

$$1. \quad f(x) = \frac{1}{1 + \exp(-x)}$$

$$f'(x) = \frac{1}{1 + \exp(-x)'} = \frac{1}{1 + (e^{-x})'} = \frac{1}{1 + \left(\frac{1}{e}\right)^x'}$$

$$= \frac{1}{1 + \left(\frac{1}{e}\right)^x} = \frac{1}{1 + e^{-x}}$$

$$2. \quad f(x_1, x_2) = x_1^2 + 2x_2$$

$$x_1 = \sin t$$

$$x_2 = \cos t$$

$$f(x_1, x_2) = (\sin t)^2 + 2(\cos t)$$

$$f'(x_1, x_2) = (\cos t)^2 +$$

$$-2\sin t$$

$$(\cos t)^2 - 2\sin t$$

$$3 \quad a = x^2$$

$$b = e^{x^2}$$

$$c = x^2 + e^{x^2}$$

$$d = \sqrt{x^2 + e^{x^2}}$$

$$e = \cos(x^2 + e^{x^2})$$

$$f = \sqrt{x^2 + e^{x^2}} + \cos(x^2 + e^{x^2})$$

$$\frac{\partial f}{\partial x} = 2x$$

$$\frac{\partial b}{\partial a} = e^{x^2}$$

$$\frac{\partial c}{\partial a} = 1 + e^{x^2}$$

$$\frac{\partial d}{\partial c} = \frac{1}{2\sqrt{x^2 + e^{x^2}}}$$

$$\frac{\partial e}{\partial c} = -\sin(x^2 + e^{x^2})$$

$$\frac{\partial f}{\partial d} = 1 - 2\sqrt{x^2 + e^{x^2}} \cdot \sin(x^2 + e^{x^2})$$

$$\frac{\partial f}{\partial c} = \frac{1}{2\sqrt{x^2 + e^{x^2}}} - \sin(x^2 + e^{x^2})$$

$$\frac{\partial f}{\partial b} = \left\{ \sqrt{x^2 + e^{x^2}} + \cos(x^2 + e^{x^2}) \right\} \left\{ \frac{1}{2\sqrt{x^2 + e^{x^2}}} - \sin(x^2 + e^{x^2}) \right\}$$

$$\frac{\partial f}{\partial a} = (1 + e^{x^2}) \left(\frac{1}{2\sqrt{x^2 + e^{x^2}}} - \sin(x^2 + e^{x^2}) \right)$$

$$\frac{\partial f}{\partial x} = 2x(e^{x^2} + 1) \left(-\sin(e^{x^2} + x^2) + \frac{1}{2\sqrt{e^{x^2} + x^2}} \right)$$