

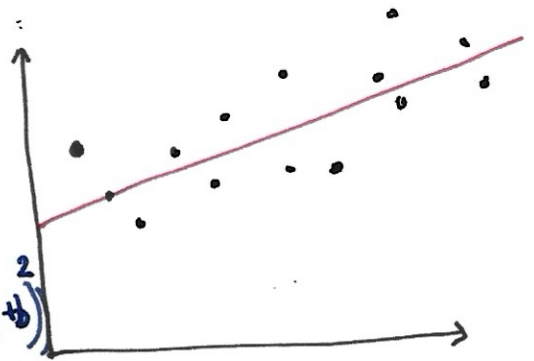
Linear Regression from scratch (using Python)

(1)

Estimation $\Rightarrow \hat{y} = wx + b$

Mean Square error

$$MSE = J(w, b) = \frac{1}{N} \sum_{i=1}^n (y_i - (wx_i + b))^2$$

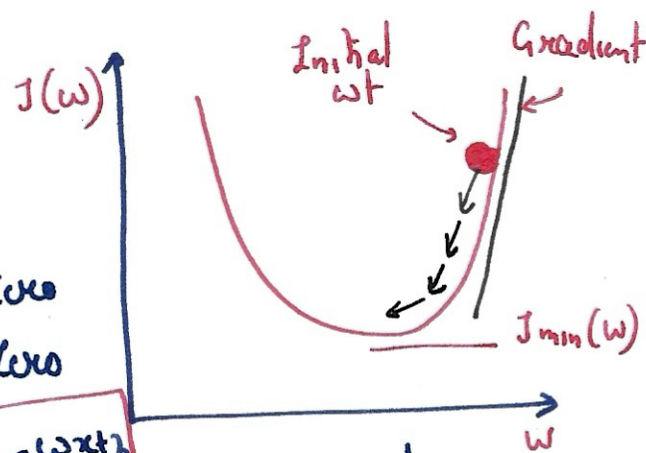


$$J'(w, b) = \begin{bmatrix} \frac{dJ}{dw} \\ \frac{dJ}{db} \end{bmatrix} = \begin{bmatrix} \frac{1}{N} \sum -2x_i (y_i - (wx_i + b)) \\ \frac{1}{N} \sum -2(y_i - (wx_i + b)) \end{bmatrix}$$

Gradient Descent

During training

- Initialize weight as zero
- Initialize bias as zero
- Predict result using $\hat{y} = wx + b$
- Calculate error
- Use gradient descent to figure out new weight & bias values
- Repeat n times
- Test using $\hat{y} = wx + b$



$$w = w - \alpha \cdot dw$$
$$b = b - \alpha \cdot db$$

(2)

updating Parameters

$$dw = \frac{dJ}{dw} = \frac{1}{N} \sum_{i=1}^n -2x_i(y_i - \underbrace{(wx_i + b)}_{\hat{y}}) = \frac{1}{N} \sum_{i=1}^n -2x_i(\underbrace{y_i - \hat{y}}_{\downarrow})$$

$$\frac{1}{N} \sum_{i=1}^n 2x_i(\hat{y} - y_i)$$

Similarly for

$$db = \frac{dJ}{db} = \frac{1}{N} \sum_{i=1}^n 2(\hat{y} - y_i)$$

Doing it efficiently i.e. all calculation for all data point in one time

$$\hat{y} = wx + b \longleftrightarrow y_{pred} = [wX + b]$$

$$X = [x_1, x_2, \dots, x_n]$$

$$X^T = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}$$

$$y_{pred} = [wx_1 + b \quad wx_2 + b \quad \dots \quad wx_n + b]$$