

This is a bit of review. Provide an interpretation for the coefficients learned by the logistic regression model (e.g., what do they mean for the prediction of whether a passenger would survive).

Solution

TODO

Reimplementation in Pytorch

Next, we'll be using `pytorch` to implement our own version of logistic regression! When creating a neural network model (remember, we can think of logistic regression as a perceptron with 2 layers, an input and an output), you create a class that inherits from `nn.Module`. We'll give you an implementation of logistic regression and then give a detailed breakdown of the key lines.

In [4]:

```
from torch import nn
import torch
from torch.autograd import Variable

class LogisticRegressionPytorch(nn.Module):
    def __init__(self):
        super(LogisticRegressionPytorch, self).__init__()
        self.linear = nn.Linear(3,1)

    def forward(self, X):
        """ Propagate data through the network.

        This model first applies the linear layer and then a sigmoid
        """
        X = self.linear(X)
        return torch.sigmoid(X)
```

Here is a breakdown of some of the key lines in this implementation.

Inherit from the super class `nn.Module`:

```
class LogisticRegressionPytorch(nn.Module):
```

Since we're inheriting from `nn.Module`, we need to make sure to call the `__init__` method of `nn.Module` when initializing our class.

```
super(LogisticRegressionPytorch, self).__init__()
```

The linear layer will store the weight vector of our model. The `3` arises from the fact that our model will have 3 inputs (age, male, and is young male). It is very important that you store your layers as attributes of your class. This is how `pytorch` knows about them and can optimize them. If you need to have a list of layers, look into `nn.ModuleList`.

```
self.linear = nn.Linear(3,1)
```

The `forward` function is the heart of the model. It runs input data through the network and returns the output. Writing such functions usually amounts to passing data between the various layers that were created in the `__init__` method. The syntax for this is a little funny. For instance, in the code below, `self.linear(X)` implicitly calls the `forward` function of the `nn.Linear` class. Yes, we find this kind of weird, but that's how it's done in `pytorch`. This is really just a syntactic quirk rather than anything

substantive that you need to worry about. The last step of the function involves applying the `sigmoid` and returning the result.

Next, we'll show how to pass some data into the model.

```
def forward(self, X):
    """ Propagate data through the network.

    This model first applies the linear layer and then a sigmoid
    """
    X = self.linear(X)
    return torch.sigmoid(X)
```

In [5]:

```
# sample_data represents a male passenger who is 10 years old
sample_data = Variable(torch.FloatTensor([1.0, 10.0, 0.0]))
model_pytorch = LogisticRegressionPytorch()
model_pytorch(sample_data)
```

Out[5]:

```
tensor([0.1327], grad_fn=<SigmoidBackward>)
```

The code we computed the probability that the specific passenger would survive. It is very important to realize that right now the model *has not been trained*. This means that we don't expect the output of the model to make any sense (although it might just by chance). If you rerun the code repeatedly, you'll get different results due to the fact that the weights are initialized randomly.

Next, we're going to actually train the network! This is where things get interesting. We'll have you run the code and then point out a couple of key components.

In [6]:

```
model_pytorch = LogisticRegressionPytorch()
model_pytorch.train()
optimizer = torch.optim.SGD(model_pytorch.parameters(), lr=0.01)
criterion = torch.nn.BCELoss()
grad_magnitudes = []

X_data = Variable(torch.Tensor(np.array(experiment_1_data)))
y_data = Variable(torch.Tensor(np.array(experiment_1_outputs)))
for epoch in range(2000):
    optimizer.zero_grad()
    # Forward pass
    y_pred = model_pytorch(X_data)
    # Compute Loss
    loss = criterion(y_pred, y_data)
    # Backward pass
    loss.backward()
    for name, param in model_pytorch.named_parameters():
        if name == 'linear.weight':
            grad_magnitudes.append(np.abs(param.grad.numpy()).mean())

    if epoch % 1000 == 0:
        print("epoch", epoch)
        for name, param in model_pytorch.named_parameters():
            print(name, "value", param.data, "gradient", param.grad)
    optimizer.step()

import matplotlib.pyplot as plt
%matplotlib inline
plt.plot(grad_magnitudes)
plt.xlabel('epoch')
plt.ylabel('average magnitude of weight gradient')
plt.show()
```

```
epoch 0
linear.weight value tensor([[ -0.0938,  0.0594, -0.3953]]) gradient tensor([[ 4.0462e-01,
 1.4941e+01, -6.0478e-03]])
linear.bias value tensor([0.2207]) gradient tensor([0.4358])
```

/anaconda3/lib/python3.6/site-packages/torch/nn/functional.py:2016: UserWarning: Using a target size (torch.Size([714])) that is different to the input size (torch.Size([714, 1])) is deprecated

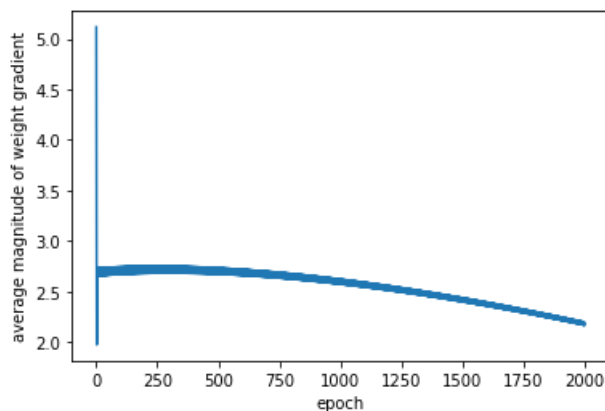
```
ze(torch.Size([14])) that is different to the input size (torch.Size([14, 1])) is deprecated. Please ensure they have the same size.
```

```
"Please ensure they have the same size.".format(target.size(), input.size()))
```

epoch 1000

```
linear.weight value tensor([[ -1.0277,  0.0269, -0.2915]]) gradient tensor([[ 0.2052,  7.6471, -0.0119]])
```

```
linear.bias value tensor([0.3365]) gradient tensor([0.2003])
```



Put the model into training mode (this only affects certain models that behave differently during training and testing). Even though it doesn't affect our logistic regression model, calling the `.train` function is a good habit to get into.

```
model_pytorch.train()
```

Create an optimizer that will tune the parameters of the network. Here we are using an algorithm called *stochastic gradient descent*. It's a very popular choice for an optimizer. Similarly to gradient descent it optimizes a function by stepping down the gradient (step size is given by learning rate or `lr`). Where it differs from normal gradient descent is that it doesn't necessarily use all of the data to compute the gradient. If you have a big dataset, it might only use a small number of data points, compute gradient over those, and then step down that estimate of the gradient. The collection of datapoints used for estimating the gradient is called a *mini batch*. In this example we are using the entire dataset each time, so we are really doing normal gradient descent.

```
optimizer = torch.optim.SGD(model_pytorch.parameters(), lr=0.01)
```

The criterion defines the loss function we are minimizing. When the training outputs are binary, the `BCELoss` function is equivalent to the log loss that we have been using in this course.

```
criterion = torch.nn.BCELoss()
```

In order to operate on data in pytorch, you have to convert any matrix or vector data into a pytorch variable. This should be familiar based on the tutorial you went through earlier.

```
X_data = Variable(torch.Tensor(np.array(experiment_1_data)))
y_data = Variable(torch.Tensor(np.array(experiment_1_outputs)))
```

An *epoch* in neural network training is a single pass through the data. In this case we are taking a single gradient step on the whole dataset, so the number of epochs is the same as the number of gradient steps.

```
for epoch in range(200):
```

This tells the optimizer to throw away any gradients it has accumulated from previous data (do not forget to call this!!!).

```
optimizer.zero_grad()
```

Apply the forward model to get predictions.

```
y_pred = model_pytorch(X_data)
```

Calculate the loss of the model by comparing its predictions with the actual outputs.

```
loss = criterion(y_pred, y_data)
```

Use backpropagation to compute the gradient of all of the model parameters with respect to the loss.

```
loss.backward()
```

Calculate the gradient magnitudes so we can make a plot after training.

```
for name, param in model_pytorch.named_parameters():
    if name == 'linear.weight':
        grad_magnitudes.append(np.abs(param.grad.numpy()).mean())
```

Print out the values of the parameters and the gradient of the parameters with respect to the loss every 50 epochs.

```
if epoch % 50 == 0:
    print("epoch", epoch)
    for name, param in model_pytorch.named_parameters():
        print(name, "value", param.data, "gradient", param.grad)
```

Perform the gradient step.

```
optimizer.step()
```

Notebook Exercise 2 (30 minutes)

(a) Explain the output you see when you run the previous code cell. How are the weights changing over time? How is the gradient changing over time? Is the algorithm close to converging (i.e., computing the optimal solution)? How would you know if it has converged?

(b) Increase the number of epochs until you get convergence. How many did it take?

(c) Tune the learning rate to some other values. How does this change the algorithm's behavior?

(d) Change the optimizer to the ADAM optimizer by swapping out the previous optimizer with this new line of code.

```
optimizer = torch.optim.Adam(model_pytorch.parameters())
```

Roughly many epochs does it take to reach convergence now?

Solution

TODO

Multilayer Perceptron

Now that we've shown you how to implement the logistic regression model, we want you to implement the MLP model from the previous companion notebook. Remember, the MLP had 2 input features (we didn't use `is young male` as an input) and 2 hidden units. We'll provide you with the skeleton of the code as well as some code to generate the visualization from the previous notebook.

In [7]:

```
# start from this and modify it
class LogisticRegressionPytorch(nn.Module):
    def __init__(self):
        super(LogisticRegressionPytorch, self).__init__()
        self.linear = nn.Linear(3,1)

    def forward(self, X):
        """ Propagate data through the network.

        This model first applies the linear layer and then a sigmoid
        """
        X = self.linear(X)
        return torch.sigmoid(X)
```

Notebook Exercise 3 (20 minutes + 20 minutes of optional work)

Non-optional: modify the code above regression class to create a class called TitanicMLP that has 2 input units and 2 hidden units. Train your network on the Titanic dataset. We have defined a function called `visualize_model_probs` for visualizing the probability plot that we saw in the last companion notebook (this code should be run after the model is done training).

Optional: visualize the hidden unit representations in the network (similar to what we did in the companion notebook last time).

In [8]:

```
def visualize_model_probs(model):
    xx, yy = np.mgrid[-.1:1.1:.01, 0:85:.1]
    grid = np.c_[xx.ravel(), yy.ravel()]
    probs = model(Variable(torch.Tensor(grid))).detach().numpy().reshape(xx.shape)

    f, ax = plt.subplots(figsize=(8, 6))
    contour = ax.contourf(xx, yy, probs, 25, cmap="RdBu",
                          vmin=0, vmax=1)
    ax_c = f.colorbar(contour)
    ax_c.set_label("$P(\text{survived})$")
    ax_c.set_ticks([0, .25, .5, .75, 1])

    ax.scatter(experiment_1_data['male'], experiment_1_data['Age'], c=experiment_1_outputs, s=50,
               cmap="RdBu", vmin=-.2, vmax=1.2,
               edgecolor="white", linewidth=1)

    ax.set(xlim=(-.1, 1.1),
           ylim=(0, 85),
           xlabel="is male", ylabel="age (years)")
    plt.show()
```

In [9]:

```
class TitanicMLP(nn.Module):
    def __init__(self):
        super(TitanicMLP, self).__init__()
        self.linear_1 = nn.Linear(2,2)
        self.linear_2 = nn.Linear(2,1)

    def forward(self, X):
        """ Propagate data through the network.

        This model first applies the linear layer, a sigmoid, a linear
        layer, and finally a sigmoid
        """
        X = self.linear_1(X)
        X = torch.sigmoid(X)
        X = self.linear_2(X)
        return torch.sigmoid(X)

    def hidden(self, X):
        """ Propagate data to the hidden layer """
        X = self.linear_1(X)
        return torch.sigmoid(X)
```

In [10]:

```
mlp_pytorch = TitanicMLP()
mlp_pytorch.train()
optimizer = torch.optim.Adam(mlp_pytorch.parameters())
criterion = torch.nn.BCELoss()
grad_magnitudes = []

X_data = Variable(torch.Tensor(np.array(experiment_1_data.drop('is_young_male',axis=1))))
y_data = Variable(torch.Tensor(np.array(experiment_1_outputs)))
for epoch in range(20000):
    optimizer.zero_grad()
    # Forward pass
    y_pred = mlp_pytorch(X_data)
    # Compute Loss
    loss = criterion(y_pred, y_data)
    # Backward pass
    loss.backward()
    for name, param in mlp_pytorch.named_parameters():
        if name == 'linear_1.weight':
            grad_magnitudes.append(np.abs(param.grad.numpy()).mean())

    if epoch % 1000 == 0:
        print("epoch", epoch)
        for name, param in mlp_pytorch.named_parameters():
            print(name, "value", param.data, "gradient", param.grad)
```

```
optimizer.step()
```

```
plt.plot(grad_magnitudes)
plt.show()
visualize_model_probs(mlp_pytorch)
```

/anaconda3/lib/python3.6/site-packages/torch/nn/functional.py:2016: UserWarning: Using a target size (torch.Size([714])) that is different to the input size (torch.Size([714, 1])) is deprecated. Please ensure they have the same size.

"Please ensure they have the same size.".format(target.size(), input.size()))

epoch 0

```
linear_1.weight value tensor([[ -0.4145, -0.1487],
                               [ 0.3383, -0.7046]]) gradient tensor([[ 0.0008, 0.0138],
                               [ 0.0002, 0.0002]])
```

```
linear_1.bias value tensor([-0.6556, 0.2074]) gradient tensor([0.0004, 0.0003])
linear_2.weight value tensor([[ 0.4555, -0.3204]]) gradient tensor([[ 0.0005, -0.0018]])
linear_2.bias value tensor([0.3661]) gradient tensor([0.1860])
```

epoch 1000

```
linear_1.weight value tensor([[ -0.6188, -0.1849],
                               [ 0.3082, -0.4217]]) gradient tensor([[ 2.5671e-03, -5.5381e-03],
                               [ 4.8384e-05, 2.5244e-04]])
linear_1.bias value tensor([0.5433, 0.6822]) gradient tensor([-0.0007, -0.0001])
linear_2.weight value tensor([[1.5560, 0.5713]]) gradient tensor([[ -0.0009, -0.0007]])
linear_2.bias value tensor([-0.3138]) gradient tensor([0.0379])
```

epoch 2000

```
linear_1.weight value tensor([[ -2.5023, 0.0119],
                               [ 1.6938, -0.5345]]) gradient tensor([[ 2.2455e-02, -1.9559e-05],
                               [-2.7376e-04, -6.3526e-06]])
linear_1.bias value tensor([-0.0939, 1.2680]) gradient tensor([-0.0004, 0.0002])
linear_2.weight value tensor([[3.2187, 1.5250]]) gradient tensor([[ -0.0092, -0.0010]])
linear_2.bias value tensor([-1.1204]) gradient tensor([0.0476])
```

epoch 3000

```
linear_1.weight value tensor([[ -3.1408, 0.0183],
                               [ 3.0238, -0.4498]]) gradient tensor([[ 7.2571e-03, 7.5334e-05],
                               [-2.9166e-04, -4.2530e-06]])
linear_1.bias value tensor([ 0.0436, -0.0271]) gradient tensor([-2.3927e-05, 2.9244e-04])
linear_2.weight value tensor([[4.0564, 2.2484]]) gradient tensor([[ -0.0037, -0.0006]])
linear_2.bias value tensor([-1.5950]) gradient tensor([0.0156])
```

epoch 4000

```
linear_1.weight value tensor([[ -3.4029, 0.0210],
                               [ 3.7194, -0.4131]]) gradient tensor([[ 1.5320e-03, -2.8388e-05],
                               [-1.0350e-04, -7.7651e-07]])
linear_1.bias value tensor([ 0.0461, -0.7248]) gradient tensor([6.8642e-06, 1.0096e-04])
linear_2.weight value tensor([[4.4297, 2.6086]]) gradient tensor([[ -0.0009, -0.0001]])
linear_2.bias value tensor([-1.7965]) gradient tensor([0.0029])
```

epoch 5000

```
linear_1.weight value tensor([[ -3.4792, 0.0210],
                               [ 4.0459, -0.4076]]) gradient tensor([[ 2.3661e-04, -5.1948e-05],
                               [-3.3050e-05, 1.5887e-08]])
linear_1.bias value tensor([ 0.0203, -1.0133]) gradient tensor([1.0550e-05, 2.1519e-05])
linear_2.weight value tensor([[4.5712, 2.6741]]) gradient tensor([[ -2.4139e-04, 3.7370e-06]])
linear_2.bias value tensor([-1.8332]) gradient tensor([-7.5017e-05])
```

epoch 6000

```
linear_1.weight value tensor([[ -3.5063, 0.0204],
                               [ 4.2207, -0.4152]]) gradient tensor([[ 9.8733e-05, -2.3553e-04],
                               [-1.1252e-05, -2.6655e-07]])
linear_1.bias value tensor([-0.0251, -1.0812]) gradient tensor([3.2779e-06, 4.7078e-07])
linear_2.weight value tensor([[4.6558, 2.6409]]) gradient tensor([[ -1.3632e-04, 1.0659e-05]])
linear_2.bias value tensor([-1.8185]) gradient tensor([-0.0002])
```

epoch 7000

```
linear_1.weight value tensor([[ -3.5322, 0.0200],
                               [ 4.3046, -0.4229]]) gradient tensor([[ 6.5952e-05, 3.6335e-05],
                               [-2.2271e-06, 1.1456e-07]])
linear_1.bias value tensor([-0.0779, -1.0685]) gradient tensor([ 8.0868e-06, -9.9563e-07])
linear_2.weight value tensor([[4.7426, 2.6048]]) gradient tensor([[ -8.4636e-05, 3.9071e-06]])
linear_2.bias value tensor([-1.7997]) gradient tensor([-0.0001])
```

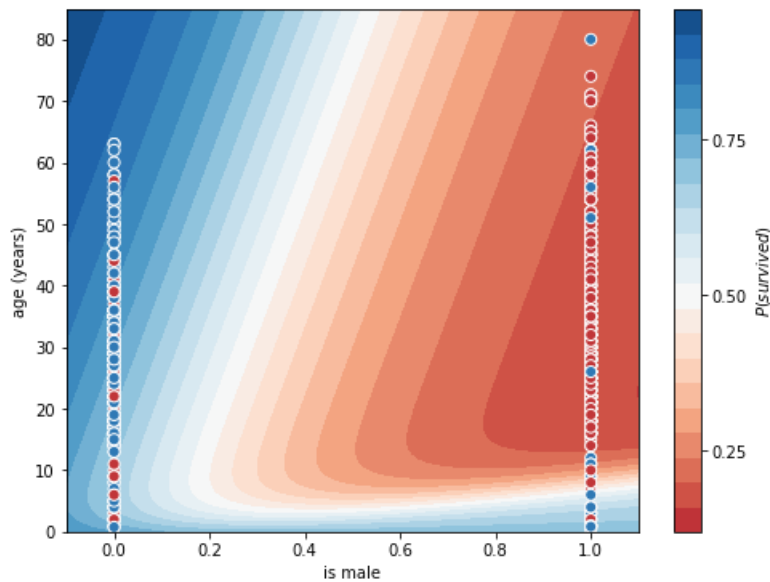
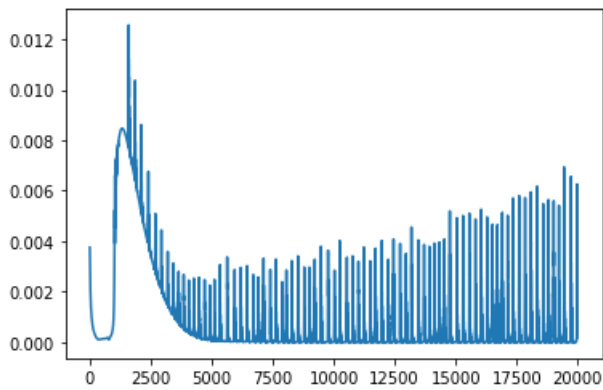
epoch 8000

```
linear_1.weight value tensor([[ -3.5590, 0.0196],
                               [ 4.3146, -0.4257]]) gradient tensor([[ 3.7913e-05, -3.9865e-05],
                               [ 4.4981e-07, -9.3525e-08]])
linear_1.bias value tensor([-0.1290, -1.0528]) gradient tensor([ 3.3678e-06, -3.7719e-07])
linear_2.weight value tensor([[4.8315, 2.5885]]) gradient tensor([[ -5.1868e-05, 7.6236e-07]])
linear_2.bias value tensor([-1.7829]) gradient tensor([-6.2459e-05])
```

epoch 9000

```
linear_1.weight value tensor([[ -3.5817, 0.0191],
```

```
linear_1.weight value tensor([[ -5.5017,  0.0171],
 [ 4.2947, -0.4257]]) gradient tensor([[ 6.4422e-06, -5.0363e-03],
 [-5.9151e-07, -1.2816e-05]])
linear_1.bias value tensor([-0.1732, -1.0448]) gradient tensor([-1.5123e-04, -1.5579e-06])
linear_2.weight value tensor([[4.9158, 2.5835]]) gradient tensor([[ -1.0626e-04, -9.5961e-07]])
linear_2.bias value tensor([-1.7695]) gradient tensor([-0.0002])
epoch 10000
linear_1.weight value tensor([[ -3.5938,  0.0189],
 [ 4.2800, -0.4254]]) gradient tensor([[ 2.1533e-06, -4.3441e-05],
 [ 1.0192e-07, -1.1148e-07]])
linear_1.bias value tensor([-0.2077, -1.0423]) gradient tensor([ 8.4356e-07, -1.9088e-08])
linear_2.weight value tensor([[4.9900, 2.5811]]) gradient tensor([[ -1.5673e-05,  5.6170e-08]])
linear_2.bias value tensor([-1.7607]) gradient tensor([-1.0403e-05])
epoch 11000
linear_1.weight value tensor([[ -3.5881,  0.0186],
 [ 4.2759, -0.4253]]) gradient tensor([[ -7.4118e-06, -1.1230e-03],
 [-2.1938e-07, -2.7583e-06]])
linear_1.bias value tensor([-0.2327, -1.0436]) gradient tensor([-3.2973e-05, -3.0063e-07])
linear_2.weight value tensor([[5.0541, 2.5797]]) gradient tensor([[ -2.4662e-05, -2.3692e-07]])
linear_2.bias value tensor([-1.7574]) gradient tensor([-3.5731e-05])
epoch 12000
linear_1.weight value tensor([[ -3.5593,  0.0182],
 [ 4.2807, -0.4254]]) gradient tensor([[ -1.3927e-05, -3.3873e-03],
 [-7.1421e-07, -8.4721e-06]])
linear_1.bias value tensor([-0.2516, -1.0484]) gradient tensor([-1.0251e-04, -9.5566e-07])
linear_2.weight value tensor([[5.1172, 2.5796]]) gradient tensor([[ -5.3764e-05, -8.1916e-07]])
linear_2.bias value tensor([-1.7597]) gradient tensor([-0.0001])
epoch 13000
linear_1.weight value tensor([[ -3.5050,  0.0179],
 [ 4.2930, -0.4255]]) gradient tensor([[ -6.2939e-06,  1.1384e-03],
 [ 1.8415e-07,  2.8340e-06]])
linear_1.bias value tensor([-0.2709, -1.0568]) gradient tensor([3.6698e-05, 3.6591e-07])
linear_2.weight value tensor([[5.1976, 2.5805]]) gradient tensor([[9.5577e-06, 2.7235e-07]])
linear_2.bias value tensor([-1.7672]) gradient tensor([3.7914e-05])
epoch 14000
linear_1.weight value tensor([[ -3.4257,  0.0174],
 [ 4.3116, -0.4257]]) gradient tensor([[ -6.9060e-06, -1.1790e-04],
 [-6.2311e-08, -2.9505e-07]])
linear_1.bias value tensor([-0.2963, -1.0688]) gradient tensor([-1.0516e-06, -1.2365e-08])
linear_2.weight value tensor([[5.3113, 2.5821]]) gradient tensor([[ -8.1146e-06, -4.1779e-08]])
linear_2.bias value tensor([-1.7795]) gradient tensor([-4.0163e-07])
epoch 15000
linear_1.weight value tensor([[ -3.3293,  0.0168],
 [ 4.3340, -0.4259]]) gradient tensor([[ -4.5459e-06,  6.7838e-06],
 [-2.4555e-08,  2.5520e-08]])
linear_1.bias value tensor([-0.3286, -1.0832]) gradient tensor([3.5741e-06, 2.1646e-08])
linear_2.weight value tensor([[5.4605, 2.5842]]) gradient tensor([[ -7.2536e-06, -7.0722e-09]])
linear_2.bias value tensor([-1.7954]) gradient tensor([2.6632e-06])
epoch 16000
linear_1.weight value tensor([[ -3.2315,  0.0162],
 [ 4.3559, -0.4261]]) gradient tensor([[ -2.6695e-06,  1.0886e-05],
 [-1.6815e-08,  2.6514e-08]])
linear_1.bias value tensor([-0.3652, -1.0975]) gradient tensor([4.2199e-06, 2.0574e-08])
linear_2.weight value tensor([[5.6316, 2.5864]]) gradient tensor([[ -7.5754e-06, -8.5856e-10]])
linear_2.bias value tensor([-1.8125]) gradient tensor([2.2664e-06])
epoch 17000
linear_1.weight value tensor([[ -3.1430,  0.0156],
 [ 4.3748, -0.4262]]) gradient tensor([[ -1.8965e-06, -1.8765e-04],
 [-5.5379e-08, -4.5043e-07]])
linear_1.bias value tensor([-0.4026, -1.1102]) gradient tensor([-1.5810e-06, -4.1339e-08])
linear_2.weight value tensor([[5.8086, 2.5883]]) gradient tensor([[ -9.6317e-06, -6.1147e-08]])
linear_2.bias value tensor([-1.8286]) gradient tensor([-3.3493e-06])
epoch 18000
linear_1.weight value tensor([[ -3.0668,  0.0151],
 [ 4.3905, -0.4263]]) gradient tensor([[ -8.9720e-07,  1.4407e-05],
 [-9.5462e-09,  4.0382e-08]])
linear_1.bias value tensor([-0.4384, -1.1208]) gradient tensor([4.5546e-06, 1.5097e-08])
linear_2.weight value tensor([[5.9807, 2.5899]]) gradient tensor([[ -7.1521e-06,  4.3947e-09]])
linear_2.bias value tensor([-1.8431]) gradient tensor([1.8266e-06])
epoch 19000
linear_1.weight value tensor([[ -3.0013,  0.0147],
 [ 4.4035, -0.4264]]) gradient tensor([[1.5571e-08, 3.1853e-04],
 [5.1470e-08, 6.7560e-07]])
linear_1.bias value tensor([-0.4717, -1.1298]) gradient tensor([1.3555e-05, 9.5572e-08])
linear_2.weight value tensor([[6.1446, 2.5912]]) gradient tensor([[ -3.8617e-06,  9.1022e-08]])
linear_2.bias value tensor([-1.8559]) gradient tensor([9.3128e-06])
```



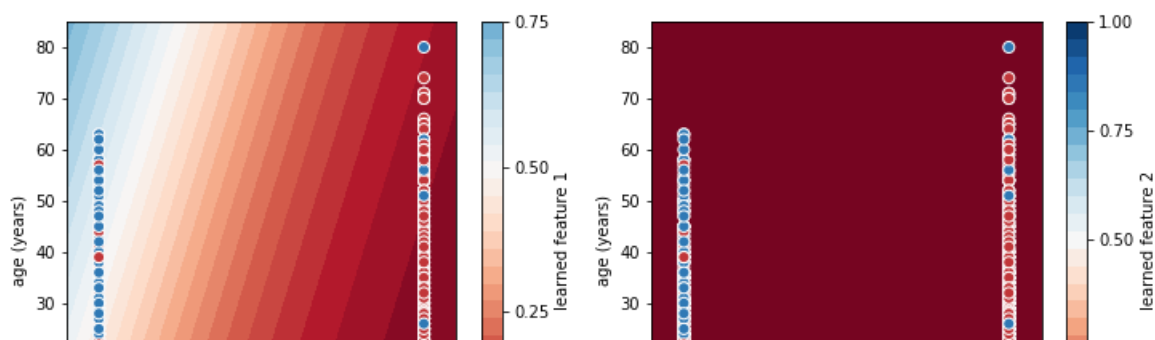
In [11]:

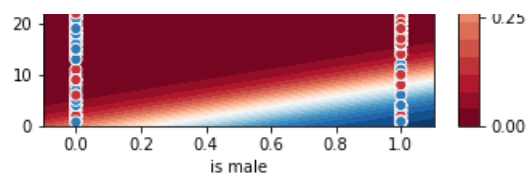
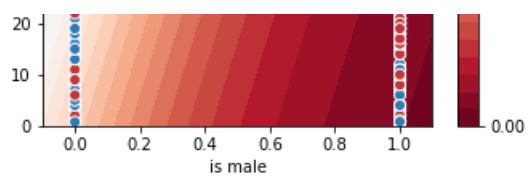
```
xx, yy = np.mgrid[-.1:1.1:.01, 0:85:.1]
grid = np.c_[xx.ravel(), yy.ravel()]

f = plt.figure(figsize=(12, 5))
hidden_units = mlp_pytorch.hidden(Variable(torch.Tensor(grid))).detach().numpy()
for i in range(2):
    ax = f.add_subplot(1,2,i+1)
    contour = ax.contourf(xx, yy, hidden_units[:,i].reshape(xx.shape), 25, cmap="RdBu",
                          vmin=0, vmax=1)

    ax.scatter(experiment_1_data['male'], experiment_1_data['Age'], c=experiment_1_outputs, s=50,
               cmap="RdBu", vmin=-.2, vmax=1.2,
               edgecolor="white", linewidth=1)
    ax_c = f.colorbar(contour)
    ax_c.set_label("learned feature %d" % (i+1))
    ax_c.set_ticks([0, .25, .5, .75, 1])

    ax.set(xlim=(-.1, 1.1),
           ylim=(0, 85),
           xlabel="is male", ylabel="age (years)")
plt.show()
```





In [0]: