

# **MATH552 Group Project**

Group 12

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# Stepwise Binomial Regression Analysis of Neonatal Care Unit Readmission Covariates

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## Abstract

Investigating the covariate relationships for High Risk Neonatal Unit (NNU) re-admission, using the quasi-binomial distribution GLM, and a forward-backward stepwise regression model. Resulting in the creation of a clear relationship between a mothers employment and education with the readmission of her child to a NNU.

## 1 Introduction

Investigating the impact of on high risk neonatal survivors within the first year of life, based on data-sets derived from Langley et al. 2002, and some statistics from that paper were influenced by Salt 2001. In this report a total of 166 units (76%) responded, and 120 (55%) were willing to participate in research, and it stated that there were no consistent guidelines / definitions for what a CNS was. Henceforth, some guidelines were created to categorise units:

1. Home visits offering nursing care and specialist advice for a minimum of five days a week for the first month after discharge from the Neonatal Unit (NNU)
2. Ad-hoc advice to families until the infant was at least 12 months old
3. A named nurse providing the link between primary and secondary health care services.

From the initial data set, a random set of 1488 samples was extracted, considering a response variable (readmission) for 10 covariates (see table 4 for 9 of the covariates, with total length of stay in hospital during initial admission not in this table). It is known that the economic impact of NNU readmission is high (Petrou et al. 2001, Boyle et al. 1983)

## 2 Methods

To analyse the data, the R packages provided by 'tidyverse' are used throughout. Before any statistical methods are created, the data is factorised, to allow for consistency. Upon this data some exploratory analysis is performed to see if there is any obvious relationships that can be seen from the visualisations of continuous variables versus factor variables. Violin plots composed upon scatter plots are used to depict the true distributions behind them. See Figure 1 for a comparison of gestation period with birthweight, it is clear that there is positive correlation between the factors, in addition, readmission to the NNU correlates with a lower birthweight respectively to each gestation period.

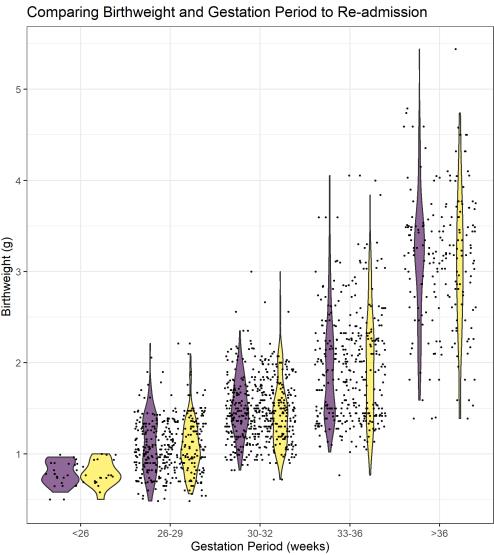


Figure 1: Gestation vs Birthweight for Re-admission. Purple - No readmission, Yellow - readmission

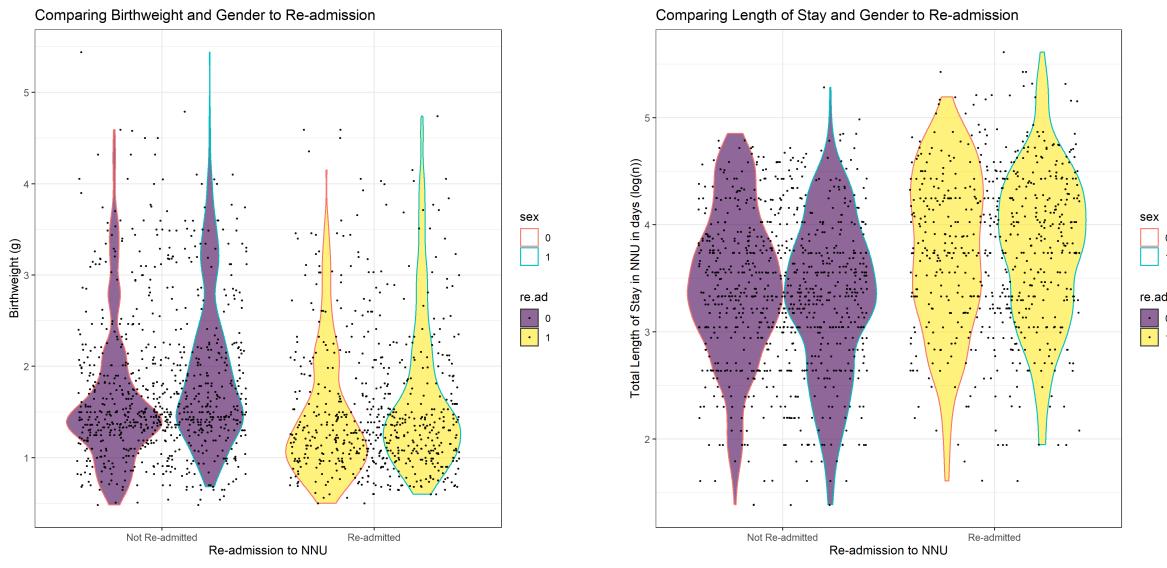


Figure 2: Birthweight and Length of Stay with Gender vs Re-admission. Outline : Blue - Male, Pink - Female

$$f(x, \pi) = \binom{n}{k} \pi^x (1 - \pi)^{n-x} \quad x = 0, 1, 2, \dots, n. \quad (1)$$

Using the binomial distribution (from Eq.1), and factoring the quantitative variables to form into dummy matrices, as in Equation 2. Where  $I$  is the identity matrix.

$$X_{\text{gest}} = \begin{bmatrix} x_1 & x_2 & x_3 & x_4 & x_5 \end{bmatrix} \Rightarrow X_{1488 \times 5} = I \quad (2)$$

By creating an initial generalised linear model (GLM), based on the binomial distribution presented in Equation 1, which considers all variable interactions and transformations. Thus the ‘los’ variable, total length of stay in hospital in log(days) during the initial admission, is added into a secondary model to determine if these are identical. Which would prove how impactful the secondary post-birth response variable is on the overall model.

	Residual DF	Residual Deviance	DF	Deviance	$P(> \chi)$
1	1404	1722.7			
2	1405	1768.7	-1	-46.068	0.0000

Table 1: Anova Comparison of Binomial GLM with and without the secondary response variable ‘los’

Knowing that ‘los’ does have an impact when included as a covariate, the model needs to be checked for over-dispersion. The expected variance of the data samples from the binomial distribution is  $\sigma^2 = n\pi(1 - \pi)$ , where  $n$  is the number of observations,  $\pi$  is the probability of belonging the set  $Y = 1$ . An over-discrepancy is defined as the observed variance of the response variable being greater than the expected variance of the binomial distribution. Over-dissociation can lead to seemingly bizarre standard error tests and imprecise significance tests. When over-dissociation occurs, the GLM function can still be used to fit the logistic regression, however the binomial distribution requires to be replaced by the Quasi-binomial Distribution. This can test for the occurrence of over-dispersion, if  $\phi > 1$ , it needs to be considered using quasi-likelihood. One way to detect an over-discrepancy is to compare the residual deviation of the binomial distribution model with the residual degrees of freedom if the ratio shown in Equation 3

$$\phi = \frac{\text{Residual Deviation}}{\text{Residual DF}} \quad (3)$$

If  $\phi > 2$ , we can consider that there is an over-dispersion. Fitting the model twice, in addition to using quasi-binomial for the second model.

The null hypothesis  $H0 : \phi = 1$  and alternative hypothesis  $H1 : \phi \neq 1$  can be tested by the provided p value. If P is very small (less than 0.05), we can reject the null hypothesis.

With both the forward and backward methods having obvious shortcomings, the forward not reflecting changes after the introduction of new independent variables, since the AIC corresponding to the regression equation is the minimum when introduced; the backward method has no chance to re-perform the regression equation, stepwise regression combines forward stepwise and backward stepwise. Whereby variables are entered one at a time, in each step it is re-evaluated, variables that do not contribute to the model are removed, and prediction variables may be added or deleted several times until the optimal model is obtained. Using ANOVA to compare the models, if there is no significant difference, we tend to use the stepwise regression model

### 3 Results

The GLM’s described in Section 2, the preliminary GLM with and without ‘los’ are graphed in Figures 4 and 3.

Comparing these two models using ANOVA, results in Table 1, it is clear that adding the ‘los’ variable has a significant effect on the model and the interactions with other covariates.

Calculating  $\phi$  from a binomial glm, using the formula in Eq.1,  $\phi = 1.254831$ . Although  $X > 1$ , it is still a small value, hence to quantitatively determine the analysis the p-value is calculated using a  $\chi^2_1$  test on the quasi-binomial model.  $P = 0.4950646$ , which is far larger than 0.05, as described in the null hypothesis, and therefore the quasi-binomial model can be used.

Using a stepwise regression model on the binomial GLM, in both directions attempting to reducing the AIC. (AIC = 1883)

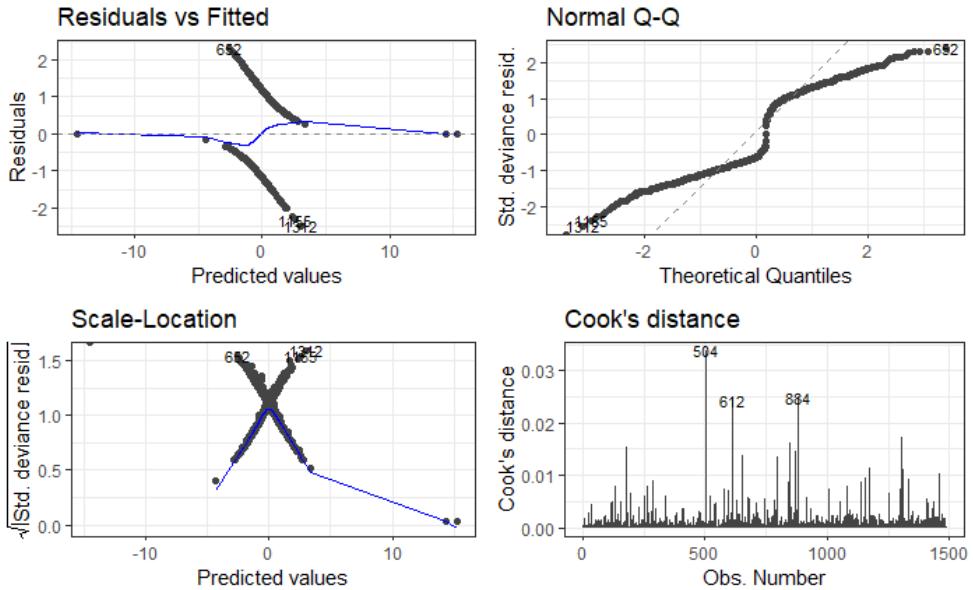


Figure 3: Preliminary GLM Model with 9 Covariates without ‘los’

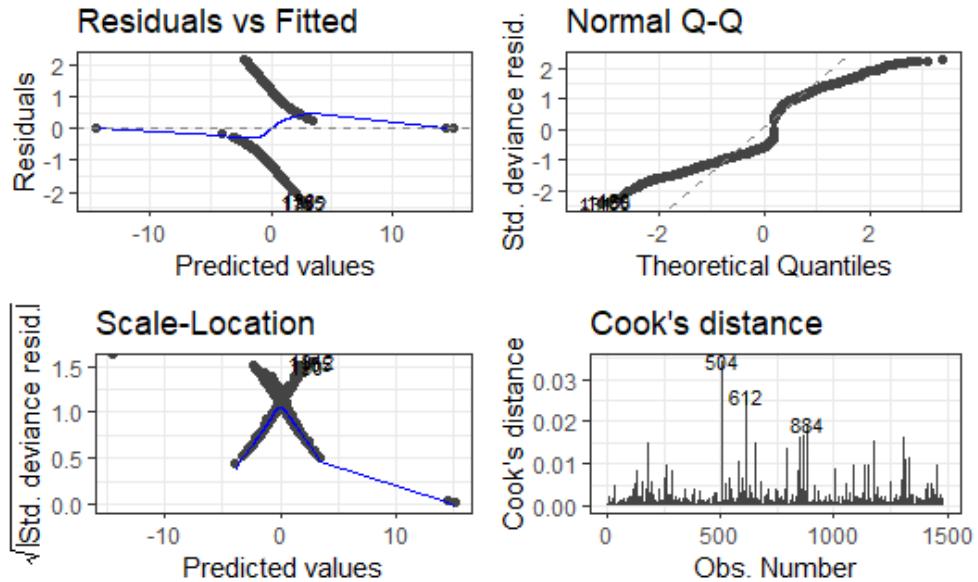


Figure 4: Preliminary GLM Model with 9 Covariates with ‘los’

and then performing an ANOVA test comparing the stepwise model with the original binomial, results in Table 2. Showing that  $P = 0.114 > 0.05$ , which is not significant. Therefore it can be judged that the two models are not significantly different at 95% confidence. The stepwise regression model is chosen to be the final model

From Table 3, mother employment (emp.f1) and mother education age (edu) have p-values larger than 0.05, which is not significant. All other coefficients of the covariates are deemed significant. Meanwhile the interaction of ‘emp.m1’ and ‘edu2’ have the greatest impact on the positive correlation of the model, and ‘emp.m1’ has the greatest impact on the negative correlation on the model. As can be seen from the residual vs fitted plot in Figure 5, there is no systematic correlation between the residual and the fitted values, which means that we do not need to perform a response

	Residual DF	Residual Deviance	DF	Deviance	$P(> \chi)$
1	1472	1850.8			
2	1452	1822.0	20	28.838	0.09101

Table 2: Anova Comparison of the standard binomial GLM with the stepwise binomial

	Estimate	Std. Error	Z Value	$P(> Z )$
	-2.92135	0.53208	-5.490	4.01e-08
cns1	-0.77454	0.36077	-2.147	0.03180
size1	1.23064	0.37916	3.246	0.00117
emp.f1	0.24307	0.35590	0.683	0.49463
emp.m1	-1.30891	0.56873	-2.301	0.02137
edu2	-0.44006	0.31121	-1.414	0.15735
edu3	0.12542	0.33830	0.371	0.71083
edu4	-0.21846	0.40323	-0.542	0.58798
los	0.76432	0.08051	9.493	1.2e-16
sex1	0.47432	0.11353	4.178	2.94e-05
accom1	-0.44403	0.14160	-3.136	0.00171
cns1:emp.f1	0.96974	0.38087	2.546	0.01089
size1:emp.f1	-1.24017	0.40183	-3.086	0.00203
emp.m1:edu2	1.39247	0.58795	2.368	0.01787
emp.m1:edu3	0.36251	0.61228	0.592	0.55381
emp.m1:edu4	1.04384	0.66234	1.576	0.11503

Table 3: Stepwise Binomial GLM Model Summary Results

transformation of the independent variables. The normal Q-Q plot shows the probability plot of the standarised residuals for the values corresponding to the normal distribution, which can be seen that the model largely satisfies the assumption of normality. If the assumption of constant variance is met, then in the Scale-Location graph, the points around the horizontal should be randomly distributed. The graph does not seem to meet this assumption. And the cooks distance plot shows a no clear skew of data.

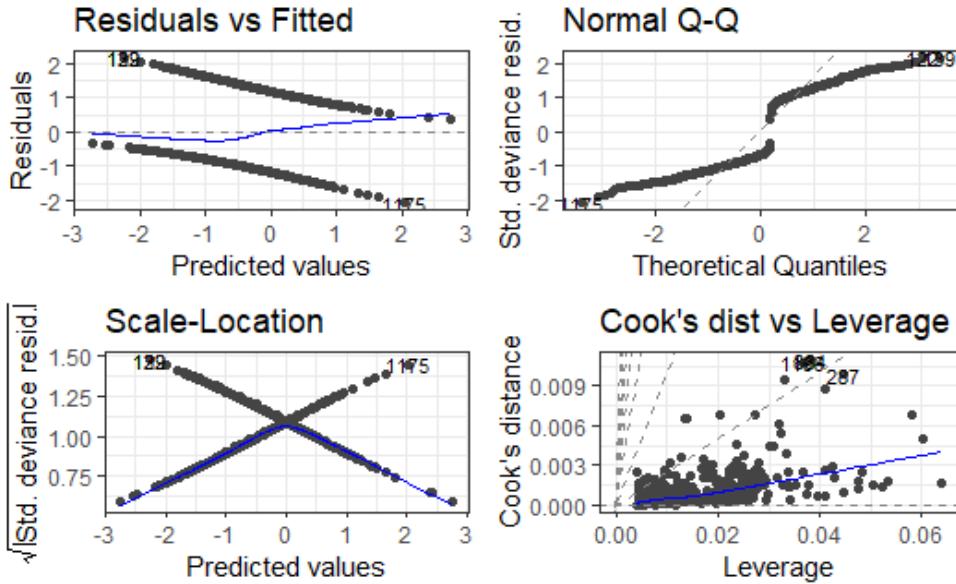


Figure 5: Stepwise Binomial GLM Model Summary Plots

## 4 Conclusions

In Section 3, various models are discussed and compared in detail, resulting in the stepwise binomial being chosen as the superior model for accuracy. This model showed that a mothers employment and the age at which she leaves full-time education largely drove her child's re-admission to hospital within 12 months. As well as, the size of the NNU; larger NNU's led to a higher probability of readmission, where as smaller NNU's let to smaller probabilities.

The model is good overall, but there are two shortcomings. Firstly, the model has high AIC values, which means that the

fit is not very good. Secondly, there are insignificant coefficients in the model, which reduces the model's goodness-of-fit and the adjusted  $R^2$

Further analysis of the data could include:

- Comparing other distributions for model fit goodness, as aswell as covariate matching, perhaps also investing de-factorisation according to normal distributions of the data
- More data points is always helpful to get a bigger picture, perhaps scaling this data to more NNU centers would result in better analysis. The NNU's that form this dataset may be from lower income areas, perhaps NNU's in higher income areas see less admission, or deviate from the main outcome of this report.

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## A Data Analysis Table

		NNU w/ CNS	NNU w/o CNS
Birth weight (g)	n	702 1649.42	786 1743.20
Gestation			
>26		19	25
26-29		191	193
30-32		261	239
33-36		209	146
>36		106	99
Gender			
Female		353	355
Male		433	347
Mother Employment			
Yes		694	631
No		92	71
Father Employment			
Yes		355	364
No		431	338
Age Mother Finish Edu			
<16		24	83
16-17		455	416
18-20		224	152
>20		83	81
Accomodation			
Yes		552	534
No		234	168
CNS Size			
Yes		552	505
No		234	197

Table 4: Covariate Values in Dataset