Computer-assisted content analysis

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Practicalities: Materials

We have a website:

http://ec2-52-207-214-68.compute-1.amazonaws.com:8787

Password: iqmr2016

Labs



Menu

Session 0: How could this possibly work?

Session 1: Dictionary-based 'classical' content analysis

Session 2: Classification and topic models

Session 3: Scaling models

Focus

Assumptions

Mechanics (in Lab)

Interpretation

Pitfalls

Topics

How to learn about

- party platforms
- legislative agendas
- parliamentary debates
- bloggers
- presidents
- international terrorists

by counting (lots of) words...

The transcendental question

What are the conditions for the possibility of learning about these things by counting words?

how could this possibly work?



ET IN ARCADIA EGO After Nicolas Poussin

Big picture

There is a *message* or *content* that cannot be *directly* observed, e.g.

The topic of my lecture, my position on a political issue, the importance of defence issues to a some political party.

and behaviour, including linguistic behaviour, e.g.

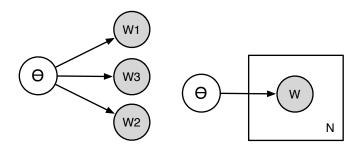
yelling, muttering, cursing, lecturing

which can be directly observed.

Focus on the expressed message and the words...

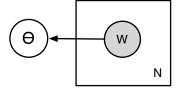
Communication

To communicate a message θ - to inform, persuade, demand, threaten, a producer (the speaker or writer) generates words of different kinds in different quantities



Communication

To *understand* a message the consumer (the hearer, reader, coder) uses those words to *reconstruct* the message



Communication

This is a stable (Searle, 1995) conventional (Lewis, 1969) but disruptable (Riker, 1996) communication process in which no finite set of words *uniquely* identifies any content (Quine, 1960; Davidson, 1977)

How to model this without having to solve the problems of linguistics (psychology, politics) first?

Rely on:

- instrumentality
- reflexivity
- randomness

Instrumentality from 'them'

Language use is as a *form of action* (Wittgenstein, 1953; Austin, 1975; Dawkins and Krebs, 1978)

Note the distinction between

'W means X'
versus

'W is used to mean X'

Instrumentality from us

The secret of quantitative political text analysis:

we aren't actually interested in words W that's for linguists...

we aren't actually interested in what's in your head θ that's for psychologists...

except as they help explain things we are interested in. They are *just data*.

Reflexivity

Politicians are often nice enough to talk as if they really do communicate this way

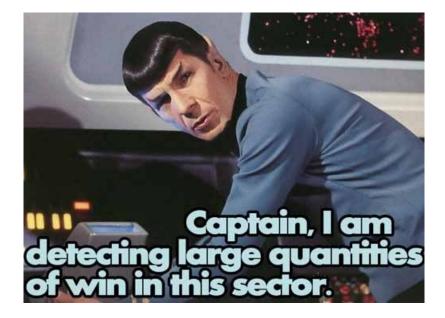
My theme here has, as it were, four heads. [...] The first is articulated by the word "opportunity" [...] the second is expressed by the word "choice" [...] the third theme is summed up by the word "strength" [and] my fourth theme is expressed well by the word "renewal" (M. Thatcher, 1979)

[2, 7, 2, 8] in 4431 words

Reflexivity

Or maybe just one theme...

A couple months ago we weren't expected to win this one, you know that, right? We weren't...Of course if you listen to the pundits, we weren't expected to win too much. And now we're winning, winning, winning the country - and soon the country is going to start winning, winning, winning.



Scope conditions

Computer-assisted content analysis works best when language usage is

stable, conventionalized, and instrumental

Implicitly, we usually condition on some institution, e.g.

courts, legislatures, online political argument, sports or financial reporting, survey responses

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(Notice that this inevitably creates a comparability problem)

Randomness

You almost never say exactly the same words twice, even when you haven't changed your mind about the message.

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We treat this process as *random* because we don't know or care about all the causes of variation

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(and because we're all secretly Bayesians)

Words as data

What do we know about words as data?

Words as data

What do we know about words as data?

They are difficult

- High dimensional
- Sparsely distributed (with skew)
- Not equally informative

Difficult words

Example: Labour party (2010) manifesto compared to other parties in two elections

High D. 8038 word types in two elections (adult native english speakers know \sim 20-35,000)

Sparse Of these, Labour only uses 4273 (53.16%)

Skewed Of these 1703 (21.19%) words appear exactly once, and 949 (11.81%) appear <5 times

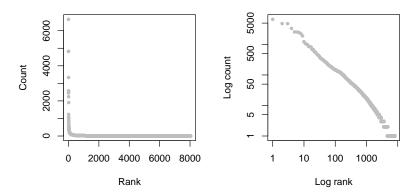
Difficult words

Words are not like your other data...

Zipf-Mandelbrot law (a pareto distribution in disguise)

$$P(w_i) \propto 1/r_i^{\alpha}$$

where r_i is the frequency rank of word i and $a \approx 1$ Very fat tailed...



Frequency is inversely proportional to substantive interestingness

Bottom 10:

| | Count |
|--------------------|-------|
| dream | 1 |
| flair | 1 |
| world-beating | 1 |
| globally-respected | 1 |
| underdog | 1 |
| heading | 1 |
| frustrations | 1 |
| unruly | 1 |
| walk | 1 |
| out-of-control | 1 |

Top 10

| | Count |
|------|-------|
| the | 6648 |
| and | 4823 |
| to | 4817 |
| of | 3335 |
| will | 2574 |
| we | 2546 |
| а | 2454 |
| in | 2237 |
| for | 1905 |
| that | 1232 |
| | |

Top 10 minus the 'standard' stopwords

| | Count |
|------------|-------|
| will | 2574 |
| people | 692 |
| new | 559 |
| government | 458 |
| local | 404 |
| work | 354 |
| support | 334 |
| britain | 326 |
| make | 322 |
| public | 311 |

Removing stopwords, while standard in computer science, is not necessarily better...

Example:

Standard collections contain, 'him', 'his', 'her' and 'she'.

Words you'd want to keep when analyzing a abortion debates.

For large amounts of text summaries are not enough.

We need a model to provide assumptions about

- equivalence
- exchangeability

The standard set of equivalence assumptions are the 'bag of words'.

Specifically:

Punctuation invariance

As I look ahead I am filled with foreboding. Like the Roman I seem to see 'the river Tiber flowing with much blood'..."
(E. Powell, 1968)

Punctuation invariance

As I look ahead I am filled with foreboding. Like the Roman I seem to see 'the river Tiber flowing with much blood'..."
(E. Powell, 1968)

| token |
|-------|
| as |
| i |
| look |
| ahead |
| i |
| am |
| ••• |
| |

| index | token |
|-------|-------|
| 1 | like |
| 2 | the |
| 3 | roman |
| 4 | i |
| 5 | seem |
| 6 | to |
| 7 | ••• |

Lexical univocality

| type | count |
|-------|-------|
| as | 1 |
| i | 2 |
| look | 1 |
| ahead | 1 |
| am | 1 |
| ••• | |

| token | count |
|-------|-------|
| like | 1 |
| the | 1 |
| roman | 1 |
| i | 1 |
| seem | 1 |
| to | 1 |
| | |

Order invariance

| | | unit | |
|------|-------|---------|---------|
| | | 'doc' 1 | 'doc' 2 |
| type | ahead | 1 | 0 |
| | am | 1 | 0 |
| | as | 1 | 0 |
| | i | 2 | 1 |
| | like | 0 | 1 |
| | look | 1 | 0 |
| | roman | 0 | 1 |
| | seem | 0 | 1 |
| | the | 0 | 1 |
| | to | 0 | 1 |
| | | | |

Count data

We have turned a corpus into a contingency table.

(Or a term-document / document-term / document-feature matrix, in the lingo)

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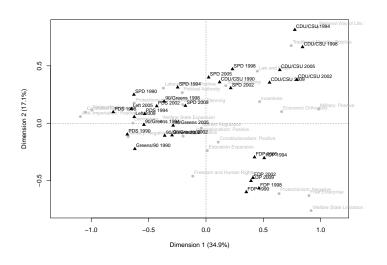
Everything you learned in your categorical data analysis course applies

except that the variables of interest: θ are not observed

What we want

| | ahead | am | i | like | look | |
|----------------|---------------|------------|-------------|--------------|----------------|-------------------------------------|
| doc 1 doc 2 | 1 0 | | | 0 1 | | $	heta_{ m doc1}$ $	heta_{ m doc2}$ |
| | eta_{ahead} | eta_{am} | β_{i} | eta_{like} | β_{look} | |

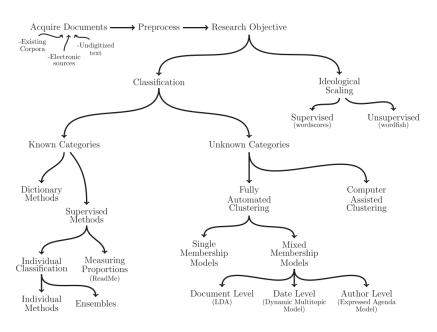
Visualized

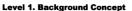


What is this content θ ?

What is the content in content analysis?

- Documents are mixtures of categories: policy agenda of a speech
- Documents have categories: topic of a press release
- Documents have positions: ideological position of a legal brief





The broad constellation of meanings and understandings associated with a given concept.

Task: Conceptualization

Formulating a systematized concept through reasoning about the background concept, in light of the goals of research.

Task: Revisiting Background

Concept. Exploring broader issues concerning the background concept in light of insights about scores, indicators, and the systematized concept.

Level 2. Systematized Concept A specific formulation of a concept used by a

A specific formulation of a concept used by a given scholar or group of scholars; commonly involves an explicit definition.

Task: Operationalization

Developing, on the basis of a systematized concept, one or more indicators for scoring/classifying cases.

Task: Modifying Systematized

Concept. Fine-tuning the systematized concept, or possibly extensively revising it, in light of insights about scores and indicators.

Level 3. Indicators

Also referred to as "measures" and "operationalizations." In qualitative research, these are the operational definitions employed in classifying cases.

Task: Scoring Cases

Applying these indicators to produce scores for the cases being analyzed.

Task: Refining Indicators

Modifying indicators, or potentially creating new indicators, in light of observed scores.

Level 4. Scores for Cases

The scores for cases generated by a particular indicator. These include both numerical scores and the results of qualitative classification

Commitment issues

What are we committing to in this quantitative content analysis framework?

Probably less than you think...

Assumptions:

 θ is socially/institutionally constructed: only linguists care about the real thing

There are no differences in θ that make no verbal difference (basically Pragmatism)

Theory / measurement separation

Discourse analytic approaches tend to *tightly couple* theory and 'measurement' components

(This is contingent...)

We will try as far as possible to separate them...

Our concerns: validity, stability

Rely on: transparency, reliability, replicability

Statistical models of words: Poisson

Word counts/rates are conditionally Poisson:

$$W_j \sim \text{Poisson}(\lambda_j)$$

Expected W_j (and its variance) is λ_j

Models are naturally *multiplicative*. Rates increase by 10%, decrease by 20% Conditional on what? Typically on θ



Statistical models of words: Multinomial

For fixed document lengths, counts are conditionally Multinomial:

$$W_1 \dots W_V \sim \text{Multinomial}(W_1 \dots W_V; \Pi_1 \dots \Pi_V, N_i)$$

Expected W_i is Nn_i

Covariance of W_i and W_j is $-N\pi_i\pi_j$ (budget constraint)



Implication: Absence is an observation

Don't be fooled...

Statistical models of text deal with *absence* as well as presence: zeros count

Absence is informative to the extent it is surprising Surprise implies expectations; expectations imply a model.

Looking ahead: Modeling strategies

We can model the content of a term-document matrix in several ways

- $\theta \leftarrow$ words: Go for $P(\theta \mid \text{words})$ directly

 Requires some observed θ , and lots of careful regression modeling, or manual coding
- $\theta \longrightarrow$ words: Get $P(\theta \mid \text{words})$ indirectly

 Model words as a function of θ , add a prior, and infer θ using Bayes theorem

$$P(\theta \mid \text{words}) = \frac{P(\text{words} \mid \theta)P(\theta)}{\sum_{k}^{\theta} P(\text{words} \mid \theta_{k})P(\theta_{k})}$$

Classical content analysis

Content is, or is constructed from, categories e.g.

human rights, welfare state, national security

Substantively these often have valence, e.g.

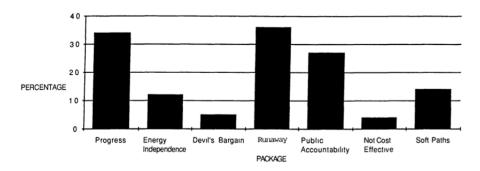
pro-welfare state vs. anti-welfare state, lots of CMP categories

But they are invariably treated as *nominal level* variables

We are typically interested in them for

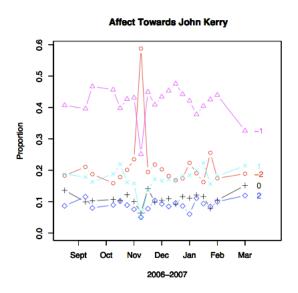
simple descriptions, making comparisons, tracing temporal dynamics

Talking Like a newspaper



Gamson and Modigliani (1989)

Talking like a candidate



Talking like a terrorist

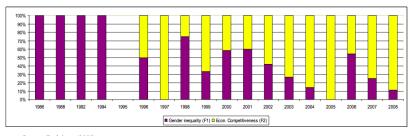
| | Bin Ladin | Zawahiri | Controls | p |
|-------------------------------------|----------------|----------------|----------|---------|
| | (1988 to 2006) | (2003 to 2006) | N = 17 | (two- |
| | N = 28 | N = 15 | | tailed) |
| Word Count | 2511.5 | 1996.4 | 4767.5 | |
| Big words (greater than 6 letters) | 21.2a | 23.6b | 21.1a | .05 |
| Pronouns | 9.15ab | 9.83b | 8.16a | .09 |
| I (e.g. I, me, my) | 0.61 | 0.90 | 0.83 | |
| We (e.g. we, our, us) | 1.94 | 1.79 | 1.95 | |
| You (e.g. you, your, yours) | 1.73 | 1.69 | 0.87 | |
| He/she (e.g. he, hers, they) | 1.42 | 1.42 | 1.37 | |
| They (e.g., they, them) | 2.17a | 2.29a | 1.43b | .03 |
| Prepositions | 14.8 | 14.7 | 15.0 | |
| Articles (e.g. a, an, the) | 9.07 | 8.53 | 9.19 | |
| Exclusive Words (but, exclude) | 2.72 | 2.62 | 3.17 | |
| Affect | 5.13a | 5.12a | 3.91b | .01 |
| Positive emotion (happy, joy, love) | 2.57a | 2.83a | 2.03b | .01 |
| Negative emotion (awful, cry, hate) | 2.52a | 2.28ab | 1.87b | .03 |
| Anger words (hate, kill) | 1.49a | 1.32a | 0.89b | .01 |
| Cognitive Mechanisms | 4.43 | 4.56 | 4.86 | |
| Time (clock, hour) | 2.40b | 1.89a | 2.69b | .01 |
| Past tense verbs | 2.21a | 1.63a | 2.94b | .01 |
| Social Processes | 11.4a | 10.7ab | 9.29b | .04 |
| Humans (e.g. child, people, selves) | 0.95ab | 0.52a | 1.12b | .05 |
| Family (mother, father) | 0.46ab | 0.52a | 0.25b | .08 |
| Content | | | | |
| Death (e.g. dead, killing, murder) | 0.55 | 0.47 | 0.64 | |
| Achievement | 0.94 | 0.89 | 0.81 | |
| Money (e.g. buy, economy, wealth) | 0.34 | 0.38 | 0.58 | |
| Religion (e.g. faith, Jew, sacred) | 2.41 | 1.84 | 1.89 | |

Note. Numbers are mean percentages of total words per text file. Statistical tests are between Bin Ladin, Zawahiri, and Controls. Documents whose source indicates "Both" (n=3) or

[&]quot;Unknown" (n=2) were excluded due to their small sample sizes.

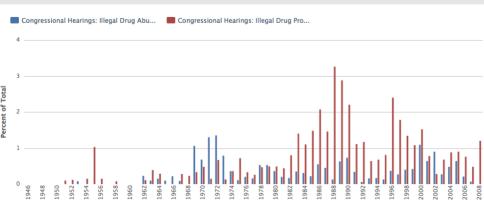
Talking like the European Commission

Figure 4.2-2 Relative proportions of policy frames F1 and F2 in secondary EU legislation



Source: Radulova (2009)

Talking About drugs



The Congressional Bills Project website (retrieved 2010)

Classical content analysis

Categories are

equivalence classes over words representable as assignments of a K-valued category membership variable Z to each word

Topics

Documents

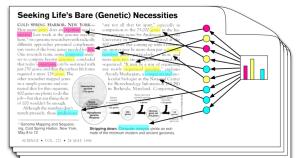
Topic proportions and assignments



life 0.02 evolve 0.01 organism 0.01

brain 0.04 neuron 0.02 nerve 0.01

data 0.02 number 0.02 computer 0.01

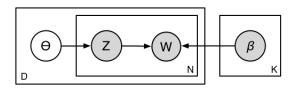


Classical content analysis

Every word W has an topic Z

The word W to topic Z mapping β is provided by the researcher as a *content analysis dictionary*

The content of a document θ is the proportion (or count) of each category



How content is generated and what we claim to know

Content analysis dictionary

```
ECONOMY
            +STATE
            accommodation
            age
            ambulance
            assist
            benefit
            -STATE
            assets
            bid
            choice*
            compet*
            constrain*
```

from Laver and Garry's (2000) dictionary

As a posterior: P(Z | W)

Dictionary is an explicit and very *certain* statement of $P(Z \mid W)$

| | Z | state reg | market econ |
|---|---------|-----------|-------------|
| W | age | 1 | 0 |
| | benefit | 1 | 0 |
| | | | ••• |
| | assets | 0 | 1 |
| | bid | 0 | 1 |
| | ••• | ••• | ••• |

...from a underspecified likelihood

The *only* way this could be true is if the data had been generated like

| | $P(W \mid Z)$ | |
|--------------------|---------------|-------------|
| | state reg | market econ |
| P(age Z) | а | 0 |
| P(benefit Z) | b | 0 |
| | | |
| P(assets Z) | 0 | С |
| <i>P</i> (bid Z) | 0 | d |
| | | ••• |
| | | |

...leading to a posterior over content

Define the category *counts*

$$Z_k = \sum_{i}^{N} P(Z = k \mid W_i)$$

and estimate category relative proportions using

$$\hat{\theta}_k = \frac{Z_k}{\sum_j^K Z_j}$$

(When θ is a set of multinomial parameters, and the model assumptions are correct, this could be a reasonable estimator)

Reconstruction

Dictionary-based content analysis was not developed this way

Originally (e.g. Stone 1966) there was no probability model at all

Connecting CCA content to politics

We're usually interested in category proportions per unit (usually document), e.g.

How much of this document is about national defense?

What is the *difference* of aggregated left and aggregated right categories (RILE)

How does the *balance* of human rights and national defense change over time?

Inference About content

Statistically speaking, the three types of measures are

- a proportion
- a difference of proportions
- a ratio of proportions

Under certain sampling assumptions we can make inferences about a population

Inference About proportions

Example: in the 2001 Labour manifesto there are 872 matches to Laver and Garry's *state reg* category

0.029 (nearly 3%) of the document's words0.066 (about 6%) of words that matched *any* categories

The document has 30157 words, so the *first* proportion is estimated as

$$\hat{\theta}_{\text{state reg}} = 0.029 \, [0.027, 0.030]$$

What does this mean?

Inference about proportions

Think of the party headquarters repeatedly *drafting* this manifesto

The true proportion - the one suitable to the party's policies - is fixed but every draft is slightly different

The confidence interval reflects the fact that we expect long manifestos to have more precise information about policy

This interval is computed as if every word was a new (conditionally) independent piece of of information

Reporting: Rates

Don't report proportions if you don't need to.

Rates/ratios are more intuitive

e.g. the rate of dictionary matches per B words is

$$\lambda_B = \theta B$$

which is a more interpretable proportion, e.g.

29 times per 1000 words

Different measures correspond to different choices of *B*.

Ratios: How new was New Labour?

Was the Conservative party in 1992 more or less for state intervention than 'New' Labour in 1997?

Compare instances of *state reg* and *market econ* in the manifestos

| Party | Counts | | |
|--------------|-----------|-------------|--|
| Conservative | state reg | market econ | |
| | 0_0 | 268 | |
| Labour | 396 | <u> </u> | |

Risk ratios

Compute two risk ratios:

$$RR_{state \ reg} = rac{P(state \ reg \mid cons)}{P(state \ reg \mid lab)}$$
 $RR_{market \ econ} = rac{P(market \ econ \mid cons)}{P(market \ econ \mid lab)}$

and 95% confidence intervals

Interpreting risk ratios

If RR = 1 then the category occurs at the same rate in labour and conservative manifestos

If RR = 2 then the conservative manifesto contains *twice* as much *state reg* language as the labour manifesto

If RR = .5 then the conservative manifesto contains half as much state reg language as the labour manifesto

If the confidence interval for RR contains 1 then we no evidence that state reg and market econ occur at different rates

Risk ratios

| | Risk Ratio |
|-------------|-------------------|
| market econ | 1.45 [1.26, 1.67] |
| state reg | 0.49 [0.42, 0.57] |

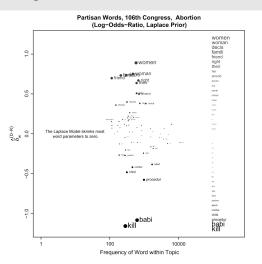
Conservative manifesto generates *market econ* words 45% more often

$$45\% = 100(1.45 - 1)\%$$

Conservative manifesto only generates 49% as many *state reg* words as Labour.

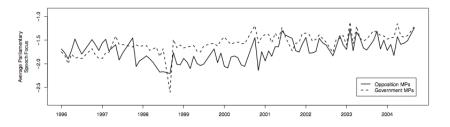
Equivalently Labour generates them about twice as often

(Regularised) log ratios



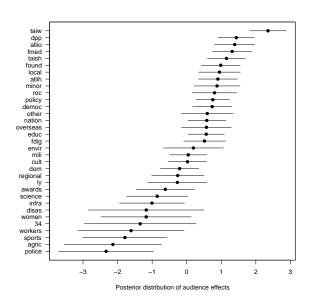
...as dependent variable

Example: district vs party focus



Data: [district words, party words] (Kellerman & Proksch, MS)
Here, a logged ratio of two categories

Content as something to explain



OK, how do I make such a dictionary?

Find a suitable tool

Maximise measurement validity

Minimise measurement error

OK, how do I make such a dictionary?

Find a suitable tool

Maximise measurement validity

Minimise measurement error

(Sell high, buy low)

Find a suitable tool

Wordstat

LIWC (maybe don't)

Hamlet

Atlas-ti (?)

Yoshikoder



The source of measurement error

Measurement error in classical content analysis is primarily failure of *this* assumption:

| | $P(Z = state \ reg \mid W)$ | $P(Z = market econ \mid W)$ |
|---------|-----------------------------|-----------------------------|
| age | 1 | 0 |
| benefit | 1 | 0 |
| ••• | | ••• |
| assets | 0 | 1 |
| bid | 0 | 1 |
| | | |

Consequences of measurement error

What are the effects of measurement error in category counts?

Being directly wrong, e.g.

Estimated rates are too low (bias)

Some of estimates are more biased than others

Being indirectly wrong, e.g.

Subtractive or ratio left-right measures are too centrist

Assume

a vocabulary of only two words 'benefit' and 'assets' a subtractive measure of position: $Z_{market\;econ}-Z_{state\;reg}$

Then we hope that

| | $P(Z = state \ reg \mid W)$ | $P(Z = market econ \mid W)$ |
|---------|-----------------------------|-----------------------------|
| benefit | 1 | 0 |
| assets | 0 | 1 |

but what if...

| | state reg | market econ |
|----------------|-----------|-------------|
| P(benefit Z) | 0.7 | 0.2 |
| P(assets Z) | 0.3 | 0.8 |

$$P(W='asset' \mid Z=state \ reg) > 0$$

SO

Assume

$$Z_{market \, econ} = 10$$

 $Z_{state \, reg} = 20$

Then the true difference is

$$\frac{(10-20)}{(10+20)} = -0.33\tag{1}$$

Under perfect measurement this would be realised on average as

20 'benefit'

10 'assets'

Under imperfect measurement it is realised on average as

```
16 'benefit'
```

(14 from state reg but 2 from market econ)

14 'assets'

(8 from market econ but 6 from state reg)

The proportional difference measure is now

$$\frac{(14-16)}{(14+16)} = -0.07\tag{2}$$

Apparently much closer to the centre, but only because of measurement error

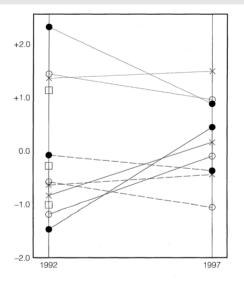
The proportional difference measure is now

$$\frac{(14-16)}{(14+16)} = -0.07\tag{2}$$

Apparently much closer to the centre, but only because of measurement error

All relative measures will have this problem

In action (Laver and Garry 2000)



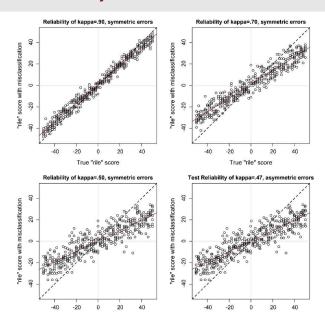
In action with people, not dictionaries

Table 3 Misclassification matrix for true versus observed Rile

| | | True Rile category | | | |
|-------|---------------------|--------------------|------|-------|-------|
| | | Left | None | Right | Total |
| | Left | 430 | 188 | 100 | 718 |
| | | 0.59 | 0.19 | 0.11 | |
| Coded | None | 254 | 712 | 193 | 1159 |
| Rile | | 0.35 | 0.70 | 0.20 | |
| | Right | 41 | 115 | 650 | 806 |
| | | 0.06 | 0.11 | 0.69 | |
| | Total | 725 | 1015 | 943 | 1668 |
| | False negative rate | 0.41 | 0.30 | 0.31 | |
| | False positive rate | 0.15 | 0.27 | 0.09 | |

Note. The top figure in each cell is the raw count; the bottom figure is the column proportion. The figures are empirically computed from combined British and New Zealand manifesto tests. The false negative rate is 1—sensitivity, whereas the false positive rate is 1—specificity.

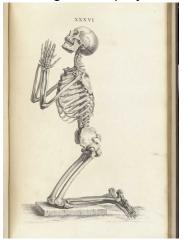
Attentuation (Mikhaylov et al. 2012)



Solutions: A quasi-theological approach

Solutions: A quasi-theological approach

'Thoughts and prayers'



Solutions: avoid it

An often non-obvious fact about content dictionaries:

precision: proportion of words used the way your dictionary assumesrecall: proportion of words used that way that are in your

recall: proportion of words used that way that are in your dictionary

always trade-off...

Aside: precision and recall

Every field reinvents this distinction:

precision and recall specificity and sensitivity users and producer's accuracy type 1 and type 2 error sins of omission and sins of commission

Tools to evaluate items

Keyword in context analyses (KWIC) allow you to scan all contexts of a word

How many of them are the sense or usage you want?

| | contextPre | keyword | contextPost |
|----|--|------------|-------------------------------------|
| 1 | also keep all the other | benefits | that pensioners currently receive, |
| 2 | regulation will have to have | benefits | exceeding costs, and regulations |
| 3 | and Controlled Immigration Britain has | benefited | from immigration. We all |
| 4 | positive contribution But if those | benefits | are to continue to flow |
| 5 | Nor ther n Ireland brings | benefits | to all parts of our |
| 6 | their home, will also | benefit | first- time buyers. |
| 7 | you help yourself; you | benefit | and the country benefits. |
| 8 | you benefit and the country | benefits | . So now, I |
| 9 | result of our tax and | benefit | measures compared to 1997. |
| 10 | result of personal tax and | benefit | measures introduced since 1997, |
| 11 | , the savings on unemployment | benefits | will go towards investing more |
| 12 | trebled the number on incapacity | benefits | . We will help 17 |
| 13 | Work programme and reform Incapacity | Benefit | , with the main elements |
| 14 | main elements of the new | benefit | regime in place from 2008 |
| 15 | stronger penalties. To the | benefit | of business and household consumers |
| 16 | effective directive to provide real | benefits | to consumers and new opportunities |
| 17 | better.We are examining the potential | benefits | of a parallel Expressway on |
| 18 | ways to lock in the | benefit | of new capacity. We |
| 19 | are determined to spread the | benefits | of enterprise to every community |
| 20 | to get ahead, to | benefit | from improving public services, |
| 21 | of the school workforce is | benefiting | staff and helping to tailor |
| 22 | teachers and pupils get the | benefit | of the range of support |

Measurement error: Confession and forgiveness

Under measurement error

- A observed category proportions are generated by a *mixture* of categories
- The weights for this mixture are the true category proportions

Given the error matrix, we can *infer* the true proportions Intuition

$$P(W) = \sum_{k}^{K} P(W \mid Z = k) P(Z = k)$$

has the form

$$Y = X\theta$$

Measurement error: model it

In our previous example

$$\begin{bmatrix} 0.53 \\ 0.46 \end{bmatrix} = \begin{bmatrix} 0.7 & 0.2 \\ 0.3 & 0.8 \end{bmatrix} \begin{bmatrix} \theta_1 \\ \theta_2 \end{bmatrix}$$

is solved exactly as [0.66, 0.33]

by inverting the error matrix

Measurement error: model it

Applied to Mikhaylov human error data:

| | L | N | R | | | L | N | R |
|---|-----|-----|-----|-------------------|---|------|------|------|
| L | 430 | 188 | 100 | \Longrightarrow | L | 0.59 | 0.19 | 0.11 |
| Ν | 254 | 712 | 193 | | Ν | 0.35 | 0.70 | 0.20 |
| R | 41 | 115 | 650 | | R | 0.06 | 0.11 | 0.69 |

Implication:

If [L, N, R] were [20, 0, 10] we would *expect* to see about [13, 9, 8]

Measurement error: model it

Invert $P(C \mid T)$:

| | L | N | R |
|---|-------|-------|-------|
| L | 2.00 | -0.50 | -0.16 |
| Ν | -1.00 | 1.75 | -0.37 |
| R | 0.00 | -0.25 | 1.52 |

and multiply to get an estimate of the true counts...

Example:

$$[13, 9, 8] \longrightarrow [20.19, -0.16, 9.98] \approx [20, 0, 10]$$

Notes:

Some patterns of measurement error cannot be corrected for...

These results hold in expectation.

We are ignoring measurement error in the error matrix

This is a linear method that may violate prior constraints

Works for anything that makes errors (human or machine)

Up next

Topic models, e.g. Latent Dirichlet Allocation (Blei et al.) we

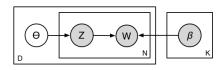
Build this idea into a complete model infer rather than assert the relationship between W and Z by learning β .

Up next

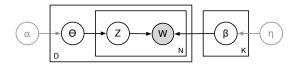
Topic models, e.g. Latent Dirichlet Allocation (Blei et al.) we

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From



to



Lab time

