

ΤΥΠΟΛΟΓΙΟ

<u>ΠΑΡΑΓΩΓΟΙ</u>	<u>ΟΛΟΚΛΗΡΩΜΑΤΑ</u>
$(c)' = 0$	$\int 0 dx = c$
$(x)' = 1$	$\int 1 dx = x + c$
$(e^x)' = e^x, (e^{\alpha x})' = \alpha e^{\alpha x}$	$\int e^x dx = e^x + c, \int e^{\alpha x} dx = \frac{e^{\alpha x}}{\alpha} + c$
$(x^\kappa)' = \alpha x^{\alpha-1}$	$\int x^\kappa dx = \frac{x^{\kappa+1}}{\kappa+1} + c$
$(\ln x)' = \frac{1}{x}$	$\int \frac{1}{x} dx = \ln x + c$
$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$	$\int \frac{1}{\sqrt{x}} dx = 2\sqrt{x} + c$
$\left(\frac{1}{x}\right)' = -\frac{1}{x^2}$	$\int \frac{1}{x^2} dx = -\frac{1}{x} + c$
$(\sin x)' = \cos x$	$\int \sin x dx = -\cos x + c, \int \sin \alpha x dx = \frac{-\cos \alpha x}{\alpha} + c$
$(\cos x)' = -\sin x$	$\int \cos x dx = \sin x + c, \int \cos \alpha x dx = \frac{\sin \alpha x}{\alpha} + c$
$(\alpha^x)' = \alpha^x \ln \alpha$	$\int \alpha^x dx = \frac{\alpha^x}{\ln \alpha} + c$
$(\tan x)' = \frac{1}{\cos^2 x}$	$\int \frac{1}{\cos^2 x} dx = \tan x + c$
$(\cot x)' = -\frac{1}{\sin^2 x}$	$\int \frac{-1}{\sin^2 x} dx = \cot x + c$
$(\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$	$\int \frac{1}{\sqrt{1-x^2}} dx = \arcsin x + c$
$(\arccos x)' = \frac{-1}{\sqrt{1-x^2}}$	$\int \frac{1}{\sqrt{1-x^2}} dx = -\arccos x + c$
$(\arctan x)' = \frac{1}{1+x^2}$	$\int \frac{1}{1+x^2} dx = \arctan x + c$ $\int \frac{dx}{x^2 + \alpha^2} = \frac{1}{\alpha} \arctan\left(\frac{x}{\alpha}\right) + c$
$(\cosh x)' = \sinh x$	$\int \cosh x dx = \sinh x + c$
$(\sinh x)' = \cosh x$	$\int \sinh x dx = \cosh x + c$

ΔΕΝ ΞΕΧΝΩ:

$$\arctan x = \varepsilon\phi^{-1}x = \tau\omicron\xi\varepsilon\varphi x$$

$$\sin x = \eta\mu x, \quad \cos x = \sigma\upsilon\nu x$$

$$\arcsin x = \eta\mu^{-1}x = \tau\omicron\xi\eta\mu x$$

$$\tan x = \varepsilon\varphi x, \quad \cot x = \sigma\varphi x$$

$$\arccos x = \sigma\upsilon\nu^{-1}x = \tau\omicron\xi\sigma\upsilon\nu x$$

$$\lim_{x \rightarrow +\infty} \arctan x = \frac{\pi}{2}, \quad \lim_{x \rightarrow -\infty} \arctan x = -\frac{\pi}{2}$$

$$\lim_{x \rightarrow -1} \arccos x = \pi, \quad \lim_{x \rightarrow 1} \arccos x = 0$$

$$\lim_{x \rightarrow 1} \arctan x = \frac{\pi}{4}, \quad \lim_{x \rightarrow -1} \arctan x = -\frac{\pi}{4}$$

$$\sinh x = \frac{e^x - e^{-x}}{2}, \quad \cosh x = \frac{e^x + e^{-x}}{2}$$

ΤΥΠΟΛΟΓΙΟ Laplace

$f(t) = \mathcal{L}^{-1}\{F(s)\}$	$F(s) = \mathcal{L}\{f(t)\}$
1	$\frac{1}{s}$
$e^{\alpha t}$	$\frac{1}{s - \alpha}$
$\sin \alpha t$	$\frac{\alpha}{s^2 + \alpha^2}$
$\cos \alpha t$	$\frac{s}{s^2 + \alpha^2}$
$e^{bt} \sin \alpha t$	$\frac{\alpha}{(s - b)^2 + \alpha^2}$
$e^{bt} \cos \alpha t$	$\frac{s - b}{(s - b)^2 + \alpha^2}$
t^n	$\frac{n!}{s^{n+1}}$
$e^{\alpha t} t^n$	$\frac{n!}{(s - \alpha)^{n+1}}$
$t \sin \alpha t$	$\frac{2\alpha s}{(s^2 + \alpha^2)^2}$
$t \cos \alpha t$	$\frac{s^2 - \alpha^2}{(s^2 + \alpha^2)^2}$
$\sinh \alpha t$	$\frac{\alpha}{s^2 - \alpha^2}$
$\cosh \alpha t$	$\frac{s}{s^2 - \alpha^2}$
$e^{bt} \sinh \alpha t$	$\frac{\alpha}{(s - b)^2 - \alpha^2}$
$t \sinh \alpha t$	$\frac{2\alpha s}{(s^2 - \alpha^2)^2}$
$e^{bt} \cosh \alpha t$	$\frac{s - b}{(s - b)^2 - \alpha^2}$
$t \cosh \alpha t$	$\frac{s^2 + \alpha^2}{(s^2 - \alpha^2)^2}$
$f'(t)$	$sF(s) - f(0)$
$f''(t)$	$s^2 F(s) - sf(0) - f'(0)$

$f'''(t)$	$s^3 F(s) - s^2 f(0) - s f'(0) - f''(0)$
$u(t)$	$\frac{1}{s}$
$u(t - \alpha)$	$\frac{e^{-\alpha s}}{s}$
$u_c(t)$	$\frac{e^{-cs}}{s}$
$\delta(t)$	1

Γενικά ισχύει:

$$L(t^n f(t))(s) = (-1)^n F^{(n)}(s)$$

$$L(e^{bt} f(t))(s) = F(s - b)$$