Assignment 6 Version: 2019-09-19

# Assignment 6: Introduction to Neural Networks and Backpropagation

Machine Learning

Fall 2019

# **◊** Learning Objectives

- Understand the difficulties that neural networks address in comparison to algorithms like logistic regression.
- Interpret the results of applying a simple neural network to a dataset.
- Understand the architecture of a particular type of neural network called a multi-layer perceptron.
- Learn how to represent the multivariable chain rule graphically.
- Understand how the backpropagation algorithm can be used to compute the gradient of a loss function with respect to the parameters of a neural network.

## 1 Assignment Structure

In this assignment we'll be doing the following things in order to meet the learning goals articulated above.

- 1. Motivate the idea of neural networks through a Jupyter notebook that examines the Titanic Dataset from Kaggle.
- 2. Introduce the architecture of a particular type of neural network called a multi-layer perceptron.
- 3. See another way to think about the chain rule for multivariable functions that uses a graphical representation.
- 4. Learn about, and ultimately derive, the backpropagation algorithm.

### ♣ Prior Knowledge Utilized

Here are some things we'll be utilizing in this assignment. When appropriate, we'll call these out in a particular section with some helpful text to jog your memory.

- Logistic regression algorithm
- Multivariable chain rule
- Binary classification problem setting

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## 2 Motivation for Neural Networks

In order to motivate the idea of neural networks, we'll be examining the Titanic Kaggle dataset. If you didn't work with this data, it might help you to briefly skim the walk-through in assignment 5.

# Z External Resource(s) (45 minutes)

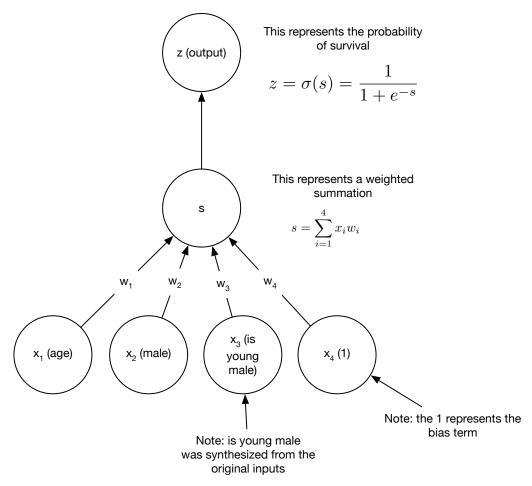
Go through the Assignment 6 Companion notebook.

## 3 Our First Neural Network: the Multilayer Perceptron (MLP)

Now that you've seen a neural network in action, we'll be digging into how a neural network works. The presentation will be specific to a particular type of neural network that we used in the companion notebook known as a multilayer perceptron (MLP), but the main ideas generalize to many other types of networks.

Thinking back to the companion notebook, we observed that the features in the original dataset (age and sex) were not conducive to predicting whether someone would survive. We showed that by augmenting the input features with a column called is young male that captured whether or not a person was young and male, that the algorithm could effectively learn the task. The fundamental idea of a neural network is that the network automatically constructs useful representations of the input data as a part of the learning process.

Graphically we can contrast these approaches in the following way. First we'll show the logistic regression model that we applied in the notebook.



Notice how we had to manually introduce the feature is young male in order for the logistic regression model to utilize it to make its prediction. Before giving you the equivalent figure for the multi-layer perceptron, let's look at a little bit more cartoonish version of the multi-layer perceptron. This version will leave off the math and the particular notation we are using. Once you have a good sense of what this is, you can look at the more precise version which is to follow.

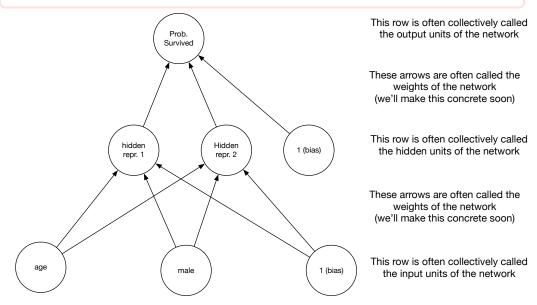
# ☑ External Resource(s)

(optional if what we give you below is not clicking) Here are some additional resources that explain the concept of a multi-layer perceptron. If the explanations we give below are not working for you, consider checking out some of these. You do not need to consult these resources if you feel like our explanations are working well for you.

- 3blue1brown What is a neural network?
- 3blue1brown video How neural networks learn?
- 3blue1brown Backpropagation

To interpret these diagrams, think of the circles (also called nodes) as representing values that are either input to or computed by the network. Directed lines (also called edges) represent data flowing in the network. Each edge multiplies the value flowing into it by a weight (represented by a text label on the edge).

### • Please add your own links via NB.



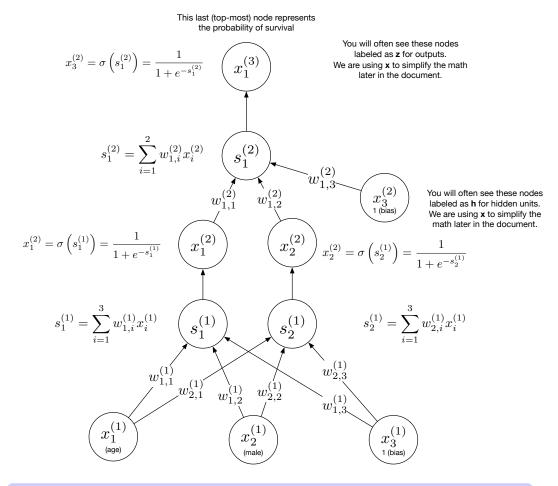
Input data (in this case we just use age, male, and a bias term) are propagated via a set of connection weights to a set of hidden representations. These hidden representations are propagated via another set of a connection weights to the output of the network. In the companion notebook we showed that for the Titanic dataset, the network learned two hidden representations: one that seemed to encode is young male and the another that encoded sex. Of particular importance is that we did not have to manually introduce the is young male feature.

Next, let's make this cartoon picture concrete. We'll use the following notation.

- $x_i^{(j)}$  will refer to the *i*th unit in the *j*th layer of the network (j=1 will correspond to the inputs, j=2 will correspond to the hidden representations, and j=3 will correspond to the output). For instance, in the figure above the circle labeled *male* would be  $x_2^{(1)}$ , *hidden repr. 1* would be  $x_1^{(2)}$  and *prob survived* would be  $x_1^{(3)}$ .
- $s_i^{(j)}$  will refer to the *i*th summation unit in the *j*th layer of the network (as before, j=1 will correspond to the inputs, j=2 will correspond to the hidden representations, and j=3 will correspond to the output). The summation unit will play a similar role to s in the logistic regression figure.
- $w_{i,k}^{(j)}$  will refer to the weight of the connection between the kth unit in layer j and the ith unit in layer j + 1.

## A Notice

There are a lot of symbols here! Take some time to unpack each of them. Make sure you know what superscripts and subscripts represent. While there is an upfront cost to introducing these symbols, it will ultimately make the derivation of the general form of the MLP easier.



# Exercise 1 (10 minutes)

Before going on, let's make sure you have a firm handle on what's being represented in the figure above.

- (a) Just as in logistic regression, we will try to tune the weights to fit the data. How many weights are there to tune in this network?
- (b) While the figure looks pretty crazy, it has a lot of similarities with the logistic regression model. Where does the logistic regression model show up in the figure?

# Exercise 2 (30 minutes)

Without using any training data (this is testing your understanding of the model itself), compute the weights in this network  $(w_{1,1}^{(1)},w_{1,2}^{(1)},w_{1,3}^{(1)},w_{2,1}^{(1)},w_{2,2}^{(1)},w_{2,3}^{(1)},w_{1,1}^{(2)},w_{1,2}^{(2)},w_{1,3}^{(2)}) \text{ such that the MLP has the following behavior. Recall that } x_1^{(1)} \text{ is the passenger's age, } x_2^{(1)} \text{ is a binary variable}$ 

that is 1 if the passenger is male and 0 if female,  $x_3^{(1)}$  and  $x_3^{(2)}$  are always 1.

- (a)  $x_1^{(2)}$  encodes whether or not the passenger is female (i.e., it should take a value close to 1 when the passenger is female and 0 when the passenger is male).
- (b)  $x_2^{(2)}$  encodes whether or not the passenger is a young male (i.e., it should take a value close to 1 when the passenger is male under the age of say 5 and 0 otherwise).
- (c)  $x_1^{(3)}$  should be close to 1 (i.e., predict survival) when the passenger is female or a male under the age of 5.

Believe it or not, computing these weights by hand was fairly common before we had algorithms for automatically tuning weights from data. The reason for this was that early techniques for learning the weights were very inefficient and often unable to converge to good solutions. Later in this document we will be learning about the backpropagation algorithm that can be used to efficiently compute the gradient of the weights in this neural network with respect to some cost function. Just as we did with logistic regression, we can use this gradient in order to optimize the weights of the network using gradient descent. What's beautiful is that even though the model itself will get more complicated, the learning algorithm and basic ideas will remain largely the same.

In order to prepare ourselves for the derivation of the backpropagation algorithm, we need to build up a new technique for applying the chain rule to multivariate functions.

## 4 A Graphical View of the Multivariable Chain Rule

In assignment 3 we learned the multivariable chain rule, which allowed us to take partial derivatives (or the gradient if we wanted to take all partial derivatives simultaneously) of the composition of a multivariable and a single variable function. In the listing below, h is a function from a vector to a scalar, f is from a vector to a scalar, and g is from a scalar to a scalar.

$$h(\mathbf{w}) = g(f(\mathbf{w}))$$
 
$$h(\mathbf{w}) \text{ is the composition of } f \text{ with } g$$
 
$$\nabla h(\mathbf{w}) = g'(f(\mathbf{w})) \nabla f(\mathbf{w})$$
 this is the multivariable chain rule 
$$(1)$$
 
$$\frac{\partial h(\mathbf{w})}{\partial w_i} = g'(f(\mathbf{w})) \frac{\partial f}{\partial w_i}$$
 this is for a single partial deriv. (rather than the gradient) 
$$(2)$$

If we were to write out the MLP example in the previous section using this notation, we'd have a huge mess. The function would probably barely fit on one line of this document. Luckily, there's another way to apply the chain rule that uses the concept of a dataflow diagram. What you will eventually see is that not only will the dataflow diagram make our lives easier from a mathematical perspective, it will actually make our

lives easier from a computational perspective (that last bit is a foreshadowing of the back-propagation algorithm).

# 🗹 External Resource(s) (20 minutes)

This HMC calculus tutorials explain the concept of the chain rule using dataflow diagrams beautifully. Go and read the HMC Multivariable Chain Rule Page and come back for some exercises to test your understanding.

## Exercise 3 (20 minutes)

- (a) Draw a dataflow diagram to represent the function  $f(x, y, z) = \cos(x^2 y) + x^2 \sqrt{z}$ . Compute  $\frac{\partial f}{\partial x}$ ,  $\frac{\partial f}{\partial y}$ , using the dataflow diagram method.
- (b) Draw a dataflow diagram to represent the function  $f(\mathbf{x}) = (\mathbf{c}^{\top}\mathbf{x})^2$ . Compute  $\nabla_{\mathbf{x}} f$  using the dataflow diagram method. Hint: we're generalizing what is on the HMC page a bit. You can have vector quantities flowing through your diagram as well and all the ideas will carry over except you will have a gradient instead of a partial derivative.

## 5 Backpropagation

Before getting into the derivation of the backpropagation algorithm, let's revisit our logistic regression model from the last few assignments. For the logistic regression model, we were given training inputs  $\mathbf{x_1}, \mathbf{x_2}, \dots \mathbf{x_n}$  with each  $\mathbf{x_i}$  being a d-dimensional vector and training outputs  $y_1, y_2, \dots, y_n$  with each  $y_i$  being a binary number that indicates the class that the *i*th instance belongs to. Given this training data, our goal was to compute the best possible set of weights by solving the following optimization problem.

$$\mathbf{w}^{\star} = \arg\min_{\mathbf{w}} \sum_{i=1}^{n} \left( -y_i \ln \sigma \left( \mathbf{w}^{\top} \mathbf{x_i} \right) - (1 - y_i) \ln \left( 1 - \sigma \left( \mathbf{w}^{\top} \mathbf{x_i} \right) \right) \right)$$
(3)

Even though you've seen this before, it might seem a bit intimidating. Remember, that this optimization problem arose from using the sigmoid function  $(\frac{1}{1+e^{-x}})$  to map  $\mathbf{w}^{\top}\mathbf{x_i}$  into a probability and then applying the log loss. We can represent the logistic regression model applied to an input point  $\mathbf{x}$  using the data flow representation shown in Figure 1.

## **A** Notice

We have moved the weights from the arrows into circles. In the dataflow graph we will label the edges with partial derivatives (or gradients).

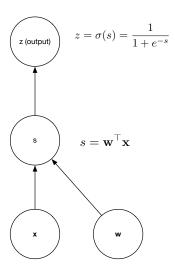


Figure 1: Dataflow in the logistic regression model

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## Exercise 4 (30 minutes)

Starting from the data flow representation of the logistic regression model shown in Figure 1, complete the following steps.

- (a) Add a new circle (node) to the graph that represents the log loss that the output z incurs when compared to the training output y.
- (b) Using the technique in the HMC calculus tutorials writeup, compute the gradient of the log loss with respect to weights,  $\mathbf{w}$ . Hint: remember when examining the arrow from  $\mathbf{x}$  to s, instead of writing the partial derivative of s with respect to its input, you can instead write the gradient. The rest of the process in the HMC calculus tutorial can be applied without modification. Note that we are only showing the path of one input  $\mathbf{x}$  through the network. If you want to work with multiple inputs to take a gradient, all you need to do is sum over the gradient with respect to each training instance.
- (c) Was computing the gradient using this approach easier, harder, or the same in comparison with what you did in assignment 3? Why? (this is subjective, so there is no right answer, we just want you to reflect on the differences between the approaches and which you liked better).e.

### 5.1 Forward Pass

# A Notice

The notation for the general case of MLP gets pretty cluttered. It's important to realize that much of the complexity in this section is simply a result of keeping track of various indices (e.g., layer, unit number) rather than anything conceptually difficult. Our advice is to be diligent in going through these figures and make sure you have a firm grasp on the notation we are using. Please post on NB if something is confusing (or even just to verify your understanding).

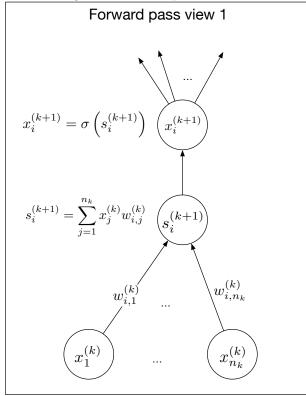
Let's generalize the diagram of the multilayer perceptron in the Titanic example in the following ways.

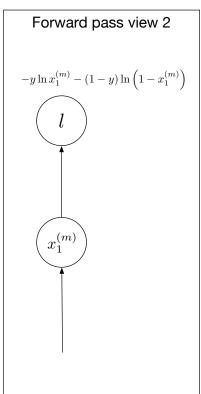
- 1. We'll allow for an arbitrary number of layers in the network. We'll call the number of layers m (the number of layers is also called the depth of the network. networks with large m are known as deep learning).
- 2. We'll allow for an arbitrary number of units at each layer in the network. We'll use the notation  $n_k$  to refer to the number of units in the kth layer of the network.

These generalizations are summarized in the following figure that shows the data flow between two layers of the network (MLP data flow view 1) and between the output layer and the loss function. You may see examples of MLP's with activation functions other

than sigmoid. The math to handle these other functions is very similar, so we are just using sigmoid here.

In the figure below we show how data propagates through the network in the forward direction. Note that this is not a dataflow diagram in the sense that the arrows are labeled with weights rather than partial derivatives.





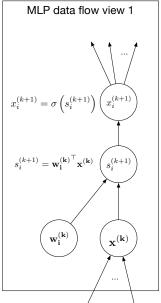
Before we get into the math of how we can compute the gradient of the weights in this network using backpropagation, we must first perform the forward pass through the network. In the forward pass, we use the formulas in the figure above to calculate the value for every circle in the network. The forward pass is thus a very straightforward application of the equations shown here. For the backward pass, we can assume that we have the values for each of these nodes.

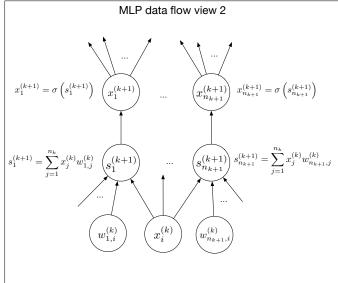
### 5.2 Backward Pass: Applying the Chain Rule

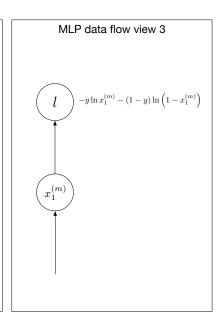
The stage is now set for you to finish the derivation of one of the most important algorithms in computer science!!! Before you finish this off, let's take a look at what you've learned and the tools you have at your disposal.

- 1. You know how to compute gradients using the data flow representation of a mutlivariable function.
- 2. We've applied this technique to deriving the gradient of the logistic regression model.
- 3. We've written the MLP in this same data flow representation.

Before we do this we'll augment the data flow graph just a little bit to provide a view that focuses more directly on the weights coming into a particular neuron. In doing this, we'll refer to the weights coming into the *i*th node in layer k+1 as  $w_i^{(k)}$ .







Let's get to it.

# Exercise 5 (75 minutes)

The backpropagation algorithm, not surprisingly, works by computing gradients in the network starting from the output and working backwards. In this exercise you'll work through the major steps of the backpropagation algorithm. This exercise should be done in reference to Figure 2.

- (a) Referencing view 1, compute the gradient of the loss with respect to  $\mathbf{w_i^{(k)}}$ ,  $\nabla_{\mathbf{w_i^{(k)}}}l$ . You can assume you have already computed  $\frac{\partial l}{\partial x_i^{(k+1)}}$ .
- (b) Referencing view 2, compute  $\frac{\partial l}{\partial x_i^{(k)}}$ . You can assume that you have already calculated the partial derivatives of the loss with respect to the layer k+1. That is, you already have  $\frac{\partial l}{\partial x_1^{(k+1)}}, \ldots, \frac{\partial l}{\partial x_{n_{k+1}}^{(k+1)}}$ .
- (c) Referencing view 3, create a data flow graph and compute  $\frac{\partial l}{\partial x_1^{(m)}}$ .

Figure 2: A data flow graph for the multi-layer perceptron.

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# 6 Summary (AKA What the Heck Just Happened?)

That was a lot of math flying at you. We hope that you realize how cool what you just did was. When you combine the gradient you computed with gradient descent, you have derived a learning rule for efficiently tuning the weights of a special type of neural network called a multi-layer perceptron (MLP). Without defining the derivatives at lower layers in terms of higher layers, we would have been left to sum over all possible paths from some unit in the network to the loss. The number of paths would grow exponentially with the depth of the network. Here, we are able to compute derivatives without a significant computational expense. The learning rules for almost every other type of neural network are just variations on this same theme. This is incredibly powerful, and you now have a very powerful mental model for how learning in neural networks is possible.

# 7 Suggestions for Going Beyond

# A Notice

If you'd like to take this material farther, here are some suggestions. We do not at all expect you to do any of this, but we felt that these suggestions might be helpful to folks who want to go into additional depth with this material. We will never make any assumption that you did any of these additional tasks in any course materials. If you also have other ideas for additional topics to explore, feel free to go in that direction instead (please let us know what you do though in case it is of interest to others).

- Implement the backpropagation algorithm to compute the gradient for an MLP. Hint: if you do this, e-mail us for hints / guidance. It is pretty challenging, but it does pay off in terms of solidifying the backpropagation algorithm.
- Make sure your implementation is correct by comparing the numerical approximation of the gradient to the gradient you calculated with the backpropagation algorithm.



# **Assignment 6 Companion Notebook: Motivation for Neural Networks**

Learning Objectives:

- Understand the limitations of logistic regression through an example
- Become familiar with feedforward, multi-layer neural networks
- Fit a neural network to a dataset and examine the results

## **Titanic: The Sequel**

In order to motivate the need for neural networks, we're going to return to the Titanic dataset and examine a particular limitation of logistic regression.

We'll begin by loading the data.

### In [0]:

### Out[0]:

	Passengerld	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	Fare	Cabin	Embarked
0	1	0	3	Braund, Mr. Owen Harris	male	22.0	1	0	A/5 21171	7.2500	NaN	S
1	2	1	1	Cumings, Mrs. John Bradley (Florence Briggs Th	female	38.0	1	0	PC 17599	71.2833	C85	С
2	3	1	3	Heikkinen, Miss. Laina	female	26.0	0	0	STON/O2. 3101282	7.9250	NaN	S
3	4	1	1	Futrelle, Mrs. Jacques Heath (Lily May Peel)	female	35.0	1	0	113803	53.1000	C123	S
4	5	0	3	Allen, Mr. William Henry	male	35.0	0	0	373450	8.0500	NaN	S
5	6	0	3	Moran, Mr. James	male	NaN	0	0	330877	8.4583	NaN	Q
6	7	0	1	McCarthy, Mr. Timothy J	male	54.0	0	0	17463	51.8625	E46	S
7	8	0	3	Palsson, Master. Gosta Leonard	male	2.0	3	1	349909	21.0750	NaN	S
8	9	1	3	Johnson, Mrs. Oscar W (Elisabeth Vilhelmina Berg)	female	27.0	0	2	347742	11.1333	NaN	S
9	10	1	2	Nasser, Mrs. Nicholas (Adele Achem)	female	14.0	1	0	237736	30.0708	NaN	С
10	11	1	3	Sandstrom, Miss. Marguerite Rut	female	4.0	1	1	PP 9549	16.7000	G6	S
11	12	1	1	Bonnell, Miss. Elizabeth	female	58.0	0	0	113783	26.5500	C103	S
12	13	0	3	Saundercock, Mr. William Henry	male	20.0	0	0	A/5. 2151	8.0500	NaN	S
13	14	0	3	Andersson, Mr. Anders Johan	male	39.0	1	5	347082	31.2750	NaN	S
14	15	0	3	Vestrom, Miss. Hulda	female	14.0	0	0	350406	7.8542	NaN	S

15		Passengerld	Survived	Pclass	Amanda Adollina <b>Name</b>	Sex	Age	SibSp	Parch	Ticket	Fare	Cahin	Embarked
16	15				Hewlett, Mrs. (Mary D								S
18	16	17	0	3	,	male	2.0	4	1	382652	29.1250	NaN	Q
18													
19	17	18	1	2		male	NaN	0	0	244373	13.0000	NaN	S
20	18	19	0	3		female	31.0	1	0	345763	18.0000	NaN	S
21   22   1   2   Beesley, Mr. Lawrence   male   34 0   0   0   246889   13,0000   D56   S   S   22   23   1   3   McGowan, Miss, Arina   ternale   15 0   0   0   330923   8.0792   NaM   C   C   C   C   C   C   C   C   C	19	20	1	3	Masselmani, Mrs. Fatima	female	NaN	0	0	2649	7.2250	NaN	С
22	20	21	0	2	Fynney, Mr. Joseph J	male	35.0	0	0	239865	26.0000	NaN	S
23	21	22	1	2	Beesley, Mr. Lawrence	male	34.0	0	0	248698	13.0000	D56	S
24	22	23	1	3		female	15.0	0	0	330923	8.0292	NaN	Q
25	23	24	1	1		male	28.0	0	0	113788	35.5000	A6	S
26	24	25	0	3		female	8.0	3	1	349909	21.0750	NaN	S
27	25	26	1	3		female	38.0	1	5	347077	31.3875	NaN	S
27	26	27	0	3	Emir, Mr. Farred Chehab	male	NaN	0	0	2631	7.2250	NaN	С
28         29         1         3         O'Dwyer, Miss. Ellen 'Nellie' female         NaN         0         0         339959         7.8792         NaN         O           29         30         0         3         Todoroff, Mr. Lalio         male         NaN         0         0         349216         7.8958         NaN         S           861         862         0         2         Gilles, Mr. Frederick Edward         male         21.0         1         0         28134         11.5000         NaN         S           862         863         1         1         Swiff, Mrs. Frederick Joel (Margaret Welles Ba         female         48.0         0         0         17466         25.9292         D17         S           864         865         0         2         Gill, Mr. John William         male         24.0         0         0         23866         13.0000         NaN         S           866         867         1         2         Duran y More, Miss.         female         24.0         0         0         238852         13.0000         NaN         S           867         888         0         1         Roebling, Mr. Washington         male         31.0 <td>27</td> <td>28</td> <td>0</td> <td>1</td> <td></td> <td>male</td> <td>19.0</td> <td>3</td> <td>2</td> <td>19950</td> <td>263.0000</td> <td>C25</td> <td>S</td>	27	28	0	1		male	19.0	3	2	19950	263.0000	C25	S
29   30   0   3   Todoroff, Mr. Lallo   male   NaN   0   0   349216   7.8958   NaN   S   Na   Na   Na   Na   Na   Na	28	29	1	3	O'Dwyer, Miss. Ellen "Nellie"	female	NaN	0	0	330959	7.8792		Q
861         862         0         2         Giles, Mr. Frederick Edward         male         21.0         1         0         28134         11.5000         NaN         S           862         863         1         1         Swift, Mrs. Frederick Joel. (Margaret Welles Ba         female         48.0         0         0         17466         25.9292         D17         S           863         864         0         3         Sage, Miss. Dorothy Edith Dolly         female         NaN         8         2         CA.2343         69.5500         NaN         S           865         866         1         2         Bystrom, Mrs. (Karolina)         female         24.0         0         0         238682         13.0000         NaN         S           866         867         1         2         Duran y More, Miss. Services         female         27.0         1         0         2278ABS         13.0000         NaN         O           867         868         0         1         Robbling, Mr. Washington         male         31.0         0         PC 17590         50.4958         A24         S           868         869         0         3         Van Melkobeles, Mr. Prancholor		30	0	3	Todoroff, Mr. Lalio	male	NaN	0	0	349216	7.8958	NaN	S
861         862         0         2         Giles, Mr. Frederick Edward         male         21.0         1         0         28134         11.5000         NaN         S           862         863         1         1         Swift, Mrs. Frederick Joal (Margaret Welles Ba         female         48.0         0         0         17466         25.9292         D17         S           863         864         0         3         Sage, Miss. Dorothy Edith Pobly*         female         NaN         8         2         CA. 2343         69.5500         NaN         S           865         866         1         2         Bystrom, Mrs. (Karolina)         female         24.0         0         0         23866         13.0000         NaN         S           866         867         1         2         Duran y More, Miss. Agencian         female         27.0         1         0         2C/PARIS         13.8883         NaN         C           867         868         867         1         3         Dornard Yameniss. Miss. Agencian         male         21.0         0         PC 17590         50.4958         A24         S           868         869         0         1         Boebling, M													
863         864         0         3         Sage, Miss. Dorothy Edith 'Dolly' female NaN         8         2         CA. 2343         69.5500         NaN         S           864         865         0         2         Gill, Mr. John William Male         24.0         0         0         23866         13.0000         NaN         S           865         866         1         2         Bystrom, Mrs. (Karolina) female         24.0         0         0         23866         13.0000         NaN         S           866         867         1         2         Bystrom, Mrs. (Karolina) female         42.0         0         0         23866         13.0000         NaN         S           867         868         0         1         Roebling, Mr. Washington Augustus II         male         27.0         1         0         SC/PARIS Sc149         13.8583         NaN         C           868         869         0         3         Probling, Mr. Washington Augustus II         male         91.0         0         PC 17590         50.4958         A24         S           868         869         0         3         Johnson, Master, Harold Theodor Th		862	0	2	Giles, Mr. Frederick Edward	male	21.0	1	0	28134	11.5000	NaN	S
864         865         0         2         Gill, Mr. John William         male         24.0         0         0         233866         13.0000         NaN         S           865         866         1         2         Bystrom, Mrs. (Karolina)         female         24.0         0         0         233866         13.0000         NaN         S           866         867         1         2         Bystrom, Mrs. (Karolina)         female         27.0         1         0         SC/PARIS         13.8583         NaN         C           867         868         0         1         Roebling, Mr. Washington Augustusi         male         31.0         0         PC 17590         50.4958         A24         S           868         869         0         3         Van Melkebeke, Mr. Pillemon         male         NaN         0         0         345777         9.5000         NaN         S           869         870         1         3         Johnson, Master Harold Theodor         male         4.0         1         1         347742         11.1333         NaN         S           871         872         1         1         Eeckwith, Mr. S. Richard Theodor         male	862	863	1	1		female	48.0	0	0	17466	25.9292	D17	S
865         866         1         2         Bystrom, Mrs. (Karolina) female         42.0         0         0         236852         13.0000         NaN         S           866         867         1         2         Duran y More, Miss. Asuncion female         27.0         1         0         SC/PARIS 2149         13.8583         NaN         C           867         868         0         1         Roebling, Mr. Washington Augustus II         male         31.0         0         0         PC 17590         50.4958         A24         S           868         869         0         3         Van Melkebeke, Mr. Philemon         male         NaN         0         0         345777         9.5000         NaN         S           869         870         1         3         Jónnson, Master, Harold Theodor Philemon         male         4.0         1         1         347742         11.1333         NaN         S           870         871         0         3         Balkic, Mr. Cerin         male         26.0         0         0         349248         7.8958         NaN         S           871         872         1         1         Carlsson, Mr. Frans Olof         male         47.0	863	864	0	3		female	NaN	8	2	CA. 2343	69.5500	NaN	s
866         867         1         2         Duran y More, Miss. Asuncion female         27.0         1         0         SC/PARIS 2149         13.8583         NaN         CR           867         868         0         1         Roebling, Mr. Washington Augustus II         male         31.0         0         0         PC 17590         50.4958         A24         S           868         869         0         3         van Melkebeke, Mr. Philemon         male         NaN         0         0         345777         9.5000         NaN         S           869         870         1         3         Jónnson, Master, Harold Theodor         male         4.0         1         1         347722         11.1333         NaN         S           870         871         0         3         Balkic, Mr. Cerin Male         4.0         1         1         347422         11.1333         NaN         S           871         872         1         1         Beckwith, Mrs. Richard Leonard (Sallie Monypeny)         female         47.0         1         1         11751         52.5542         D35         S           872         873         0         1         Carlsson, Mr. Frans Olof         male	864	865	0	2	Gill, Mr. John William	male	24.0	0	0	233866	13.0000	NaN	S
867         868         0         1         2         Asuncion female 27.0         1         0         2149         13.533         Nam         0           867         868         0         1         Roebling, Mr. Washington Augustus II         male         31.0         0         0         PC 17590         50.4958         A24         S           868         869         0         3         Van Melkebeke, Mr. Philemon Philemon         male         NaN         0         0         345777         9.5000         NaN         S           869         870         1         3         Johnson, Master. Harold Theodor Philemon         male         4.0         1         1         347742         11.1333         NaN         S           870         871         0         3         Balkic, Mr. Cerin         male         26.0         0         0         349248         7.8958         NaN         S           871         872         1         1         Beckwith, Mrs. Richard Leonard (Sallie Monypeny)         female         47.0         1         1         11751         52.5542         D35         S           872         873         0         1         Cartsson, Mr. Samuel (Hannah Wizosky)	865	866	1	2	Bystrom, Mrs. (Karolina)	female	42.0	0	0	236852	13.0000	NaN	S
868         869         0         3         Van Melkebeke, Mr. Philemon         male         NaN         0         0         345777         9.5000         NaN         S           869         870         1         3         Johnson, Master. Harold Theodor Theodo	866	867	1	2		female	27.0	1	0		13.8583	NaN	С
869         869         0         3         Philemon Male Man         Nan         0         0         3497/7         9:5000         Nan         S           869         870         1         3         Johnson, Master. Harold Theodor         male         4.0         1         1         347742         11.1333         Nan         S           870         871         0         3         Balkic, Mr. Cerin         male         26.0         0         0         349248         7.8958         Nan         S           871         872         1         1         Beckwith, Mrs. Richard (Sallie Monypeny)         female         47.0         1         1         11751         52.5542         D35         S           872         873         0         1         Carlsson, Mr. Frans Olof         male         33.0         0         0         695         5.0000         B53         B55         S           873         874         0         3         Vander Cruyssen, Mr. Victor         male         47.0         0         0         345765         9.0000         Nan         S           874         875         1         2         Abelson, Mrs. Samuel (Hannah Wizosky)         female	867	868	0	1		male	31.0	0	0	PC 17590	50.4958	A24	S
870         1         3         Theodor         It lies         4.0         1         347/42         11.333         NaN         S           870         871         0         3         Balkic, Mr. Cerin         male         26.0         0         0         349248         7.8958         NaN         S           871         872         1         1         Beckwith, Mrs. Richard Leonard (Sallie Monypeny)         female         47.0         1         1         11751         52.5542         D35         S           872         873         0         1         Carlsson, Mr. Frans Olof         male         33.0         0         0         695         5.0000         B51 B53         S           873         874         0         3         Vander Cruyssen, Mr. Victor         male         47.0         0         0         345765         9.0000         NaN         S           874         875         1         2         Abelson, Mrs. Samuel (Hannah Wizosky)         female         28.0         1         0         P/PP 3381         24.0000         NaN         C           875         876         1         3         Najib, Miss. Adele Kiamie "Jane"         female         15.0	868	869	0	3		male	NaN	0	0	345777	9.5000	NaN	S
871         872         1         1         Beckwith, Mrs. Richard Leonard (Sallie Monypeny)         female         47.0         1         1         11751         52.5542         D35         S           872         873         0         1         Carlsson, Mr. Frans Olof         male         33.0         0         0         695         5.0000         B51 B55 B55         S           873         874         0         3         Vander Cruyssen, Mr. Victor         male         47.0         0         0         345765         9.0000         NaN         S           874         875         1         2         Abelson, Mrs. Samuel (Hannah Wizosky)         female         28.0         1         0         P/PP 3381         24.0000         NaN         C           875         876         1         3         Najib, Miss. Adele Kiamie "Jane"         female         15.0         0         0         2667         7.2250         NaN         C           876         877         0         3         Gustafsson, Mr. Alfred Ossian         male         20.0         0         7534         9.458         NaN         S           877         878         0         3         Petroff, Mr. Kristo	869	870	1	3		male	4.0	1	1	347742	11.1333	NaN	S
872       1       1       Leonard (Sallie Monypeny)       1       1       11751       \$2.5542       D35       \$3         872       873       0       1       Carlsson, Mr. Frans Olof       male       33.0       0       0       695       5.0000       B51 B55 B55       \$8         873       874       0       3       Vander Cruyssen, Mr. Victor       male       47.0       0       0       345765       9.0000       NaN       \$8         874       875       1       2       Abelson, Mrs. Samuel (Hannah Wizosky)       female       28.0       1       0       P/PP 3381       24.0000       NaN       C         875       876       1       3       Najib, Miss. Adele Kiamie "Jane"       female       15.0       0       0       2667       7.2250       NaN       C         876       877       0       3       Gustafsson, Mr. Alfred Ossian       male       20.0       0       0       7534       9.8458       NaN       S         877       878       0       3       Petroff, Mr. Nedelio       male       19.0       0       349212       7.8958       NaN       S         878       879       0       3 </td <td>870</td> <td>871</td> <td>0</td> <td>3</td> <td>Balkic, Mr. Cerin</td> <td>male</td> <td>26.0</td> <td>0</td> <td>0</td> <td>349248</td> <td>7.8958</td> <td>NaN</td> <td>S</td>	870	871	0	3	Balkic, Mr. Cerin	male	26.0	0	0	349248	7.8958	NaN	S
872       873       0       1       Carlsson, Mr. Frans Olof       male       33.0       0       0       695       5.0000       B53 B55       S         873       874       0       3       Vander Cruyssen, Mr. Victor       male       47.0       0       0       345765       9.0000       NaN       S         874       875       1       2       Abelson, Mrs. Samuel (Hannah Wizosky)       female       28.0       1       0       P/PP 3381       24.0000       NaN       C         875       876       1       3       Najib, Miss. Adele Kiamie "Jane"       female       15.0       0       0       2667       7.2250       NaN       C         876       877       0       3       Gustafsson, Mr. Alfred Ossian       male       20.0       0       0       7.534       9.8458       NaN       S         877       878       0       3       Petroff, Mr. Nedelio       male       19.0       0       0       349212       7.8958       NaN       S         878       879       0       3       Laleff, Mr. Kristo       male       NaN       0       0       349217       7.8958       NaN       S	871	872	1	1		female	47.0	1	1	11751	52.5542	D35	S
874         875         1         2         Abelson, Mrs. Samuel (Hannah Wizosky)         female         28.0         1         0         P/PP 3381         24.0000         NaN         Company           875         876         1         3         Najib, Miss. Adele Kiamie "Jane"         female         15.0         0         0         2667         7.2250         NaN         Company           876         877         0         3         Gustafsson, Mr. Alfred Ossian         male         20.0         0         0         7534         9.8458         NaN         S           877         878         0         3         Petroff, Mr. Nedelio         male         19.0         0         0         349212         7.8958         NaN         S           878         879         0         3         Laleff, Mr. Kristo         male         NaN         0         349217         7.8958         NaN         S           879         880         1         1         Potter, Mrs. Thomas Jr (Lily Alexenia Wilson)         female         56.0         0         1         11767         83.1583         C50         C           880         881         1         2         Shelley, Mrs. William (Imanita Parrish Hal	872	873	0	1	Carlsson, Mr. Frans Olof	male	33.0	0	0	695	5.0000	B53	S
875       1       2       (Hannah Wizosky)       Iemale       28.0       1       0       PPPP 3381       24.0000       Nain       C         875       876       1       3       Najib, Miss. Adele Kiamie "Jane"       female       15.0       0       0       2667       7.2250       NaN       C         876       877       0       3       Gustafsson, Mr. Alfred Ossian       male       20.0       0       0       7534       9.8458       NaN       S         877       878       0       3       Petroff, Mr. Nedelio       male       19.0       0       0       349212       7.8958       NaN       S         878       879       0       3       Laleff, Mr. Kristo       male       NaN       0       0       349217       7.8958       NaN       S         879       880       1       1       Potter, Mrs. Thomas Jr (Lily Alexenia Wilson)       female       56.0       0       1       11767       83.1583       C50       C         880       881       1       2       Shelley, Mrs. William (Imanita Parrish Hall)       female       25.0       0       1       230433       26.0000       NaN       S </td <td>873</td> <td>874</td> <td>0</td> <td>3</td> <td>Vander Cruyssen, Mr. Victor</td> <td>male</td> <td>47.0</td> <td>0</td> <td>0</td> <td>345765</td> <td>9.0000</td> <td>NaN</td> <td>S</td>	873	874	0	3	Vander Cruyssen, Mr. Victor	male	47.0	0	0	345765	9.0000	NaN	S
876       1       3       "Jane" female       15.0       0       0       2667       7.2250       NaN       C         876       877       0       3       Gustafsson, Mr. Alfred Ossian       male       20.0       0       0       7.534       9.8458       NaN       S         877       878       0       3       Petroff, Mr. Nedelio       male       19.0       0       0       349212       7.8958       NaN       S         878       879       0       3       Laleff, Mr. Kristo       male       NaN       0       0       349217       7.8958       NaN       S         879       880       1       1       Potter, Mrs. Thomas Jr (Lily Alexenia Wilson)       female       56.0       0       1       11767       83.1583       C50       C         880       881       1       2       Shelley, Mrs. William (Imanita Parrish Hall)       female       25.0       0       1       230433       26.0000       NaN       S	874	875	1	2	Abelson, Mrs. Samuel (Hannah Wizosky)	female	28.0	1	0	P/PP 3381	24.0000	NaN	С
877       0       3       Ossian       male 20.0       0       7534       9.8458       Nain       S         877       878       0       3       Petroff, Mr. Nedelio male 19.0       0       0       349212       7.8958       NaN       S         878       879       0       3       Laleff, Mr. Kristo male NaN       0       0       349217       7.8958       NaN       S         879       880       1       1       Potter, Mrs. Thomas Jr (Lily Alexenia Wilson)       female 56.0       0       1       11767       83.1583       C50       C         880       881       1       2       Shelley, Mrs. William (Imanita Parrish Hall)       female 25.0       0       1       230433       26.0000       NaN       S	875	876	1	3		female	15.0	0	0	2667	7.2250	NaN	С
878       879       0       3       Laleff, Mr. Kristo       male       NaN       0       0       349217       7.8958       NaN       S         879       880       1       1       Potter, Mrs. Thomas Jr (Lily Alexenia Wilson)       female       56.0       0       1       11767       83.1583       C50       C         880       881       1       2       Shelley, Mrs. William (Imanita Parrish Hall)       female       25.0       0       1       230433       26.0000       NaN       S	876	877	0	3		male	20.0	0	0	7534	9.8458	NaN	S
879       880       1       1       Potter, Mrs. Thomas Jr (Lily Alexenia Wilson)       female       56.0       0       1       11767       83.1583       C50       C50         880       881       1       2       Shelley, Mrs. William (Imanita Parrish Hall)       female       25.0       0       1       230433       26.0000       NaN       S	877	878	0	3	Petroff, Mr. Nedelio	male	19.0	0	0	349212	7.8958	NaN	S
880 881 1 2 Shelley, Mrs. William (Imanita Parrish Hall) female 25.0 0 1 230433 26.0000 NaN S	878	879	0	3	Laleff, Mr. Kristo	male	NaN	0	0	349217	7.8958	NaN	S
880 881 I 2 (Imanita Parrish Hall) Temale 25.0 0 I 230433 26.0000 Nain S	879	880	1	1		female	56.0	0	1	11767	83.1583	C50	С
881 882 0 3 Markun, Mr. Johann male 33.0 0 0 349257 7.8958 NaN S	880	881	1	2		female	25.0	0	1	230433	26.0000	NaN	S
	881	882	0	3	Markun, Mr. Johann	male	33.0	0	0	349257	7.8958	NaN	S

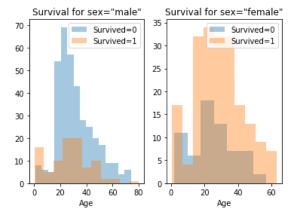
882	Passengerid	Survived	Pclass	Dahlberg, Miss. Gerda Ulrika	female	<u> <del>2</del>9</u> 8	SibSp	Parch	Ticket	10.5 <b>769</b>	Cabin	Embarked
883	884	0	2	Banfield, Mr. Frederick James	male	28.0	0	0	C.A./SOTON 34068	10.5000	NaN	S
884	885	0	3	Sutehall, Mr. Henry Jr	male	25.0	0	0	SOTON/OQ 392076	7.0500	NaN	S
885	886	0	3	Rice, Mrs. William (Margaret Norton)	female	39.0	0	5	382652	29.1250	NaN	Q
886	887	0	2	Montvila, Rev. Juozas	male	27.0	0	0	211536	13.0000	NaN	S
887	888	1	1	Graham, Miss. Margaret Edith	female	19.0	0	0	112053	30.0000	B42	S
888	889	0	3	Johnston, Miss. Catherine Helen "Carrie"	female	NaN	1	2	W./C. 6607	23.4500	NaN	S
889	890	1	1	Behr, Mr. Karl Howell	male	26.0	0	0	111369	30.0000	C148	С
890	891	0	3	Dooley, Mr. Patrick	male	32.0	0	0	370376	7.7500	NaN	Q

891 rows × 12 columns

From some of the exploratory analysis in the <u>assignment 5 walkthrough</u>, we know that both age and sex are good predictors of whether or not someone survived the Titanic sinking. That said, we saw that the effect survival rate for women wasn't dramatically changed by age, but the survival rate for men was dramatically changed. Here are some plots showing this result.

### In [0]:

```
import seaborn as sns
import matplotlib.pyplot as plt
%matplotlib inline
legend_entries = []
plt.subplot(1,2,1)
for groups in df[df['Sex'] == 'male'].groupby('Survived'):
    sns.distplot(groups[1]['Age'].dropna(), kde=False)
    legend_entries.append('Survived=%d'% groups[0])
plt.legend(legend_entries)
plt.title('Survival for sex="male"')
plt.subplot(1,2,2)
legend_entries = []
for groups in df[df['Sex'] == 'female'].groupby('Survived'):
    sns.distplot(groups[1]['Age'].dropna(), kde=False)
    legend_entries.append('Survived=%d'% groups[0])
plt.legend(legend_entries)
plt.title('Survival for sex="female"')
plt.show()
# while we're at it, silence annoying sklearn warnings
# import warnings filter
from warnings import simplefilter
# ignore all future warnings
simplefilter(action='ignore', category=FutureWarning)
```



It would be great if we could use logistic regression in order to leverage this information. A good first pass would be to take both of these features (where we will encode sex using an is\_male feature) and pass them into a logistic regression. The plot below

shows the results of this analysis where we represent the training data along with the lines of equal probability for the resultant model. We'll divide this into two cells, one where we prepare the data and the other where we fit the model and show the plot

### In [0]:

```
# get rid of null values for age since this is just an illustrative example.
# this would not be a good thing to do if we were trying to evalutate the
# performance of a model.
df_filtered = df[['Age', 'Sex', 'Survived']].dropna()
experiment_1_data = pd.concat((pd.get_dummies(df_filtered['Sex'], drop_first=True),
df_filtered['Age']), axis=1)
experiment_1_outputs = df_filtered['Survived']
experiment_1_data
```

### Out[0]:

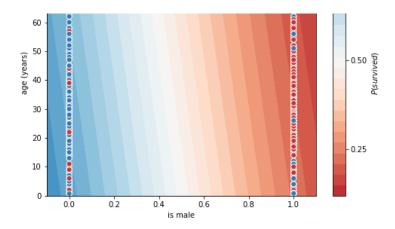
male Age

	male	Age
0	1	22.0
1	0	38.0
2	0	26.0
3	0	35.0
4	1	35.0
6	1	54.0
7	1	2.0
8	0	27.0
9	0	14.0
10	0	4.0
11	0	58.0
12	1	20.0
13	1	39.0
14	0	14.0
15	0	55.0
16	1	2.0
18	0	31.0
20	1	35.0
21	1	34.0
22	0	15.0
23	1	28.0
24	0	8.0
25	0	38.0
27	1	19.0
30	1	40.0
33	1	66.0
34	1	28.0
35	1	42.0
37	1	21.0
38	0	18.0
856	0	45.0
857	1	51.0
858	0	24.0
860	1	41.0
861	1	21.0
060	Λ	40 N

80∠ U 40.U male Age 865 0 42.0 0 27.0 866 1 31.0 867 1 4.0 869 1 26.0 871 0 47.0 1 33.0 872 1 47.0 873 874 0 28.0 875 0 15.0 1 20.0 876 1 19.0 877 879 0 56.0 0 25.0 1 33.0 881 0 22.0 882 1 28.0 883 1 25.0 0 39.0 885 1 27.0 886 0 19.0 887 889 1 26.0 1 32.0

714 rows × 2 columns

```
from sklearn.linear_model import LogisticRegression
import numpy as np
model = LogisticRegression()
model.fit(experiment_1_data, experiment_1_outputs)
xx, yy = np.mgrid[-.1:1.1:.01, 0:85:.1]
grid = np.c_[xx.ravel(), yy.ravel()]
probs = model.predict_proba(grid)[:, 1].reshape(xx.shape)
f, ax = plt.subplots(figsize=(8, 6))
contour = ax.contourf(xx, yy, probs, 25, cmap="RdBu",
                       vmin=0, vmax=1)
ax c = f.colorbar(contour)
ax_c.set_label("$P(survived)$")
ax_c.set_ticks([0, .25, .5, .75, 1])
ax.scatter(experiment_1_data['male'], experiment_1_data['Age'], c=experiment_1_outputs, s=50,
           cmap="RdBu", vmin=-.2, vmax=1.2,
edgecolor="white", linewidth=1)
ax.set(xlim=(-.1, 1.1),
       ylim=(0, 85),
       xlabel="is male", ylabel="age (years)")
plt.show()
```



### Notebook Exercise 1 (10 minutes)

- (a) In English, explain what this graph is showing (defer interpretation for now, we just want to make sure you have an idea of what is represented in the plot, e.g., x-axis, y-axis, colored areas).
- (b) Given the decision boundary, how does the model predict who will survive versus not survive? What does it predict for male babies?

## Adding the is\_young\_male feature

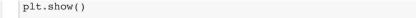
Based on this plot it seems that what we need is to have a model that is able to simulataneously predict that all women survived and that all very young boys survived. One way we can achieve this is by engineering a special <code>is\_young\_male</code> feature that is 1 if the person is under the age of 5 and male. The feature will take a value of 0 otherwise.

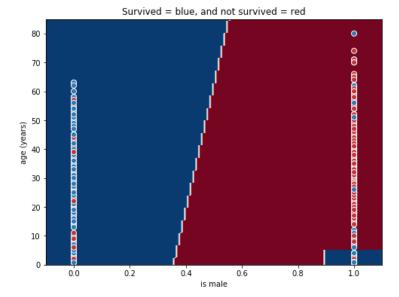
#### In [0]:

```
is_young_male = (experiment_1_data['male']) & (experiment_1_data['Age'] < 5).astype(int)
is_young_male.name = 'is_young_male'
experiment_2_data = pd.concat((experiment_1_data, is_young_male), axis=1)
experiment_2_data
# these don't change, but just to be consistent with variable naming
experiment_2_outputs = experiment_1_outputs</pre>
```

Next, we can take fit the model to this new dataset and create a plot that shows the results of fitting the model. To make the plot a bit easier to interpret, we'll just plot the model's binary output (0 or 1) rather than the probability. This will make it really clear what the model is doing with the points in the lower righthand corner.

```
model = LogisticRegression()
model.fit(experiment_2_data, experiment_1_outputs)
xx, yy = np.mgrid[-.1:1.1:.01, 0:85:.1]
grid = np.c_[xx.ravel(), yy.ravel()]
# Note: we are setting the is_young_male feature for a male value above 0.9 to
# aid in visualization. Of course, the feature can only take on value 0 or 1
is_young_male_grid = np.logical_and(grid[:,0] >= 0.9, grid[:,1] < 5).astype(np.int)[:,np.newaxis]</pre>
grid = np.hstack((grid, is young male grid))
outputs = model.predict(grid).reshape(xx.shape)
f, ax = plt.subplots(figsize=(8, 6))
contour = ax.contourf(xx, yy, outputs, 25, cmap="RdBu",
                      vmin=0, vmax=1)
ax.set_title('Survived = blue, and not survived = red')
ax.scatter(experiment_1_data['male'], experiment_1_data['Age'], c=experiment_2_outputs, s=50,
           cmap="RdBu", vmin=-.2, vmax=1.2,
           edgecolor="white", linewidth=1)
ax.set(xlim=(-.1, 1.1),
       ylim=(0, 85),
       xlabel="is male", ylabel="age (years)")
```





### Notebook Exercise 2 (10 minutes)

- (a) Based on this graph, given a passenger's sex and age, what would the model predict?
- (b) This seems to have achieved our goal of predicting that young males survived. What are the limitations of this approach of hand coding these sorts of features?

### **Enter the Neural Network!**

Next, we're going to learn about a particular type of neural network called a multilayer perceptron (you'll know exactly what one is by the end of this assignment!). For now, we won't give you a very sophisticated mental model of what this neural network is doing. Just think of it as automating the process of discovering useful representations for learning. We are trying to avoid needing to hand engineer features, such as we did with the is young male feature.

### In [0]:

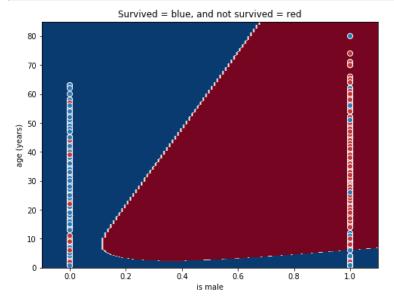
```
from sklearn.neural_network import MLPClassifier

model = MLPClassifier(hidden_layer_sizes=(2), activation='logistic', solver='lbfgs', random_state=5
0)
model.fit(experiment_1_data, experiment_1_outputs)
```

### Out[0]:

```
edgecolor="white", linewidth=1)

ax.set(xlim=(-.1, 1.1),
    ylim=(0, 85),
    xlabel="is male", ylabel="age (years)")
plt.show()
```



### Notebook Exercise 3 (5 minutes)

Based on this graph, what does the network predict about whether a passenger will survive or not survive?

### **Examining the Intermediate Representations in the Network**

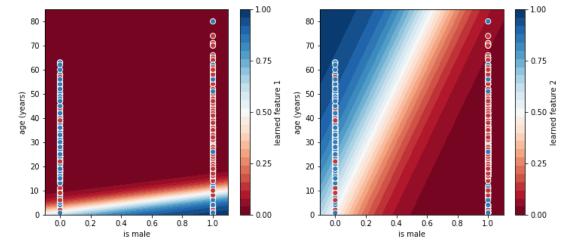
While we have yet to really unpack *how* the neural network was able to achieve this feat, we can start to interrogate the learned model to undrestand a bit of what it is doing.

For the purposes of this next set of plots and exercise, you should have the following mental model of what the network is doing (all of this will be made 100% precise when you go through the rest of the assignment document, but for now things will be explained on a conceptual level).

- Neural networks learn internal representations of the input data that help them make predictions (you may recall that this was Big Idea #4 in assignment 1).
- In this case we instructed the neural network to learn exactly \$2\$ internal representations of the input data.
- The network will use these two internal representations, not the original input data, in order to arrive at its final decision.

In the plot below, we show the values for each of the \$2\$ learned internal representations in the network. You can think of these representations as providing a remapping of the data into a new space that is then used to make the prediction as to whether the person was likely to surive or not survive.

```
ax.set(xlim=(-.1, 1.1),
    ylim=(0, 85),
    xlabel="is male", ylabel="age (years)")
plt.show()
```



### Notebook Exercise 4 (10 minutes)

- (a) What does first learned feature (left plot) appear to encode?
- (b) What does the second learned feature (right plot) appear to encode?

### Key takeaways

While this was a relatively simple example of how a neural network could be applied, the capabilities that you just saw in this notebook have immense significance. The ability of a neural network to take input data that may not be suited for prediction (e.g., sex and age) and transform it into a representation that is more useful for prediction is perhaps the most significant aspect of neural networks. Here is a summmary of what happened in this notebook.

- We reexamined the Titanic dataset and showed that adding the age feature doesn't really help in making predictions versus just using sex.
- We showed that we can manually add a feature called is young male that can help us in prediction.
- We showed that neural networks can automate this process of feature learning by developing their own internal representations.
- We showed that the neural network, in this case, learned an internal representation that is very similar to the is\_young\_male and sex representation.

In the rest of the assignment we'll be unpacking what exactly a neural network is. You'll learn how it functions and how you would fit the parameters of one.