Perception IV: Place Recognition & Line Fitting

Line fitting with RANSAC

RANSAC iterations

RANSAC is one of the most commonly used technique for fitting a model to a given dataset. In the line fitting RANSAC paradigm that we have studied this week, on every iteration we select 2 points from the set randomly to hypothesize a candidate line. Following a certain number iterations the line with the biggest agreement in the set is selected to be the final answer. But how many RANSAC iterations are "enough"? This Unit is designed to enhance your understanding of how to work out the number of RANSAC iterations and how this is affected by the parameters involved.

Problem 1

Suppose that you are given a point cloud of 1000 points, 20% of which are inliers and a function "one_RANSAC_iteration", which performs one iteration of RANSAC on a given set of points.

How many times do you need to call this function (i.e. how many RANSAC iterations are required) to find at least one set of all inliers with probability p=95%? You may assume that the set of points is large such that the portion of outliers do not change when removing a point.

Answer

The number of RANSAC iteration is as follows:

$$k = \frac{\log(1-p)}{\log(1-w^2)} \tag{1}$$

where success probability p = 0.95, inlier ration w = 0.2 and the number of data points n = 1000 (the number of RANSAC iteration is independent on the number of data points).

The number of iterations required is: $k \geq 73.3$

Problem 2

If instead of selecting a pre-specified number of iterations, we performed RANSAC iterations indefinitely then all the possible line candidates would have been checked. How may possible line candidates are there in this dataset?

Answer

Exhaustive search takes $\binom{n}{2}$ candidates thus $\binom{1000}{2}=\frac{1000\times999}{2}=499500$