Handout 8

Student von Student III

In this handout, we will learn how to test difference-in-means using the function 1m. We will include some more practice using loops.

Topics and Concepts Covered

- attach to attach data frames
- \$res and \$fit to recover the fitted values and residuals in a linear model
- I() to add new terms to a linear model
- coplot for a conditional plot
- pch for plotting characters in a figure (1 = open circle, 19=filled circle)

Before working on these problems, please make sure that you have worked through the online handout: link

attach to Attach Data Frames

So far, you have had to use the syntax data.frame\$variable in order to recover variable from the object data.frame. After using the command attach once at the beginning of your code, you can call the variable directly. For an example, the file GDPNorAm.csv in the data folder contains 188 observations, which consist of the country name, 2008 GDP (according to the World Bank), and an indicator variable that takes on a value of 1 if the country is in North America. To see how attach works, first load in the data, and make a table of the variable north.america:

```
Data.gdp <- read.csv("data/GDP_NorAm.csv", header = TRUE)
table(Data.gdp$north.america)</pre>
```

0 1 167 20

which tells us that there are 20 North American countries in this dataset.

To see which countries are in North America, we can run

Data.gdp\$country[Data.gdp\$north.america == 1]

```
[1] Antigua and Barbuda Bahamas, The
                                              Barbados
 [4] Belize
                         Canada
                                              Costa Rica
 [7] Dominica
                         Dominican Republic El Salvador
[10] Grenada
                         Guatemala
                                              Haiti
[13] Honduras
                         Jamaica
                                              Mexico
[16] Nicaragua
                         Panama
                                              St. Kitts and Nevis
[19] Trinidad and Tobago United States
187 Levels: Afghanistan Albania Algeria Angola ... Zimbabwe
```

Now, if we wanted to access these variables without having to write out Data.gdp\$ each time, we could run

```
attach(Data.gdp)
table(north.america)
```

```
north.america
0 1
167 20
```

country[north.america == 1]

```
[1] Antigua and Barbuda Bahamas, The
                                              Barbados
 [4] Belize
                         Canada
                                              Costa Rica
 [7] Dominica
                         Dominican Republic El Salvador
[10] Grenada
                         Guatemala
                                              Haiti
[13] Honduras
                         Jamaica
                                              Mexico
[16] Nicaragua
                         Panama
                                              St. Kitts and Nevis
[19] Trinidad and Tobago United States
187 Levels: Afghanistan Albania Algeria Angola ... Zimbabwe
```

Be careful to attach only once each R session!

If you attach the same data frame multiple times, you run the risk of confusing both R and yourself.

\$res and \$fit to Recover Fitted Values and Residuals

We have been using lm to generate linear models. This function follows the syntax $lm(Y \sim X1 + X2 + X3)$ where Y is the dependent variable and the independent variables are X1, X2, and X3. Let's say we save a linear model as

```
lm1 < - lm(Y \sim X1 + X2 + X3)
```

If we wanted to add $X1^2$ to the model we need to do the calculation *inside* the I function so that the new variable we make on the fly is computed before R thinks about interpreting the rest of the formula. Like this:

```
lm1 \leftarrow lm(Y \sim X1 + I(X1^2) + X2 + X3)
```

We could also accomplish through defining a new variable X1.sq <- X1^2 and then write

```
lm1 < - lm(Y ~ X1 + X1.sq + X2 + X3)
```

Either method is acceptable.

If we wanted to look at the residuals, we would type lm1\$res. To get the fitted values we would type lm1\$fit

Alternatively there are functions fitted and resid that do this extraction for you. Often these are a bit clearer. Then to get the residuals you would type resid(lm1) and to get the fitted values you would type fitted(lm1).

Again, either method is acceptable.

To plot residuals against fitted values - a useful diagnostic - we could either

```
plot(lm1$fit, lm1$res,
    main = "Fitted vs. Residual Plot",
    xlab="Fitted Values", ylab = "Residuals")
```

or

```
plot(fitted(lm1), resid(lm1),
    main = "Fitted vs. Residual Plot",
    xlab="Fitted Values", ylab = "Residuals")
```

R knows that this is a useful plot, so you can get it directly using plot on the linear model object like this:

Using I to Add New Terms to a Linear Model

In a classic paper Mankiw, Romer, and Weil (1992) investigate the determinants of long-term economic growth. In particular, they empirically explore the Solow growth model using cross-country data. The paper uses as its starting point the Solow growth model, which predicts both the steady-state GDP per capital of a country as a function of its savings rate and population growth, in addition to predicting the rate at which countries 'converge' to this steady-state. The paper demonstrates empirically that the Solow growth models the data well when both human capital and physical capital are considered.

In the data folder you will find the file international_growth_data.csv, which contains the data from the Mankiw, et al. study. First, we are going to read it in, and take a look at what variables it contains

The following object is masked from Data.gdp:

country

The Solow growth model makes some very specific predictions about the relationships among these variables. Specifically,

```
\log[\text{gdpperadult}1985]_i = \alpha + \beta_k \log[\text{investmentpergdp}/100]_i + \tag{1}
```

$$\beta_P log[\text{workingagepopgrowth}/100 + 0.05]_i + \epsilon_i$$
 (2)

The model predicts $\beta_k = \frac{1}{2}$, $\beta_p = -\frac{1}{2}$. Unfortunately, our data is defined in terms of the raw values, not logs. Therefore, in this example, we will use I to put in the correct variables.

```
Call:
```

Coefficients:

```
Estimate Std. Error
(Intercept)
                                                                1.6496
                                                      9.6293
I(log(investment_per_gdp/100))
                                                      1.4780
                                                                 0.1631
I(log(working_age_pop_growth_1960to198/100 + 0.05)) -0.4573
                                                                 0.5837
                                                    t value Pr(>|t|)
(Intercept)
                                                      5.837 6.08e-08 ***
I(log(investment_per_gdp/100))
                                                      9.063 8.32e-15 ***
I(log(working_age_pop_growth_1960to198/100 + 0.05)) -0.784
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.7938 on 104 degrees of freedom
  (14 observations deleted due to missingness)
Multiple R-squared: 0.4767,
                               Adjusted R-squared: 0.4667
F-statistic: 47.37 on 2 and 104 DF, p-value: 2.365e-15
```

These names are too long, so let's clean them up through creating new variables, instead of using I:

```
log.dv <- log(gdp_per_adult_1985)
log.invest <- log(investment_per_gdp / 100)
log.pop <- log(working_age_pop_growth_1960to198 / 100 + .05)
lm1 <- lm(log.dv ~ log.invest + log.pop)</pre>
```

From looking at the output, the second coefficient is approximately -0.5, as expected. The first coefficient is not very close. In fact, we can calculate how far away it is:

```
summary(lm1)$coef
```

```
Estimate Std. Error t value Pr(>|t|)

(Intercept) 9.6292513 1.6495650 5.8374487 6.082868e-08

log.invest 1.4779957 0.1630853 9.0627170 8.316214e-15

log.pop -0.4573491 0.5836656 -0.7835807 4.350671e-01

beta <- summary(lm1)$coef[2,1]

beta
```

[1] 1.477996

```
sigma <- summary(lm1)$coef[2,2]
sigma</pre>
```

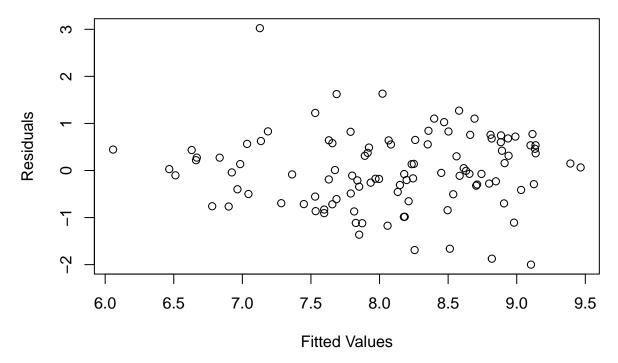
[1] 0.1630853

```
(beta - 0.5) / sigma
```

[1] 5.996836

The estimate coefficient is about 6 standard deviations from the value predicted by Solow's theory - a discrepancy not likely to occur due to chance (i.e. a 'significant difference').

```
plot(lm1$fit, lm1$res,
    main = "Fitted vs. Residual Plot",
    xlab = "Fitted Values", ylab = "Residuals")
```

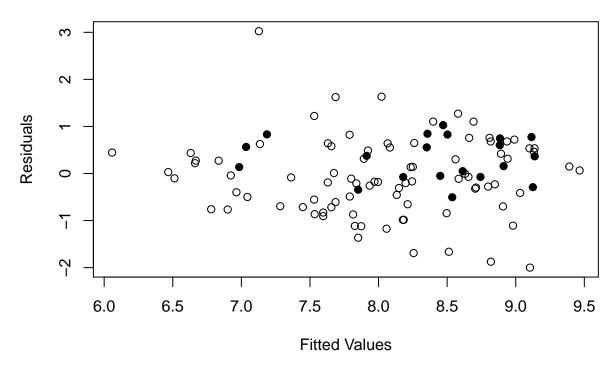


Simply by looking at the figure, there appears nothing wrong - no signs of 'fanning out' to indicate heteroskedasticity, and no curvature that would leave you worried about missing quadratic terms.

Using pch to Vary Plotted Points on a Figure

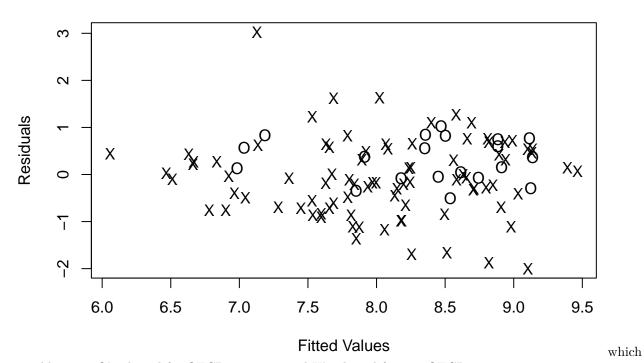
Now, Professor Solow is no slouch; neither is Professor Mankiw. In this section, we are going to examine the residual plots in order to identify an additional variable, schooling, that needs to be included in order to recover Solow's results. First, we are going to explore whether being in the OECD is a missing variable. If the OECD countries have residuals systematically above or below the residuals of non-OECD countries, we would argue that we need to add OECD to the regression. We can assess this in the fitted-residual plot, by plotting OECD countries with a solid dot and non-OECD countries with an open dot:

```
pch.oecd <- ifelse(oecd, 19, 1)
plot(lm1$fit, lm1$res,
    main = "Fitted vs. Residual Plot",
    xlab = "Fitted Values", ylab = "Residuals",
    pch = pch.oecd)</pre>
```



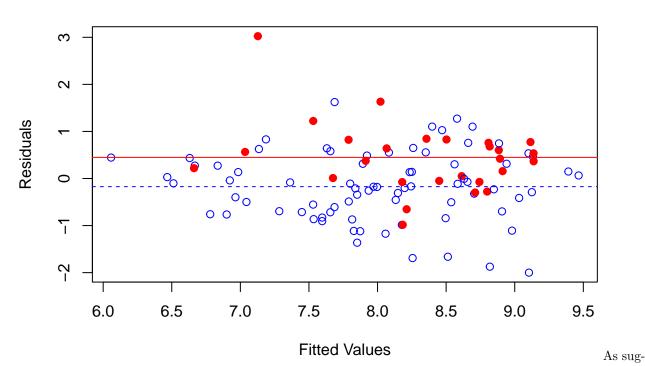
Since the OECD countries seem to have residuals that are indistinguishable from non-OECD countries, we can conclude that OECD is probably not a missing variable. Notice that plot takes the option pch, which stands for 'plotting character.' If we wanted to use X's and O's instead of solid and open points, we could have simply run

```
pch.oecd <- ifelse(oecd, "0", "X")
plot(lm1$fit, lm1$res,
    main = "Fitted vs. Residual Plot",
    xlab = "Fitted Values", ylab = "Residuals",
    pch = pch.oecd)</pre>
```



would return O's plotted for OECD countries and X's plotted for non-OECD countries.

Next, let's see if schooling is an omitted variable. For this figure, we are going to use solid, red dots for countries with high levels of schooling, and open, blue dots for countries with low levels of schooling. Finally, we are going to add lines at the mean residual for countries with high- and low-levels of schooling:



gested by the residual plot, we could add the variable log.schooling to our regression:

```
log.schooling <- log(schooling)
lm2 <- lm(log.dv ~ log.invest + log.pop + log.schooling)
summary(lm2)</pre>
```

Call:

lm(formula = log.dv ~ log.invest + log.pop + log.schooling)

Residuals:

Min 1Q Median 3Q Max -1.39277 -0.39848 0.00573 0.39105 2.06954

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
                          1.31397
(Intercept)
               6.94529
                                    5.286 7.15e-07 ***
               0.70293
log.invest
                          0.15542
                                    4.523 1.65e-05 ***
log.pop
              -0.58055
                          0.45245
                                    -1.283
                                              0.202
log.schooling
               0.68567
                          0.08161
                                    8.401 2.73e-13 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

signii. codes. 0 *** 0.001 ** 0.01 * 0.05 . 0.1 1

(15 observations deleted due to missingness)
Multiple R-squared: 0.6897, Adjusted R-squared: 0.6806
F-statistic: 75.56 on 3 and 102 DF, p-value: < 2.2e-16

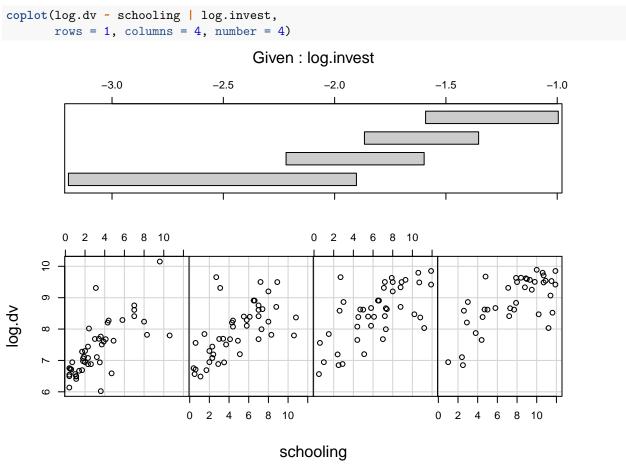
Residual standard error: 0.6129 on 102 degrees of freedom

and when we do so, as predicted by theory, we find that the first two coefficients are far closer to their predicted values of $\beta_k = \frac{1}{2}$ an $\beta_p = -\frac{1}{2}$.

coplot for Conditional Plots

Now, we just added the variable log.schooling to our linear regression. We are assuming, in this multivariate regression, that schooling has an additive, linear effect on the dependent variable. Of course, a reasonable scholar might argue that the effect of schooling varies systematically with investment and population levels: the returns to schooling might be larger in high-investment and high-population areas. When the effect of one variable varies systematically with another variable, we call this an *interaction effect*, a concept we will discuss in some detail throughout the course. For now, we are simply assessing whether the slope of schooling varies with the values of investment or population. To assess, we can use a *conditional plot*

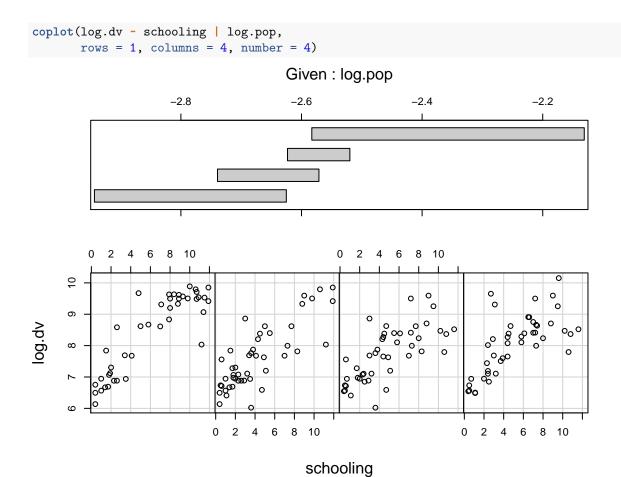
A conditional plot produces a figure with several panels. Each panel plots the dependent variable against an independent variable, within the range of a *conditioning variable*. This is perhaps better explained after you see one:



Missing rows: 14, 16, 36, 44, 45, 66, 68, 72, 78, 81, 82, 91, 111, 114, 118

This figure shows GDP vs. schooling, for low levels of investment (left) through high levels of investment (right). Notice that the panel up top shows what range of log.invest each plot is showing us. The relationship between schooling an GDP seems linear, regardless of the level of investment. The options rows, columns, and number give the number of rows, number of columns, and total number of figures in the conditional plot. I prefer 1 x 3 or 1 x 4 figures, based off of how much data you have. The more data you have, the more subsets you can explore.

Next, let's look at the same figure, except now we are going to use log.pop as the conditioning variable:



Missing rows: 14, 16, 36, 44, 45, 66, 68, 72, 78, 81, 82, 91, 111, 114, 118 From these figures, it appears that schooling is having an independent, additive effect on GDP.

Precept Questions

We will revisit Mankiw's data next week. For now, let's consider the Ross data from the homework assignment.

Question 1

First, plot female labor participation versus oil rents. Plot the Middle Eastern countries red and non-Middle Eastern countries blue. Plot 'high Muslim' countries, for which zislam > 0 with solid dots, and 'low Muslim' countries with open dots. Make sure to include a title, informative axis labels, and a legend. Please note that the legend command takes options pch and col just like plot does.

Which countries are driving the negative correlation between oil and female labor force participation? What does this imply for Ross's claim that oil, not Islam, is leading to a decrease in labor force participation?

Question 2

Create a conditional plot with 1 row and 4 columns, as above. Plot labor participation versus proportion Muslim in each square, using oil rents as the conditioning variable. Plot the Middle Eastern countries in red,

and the remainder in blue (coplot) takes the option col, just as plot does).

Please add coplot(..., panel = panel.smooth) in order to add a 'smooth' curve to each figure in your conditional plot.

This figure indicates a clear interaction between proportion Muslim, oil, and Middle Eastern countries. Please explain where we see a relationship between proportion Muslim and female labor participation, and where we do not.

References

Mankiw, N. G., D. Romer, and D. N. Weil. 1992. "A Contribution to the Empirics of Economic Growth." *The Quarterly Journal of Economics* 107 (2): 407–37. doi:10.2307/2118477.