

# Problem C

## Completely Independent Spanning Trees

Input File: *testdata.in*

Time Limit: 2 seconds

### Problem Description

Let  $G$  be a graph with vertex set  $V(G)$  and edge set  $E(G)$ . A *tree* is a connected and acyclic graph. A *leaf* of a tree is a node with degree 1. A *spanning tree* of a graph  $G$  is a subgraph of  $G$  that forms a tree of  $n - 1$  edges.

Two paths  $P_1$  and  $P_2$  between vertices  $x$  and  $y$  are called *openly disjoint* if no vertex appears in both paths except their end vertices. Let  $T_1, T_2, \dots, T_k$  be spanning trees of  $G$ . If, for any two vertices  $x, y$  of  $G$ , the paths from  $x$  to  $y$  in  $T_1, T_2, \dots, T_k$  are pairwise openly disjoint, then  $T_1, T_2, \dots, T_k$  are called *completely independent spanning trees* (abbreviated as CISTs) in  $G$ . Spanning trees  $T_1, T_2, \dots, T_k$  are CISTs in a graph  $G$  if and only if no edge appears in different spanning trees and, for any  $v \in V(G)$ , there is at most one  $T_i$  in which  $v$  is a nonleaf vertex. Given a set of spanning trees of  $G$ , you are asked to determine if they are CISTs.

### Technical Specifications

1. The number of test cases is smaller than or equal to 10.
2. The number of edges of a spanning tree is smaller than or equal to 20.

### Input Format

The first line contains an integer ( $\leq 10$ ) indicating the number of test cases. In each test case, the first line contains an integer  $2 \leq k \leq 10$  indicating the number of spanning trees. In the following  $k$  lines, each line contains the

descripton of a spanning tree. An edge between vertices  $x$  and  $y$  are denoted by  $x-y$  and there is a blank between two edges.

## Output Format

For each test case, output YES in a line if  $T_1, T_2, \dots, T_k$  are CISTs in a graph  $G$ , and NO otherwise.

## Sample Input

```
4
4
1-2 1-3 1-4 1-5 5-6 5-7 5-8
2-3 2-4 2-5 2-6 6-1 6-7 6-8
3-4 3-7 3-5 3-6 7-8 7-1 7-2
4-8 4-5 4-6 4-7 8-1 8-2 8-3
2
1-5 2-3 2-4 4-5 4-6
1-3 1-4 1-6 2-6 3-5
2
1-5 2-3 2-4 4-5 4-6
1-3 1-6 4-6 2-6 3-5
2
1-5 2-3 2-4 4-5 4-6
2-5 1-3 2-6 4-1 3-6
```

## Sample Output

```
YES
YES
NO
NO
```