The sudoku bundle for displaying, solving and generating Sudoku puzzles*

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Abstract

The sudoku bundle provides a coordinated set of packages for displaying, solving, and generating Sudoku puzzles. A set of over 50 puzzles is also supplied.

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1 Introduction

In December 2005 the *PracTeX Journal* [PJ05] set a competition about Sudoku puzzles. Depending on their experience with TEX contestants were asked to (a) typeset a particular puzzle, (b) typeset a puzzle described in a 'sudoku' file, (c) create a solver for sudoku puzzles. I entered the competition with a printer and solver. Following from this it was no great effort to develop a matching Soduko puzzle generator.

The packages described here have been developed completely independently from Paul Abraham's sudoku package [Abr05], which I did not see until after I had finished work on them.

A Sudoku puzzle consists a 9 by 9 grid of cells with some of the cells containing a number between 1 and 9, such as is shown in Figure 1. The problem is to place a number between 1 and 9 in each cell such that no number appears more than once in each row and in each column and in each minor 3 by 3 grid. The solution to the example puzzle is shown in Figure 3. The puzzle and answer have been typeset using the printsudoku package.

Among many other sources the *Sudoku Solver by logic* website [SSBL] provides much information on Sudoku puzzles and their solutions, as does the *Sudoku Online* [SOL] website.

A Sudoku puzzle may be represented as a simple text file consisting of nine rows of numbers and dots, nine numbers and dots in each row. The numbers are the clues to the puzzle and the dots represent blanks in the grid. A sudoko file for the example puzzle is given in Figure 2.

This manual is typeset according to the conventions of the LATEX DOC-STRIP utility which enables the automatic extraction of the LATEX macro source files [MG04].

2 Usage

The bundle provides three packages; one for typesetting a puzzle, one for solving a puzzle, and the third for generating a puzzle. Each package requires the previous one(s).

A file is also provided that contains over 50 puzzles and their answers — all you have to do is run LaTeX on it, print it, and get to work on the puzzles (or give them to someone else).

		4	8	3			7	2
	1	2					8	
		5	2		1	3		
				6	2		9	1
7			5		9			3
9	4		7	8				
		3	9		7	4		
	5					6	1	
	8			4	6	9		

Figure 1: Example Sudoku puzzle

```
..483..72
.12....8.
..52.13..
....62.91
7..5.9..3
94.78....
..39.74..
.5....61.
```

Example puzzle

(anything can come after the nine puzzle lines)

Figure 2: A sudoku file for the example puzzle

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6	9	4	8	3	5	1	7	2
3	1	2	6	7	4	5	8	9
8	7	5	2	9	1	3	6	4
5	3	8	4	6	2	7	9	1
7	2	6	5	1	9	8	4	3
9	4	1	7	8	3	2	5	6
1	6	3	9	5	7	4	2	8
4	5	9	3	2	8	6	1	7
2	8	7	1	4	6	9	3	5

Figure 3: Solution to example puzzle

2.1 Typesetting

The printsudoku package enables you to typeset a Sudoku puzzle given in a sudoku file.

\sudoku

The command $\boldsymbol{\dot{file}}$ typesets the sudoku puzzle from the sudoku file named $\boldsymbol{\dot{file}}$. For example:

\begin{center} \sudoku{puzzle1.sud} \end{center}

The command reads only the first nine lines in the file, which must contain the puzzle's description. Anything after these lines is ignored, so comments, such as a title or other explanatory text, can be put at the end of the file.

\cluefont

Following $\clue{font}\$ the clues are typeset using the $\langle font \rangle$ font specification. The default is:

\cluefont{\Huge}

\cellsize

The puzzle is typeset as a IATEX picture and $cellsize{\langle length \rangle}$ specifies the size of the cells in the grid. To match the cluefont the default is:

\cellsize{2.5\baselineskip}

Figure 1 was set using the default \cluefont and \cellsize. On the other hand, Figure 3 was set via:

```
\begin{figure}
\centering
\cluefont{\normalsize}\cellsize{1.5\baselineskip}
\sudoku{examout.ans}
\caption{Solution to example puzzle}\label{fig:ans1}
\end{figure}
```

\writepuzzle \puzzlefile \sudpuzznewline

The command \writepuzzle, which takes nine required arguments each of which is a line in the puzzle, writes the puzzle to the file \puzzlefile, where the default is:

\newcommand*{\puzzlefile}{puzz.sud}

2.2 Solving 5

The nine required arguments to \writepuzzle are the lines describing a puzzle as they would appear in a sudoku file. There is an optional tenth argument after the nine required arguments which you may use to write a comment at the end of the file. For instance, earlier I used the following to write out the example puzzle to the file examout.sud:

```
\renewcommand*{\puzzlefile}{examout.sud}
\writepuzzle%
{..483..72}%
{.12....8.}%
{..52.13...}%
{....62.91}%
{7..5.9...3}%
{94.78....}%
{..39.74...}%
{.5....61.}%
{.8...469...}%
[Example puzzle \sudpuzznewline
(anything can come after the nine puzzle lines)]
```

And similarly for writing out the file with the solution.

If you want a multiline comment, use the \sudpuzznewline macro to start a new line (\\ or \newline will not work).

2.2 Solving

\sudokusolve

The solvesudoku package lets you use LATEX to try and solve a Sudoku puzzle.

The macro \sudokusolve{ $\langle file \rangle$ } attempts to find a solution to the puzzle in the sudoku file $\langle file \rangle$. It uses the printsudoku package for typesetting the puzzle.

It first prints the puzzle as given and then attempts to solve it. The solution, or as much as was obtainable, is typeset in a smaller font below the original. Here is the definition:

```
\newcommand*{\sudokusolve}[1]{%
  \begin{center}
  \sudoku{#1}
  \end{center}
  \getproblem{#1}
  \reduceallcells \keepreducing
  \writegame
  \noindent\begin{minipage}{\linewidth}
  THE ANSWER
  \begin{center}
  \cluefont{\normalsize}
  \cellsize{1.5\baselineskip}
  \sudoku{sud.out}
  \end{center}
  \end{center}
  \end{minipage}}
```

6 2 Usage

You may use the macros in \sudokusolve separately if you wish.

\getproblem

 $\ensuremath{\mbox{getproblem}\{\langle file\rangle\}\mbox{ reads in the puzzle from the sudoku file }\langle file\rangle$ and initialises the solution.}$

\reduceallcells

\reduceallcells takes a simple-minded approach to develop a solution to the puzzle.

\keepreducing

If \reduceallcells does not completely solve the puzzle then \keepreducing applies increasingly sophisticated solution methods, which may or may not lead to a complete solution.

\writegame \sudsolnfile

\writegame writes out a (partially) solved puzzle to the sudoku file \sudsolnfile (default sud.out). Later this is read in again by \sudoku to typeset the solution.

Here's a small example of how you might use the package. This will keep asking on the terminal for sudoku files to solve.

```
Solve Sudoku files
%%% solvethem.tex
                    Peter Wilson
%%%
 \documentclass{article}
 \usepackage{solvesudoku}
 \newcommand*{\solvefile}[1]{\begingroup
   \sudokusolve{#1}%
   \vspace{\baselineskip}
   Number of clues = \the\numcluesctr\ and difficulty = \the\difficultyctr.
 \endgroup}
 \def\yesans{y}
 \begin{document}
 \loop
   \typein[\getans]{New file? y/n}
   \ifx\yesans\getans
     \typein[\sudfile]{Enter the file name}
     \clearpage
     \begin{center} \Huge \sudfile \end{center}
     \solvefile{\sudfile}
 \repeat
 \end{document}
```

\numcluesctr \difficultyctr

These are two TEX \counts. \numcluesctr is the number of clues in the initial puzzle, and \difficultyctr is a numerical indication of how hard the solver had to work, but it doesn't really mean much as the solver has had successes with some puzzles with a high \difficultyctr rating but failed to solve some with medium values of \difficultyctr.

2.3 Generation

With the createsudoku package you can get LATEX to automatically generate a Sudoku puzzle. This package does require the use of Donald Arseneau's random code [Ars95] for generating random numbers.

\generategrid

 $\gray \gray \gra$

2.3 Generation 7

given in the sudoku file $\langle file \rangle$. If the file is not given then it will start from a solution provided by the package.

The puzzle is generated by taking the solution and randomly exchanging rows and columns for some (random) number of times. Then clues are eliminated until it is no longer soluble by \sudokusolve. The last clue that was deleted is put back and then the resulting grid is presented as the puzzle.

An initial set of clues are deleted before the solver is called. It can happen that the puzzle even then is too difficult for the solver, so you have to check the solution as presented is a complete one for the puzzle.

\genfile \prevfile \currfile The generated puzzle, and its solution, is typeset and the puzzle is also output in the sudoku file \genfile. The default is:

\newcommand*{\genfile}{gensud.sud}

Two temporary sudoku files, \prevfile and \currfile, are used during the generation. The defaults are:

\newcommand*{\prevfile}{genprev.sdx}
\newcommand*{\currfile}{gencurr.sdx}

A pre-existing version of any of these three files will be overwritten.

\setsudrandom

The random number generater is initialised via a seed based on a number (the internal value of \randomi) in the range $-1 \le \text{randomi} \le 2147483646$. If its value is -1 (set via \setsudrandom{-1}) then the actual seed will be calculated based on the time and date. For any given seed the sequence of the generated random numbers is the same. The value of the seed is output via a \typeout if you need to repeat a generation.

You should not attempt to set \randomi directly but use \setsudrandom{ $\langle num \rangle$ }.

The default setting is:

\setsudrandom{-1}

and as that means that the seed depends on the time and date, a new puzzle will be generated each time (unless the time interval is very short). The maximum number of puzzles that can be generated from one initial solution is 2,147,483,646 which is the range of the random number generator.

\initialelimination

The macro \initialelimination eliminates an initial set of solutions from the randomized starting grid. Various predefined sets are provided and you can either provide your own definition for \initialelimination or \let it to one of the predefined sets, e.g.,

\let\initialelimination\elimcrossandnines

\elimseventeen
\elimnum
\elimcross
\elimex
\elimcrossandnines
\elimcrossandex
\elimcrossandexandnines

\elimseventeen randomly eliminates 17 solutions from the grid — apparently the solution to a puzzle can be ambiguous if two numbers are completely absent. \elimnum{ $\langle num \rangle$ } eliminates every solution $\langle num \rangle$ (e.g. \elimnum{7} will eliminate every 7 from the grid). \elimcross eliminates all numbers from column 5 and from row 5, while \elimex eliminates all numbers on the diagonals.

\elimcrossandnines is a combination of \elimcross and \elimnum{9}. Similarly the macros \elimcrossandex and \elimcrossandex and nines are combinations of some of the earlier macros.

3 Code

31 \firsts@dcluetrue

3.1 The printsudoku package

```
1 \langle *print \rangle
                2 \NeedsTeXFormat{LaTeX2e}
                3 \ProvidesPackage{printsudoku}[2006/02/16 v1.0 typeset sudoku puzzles]
               We are going to be reading and writing some files.
    \s@dread
   \s@dwrite
                5 \newread\s@dread
                6 \newwrite\s@dwrite
              \reads@dgame{\langle file \rangle} opens a sudoku file \langle file \rangle for reading.
\reads@dgame
                8 %%%% open game file
                9 \newcommand*{\reads@dgame}[1]{%
                   \closein\s@dread
               11
                   \openin\s@dread=#1}
               12
\halfs@dcell
              We're going to use a picture environment for drawing the grid, and to
   \cellsize
               keep numbers neatly we'll use the length \halfs@dcell as the \unitlength.
               \left(\frac{length}{length}\right) is the use command for setting the size of a cell. The clues
   \cluefont
               are typeset using the \cluefont font.
               13 %%% set size of a game cell
               14 \newlength\halfs@dcell
               15 \newcommand*{\cellsize}[1]{%
                   \halfs@dcell=#1\relax
               16
                   \halfs@dcell=0.5\halfs@dcell}
               18 \cellsize{2.5\baselineskip}
               19 %% set font for the numbers
               20 \newcommand*{\cluefont}[1]{\def\s@dfont{#1}}
               21 \cluefont{\Huge}
               22
              Counts for looping and cell positions
    \s@dncol
    \s@dnrow
               23 %% counts for looping and cell positions
  \s@dcolpos
               24 \newcount\s@dncol
  \s@drowpos
              25 \newcount\s@dnrow
               26 \newcount\s@dcolpos
               27 \newcount\s@drowpos
               \adds@dclues inserts the clues into the game grid. It reads the sudoku file line
\adds@dclues
               by line insert the clues into the grid for one line before going on to the next line.
               29 %% insert the clues into the game array
               30 \newcommand*{\adds@dclues}{%
```

```
\s@dnrow\@ne
                     32
                     33
                         \loop
                            \ifnum\s@dnrow<10\relax
                     34
                            \read\s@dread to \s@dline
                     35
                           \firsts@dcluetrue
                     36
                     37
                            \s@drowpos=\s@dnrow
                     38
                            \multiply\s@drowpos\tw@
                            \advance\s@drowpos\m@ne
                     39
                           \s@dncol\@ne
                     40
                            \dos@dcols
                     41
                            \advance\s@dnrow\@ne
                     42
                     43
                         \repeat
                     44
                         \closein\s@dread}
        \dos@dcols \dos@dcols inserts one row of clues into the game grid.
                     46 \% insert a row of clues
                     47 \newcommand*{\dos@dcols}{%
                     48 \setminus bgroup
                     49
                         \loop
                            \ifnum\s@dncol<10\relax
                     50
                            \s@dcolpos=\s@dncol
                     51
                     52
                            \multiply\s@dcolpos\tw@
                            \advance\s@dcolpos\m@ne
                     53
                            \put(\s@dcolpos, -\s@drowpos){\makebox(0,0){\s@dfont\gets@dclue}}%
                     54
                            \advance\s@dncol\@ne
                     55
                         \repeat
                     57 \egroup}
           \gettwo \splitofff\{\langle string \rangle\} gets the next character in a string. The next character is
             \nowt made available as \istchar and the remainder of the string as \restchars. This
                     is explained in a forthcoming Glisterings column in TUGboat.
          \istchar
        \restchars
                    59 %% get the next character in a string
         \splitoff
                    60 \def\gettwo#1#2\nowt{%
                     61 \gdef\istchar{#1}\gdef\restchars{#2}}
                     62 \def\splitoff#1{\gettwo#1\nowt}
         \s@dfstop We use this for checking if a character extracted from a string is a '.'.
                     63 %% a full stop (period)
                     64 \gdef\s@dfstop{.}
                     65
   \iffirsts@dclue
                     \gets@dclue gets the next clue (character) from a line of clues. We do slightly
 \firsts@dcluetrue
                     different things if we are dealing with the first clue or the others.
\firsts@dcluefalse
                     66 %% get the next clue in the line
       \gets@dclue
                    67 \newif\iffirsts@dclue
                     68 \firsts@dcluetrue
                     69 \newcommand*{\gets@dclue}{%
```

```
\iffirsts@dclue
                   70
                           \expandafter\splitoff\expandafter{\s@dline}%
                   71
                           \global\firsts@dcluefalse
                   72
                   73
                           \expandafter\splitoff\expandafter{\restchars}%
                   74
                   75
                        \fi
                   76
                        \ifx\s@dfstop\istchar
                   77
                        \else
                           \istchar
                   78
                        \fi}
                   79
                   80
                   \s@dgame typesets the grid, then adds in the clues.
        \s@dgame
                   81 %% typeset the grid, then add the clues
                   82 \newcommand*{\s@dgame}{%
                        \setlength\unitlength\halfs@dcell
                        \begin{picture}(18,18)(0,-18)
                   84
                           \thinlines
                   85
                           \mathsf{Multiput}(0,0)(2,0)\{10\}\{\mathsf{line}(0,-1)\{18\}\}\
                   86
                           \mathsf{Multiput}(0,0)(0,-2)\{10\}\{\mathsf{line}(1,0)\{18\}\}
                   87
                           \thicklines \linethickness{1pt}
                   88
                           \mathsf{Multiput}(0,0)(6,0){4}{\mathsf{line}(0,-1){18}}
                   89
                           \mathsf{Multiput}(0,0)(0,-6){4}{\mathsf{line}(1,0){18}}
                   90
                           \adds@dclues
                   91
                        \end{picture}}
                   92
                   93
                   \ reads a game from \langle file \rangle and then typesets it.
                   94 %% the whole shebang, where #1 is the name of the game file
                   95 \newcommand*{\sudoku}[1]{%
                        \reads@dgame{#1}%
                   96
                        \s@dgame}
                   97
                   98
                   \writepuzzle takes nine arguments — the nine lines specifying a puzzle — and
     \puzzlefile
    \writepuzzle
                   writes them to the \puzzlefile file.
                       \verb|\writes@dpuzzend[|\langle comment|\rangle|| writes |\langle comment|\rangle| at the end of the \verb|\puzzlefile||
\writes@dpuzzend
                   file.
\sudpuzznewline
                       \sudpuzznewline provides a \newline macro for use in a comment being
                   written to a puzzle file.
                   99 \newcommand*{\puzzlefile}{puzz.sud}
                   100 \newcommand*{\writepuzzle}[9]{%
                        \immediate\closeout\s@dwrite
                        \immediate\openout\s@dwrite=\puzzlefile
                   102
                        \immediate\write\s@dwrite{#1}%
                   103
                        \immediate\write\s@dwrite{#2}%
                   104
                        \immediate\write\s@dwrite{#3}%
                   105
                   106
                        \immediate\write\s@dwrite{#4}%
                        \immediate\write\s@dwrite{#5}%
```

139 \newcount\sumctr 140 \newcount\toprangectr

```
\immediate\write\s@dwrite{#6}%
               108
                     \immediate\write\s@dwrite{#7}%
               109
                    \immediate\write\s@dwrite{#8}%
               110
                    \immediate\write\s@dwrite{#9}%
               111
                    \writes@dpuzzend}
               112
               113 \newcommand*{\writes@dpuzzend}[1][\@empty]{
               114
                    \ifx\@empty #1\else
                       \immediate\write\s@dwrite{ }%
               115
                       \immediate\write\s@dwrite{#1}%
               116
                    \fi
               117
                    \immediate\closeout\s@dwrite}
               118
               119 \newcommand*{\sudpuzznewline}{^^J}
                   The end of the package.
               121 \langle /print \rangle
                3.2
                       The solvesudoku package
                The package requires the printsudoku package to do some puzzle typesetting.
               122 \langle *solve \rangle
               123 \NeedsTeXFormat{LaTeX2e}
               124 \ProvidesPackage{solvesudoku}[2006/02/16 v1.0 solve sudoku puzzles]
               125 \RequirePackage{printsudoku}
               126
                3.2.1 Setup
  \commentary It can be useful to control the amount of output to the log file.
               127 \newcommand{\commentary}[1]{\typeout{#1}}
               128
                   The following counts are defined in the printsudoku package:
                \s@dncol, \s@dnrow, \s@dcolpos, \s@drowpos
     \selcnta A bunch of \counts. They could probably be reduced in number but they help
      \solcnt me to keep the code less mysterious.
     \tenscnt _{129} %%% too many counts, maybe they should be reduced
    \tempcntz 130 \newcount\s@lcnta
                                         % a cell number
                                          % number of solved cells
    \tempcnty 131 \newcount\solcnt
   \tmpsetctr 132 \newcount\settonumcnt
\verb|\tmpsetansctr|| 133 \\ \verb|\newcount| tenscnt|
      \boxctr 134 \newcount\tempcntz
      \sumctr 135 \newcount\tempcnty
               136 \newcount\tmpsetctr
 \toprangectr
               137 \newcount\tmpsetansctr
               138 \newcount\boxctr
```

```
\lonecellctr
           \verb|\reducedctr||_{141} \\ \verb|\newcount|\\ lonecellctr|
           \numlistctr 142 \newcount\reducedctr
    \difficultyctr 143 \newcount\numlistctr
         \s@dtempcnta 144 \newcount\difficultyctr
         \verb|\s@dtempcntb| 145 \verb|\newcount| s@dtempcnta|
\s@dtemploopcnta ^{146} \newcount\s@dtempcntb
        \maxrangectr 147 \newcount\s@dtemploopcnta
             \digitictr
           \verb|\digitiictr||_{151} \\ \verb|\newcount| \\ \verb|\digitictr||
       \numdigitsctr 152 \newcount\digitiictr
         \numcluesctr 153 \newcount\numdigitsctr
                                        154 \newcount\numcluesctr
 \iffirsts@dclue
         \iffirstchar _{156} %%% \iffirsts@dclue% defined in printsudoku package
\ifsetchanged 158 \newif\ifnotgotthechar
              \ifchanged 159 \newif\ifsetchanged
      \iflonerchanged 161 \neq 161
    \verb|\label{limits}| 162 \verb|\label{limits}| 16
                \ifkeepon 163 \newif\ifstilldigits
                                         164 \newif\ifkeepon
   \label{eq:linear_continuous_linear_continuous} \begin{array}{c} 104 \text{ \nestrictions} \\ 165 \text{ \newif\ifpairchanged} \end{array}
                     \useknt
    \createsudsets
                                          kernel \Cnamedef and \Cnameuse. In particular we will use 81 'numbered' counts,
                                          one for each cell in the sudoku grid, using \createsudsets to generate them.
                                         167 %% create and use a numbered count
                                         168 %% we'll use 81 of these, one for each cell in the grid
                                         169 \verb|\newcommand*{\newknt}[1]{\newcount\csname #1\endcsname}|
                                         170 \newcommand*{\useknt}[1]{\csname #1\endcsname}
                                        171 %% create potential answer sets
                                        172 \newcommand*{\createsudsets}{%
                                        173 \global\s@lcnta\@ne
                                        174 \global\solcnt\z@
                                        175 \loop
                                        176
                                                     \ifnum\s@lcnta<82\relax
                                        177
                                                     \newknt{s@lans\the\s@lcnta}%
                                                    \advance\s@lcnta\@ne
                                         179 \repeat}
```

```
180 \createsudsets 181
```

3.2.2 Binary solution sets

The major concern was deciding on the datastructure for the problem (the value of \useknt{\s@lans \the \s@lcnta}} for the \s@lcnta cell). In the end I used a 9 digit 'binary solution set' for the potential solutions for each cell. ([111111111] \leftrightarrow 123456789 and [101010101] \leftrightarrow 13579). A cell solution, say N, is represented as the 'set' -N (e.g., a potential solution 3 is represented as [001000000] and the actual solution 3 is represented by [-3]).

\initialisesuddata This sets each of the 81 cells to 1111111111. 182 %% initialise potential answer sets 183 \newcommand*{\initialisesuddata}{\bgroup 184 \global\s@lcnta\@ne 185 \global\solcnt\z@ 186 \global\difficultyctr\z@ 187 \global\numcluesctr\z@ 188 \loop \ifnum\s@lcnta<82\relax 189 \global\useknt{s@lans\the\s@lcnta}=111111111\relax 190 \advance\s@lcnta\@ne 192 \repeat 193 \egroup} 194 \settonum{ $\langle set \rangle$ }{ $\langle cnt \rangle$ } converts a potential solution binary set $\langle set \rangle$ to the cor-\settonum responding set of digits; that is [11....1] -> 12...9. The result of the conversion is assigned to the \count $\langle cnt \rangle$ which must be supplied by the calling macro. If the set is negative then the result is that number (e.g. [-3] -> -3). If the set contains only a single non-zero entry, that is converted to the negative of the corresponding digit (e.g. $[100] \rightarrow -7$). 197 %%\settonum{110011...}{cnt}

```
198 %% converts a potential solution set to a number ([11....1] -> 12...9)
199 %% returns the input if it is negative ([-3] -> -3)
200 %% returns a negative number if the set represents a single digit ([10] -> -8)
201 \newcommand*{\settonum}[2]{%
202
    \settonumcnt=#1\relax
     \tempcnty=\z@
203
204
     \tenscnt=\@ne
     \ifnum\settonumcnt<\z@ % just return the number
205
       \tempcnty=\settonumcnt
206
       #2=\tempcnty
207
     \else
208
       \ifodd\settonumcnt
                              % 9 flagged
```

```
210
          \tempcntz=9\relax
211
          \multiply\tempcntz \tenscnt
212
          \advance \tempcnty by \tempcntz
          \multiply\tenscnt 10\relax
213
       \fi
214
215
       \divide\settonumcnt by 10\relax
216
       \ifodd\settonumcnt
                              % 8 flagged
          \tempcntz=8\relax
217
218
          \multiply\tempcntz \tenscnt
          \advance \tempcnty \tempcntz
219
          \mathsf{Multiply}\mathsf{tenscnt}\ 10\mathsf{relax}
220
221
222
       \divide\settonumcnt by 10\relax
223
       \ifodd\settonumcnt
                              % 7 flagged
224
          \tempcntz=7\relax
          \multiply\tempcntz \tenscnt
225
          \advance \tempcnty \tempcntz
226
          \mathsf{Multiply}\mathsf{tenscnt}\ 10\mathsf{relax}
227
228
229
       \divide\settonumcnt by 10\relax
       \ifodd\settonumcnt
                              % 6 flagged
230
231
          \tempcntz=6\relax
232
          \multiply\tempcntz \tenscnt
233
          \advance \tempcnty \tempcntz
234
          \multiply\tenscnt 10\relax
235
       \fi
236
       \divide\settonumcnt by 10\relax
       \ifodd\settonumcnt
                              % 5 flagged
237
          \tempcntz=5\relax
238
          \multiply\tempcntz \tenscnt
239
          \advance \tempcnty \tempcntz
240
241
          \multiply\tenscnt 10\relax
242
       \divide\settonumcnt by 10\relax
243
       \ifodd\settonumcnt
                              % 4 flagged
244
          \tempcntz=4\relax
245
          \multiply\tempcntz \tenscnt
246
          \advance \tempcnty \tempcntz
247
248
          \multiply\tenscnt 10\relax
^{249}
250
       \divide\settonumcnt by 10\relax
251
       \ifodd\settonumcnt
                              % 3 flagged
          \tempcntz=3\relax
252
          \multiply\tempcntz \tenscnt
253
254
          \advance \tempcnty \tempcntz
255
          \multiply\tenscnt 10\relax
256
257
       \divide\settonumcnt by 10\relax
258
       \ifodd\settonumcnt
                              % 2 flagged
259
          \tempcntz=2\relax
```

```
\multiply\tempcntz \tenscnt
260
         \advance \tempcnty \tempcntz
261
         \multiply\tenscnt 10\relax
262
263
       \fi
       \divide\settonumcnt by 10\relax
264
265
       \ifodd\settonumcnt % 1 flagged
266
         \tempcntz=1\relax
267
         \multiply\tempcntz \tenscnt
         \advance \tempcnty \tempcntz
268
            \multiply\tenscnt 10\relax
269 %%
       \fi
270
       \ifnum \tempcnty<10
271
272
         \ifnum\tempcnty>\z@
            \tempcnty = -\tempcnty
273
274
         \fi
       \fi
275
       #2=\tempcnty
276
277 \fi}
278
```

\numofnuminset

\numofnuminset{\langle digit \rangle} \{\langle ent \rangle} \{\langle ent \rangle} \text{ the \count \langle ent \rangle} to the number of times the digit \langle digit \rangle is represented in the binary set \langle set \rangle. For example, the number of digits in the set [200000013] are 1 -> 2, 2 -> 0, ..., 8 -> 1 and 9 -> 3.

```
279 %%\numofnuminset{digit}{set}{returnctr}
280\ \% returns the number of times digit is represented in the set
281 %% e.g. if the set is [200000013] then 1 -> 2, 2 -> 0,... 8 -> 1, 9 -> 3
282 \newcommand*{\numofnuminset}[3]{%}
    \tmpsetctr=#2\relax
283
284
     \tmpsetansctr=\tmpsetctr
     \ifnum\tmpsetctr<\z0% solution, not a set
285
286
       \tmpsetansctr=\z@
     \else
287
       \ifcase #1\relax
288
                         % 1
289
       \or
290
         \divide\tmpsetansctr by 10000000\relax
291
         \divide\tmpsetansctr by 10000000\relax
292
         \tmpsetctr=\tmpsetansctr
293
         294
         \advance\tmpsetansctr -\tmpsetctr
295
                        % 3
296
         \divide\tmpsetansctr by 1000000\relax
297
         \tmpsetctr=\tmpsetansctr
298
         \divide\tmpsetctr 10\relax \multiply\tmpsetctr 10\relax
299
         \advance\tmpsetansctr -\tmpsetctr
300
                        % 4
301
         \displaystyle \divide\tmpsetansctr\ by\ 100000\relax
302
303
         \tmpsetctr=\tmpsetansctr
304
         \divide\tmpsetctr 10\relax \multiply\tmpsetctr 10\relax
```

```
305
                                                               \advance\tmpsetansctr -\tmpsetctr
                                         306
                                                          \or
                                                                                                    % 5
                                                               \divide\tmpsetansctr by 10000\relax
                                         307
                                                               \tmpsetctr=\tmpsetansctr
                                         308
                                                               \divide\tmpsetctr 10\relax \multiply\tmpsetctr 10\relax
                                         309
                                         310
                                                               \advance\tmpsetansctr -\tmpsetctr
                                         311
                                                          \or
                                                                                                   % 6
                                                               \divide\tmpsetansctr by 1000\relax
                                         312
                                                               \tmpsetctr=\tmpsetansctr
                                         313
                                                               \divide\tmpsetctr 10\relax \multiply\tmpsetctr 10\relax
                                         314
                                                               \advance\tmpsetansctr -\tmpsetctr
                                         315
                                         316
                                                          \or
                                                                                                   % 7
                                         317
                                                               \divide\tmpsetansctr by 100\relax
                                                               \tmpsetctr=\tmpsetansctr
                                         318
                                                               \divide\tmpsetctr 10\relax \multiply\tmpsetctr 10\relax
                                         319
                                                               \advance\tmpsetansctr -\tmpsetctr
                                         320
                                                                                                   % 8
                                         321
                                                               \divide\tmpsetansctr by 10\relax
                                         322
                                         323
                                                               \tmpsetctr=\tmpsetansctr
                                         324
                                                               \divide\tmpsetctr 10\relax \multiply\tmpsetctr 10\relax
                                                               \advance\tmpsetansctr -\tmpsetctr
                                         325
                                         326
                                                          \or
                                                                                                    % 9
                                                               \tmpsetctr=\tmpsetansctr
                                         327
                                                               \divide\tmpsetctr 10\relax \multiply\tmpsetctr 10\relax
                                         328
                                                               \advance\tmpsetansctr -\tmpsetctr
                                         329
                                         330
                                                          \else
                                                                                                   % error
                                                               \tmpsetansctr=\z@
                                         331
                                                          \fi
                                         332
                                                     \fi
                                         333
                                                     #3=\tmpsetansctr}
                                         334
                                         335
                                           \del{cont} \del{cont
\deletenumfromset
                                           sets the \count \langle cnt \rangle to the reulting modified set. If \langle digit \rangle was the only member
                                           then the result is that digit negated. For example:
                                           9 from [...11] -> [...10]
                                           8 from [0...010] -> -8
                                         336 %%\deletenumfromset{digit}{set}{returnctr}
                                         337 %% deletes num from the [set], returning the modified set or a -ve number if
                                         338 \ \%\% the digit was the only member.
                                         339 %% e.g., 9 from [...11] \rightarrow [...10], 8 from [0...010] \rightarrow -8
                                         340 \ensuremath{ \mbox{\mbox{$1$}} (3] {} \\
                                                     \global\setchangedfalse
                                                     \tmpsetctr=#2\relax
                                         342
                                                     \tmpsetansctr=#2\relax
                                         344 \leftarrow tmpsetctr \leq 20 \% represents a solved number, do nothing
                                         345 \ensuremath{\setminus} \texttt{else}
                                         346
                                                     \ifcase #1\relax
                                                                                               % 1
                                         347
                                                     \or
```

```
\divide\tmpsetctr by 10000000\relax
348
       \ifodd\tmpsetctr%
                                          it's there
349
         \verb|\advance| tmpsetansctr -100000000| relax|
350
         \global\setchangedtrue
351
       \fi
352
353
     \or
                        % 2
354
       \divide\tmpsetctr by 10000000\relax
355
       \ifodd\tmpsetctr%
                                          it's there
         \advance\tmpsetansctr -10000000\relax
356
         \global\setchangedtrue
357
       \fi
358
359
                        % 3
360
       \divide\tmpsetctr by 1000000\relax
       \ifodd\tmpsetctr%
                                          it's there
361
         \advance\tmpsetansctr -1000000\relax
362
         \global\setchangedtrue
363
       \fi
364
                        % 4
365
366
       \divide\tmpsetctr by 100000\relax
367
       \ifodd\tmpsetctr%
                                          it's there
         \advance\tmpsetansctr -100000\relax
368
         \global\setchangedtrue
369
       \fi
370
     \or
                        % 5
371
       \divide\tmpsetctr by 10000\relax
372
373
       \ifodd\tmpsetctr%
                                          it's there
         \advance\tmpsetansctr -10000\relax
374
          \global\setchangedtrue
375
       \fi
376
                        % 6
     \or
377
       378
379
       \ifodd\tmpsetctr%
                                          it's there
380
         \advance\tmpsetansctr -1000\relax
         \global\setchangedtrue
381
382
       \fi
383
     \or
                        % 7
       \divide\tmpsetctr by 100\relax
384
       \ifodd\tmpsetctr%
385
                                          it's there
386
         \advance\tmpsetansctr -100\relax
         \global\setchangedtrue
387
388
       \fi
                        % 8
389
       \divide\tmpsetctr by 10\relax
390
       \ifodd\tmpsetctr%
                                          it's there
391
392
         \advance\tmpsetansctr -10\relax
393
         \global\setchangedtrue
394
       \fi
395
     \or
                        % 9
       \ifodd\tmpsetctr%
                                          it's there
396
397
         \advance\tmpsetansctr -1\relax
```

```
398 \global\setchangedtrue
399 \fi
400 \fi
401 \fi
402 #3=\tmpsetansctr}
403
```

\displaystatus

This macro typesets a tabular showing the current real and potential solutions for the grid. A real solution is shown as a negative number; positive numbers are the potential solution digits for the cell.

```
404 %% typeset current answers plus potential answer digits
405 \newcommand*{\displaystatus}{%
407 \settonum{\the\useknt{s@lans1}}{\s@dtempcnta}\the\s@dtempcnta &
408 \settonum{\the\useknt{s@lans2}}{\s@dtempcnta}\the\s@dtempcnta &
409 \settonum{\the\useknt{s@lans3}}{\s@dtempcnta}\the\s@dtempcnta &
410 \settonum{\the\useknt{s@lans4}}{\s@dtempcnta}\the\s@dtempcnta &
411 \settonum{\the\useknt{s@lans5}}{\s@dtempcnta}\the\s@dtempcnta &
412 \settonum{\the\useknt{s@lans6}}{\s@dtempcnta}\the\s@dtempcnta &
413 \settonum{\the\useknt{s@lans7}}{\s@dtempcnta}\the\s@dtempcnta &
414 \settonum{\the\useknt{s@lans8}}{\s@dtempcnta}\the\s@dtempcnta &
415 \settonum{\the\useknt{s@lans9}}{\s@dtempcnta}\the\s@dtempcnta \\ \hline
416 \settonum{\the\useknt{s@lans10}}{\s@dtempcnta}\the\s@dtempcnta &
417 \settonum{\the\useknt{s@lans11}}{\s@dtempcnta}\the\s@dtempcnta &
418 \settonum{\the\useknt{s@lans12}}{\s@dtempcnta}\the\s@dtempcnta &
419 \settonum{\the\useknt{s@lans13}}{\s@dtempcnta}\the\s@dtempcnta &
420 \settonum{\the\useknt{s@lans14}}{\s@dtempcnta}\the\s@dtempcnta &
421 \settonum{\the\useknt{s@lans15}}{\s@dtempcnta}\the\s@dtempcnta &
422 \settonum{\the\useknt{s@lans16}}{\s@dtempcnta}\the\s@dtempcnta &
423 \settonum{\the\useknt{s@lans17}}{\s@dtempcnta}\the\s@dtempcnta &
424 \settonum{\the\useknt{s@lans18}}{\s@dtempcnta}\the\s@dtempcnta \\ \hline
425 \settonum{\the\useknt{s@lans19}}{\s@dtempcnta}\the\s@dtempcnta &
426 \settonum{\the\useknt{s@lans20}}{\s@dtempcnta}\the\s@dtempcnta &
427 \settonum{\the\useknt{s@lans21}}{\s@dtempcnta}\the\s@dtempcnta &
428 \settonum{\the\useknt{s@lans22}}{\s@dtempcnta}\the\s@dtempcnta &
429 \settonum{\the\useknt{s@lans23}}{\s@dtempcnta}\the\s@dtempcnta &
430 \settonum{\the\useknt{s@lans24}}{\s@dtempcnta}\the\s@dtempcnta &
431 \settonum{\the\useknt{s@lans25}}{\s@dtempcnta}\the\s@dtempcnta &
432 \settonum{\the\useknt{s@lans26}}{\s@dtempcnta}\the\s@dtempcnta &
433 \end{the \useknt so lans 27} {\so dtempcnta \the \so dtempcnta \the \noindent \n
434 \settonum{\the\useknt{s@lans28}}{\s@dtempcnta}\the\s@dtempcnta &
435 \settonum{\the\useknt{s@lans29}}{\s@dtempcnta}\the\s@dtempcnta &
436 \settonum{\the\useknt{s@lans30}}{\s@dtempcnta}\the\s@dtempcnta &
437 \settonum{\the\useknt{s@lans31}}{\s@dtempcnta}\the\s@dtempcnta &
438 \settonum{\the\useknt{s@lans32}}{\s@dtempcnta}\the\s@dtempcnta &
439 \settonum{\the\useknt{s@lans33}}{\s@dtempcnta}\the\s@dtempcnta &
440 \settonum{\the\useknt{s@lans34}}{\s@dtempcnta}\the\s@dtempcnta & \&
441 \settonum{\the\useknt{s@lans35}}{\s@dtempcnta}\the\s@dtempcnta &
442 \settonum{\the\useknt{s@lans36}}{\s@dtempcnta}\the\s@dtempcnta \\ \hline
443 \settonum{\the\useknt{s@lans37}}{\s@dtempcnta}\the\s@dtempcnta &
```

```
444 \settonum{\the\useknt{s@lans38}}{\s@dtempcnta}\the\s@dtempcnta &
446 \end{\text{\colored}} \hbegin{tabular}{l} \hbegin{tabular}{\cline{colored}} \hbegin{tabular}{l} \hbegin{
447 \settonum{\the\useknt{s@lans41}}{\s@dtempcnta}\the\s@dtempcnta &
448 \settonum{\the\useknt{s@lans42}}{\s@dtempcnta}\the\s@dtempcnta &
449 \settonum{\the\useknt{s@lans43}}{\s@dtempcnta}\the\s@dtempcnta &
450 \settonum{\the\useknt{s@lans44}}{\s@dtempcnta}\the\s@dtempcnta &
451 \settonum{\the\useknt{s@lans45}}{\s@dtempcnta}\the\s@dtempcnta \\
452 \settonum{\the\useknt{s@lans46}}{\s@dtempcnta}\the\s@dtempcnta &
453 \ensuremath{\lower=153}\\\hswl{\lower=150} \hswl{\lower=150} \hswl{\lower=150} \hswl{\lower=150} \hsswl{\lower=150} \hsswl
455 \settonum{\the\useknt{s@lans49}}{\s@dtempcnta}\the\s@dtempcnta &
456 \ensuremath{\lowerntasol}}{\scalentering} \hspace{2.5cm} \hspace{2.5cm} 456 \ensuremath{\scalentering} \hspace{2.5cm} \h
457 \settonum{\the\useknt{s@lans51}}{\s@dtempcnta}\the\s@dtempcnta &
458 \operatorname{lans52}}{\s@dtempcnta}\the\s@dtempcnta &
459 \ensuremath{\lower.eng}\\ \the\sQdtempcnta &
460 \end{the} 
461 \settonum{\the\useknt{s@lans55}}{\s@dtempcnta}\the\s@dtempcnta &
462 \settonum{\the\useknt{s@lans56}}{\s@dtempcnta}\the\s@dtempcnta &
463 \settonum{\the\useknt{s@lans57}}{\s@dtempcnta}\the\s@dtempcnta &
464 \settonum{\the\useknt{s@lans58}}{\s@dtempcnta}\the\s@dtempcnta &
465 \settonum{\the\useknt{s@lans59}}{\s@dtempcnta}\the\s@dtempcnta &
466 \end{the\useknt} $$ 466 \end{the\useknt} \end{the\useknt} $$ \end{the\useknt} $$ $$ 466 \end{the\useknt} $$ \end{the\useknt} $$ $$ \end{the\useknt} $$ \end{the\useknt} $$ $$ \end{the\useknt} $$ \end{t
467 \settonum{\the\useknt{s@lans61}}{\s@dtempcnta}\the\s@dtempcnta &
468 \settonum{\the\useknt{s@lans62}}{\s@dtempcnta}\the\s@dtempcnta &
470 \settonum{\the\useknt{s@lans64}}{\s@dtempcnta}\the\s@dtempcnta &
471 \settonum{\the\useknt{s@lans65}}{\s@dtempcnta}\the\s@dtempcnta &
472 \settonum{\the\useknt{s@lans66}}{\s@dtempcnta}\the\s@dtempcnta &
473 \settonum{\the\useknt{s@lans67}}{\s@dtempcnta}\the\s@dtempcnta &
474 \end{the\useknt} $$ 474 \end{the\useknt} \end{the\useknt} \label{the\useknt} $$ 474 \end{the\useknt} $$ 474 \end{the\use
475 \settonum{\the\useknt{s@lans69}}{\s@dtempcnta}\the\s@dtempcnta &
476 \settonum{\the\useknt{s@lans70}}{\s@dtempcnta}\the\s@dtempcnta &
477 \settonum{\the\useknt{s@lans71}}{\s@dtempcnta}\the\s@dtempcnta &
478 \settonum{\the\useknt{s@lans72}}{\settonum{\the\sedtempcnta}\the\sedtempcnta} \
479 \settonum{\the\useknt{s@lans73}}{\s@dtempcnta}\the\s@dtempcnta &
480 \settonum{\the\useknt{s@lans74}}{\s@dtempcnta}\the\s@dtempcnta &
481 \settonum{\the\useknt{s@lans75}}{\s@dtempcnta}\the\s@dtempcnta &
482 \settonum{\the\useknt{s@lans76}}{\s@dtempcnta}\the\s@dtempcnta &
483 \settonum{\the\useknt{s@lans77}}{\s@dtempcnta}\the\s@dtempcnta &
484 \settonum{\the\useknt{s@lans78}}{\s@dtempcnta}\the\s@dtempcnta &
485 \settonum{\the\useknt{s@lans79}}{\s@dtempcnta}\the\s@dtempcnta &
486 \ensuremath{\lowernt{s@lans80}}{\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensuremath{\lowernta}\ensur
487 \settonum{\the\useknt{s@lans81}}{\s@dtempcnta}\the\s@dtempcnta \\ \hline\hline
488 \end{tabular}}
489
```

3.2.3 Problem initialisation

 $\getproblem{\langle file\rangle}$ initialises the solution grid and reads the puzzle from the \getproblem sudoku file $\langle file \rangle$. It calls \initialsoln to read the file and insert the clues into the grid. 492 % read the problem and initialise the problem (solution) 493 \newcommand*{\getproblem}[1]{\bgroup \initialisesuddata \global\solcnt\z@ 495496 \immediate\closein\s@dread 497\immediate\openin\s@dread=#1 498 \initialsoln \typeout{Sudoku problem #1, \the\solcnt\space initial clues} 499 500 \egroup} \initialsoln Get the clues from the puzzle file, line by line, and insert them into the grid. \s@dline holds one line from the file. 502 % insert the clues from the input game file 503 \newcommand*{\initialsoln}{% \firsts@dcluetrue 505 \s@dnrow\@ne \s@lcnta\@ne 506 507 \loop 508 \ifnum\s@dnrow<10\relax 509 \read\s@dread to \s@dline \firsts@dcluetrue 510 \s@dncol\@ne 511 \dos@dinitialcols 512 \advance\s@dnrow\@ne 513 \repeat 514 515 \immediate\closein\s@dread} \dos@dinitialcols Insert the clues from one line of the puzzle file into one row of the grid. 517 %% insert the clues from one line of the game file 518 \newcommand*{\dos@dinitialcols}{\bgroup 519\loop \ifnum\s@dncol<10\relax 520521 \fixentry \advance\s@dncol\@ne 522 \repeat 523524 \egroup}

\fixentry Inserts a clue from the current line into the grid.

525

```
\expandafter\splitoff\expandafter{\s@dline}%
529
       \global\firsts@dcluefalse
530
     \else
531
       \expandafter\splitoff\expandafter{\restchars}%
532
533
534
     \ifx\s@dfstop\istchar
535
     \else
        \global\useknt{s@lans\the\s@lcnta}=-\istchar
536
       \global\advance\solcnt\@ne
537
       \global\advance\numcluesctr\@ne
538
539
     \global\advance\s@lcnta\@ne}
540
541
542
```

3.3 Solution methods

Three facts are used to generate a solution.

- 1. A digit must be unique within a row, a column, and a block Thus, if a solution, say N, is known for a cell, then the potential solution N must be deleted from all cells in the row, column, and block that the solved cell is in. I have called this a simple reduction. The simple reductions are repeated until there are no changes to the potential solutions.
- 2. If among all the cells in a row (column, block) there is a digit that occurs only once among all the potential solutions, then that digit is the solution for its cell. I have termed this a loner. If a loner solution is found then simple reductions are repeated.
- 3. If among all the cells in a row (column, block) there are two digits which occur twice only in the row, each time as a pair (e.g., 39 and 39) then one or other of the two digits must be a solution for a cell in which the pairs occur. This means that the two digits in the pair cannot occur anywhere else in the row (column, block). If there are no loners then the problem is examined for pairs. If there is any change in a potential solution then the simple reduction process is applied.

The process stops either when all 81 cells have been solved or there is no change in any potential solution after going through all the above reductions.

There are more sophisticated solution techniques that could be applied but they are also increasingly difficult to code in TeX.

\reduceacell

\reduceacell looks at the solution set for the current cell (the \s@lcnta cell) and if the cell has been solved then it deletes the solution digit from the row, column, and box in which the cell appears. This may result in new solutions for other cells.

Given a cell number N (0 < N < 82) and, using integer arithmetic, putting M = (N-1)/9 then

• Cell number C at top of column: C = N - 9M

• Cell number R at left of row: R = 9M + 1

```
• Cell number b at top left of 3 by 3 box: B = 27(M/3) + 3((N-1-9M)/3) + 1
            543 \% Eliminate a solution digit from its row, column and box.
            544 %% This may result in some new solutions.
            545 \newcommand*{\reduceacell}{\bgroup
                 \ifnum\useknt{s@lans\the\s@lcnta}<\z@
                                                             % solved cell
                    \s@dtempcnta=-\useknt{s@lans\the\s@lcnta}
            547
            548 %% get the col, row and box numbers
                    \tempcnty=\s@lcnta
                                               % M in the formulae
            549
                    \advance\tempcnty\m@ne
                                               \divide\tempcnty 9\relax
            550
                                               \multiply\tempcntz 9\relax
            551
                    \tempcntz=\tempcnty
                    \s@dcolpos=\s@lcnta
                                                  \advance\s@dcolpos -\tempcntz % col
            552
                    \s@drowpos\tempcntz
                                                  \advance\s@drowpos\@ne
            553
                                                                                     % row
                    \boxctr=\tempcnty
                                               % box
            554
                    \divide\boxctr\thr@@
                                               \multiply\boxctr 27\relax
            555
                                               % reuse \tempcnty
                    \tempcnty=\s@lcnta
            556
                                               \advance\tempcnty -\tempcntz
            557
                    \advance\tempcnty\m@ne
            558
                    \divide\tempcnty\thr@@
                                              \multiply\tempcnty \thr@@
                    \advance\boxctr\tempcnty \advance\boxctr \@ne
            559
            560 %% reduce the row, column, and the box
                    \reducerow{\the\s@drowpos}{\the\s@dtempcnta}
            561
                    \reducecol{\the\s@dcolpos}{\the\s@dtempcnta}
            562
                    \reducebox{\the\boxctr}{\the\s@dtempcnta}
            563
            564
                 \fi
            565 \egroup}
            \ensuremath{\mbox{reducerow}\{\langle row \rangle\}} \{\langle digit \rangle\}\ eliminates\ \langle digit \rangle\ from\ the\ binary\ solution\ sets\ of
\reducerow
            the cells in the row starting at cell number \langle row \rangle.
            567 %% \reducerow{rowcellnumber}{digit}
            568 %% simple reduction for digit in a row
            569 \newcommand*{\reducerow}[2]{\bgroup
                 \s@dncol=#1\relax
                 \toprangectr=\s@dncol
            571
            572
                 \advance\toprangectr 9\relax
                 \bgroup
            573
                 \loop
            574
                    \ifnum\s@dncol<\toprangectr
            575
                    \deletenumfromset{#2}{\the\useknt{s@lans\the\s@dncol}}{\reducedctr}
            576
                    \ifsetchanged
            577
            578
                      \global\changedtrue
            579
                      \settonum{\the\reducedctr}{\numlistctr}
            580
                      \ifnum\numlistctr<10\relax
                        \global\advance\solcnt\@ne
            581
            582 \commentary{\the\solcnt\space solved
            583
                            (\the\s@dncol\space = \the\numlistctr\space in row starting #1)}%
```

```
\global\useknt{s@lans\the\s@dncol}=\numlistctr
            584
                       \else
            585
                         \global\useknt{s@lans\the\s@dncol}=\reducedctr
            586
                       \fi
            587
                     \fi
            588
            589
                     \advance\s@dncol\@ne
            590
                  \repeat
            591
                  \egroup
            592 \egroup}
            593
\reducecol \reducecol\{\langle col\}\{\langle digit\}\ eliminates \langle digit\rangle from the binary solution sets of the
             cells in the column starting at cell number \langle col \rangle.
            594 %% \reducecol{colcellnumber}{digit}
            595 \% simple reduction of a digit in a column
            596 \newcommand*{\reducecol}[2]{\bgroup
            597
                  \s@dnrow=#1\relax
            598
                  \toprangectr=\s@dnrow
                  \advance\toprangectr 73\relax
            599
                  \bgroup
            600
                  \loop
            601
                    \ifnum\s@dnrow<\toprangectr
            602
                     \deletenumfromset{#2}{\the\useknt{s@lans\the\s@dnrow}}{\reducedctr}
            603
            604
                    \ifsetchanged
                       \global\changedtrue
            605
                       \settonum{\the\reducedctr}{\numlistctr}
            606
            607
                       \ifnum\numlistctr<10\relax
            608
                           \global\advance\solcnt\@ne
            609 \commentary{\the\solcnt\space solved
                              (\the\s@dnrow\space = \the\numlistctr\space in column starting #1)}%
            610
            611
                           \global\useknt{s@lans\the\s@dnrow}=\numlistctr
            612
                         \global\useknt{s@lans\the\s@dnrow}=\reducedctr
            613
                       \fi
            614
                     \fi
            615
                     \advance\s@dnrow 9\relax
            616
            617
                  \repeat
                  \egroup
            618
            619 \egroup}
\reducebox \reducebox{\langle box \rangle}{\langle digit \rangle} eliminates \langle digit \rangle from the binary solution sets of the
             cells in the box starting at cell number \langle box \rangle.
            621 %% \reducebox{boxcellnumber}{digit}
            622 %% simple reduction of a digit in a box
            623 \newcommand*{\reducebox}[2]{\bgroup
                  \s@dncol=#1\relax
            624
            625
                  \toprangectr=\s@dncol
            626
                  \advance\toprangectr \thr@@
```

```
\bgroup
627
     \loop
628
       \ifnum\s@dncol<\toprangectr
629
       \s@dnrow=\s@dncol
630
       \deletenumfromset{#2}{\the\useknt{s@lans\the\s@dnrow}}{\reducedctr}
631
632
       \ifsetchanged
633
         \global\changedtrue
         \settonum{\the\reducedctr}{\numlistctr}
634
635
         \ifnum\numlistctr<10\relax
             \global\advance\solcnt\@ne
636
637 \commentary{\the\solcnt\space solved
                (\the\s@dnrow\space = \the\numlistctr\space in box starting #1)}%
638
639
              \global\useknt{s@lans\the\s@dnrow}=\numlistctr
640
            \global\useknt{s@lans\the\s@dnrow}=\reducedctr
641
         \fi
642
       \fi
643
       \advance\s@dnrow 9\relax
644
645
       \deletenumfromset{#2}{\the\useknt{s@lans\the\s@dnrow}}{\reducedctr}
646
       \ifsetchanged
647
         \global\changedtrue
648
         \settonum{\the\reducedctr}{\numlistctr}
         \ifnum\numlistctr<10\relax
649
             \global\advance\solcnt\@ne
650
651 \commentary{\the\solcnt\space solved
652
                (\the\s@dnrow\space = \the\numlistctr\space in box starting #1)}%
              \global\useknt{s@lans\the\s@dnrow}=\numlistctr
653
654
           \global\useknt{s@lans\the\s@dnrow}=\reducedctr
655
         \fi
656
657
658
       \advance\s@dnrow 9\relax
659
       \deletenumfromset{#2}{\the\useknt{s@lans\the\s@dnrow}}{\reducedctr}
660
       \ifsetchanged
661
         \global\changedtrue
         \settonum{\the\reducedctr}{\numlistctr}
662
         \ifnum\numlistctr<10\relax
663
664
             \global\advance\solcnt\@ne
665 \commentary{\the\solcnt\space solved
                (\the\s@dnrow\space = \the\numlistctr\space in box starting #1)}%
666
667
              \global\useknt{s@lans\the\s@dnrow}=\numlistctr
668
         \else
           \global\useknt{s@lans\the\s@dnrow}=\reducedctr
669
         \fi
670
671
       \fi
       \advance\s@dncol \@ne
672
673
     \repeat
674
     \egroup
675 \geq 675
676
```

\reduceallcells examines all 81 cells, eliminating solution digits from the binary solution sets of the other cells in the row, column, and box.

```
677 %% loop over every cell, removing solution digits from the potential sets
678 %% in the cell's row, column and box.
679 \newcommand*{\reduceallcells}{\bgroup
680
     \ifnum\difficultyctr<\One
681
       \global\difficultyctr\@ne
     \fi
682
683
     \s@lcnta\@ne
     \global\changedfalse
684
685
     \loop
       \ifnum\s@lcnta<82\relax
686
687
       \reduceacell
       \advance\s@lcnta\@ne
688
     \repeat
689
690 \egroup}
```

\keepreducing

\keepreducing performs simple reductions on all the cells until either the puzzle is solved or no changes have been made. It then tries loner reductions, returning to simple reductions following any change. If no change has been made after loner reductions it then tries pair reductions. After any change it goes back to simple reductions. This iterative process continues until either the puzzle has been solved (\solcnt = 81) or no further changes can be made.

A measure of the difficulty of the puzzle could be made by incrementing a count each time a new kind of reduction is tried. The increment increases with the complexity of the reduction.

```
692 \newcommand*{\keepreducing}{%
     \anychangetrue
693
     \keepontrue
694
695
     \loop
696
       \ifkeepon
       \keepreducingcells
697
       \ifnum\solcnt<81\relax
698
699 %%%
             \advance\difficultyctr 4\relax
700
         \reduceloners
701
        \anychangefalse
702
       \iflonerchanged
703
         \anychangetrue
704
705
       \ifanychange\else
706
         \ifnum\solcnt<81\relax
707
               \advance\difficultyctr 8\relax
708 %%%
            \pairchangedfalse
709
            \reducepairs
710
            \ifpairchanged
711
712
              \anychangetrue
713
            \fi
```

```
715
                                                                                    \fi
                                                                716
                                                                                    \checkkeepon
                                                                              \repeat
                                                                717
                                                                              \  \in \ \sl \ \
                                                                718
                                                                719
                                                                                    \global\multiply \difficultyctr 10\relax
                                                                720
                                                                              \fi
                                                                721 \typeout{********* Number of solutions = \the\solcnt}
                                                                722 \typeout{******** Difficulty rating = \the\difficultyctr}
                                                                723 }
                                                                724
                           \checkkeepon Determines whether or not to keep on trying to reach the solution.
                                                                725 \newcommand*{\checkkeepon}{%
                                                                              \ifnum\solcnt>80\relax
                                                                727
                                                                                    \keeponfalse
                                                                728
                                                                              \ifanychange\else
                                                                                    \keeponfalse
                                                                730
                                                                              \fi}
                                                                731
                                                                732
          \keepreducingcells
                                                               Keep on trying the simple reduction.
                                                                733 %% Keep performing the simple reduction
                                                                734 \newcommand*{\keepreducingcells}{\bgroup
                                                                735 \commentary{Simple reductions}%
                                                                              \ifnum\difficultyctr<\tw0
                                                                737
                                                                                    \global\difficultyctr\tw@
                                                                              \fi
                                                                738
                                                                              \changedtrue
                                                                739
                                                                              \loop
                                                                740
                                                                                    \ifchanged
                                                                741
                                                                742
                                                                                    \reduceallcells
                                                                743
                                                                                    \checksimplereductions
                                                                              \repeat
                                                                744
                                                                745 \egroup}
                                                                746
\checksimplereductions
                                                                 Determines whether or not to keep on trying simple reductions.
                                                                747 \newcommand*{\checksimplereductions}{%
                                                                              \ifchanged\else
                                                                748
                                                                                    \typesimplestatus
                                                                749
                                                                              \fi
                                                                750
                                                                751
                                                                              \ifnum\solcnt>80\relax%
                                                                                                                                                       solution found!
                                                                752
                                                                                    \changedfalse
                                                                753
                                                                              \fi}
                                                                754
                                                                756
```

714

\fi

796 797

798

\repeat}

Reduce via the loner digits, trying rows first, and if no change then trying columns, \reduceloners and if still no change then trying boxes. 757 %% reduce the loner digits, per row, column and box 758 \newcommand*{\reduceloners}{% 759 \commentary{reduceloners}% 760 \global\lonerchangedfalse \ifnum\difficultyctr<4\relax 761762 \global\difficultyctr=4\relax 763 \ifnum\solcnt>80\else 764 765 \bgroup 766 \reducerowloners 767 \iflonerchanged\else \reducecolloners 768 \iflonerchanged\else 769 770 \reduceboxloners 771 772 \fi \typelonestatus 773 774 \egroup 775 \fi} 776 \reducerowloners Loop through the rows and reduce the first loner found. 777 %% Loop through the rows, reducing loners 778 \newcommand*{\reducerowloners}{% 779 \sumctr\z@ \s@dnrow\@ne 780 781\loop 782\ifnum\s@dnrow<10\relax \s@lcnta=\s@dnrow \advance\s@lcnta\m@ne 783 \multiply\s@lcnta 9\relax \advance\s@lcnta\@ne 784 785 \sumrowsets \ifnum\sumctr>\z@ 786 \getloner{\the\sumctr}{\s@dtempcntb} 787 \ifnum\s@dtempcntb=\z@ 788 \else \reducelonerrowcell{\the\s@lcnta}{\the\s@dtempcntb} 790 \iflonerchanged 791 \advance\s@dnrow 10\relax 792 793 \fi \fi 794795 \fi \advance\s@dnrow\@ne

\sumrowsets Add together all the solution binary sets for the unsolved cells in the current row (\s@lcnta). The result is in \sumctr.

799 %% add the sets in the current row

```
800 \newcommand*{\sumrowsets}{%
                 \bgroup
           801
                 \s@dncol=\s@lcnta
           802
                 \toprangectr=\s@dncol
           803
           804
                 \advance\toprangectr 9\relax
           805
                 \global\sumctr\z0
           806
                 \loop
                   \ifnum\s@dncol<\toprangectr
           807
                   \ifnum\useknt{s@lans\the\s@dncol}>\z@
           808
                     \global\advance\sumctr\useknt{s@lans\the\s@dncol}
           809
           810
                   \advance\s@dncol\@ne
           811
           812
                 \repeat
                 \egroup}
           813
           814
            \ensuremath{\mbox{getloner}\{\langle setsum\rangle\}\{\langle cnt\rangle\}} examines (the sum of) a solution set and returns
\getloner
            the first loner (i.e., the first occurrence of the digit 1), or zero if there is none. The
            result is converted to a solution digit and assigned to the \count \langle cnt \rangle.
               For example, given the set [000200110] it will return 7 (the set indicates two
            4s, one 7, and one 8).
           815 \%\% get the loner from a setsum
           816 %% \getloner{setsum}{returnctr} returnes the (first) loner in a potential set,
           817 %% or zero
           818 \newcommand*{\getloner}[2]{\bgroup
           819
                 \ifnum #1>\z@
                   \s@dtemploopcnta\@ne
           820
           821
                   \loop
                     \ifnum\s@dtemploopcnta<10\relax
           822
                     \numofnuminset{\the\s@dtemploopcnta}{#1}{\s@dtempcnta}
           823
                     \ifnum\s@dtempcnta=\@ne%
                                                          found a lone digit
           824
                       \s@dtempcnta=\s@dtemploopcnta
           825
                       \scalebox{0.000cmta=100\relax}
           826
           827
                     \advance\s@dtemploopcnta\@ne
           828
           829
                   \ifnum\s@dtemploopcnta>99 \else \s@dtempcnta=\z@ \fi
           830
           831
                   \global#2=\s@dtempcnta
           832
                 \else
                   \s@dtempcnta=\z@
           833
           834
                   \global#2=\s@dtempcnta
           835
                 \fi
           836 \egroup}
```

\reducelonerowcell \(\lambda colonerowcell\)\{\(\lambda digit\)\}. Given (the cell at) the start of a row and a lone digit, find the cell in the row with that digit in its solution set, and make the digit the solution of that cell.

838 %% \reducelonerowcell{startofrowcell}{digit}

```
839\ \mbox{\%\%} given a row and a lone digit, find the cell containing the digit
                  840\ \mbox{\%\%} and make the digit a solution of that cell.
                  841 \newcommand*{\reducelonerrowcell}[2]{\bgroup
                       \s@dncol=#1
                  842
                  843
                       \toprangectr=\s@dncol
                  844
                       \advance\toprangectr 9\relax
                       \ifnum #2<\@ne
                  845
                         \advance\s@dncol 100\relax
                  846
                       \fi
                  847
                  848
                       \loop
                  849
                         \ifnum\s@dncol<\toprangectr
                          \numofnuminset{#2}{\the\useknt{s@lans\the\s@dncol}}{\lonecellctr}
                  850
                          \ifnum\lonecellctr=\@ne%
                                                       this cell has the loner
                  851
                            \lonecellctr=#2
                  852
                            \global\useknt{s@lans\the\s@dncol}=-\lonecellctr
                  853
                            \global\lonerchangedtrue
                  854
                            \global\advance\solcnt\@ne
                  856 \commentary{\the\solcnt\space solved (#2 loner in row starting #1)}%
                  857
                            \s@dncol=\toprangectr
                  858
                  859
                         \advance\s@dncol\@ne
                       \repeat
                  860
                  861 \egroup}
                  862
\reducecolloners Loop through the columns and reduce the first loner found.
                  863 \% Loop through the columns, reducing loners
                  864 \newcommand*{\reducecolloners}{\bgroup
                       \sumctr\z@
                  865
                       \s@dncol\@ne
                  866
                  867
                       \loop
                         \ifnum\s@dncol<10\relax
                  868
                          \s@lcnta=\s@dncol
                  869
                  870
                          \sumcolsets
                  871
                          \ifnum\sumctr>\z@
                            \getloner{\the\sumctr}{\s@dtempcntb}
                  872
                            \ifnum\s@dtempcntb=\z@
                  873
                            \else
                  874
                              \reducelonercolcell{\the\s@lcnta}{\the\s@dtempcntb}
                  875
                              \iflonerchanged
                  876
                                \advance\s@dncol 10\relax
                  877
                              \fi
                  878
                           \fi
                  879
                  880
                         \fi
                  881
                         \advance\s@dncol\@ne
                       \repeat
                  882
                  883 \egroup}
                  884
```

```
Sum all the solution sets of the unsolved cells in the current column (\sclcnta).
                      The result is in \sumctr.
                     885 \% add the sets in the current column
                     886 \newcommand*{\sumcolsets}{\bgroup
                          \s@dnrow=\s@lcnta
                     887
                          \toprangectr=\s@dnrow
                     888
                          \advance\toprangectr 73\relax
                     889
                     890
                          \global\sumctr\z0
                     891
                            \ifnum\s@dnrow<\toprangectr
                     892
                     893
                            \ifnum\useknt{s@lans\the\s@dnrow}>\z@
                     894
                               \global\advance\sumctr\useknt{s@lans\the\s@dnrow}
                            \fi
                     895
                            \advance\s@dnrow 9\relax
                     896
                     897
                          \repeat
                     898 \egroup}
\reducelonercolcell \reducelonercolcell{\langle colcell}\{\langle digit\}\}. Given (the cell at) the start of a col-
                      umn and a lone digit, find the cell in the column with that digit in its solution
                      set, and make the digit the solution of that cell.
                     900 %% \reducelonercolcell{startofcolcell}{digit}
                     901 %% given a col and a lone digit, find the cell containing the digit
                     902 %% and make the digit a solution of that cell.
                     903 \newcommand*{\reducelonercolcell}[2]{\bgroup
                     904
                          \s@dnrow=#1
                     905
                          \toprangectr=\s@dnrow
                     906
                          \advance\toprangectr 73\relax
                          \ifnum #2<\@ne
                     907
                            \advance\s@dnrow 7300\relax
                     908
                          \fi
                     909
                     910
                          1000
                            \ifnum\s@dnrow<\toprangectr
                     911
                            \numofnuminset{#2}{\the\useknt{s@lans\the\s@dnrow}}{\lonecellctr}
                     912
                                                          this cell has the loner
                            \ifnum\lonecellctr=\@ne%
                     913
                     914
                               \lonecellctr=#2
                               \global\useknt{s@lans\the\s@dnrow}=-\lonecellctr
                     915
                     916
                              \global\lonerchangedtrue
                     917
                              \global\advance\solcnt\@ne
                     918 \commentary{\the\solcnt\space solved (#2 loner in column starting #1)}%
                     919
                              \s@dnrow=\toprangectr
                     920
                            \fi
                     921
                            \advance\s@dnrow 9\relax
                          \repeat
                     922
                     923
                          \egroup}
                     924
   \reduceboxloners Loop through the boxes and reduce the first loner found.
                     925 %% Loop through the boxes, reducing loners
```

```
926 \newcommand*{\reduceboxloners}{\bgroup
            927
                  \sumctr\z@
                  \boxctr\@ne
            928
                  \loop
            929
                    \ifnum\boxctr<10\relax
            930
             The next bit of code calculates the corner cell of the Nth box.
                      \ifcase\boxctr
            932
                      \or \s@lcnta=\@ne
            933
                      \or \s@lcnta=4\relax
                      \or \s@lcnta=7\relax
            934
                      \or \s@lcnta=28\relax
            935
            936
                      \or \s@lcnta=31\relax
            937
                      \or \s@lcnta=34\relax
                      \or \s@lcnta=55\relax
            938
                      \or \s@lcnta=58\relax
            939
                      \or \s@lcnta=61\relax
            940
                      \fi
            941
                      \sumboxsets
            942
                      \ifnum\sumctr>\z0
            943
                        \getloner{\the\sumctr}{\s@dtempcntb}
            944
                        \ifnum\s@dtempcntb=\z@
            945
            946
                        \else
                          \reducelonerboxcell{\the\s@lcnta}{\the\s@dtempcntb}
            947
            948
                             \iflonerchanged
                               \advance\boxctr 10\relax
            949
            950
                             \fi
                        \fi
            951
                      \fi
            952
                    \advance\boxctr\@ne
            953
                  \repeat
            954
            955 \egroup}
\sumboxsets Sum all the solution sets of the unsolved cells in the current box (\s@lcnta). The
             result is in \sumctr.
            957 %% add the sets in the current box
            958 \newcommand*{\sumboxsets}{\bgroup
                  \s@dncol=\s@lcnta
            959
                  \toprangectr=\s@dncol
            960
                  \advance\toprangectr 3\relax
            961
                  \global\sumctr\z@
            962
            963
                  \loop
                    \ifnum\s@dncol<\toprangectr
            964
                    \s@dnrow=\s@dncol
            965
                    \ifnum\useknt{s@lans\the\s@dnrow}>\z@
            966
                      \global\advance\sumctr\useknt{s@lans\the\s@dnrow}
            967
            968
            969
                    \advance\s@dnrow 9\relax
            970
                    \ifnum\useknt{s@lans\the\s@dnrow}>\z@
```

```
\global\advance\sumctr\useknt{s@lans\the\s@dnrow}
                    971
                    972
                            \advance\s@dnrow 9\relax
                    973
                            974
                              \global\advance\sumctr\useknt{s@lans\the\s@dnrow}
                    975
                    976
                    977
                            \advance\s@dncol\@ne
                    978
                         \repeat
                    979 \egroup}
                    980
\reducelonerboxcell \reducelonerboxcell{\langle boxcell}\}{\langle digit\}. Given (the cell at) the start of a box
                     and a lone digit, find the cell in the box with that digit in its solution set, and
                     make the digit the solution of that cell.
                    981 %% \reducelonerboxcell{startofboxcell}{digit}
                    982 \% given a box and a lone digit, find the cell containing the digit
                    983 %% and make the digit a solution of that cell.
                    984 \newcommand*{\reducelonerboxcell}[2]{\bgroup
                         \s@dncol=\s@lcnta
                    985
                         \toprangectr=\s@dncol
                    986
                         \advance\toprangectr 3\relax
                    987
                    988
                         \global\sumctr\z@
                    989
                          \loop
                    990
                            \ifnum\s@dncol<\toprangectr
                            \s@dnrow=\s@dncol
                    991
                            \numofnuminset{#2}{\the\useknt{s@lans\the\s@dnrow}}{\lonecellctr}
                    992
                            \ifnum\lonecellctr=\@ne%
                                                        this cell has the loner
                    993
                              \lonecellctr=#2
                    994
                              \global\useknt{s@lans\the\s@dnrow}=-\lonecellctr
                    995
                              \global\lonerchangedtrue
                    996
                              \global\advance\solcnt\@ne
                    997
                    998 \commentary{\the\solcnt\space solved (#2 loner in box starting #1)}%
                              \s@dncol=\toprangectr
                    999
                            \fi
                    1000
                            \iflonerchanged\else
                    1001
                    1002
                              \advance\s@dnrow 9\relax
                    1003
                              \numofnuminset{#2}{\the\useknt{s@lans\the\s@dnrow}}{\lonecellctr}
                              \ifnum\lonecellctr=\@ne%
                                                           this cell has the loner
                    1004
                                \lonecellctr=#2
                    1005
                                \global\useknt{s@lans\the\s@dnrow}=-\lonecellctr
                    1006
                                \global\lonerchangedtrue
                    1007
                                \global\advance\solcnt\@ne
                    1008
                    1009 \commentary{\the\solcnt\space solved (#2 loner in box starting #1)}%
                    1010
                                \s@dncol=\toprangectr
                    1011
                              \fi
                            \fi
                    1012
                            \iflonerchanged\else
                    1013
                              \advance\s@dnrow 9\relax
                    1014
                    1015
                              \numofnuminset{#2}{\the\useknt{s@lans\the\s@dnrow}}{\lonecellctr}
                    1016
                              \ifnum\lonecellctr=\@ne%
                                                           this cell has the loner
```

```
\lonecellctr=#2
               1017
                           \global\useknt{s@lans\the\s@dnrow}=-\lonecellctr
               1018
               1019
                           \global\lonerchangedtrue
                           \global\advance\solcnt\@ne
               1020
               1021 \commentary{\the\solcnt\space solved (#2 loner in box starting #1)}%
               1022
                           \s@dncol=\toprangectr
               1023
                         \fi
                       \fi
               1024
               1025
                       \advance\s@dncol\@ne
                     \repeat
               1026
               1027 \egroup}
               1028
               \reducepairs Perform pair reduction, reducing the first pair found. First try by row, then by
                column, and lastly by box.
               1031 %% reduce the pairs, per row, column and box
               1032 \newcommand*{\reducepairs}{\bgroup
               1033 \commentary{reducepairs}% *******
                                                       *********************
                     \global\pairchangedfalse
               1034
                     \ifnum\difficultyctr<8\relax
               1035
                       \global\difficultyctr=8\relax
               1036
               1037
                     \ifnum\solcnt>80\else
               1038
               1039
                       \reducerowpairs
                       \ifpairchanged\else
               1040
                         \reducecolpairs
               1041
               1042
                         \ifpairchanged\else
                           \reduceboxpairs
               1043
               1044
                         \fi
               1045
                       \fi
                     \fi
               1046
               1047 \egroup}
               1048
\reducerowpairs Loop through the rows and reduce the first pair found.
               1049 %% Loop through the rows, reducing pairs
               1050 \newcommand*{\reducerowpairs}{%
                     \sumctr\z@
               1051
                     \s@dnrow\@ne
               1052
               1053
                     \loop
                       \ifnum\s@dnrow<10\relax
               1054
                       \s@lcnta=\s@dnrow \advance\s@lcnta\m@ne
               1055
               1056
                       \multiply\s@lcnta 9\relax \advance\s@lcnta\@ne
               1057
                       \sumrowsets
                       \ifnum\sumctr>\z@
               1058
               1059
                         \reducearowpair{\the\s@lcnta}
               1060
                         \ifpairchanged
```

```
1061
                              \advance\s@dnrow 10\relax
                 1062
                            \fi
                         \fi
                 1063
                         \advance\s@dnrow\@ne
                 1064
                       \repeat}
                 1065
                 1066
\reducearowpair \reducearowpair{\langle rowcell \rangle} reduces a pair in the row starting with cell \langle rowcell \rangle.
                1067 %% reducearowpair{row}
                 1068 \newcommand*{\reducearowpair}[1]{%
                       \bgroup
                       \s@dncol=#1\relax
                1070
                       \toprangectr=\s@dncol
                1071
                       \advance\toprangectr 9\relax
                1072
                       \maxrangectr=\toprangectr
                 1073
                       \advance\maxrangectr\m@ne
                 1074
                       \global\sumctr\z0
                 1075
                       \loop
                 1076
                         \ifnum\s@dncol<\maxrangectr
                1077
                 1078
                         \asetctr=\useknt{s@lans\the\s@dncol}%
                         \int \sum_{x \in \mathbb{Z}_0} 
                1079
                            \findrowpair
                 1080
                 1081
                         \fi
                         \advance\s@dncol\@ne
                       \repeat
                1083
                       \egroup}
                1084
                1085
   \findrowpair \findrowpair attempts to find a pair in the current row.
                 1086 \newcommand*{\findrowpair}{\bgroup
                       \secondctr=\s@dncol
                 1087
                       \advance\secondctr\@ne
                1088
                       \loop
                 1089
                         \ifnum\secondctr<\toprangectr
                 1090
                            \ifnum\asetctr=\useknt{s@lans\the\secondctr}
                 1091
                              \checksetforpair{\the\asetctr}
                1092
                1093
                              \ifnum\numdigitsctr=\tw@
                 1094 %% first row cell is \s@lcnta
                 1095 %% first pair cell is \s@dncol, second pair cell is \secondctr
                 1096 %% digits are \digitictr and \digitiictr
                 1097
                                \deleterowpairdigits
                 1098
                              \fi
                            \fi
                 1099
                            \advance\secondctr\@ne
                1100
                         \repeat
                1101
                       \egroup}
                1102
                1103
```

\checksetforpair \checksetforpair{ $\langle set \rangle$ } attempts to find a pair in a set. It sets \digitictr and \digitiictr as the first and second digits in the set and \numdigitsctr to

the total number of digits in the set (which is 2 for a pair).

```
1104 %% \checksetforpair{set} returns with:
1105 %%
            \digitictr = first digit
1106 %%
            \digitiictr = second digit
1107 %%
            \numdigitsctr = number of digits (2 for a pair)
1108 \newcommand*{\checksetforpair}[1]{\bgroup
      \s@dtemploopcnta\@ne
1110
      \global\numdigitsctr\z@
1111
      \global\digitictr\z@
1112
      \global\digitiictr\z@
      \loop
1113
1114
        \ifnum\s@dtemploopcnta<10\relax
        \numofnuminset{\the\s@dtemploopcnta}{#1}{\s@dtempcnta}
1115
1116
        \ifnum\s@dtempcnta=\@ne
1117
          \global\advance\numdigitsctr\@ne
1118
          \ifcase\numdigitsctr
1119
          \or \global\digitictr=\s@dtemploopcnta
          \or \global\digitiictr=\s@dtemploopcnta
1120
          \else \advance\s@dtemploopcnta 10\relax
1121
          \fi
1122
1123
1124
        \advance\s@dtemploopcnta\@ne
1125
     \repeat
1126 \egroup}
1127
```

\deleterowpairdigits \deleterowpairdigits deletes the pair digits from non-pair cells in a row. The first cell in the row is \s@lcnta, the cells that contain the two pairs are \s@dncol and \secondctr, and the digits are \digitictr and \digitictr.

```
1128 %% first row cell is \s@lcnta
1129 %% first pair cell is \s@dncol, second pair cell is \secondctr
1130 \% digits are \digitictr and \digitiictr
1131 \newcommand*{\deleterowpairdigits}{\bgroup
      \global\pairchangedfalse
1132
1133
      \s@dtemploopcnta=\s@lcnta
1134
      \toprangectr=\s@dtemploopcnta \advance\toprangectr 9\relax
1135
        \ifnum\s@dtemploopcnta<\toprangectr
1136
        \ifnum\s@dtemploopcnta=\s@dncol
1137
        \else
1138
          \ifnum\s@dtemploopcnta=\secondctr
1139
          \else
1140
            \deletenumfromset{\the\digitictr}%
1141
                             {\the\useknt{s@lans\the\s@dtemploopcnta}}{\s@dtempcnta}
1142
            \ifsetchanged
1143
              \global\useknt{s@lans\the\s@dtemploopcnta}=\s@dtempcnta
1144
              \global\pairchangedtrue
1145
1146
            \fi
1147
            \deletenumfromset{\the\digitiictr}%
```

```
{\the\useknt{s@lans\the\s@dtemploopcnta}}{\s@dtempcnta}
                1148
                            \ifsetchanged
                1149
                               \global\useknt{s@lans\the\s@dtemploopcnta}=\s@dtempcnta
                1150
                               \global\pairchangedtrue
                1151
                            \fi
                1152
                1153
                          \fi
                1154
                        \fi
                      \advance\s@dtemploopcnta\@ne
                1155
                      \repeat
                1156
                1157 \egroup}
                1158
\reducecolpairs Loop through the rows and reduce the first pair found.
                1159 %% Loop through the columns, reducing pairs
                1160 \newcommand*{\reducecolpairs}{%
                      \sumctr\z@
                1161
                      \s@dncol\@ne
                1162
                     \loop
                1163
                1164
                        \ifnum\s@dncol<10\relax
                1165
                        \s@lcnta=\s@dncol
                        \sumcolsets
                1166
                        \ifnum\sumctr>\z@
                1167
                          \reduceacolpair{\the\s@lcnta}
                1168
                          \ifpairchanged
                1169
                            \advance\s@dncol 10\relax
                1170
                1171
                          \fi
                1172
                        \advance\s@dncol\@ne
                1173
                      \repeat}
                1174
                1175
\ reduceacolpair \ reduceacolpair \ reduces a pair in the column starting with cell
                  \langle colcell \rangle.
                1176 %% reduceacolpair{col}
                1177 \newcommand*{\reduceacolpair}[1]{\bgroup
                      \s@dnrow=#1\relax
                1179
                      \toprangectr=\s@dnrow
                      \advance\toprangectr 73\relax
                1180
                      \maxrangectr=\toprangectr
                1181
                      \advance\maxrangectr -9\relax
                1182
                      \global\sumctr\z0
                1183
                      \loop
                1184
                        \ifnum\s@dnrow<\maxrangectr
                1185
                        \asetctr=\useknt{s@lans\the\s@dnrow}%
                1186
                        \ifnum\asetctr>\z@
                1187
                          \findcolpair
                1188
                        \fi
                1189
                        \advance\s@dnrow 9\relax
                1190
                1191
                      \repeat
                1192
                      \egroup}
```

1193

\findcolpair \findcolpair attempts to find a pair in the current column.

```
1194 \newcommand*{\findcolpair}{\bgroup
      \secondctr=\s@dnrow
1195
1196
      \advance\secondctr 9\relax
1197
        \ifnum\secondctr<\toprangectr
1198
1199
          \ifnum\asetctr=\useknt{s@lans\the\secondctr}
1200
            \checksetforpair{\the\asetctr}
            \ifnum\numdigitsctr=\tw@
1201
1202 %% first row cell is \s@lcnta
1203 %% first pair cell is \s@dnrow, second pair cell is \secondctr
1204 %% digits are \digitictr and \digitiictr
              \deletecolpairdigits
1205
            \fi
1206
          \fi
1207
          \advance\secondctr 9\relax
1208
1209
        \repeat
1210
      \egroup}
1211
```

\deletecolpairdigits \deletecolpairdigits deletes the pair digits from non-pair cells in a column.

The first cell in the column is \s@lcnta, the cells that contain the two pairs are \s@dncol and \secondctr, and the digits are \digitictr and \digitictr.

```
1212 %% first col cell is \s@lcnta
1213 %% first pair cell is \s@dnrow, second pair cell is \secondctr
1214 \% digits are \digitictr and \digitiictr
1215 \newcommand*{\deletecolpairdigits}{\bgroup
      \global\pairchangedfalse
1216
1217
      \s@dtemploopcnta=\s@lcnta
      \toprangectr=\s@dtemploopcnta \advance\toprangectr 73\relax
1218
      \loop
1219
        \ifnum\s@dtemploopcnta<\toprangectr
1220
1221
        \ifnum\s@dtemploopcnta=\s@dnrow
1222
        \else
          \ifnum\s@dtemploopcnta=\secondctr
1223
1224
          \else
            \deletenumfromset{\the\digitictr}%
1225
                              {\the\useknt{s@lans\the\s@dtemploopcnta}}{\s@dtempcnta}
1226
            \ifsetchanged
1227
              \global\useknt{s@lans\the\s@dtemploopcnta}=\s@dtempcnta
1228
              \global\pairchangedtrue
1229
1230
            \deletenumfromset{\the\digitiictr}%
1231
                              {\the\useknt{s@lans\the\s@dtemploopcnta}}{\s@dtempcnta}
1232
            \ifsetchanged
1233
1234
              \global\useknt{s@lans\the\s@dtemploopcnta}=\s@dtempcnta
1235
              \global\pairchangedtrue
```

```
1236
                               \fi
                 1237
                             \fi
                           \fi
                 1238
                        \advance\s@dtemploopcnta 9\relax
                 1239
                 1240
                        \repeat
                 1241 \egroup}
                 1242
\reduceboxpairs Loop through the boxes and reduce the first pair found.
                 1243 %% Loop through the boxes, reducing pairs
                 1244 \newcommand*{\reduceboxpairs}{\bgroup
                 1245
                        \sumctr\z@
                 1246
                        \boxctr\@ne
                        \loop
                 1247
                           \ifnum\boxctr<10\relax
                 1248
                             \ifcase\boxctr
                 1249
                             \or \s@lcnta=\@ne
                 1250
                             \or \s@lcnta=4\relax
                 1251
                 1252
                             \or \s@lcnta=7\relax
                 1253
                             \or \s@lcnta=28\relax
                             \or \s@lcnta=31\relax
                 1254
                 1255
                             \or \s@lcnta=34\relax
                             \or \s@lcnta=55\relax
                 1256
                             \or \s@lcnta=58\relax
                 1257
                 1258
                             \or \s@lcnta=61\relax
                 1259
                             \fi
                 1260
                             \sumboxsets
                             \ifnum\sumctr>\z@
                 1261
                 1262
                               \reduceaboxpair{\the\s@lcnta}
                 1263
                               \ifpairchanged
                 1264
                                   \advance\boxctr 10\relax
                 1265
                               \fi
                 1266
                             \fi
                 1267
                             \advance\boxctr\@ne
                 1268
                        \repeat
                 1269 \egroup}
                 1270
 \getnthboxcell \getnthboxcell\{\langle n \rangle\}\{\langle firstcell \rangle\}\{\langle cnt \rangle\}. Given the first cell (\langle firstcell \rangle) in a box
                   and a number, \langle n \rangle, between 1 and 9, set the \count \langle cnt \rangle to the cell number of
                   the \langle n \rangleth cell in the box.
                 1271 %% \getnthboxcell{n}{firstcell}{returnctr}
                 1272 \newcommand*{\getnthboxcell}[3]{\bgroup
                        \s@dtempcnta=#2
                 1273
                        \ifcase#1
                 1274
                        \or
                 1275
                        \or \advance\s@dtempcnta 9\relax
                 1276
                 1277
                        \or \advance\s@dtempcnta 18\relax
                        \or \advance\s@dtempcnta \@ne
```

```
\or \advance\s@dtempcnta 10\relax
                1279
                      \or \advance\s@dtempcnta 19\relax
                1280
                      \or \advance\s@dtempcnta \tw@
                1281
                      \or \advance\s@dtempcnta 11\relax
                1282
                      \or \advance\s@dtempcnta 20\relax
                1283
                1284
                1285
                      \global #3=\s@dtempcnta
                1286 \egroup}
                1287
\reduceaboxpair \reduceaboxpair{\langle boxcell \rangle} reduces a pair in the box starting with cell \langle boxcell \rangle.
                1288 %% \reduceaboxpair{startofboxcell}
                1289 \newcommand*{\reduceaboxpair}[1]{\bgroup
                      \s@dtemploopcnta\@ne
                1290
                      \toprangectr=\s@dtemploopcnta
                1291
                      \advance\toprangectr 9\relax
                1292
                      \maxrangectr=\toprangectr
                1293
                      \advance\maxrangectr\m@ne
                1294
                1295
                      \loop
                1296
                        \ifnum\s@dtemploopcnta<\maxrangectr
                         \getnthboxcell{\the\s@dtemploopcnta}{#1}{\s@dtempcnta}
                1297
                         \asetctr=\useknt{s@lans\the\s@dtempcnta}
                1298
                         \ifnum\asetctr>\z@
                1299
                           \s@dnrow=\s@dtemploopcnta
                1300
                           \findboxpair{#1}
                1301
                1302
                         \advance\s@dtemploopcnta\@ne
                1303
                1304
                      \repeat
                1305 \geq 1305
                1306
   \findboxpair \findboxpair attempts to find a pair in the current box, and then does a pair
                  reduction for the box.
                1307 %% \findboxpair{startofboxcell}
                1308 \newcommand*{\findboxpair}[1]{%
                1309
                      \bgroup
                1310
                         \secondctr=\s@dtemploopcnta
                         \advance\secondctr\@ne
                1311
                        \loop
                1312
                           \ifnum\secondctr<\toprangectr
                1313
                           \getnthboxcell{\the\secondctr}{#1}{\s@dtempcntb}
                1314
                           \ifnum\asetctr=\useknt{s@lans\the\s@dtempcntb}
                1315
                1316
                             \checksetforpair{\the\asetctr}
                             \ifnum\numdigitsctr=\tw0
                1318 %% first box cell is #1 (=\s@lcnta)
                1319 %% first pair cell is \s@dnrow, second pair cell is \secondctr
                1320 %% digits are \digitictr and \digitiictr
                               \deleteboxpairdigits{#1}
                1321
                1322
                             \fi
                1323
                           \fi
```

```
1324 \advance\secondctr \@ne
1325 \repeat
1326 \egroup}
1327
```

\deleteboxpairdigits

\deleteboxpairdigits{ $\langle boxcell \rangle$ } deletes the pair digits from non-pair cells in a box. The first cell in the box is $\langle boxcell \rangle$, the cells that contain the two pairs are \s@dnrow and \secondctr, and the digits are \digitictr and \digitictr.

```
1328 %% first box cell is #1
1329 %% first pair cell is \s@dnrow, second pair cell is \secondctr
1330 %% digits are \digitictr and \digitiictr
1331 \newcommand*{\deleteboxpairdigits}[1]{\bgroup
1332
      \global\pairchangedfalse
      \s@dtemploopcnta=\@ne
1333
      \toprangectr=\s@dtemploopcnta \advance\toprangectr 9\relax
1334
1335
1336
        \ifnum\s@dtemploopcnta<\toprangectr
        \ifnum\s@dtemploopcnta=\s@dnrow
1337
1338
          \ifnum\s@dtemploopcnta=\secondctr
1339
1340
             \getnthboxcell{\the\s@dtemploopcnta}{#1}{\s@dtempcntb}
1341
            \deletenumfromset{\the\digitictr}%
1342
1343
                               {\the\useknt{s@lans\the\s@dtempcntb}}{\s@dtempcnta}
1344
            \ifsetchanged
               \global\useknt{s@lans\the\s@dtempcntb}=\s@dtempcnta
1345
               \global\pairchangedtrue
1346
1347
            \deletenumfromset{\the\digitiictr}%
1348
                               {\the\useknt{s@lans\the\s@dtempcntb}} {\the\useknt{s@dtempcnta}}
1349
            \ifsetchanged
1350
               \global\useknt{s@lans\the\s@dtempcntb}=\s@dtempcnta
1351
1352
               \global\pairchangedtrue
            \fi
1353
          \fi
1354
1355
1356
      \advance\s@dtemploopcnta \@ne
      \repeat
1358
    \egroup}
1359
```

3.3.1 Checking the solution

We have found a solution when all the binary sets are negative. It's less efficient, but probably more useful, to check each row, column, and block (3 times 81 tests instead of 81).

1401

\boxctr\@ne

```
\checksolution Check the solution by rows, columns, and boxes.
               1362 \newcommand*{\checksolution}{%
                     \checkrows
               1363
                     \checkcols
               1364
               1365
                     \checkboxes}
    \checkrows Check the row solutions. A row is said to be correct if a solution has been assigned
                to each cell in the row, thus relying on the assumption that the solver never makes
                a mistake. The check is not sufficient for a solution obtained in another manner.
               1367 \newcommand*{\checkrows}{%
                     \sumctr\z@
               1368
                     \s@dnrow\@ne
               1369
               1370
                     \loop
                       \ifnum\s@dnrow<10\relax
               1371
                       \s@lcnta=\s@dnrow \advance\s@lcnta\m@ne
               1372
                       \multiply\s@lcnta 9\relax \advance\s@lcnta\@ne
               1373
                       \sumrowsets
               1374
                       \ifnum\sumctr=\z0\else
               1375
               1376 \typeout{Row \the\s@dnrow\space is incorrect}%
               1377
                         Row \the\s@dnrow\space is incorrect. \\
               1378
                       \advance\s@dnrow\@ne
               1379
                     \repeat}
               1380
               1381
    \checkcols Check the column solutions.
               1382 \newcommand*{\checkcols}{%
               1383 \bgroup
                     \sumctr\z@
               1384
                     \s@dncol\@ne
               1385
                     \loop
               1386
                       1387
                       \s@lcnta=\s@dncol
               1388
               1389
                       \sumcolsets
                       \ifnum\sumctr=\z@\else
               1390
               1391 \typeout{Column \the\s@dncol\space is incorrect}%
                         Column \the\s@dncol\space is incorrect. \\
               1392
                       \fi
               1393
                       \advance\s@dncol\@ne
               1394
               1395
                     \repeat
               1396 \egroup}
   \checkboxes Check the box solutions.
               1398 \newcommand*{\checkboxes}{%
               1399 \bgroup
               1400
                     \sumctr\z@
```

```
1402
                     \loop
                1403
                       \ifnum\boxctr<10\relax
                1404 \ifcase\boxctr
                1414 \fi
                1415
                       \sumboxsets
                       \ifnum\sumctr=\z@\else
                1416
                1417 \typeout{Box \the\boxctr\space is incorrect}%
                        Box \the\boxctr\space is incorrect. \\
                       \fi
                1419
                1420
                       \advance\boxctr\@ne
                1421 \repeat
                1422 \egroup}
                1423
\typesimplestatus X May be used to display the cuurrent status of the (partial) solution following
                 simple reductions.
                1424 \% typeset the current status of the partial solution
                1425 \newcommand*{\typesimplestatusX}{%
                1426 \par\noindent\begin{minipage}{\linewidth}
                1427 \begin{center}
                1428 Simple reductions stopped (with \t \solcnt\space solutions)\\
                1429 %\footnotesize
                1430 \displaystatus
                1431 \end{center}
                1432 \end{minipage}}
 \typelonestatusX May be used to display the current status of the (partial) solution after a loner
                 reduction.
                1434 %% typeset the current status after loner processing
                1435 \newcommand*{\typelonestatusX}{%
                1436 \par\noindent\begin{minipage}{\linewidth}
                1437 \begin{center}
                1438 Loners processed (with \the\solcnt\space solutions)\\
                1439 %\footnotesize
                1440 \displaystatus
                1441 \end{center}
                1442 \end{minipage}}
    \hideprogress Normally the progress towards a solution is not displayed. It will be displayed in
```

\showprogess

the document, though, after the \showprogress declaration. The \hideprogress declaration switches off the displays. 1444 %% For curiosity as to how a solution is developing call the \showprogess 1445 %% declaration (\hideprogess turns this off). 1446 \newcommand*{\hideprogress}{% \let\typesimplestatus\relax \let\typelonestatus\relax} 1448 1449 \newcommand*{\showprogress}{% \let\typesimplestatus\typesimplestatusX \let\typelonestatus\typelonestatusX} 1452 \hideprogress 1453 %\showprogress 1454 1456 \sudsolnfile \writegame writes the (partial) solution to the file \sudsolnfile (default \writegame sud.out). 1457 % write out the solution to game file \sudsolnfile. 1458 \newcommand*{\sudsolnfile}{sud.out} 1459 \newcommand*{\writegame}{% \immediate\closeout\s@dwrite 1461 \immediate\openout\s@dwrite=\sudsolnfile \s@dnrow\@ne 1462 \loop 1463 \ifnum\s@dnrow<81\relax 14641465\gatherline{\the\s@dnrow} \immediate\write\s@dwrite{\sudaline} 1466 1467\advance\s@dnrow 9\relax 1468 \repeat \immediate\closeout\s@dwrite} 1469 1470 \gatherline \gatherline $\{ rowstartcell \} \}$ collects the solutions from one row in the grid and \sudaline converts them into the corresponding characters for one line in a sudoku file, putting the characters into the \sudaline macro. 1471 %% \gatherline{colstart} 1472 %% collect all the characters for one line in a game file 1473 \newcommand*{\gatherline}[1]{\bgroup \gdef\sudaline{} 1474 \s@dncol=#1\relax 1475\toprangectr=\s@dncol 1476 \advance\toprangectr 9\relax 14771478 \ifnum\s@dncol<\toprangectr 1479 \s@dtempcnta=\useknt{s@lans\the\s@dncol} 1480 1481 \ifnum\s@dtempcnta>\m@ne 1482 \g@addto@macro{\sudaline}{.}

3 Code

```
\else
            1483
                     \s@dtempcnta=-\s@dtempcnta
            1484
                     \ifcase\s@dtempcnta
            1485
                     \or \g@addto@macro{\sudaline}{1}
            1486
                     \or \g@addto@macro{\sudaline}{2}
            1487
            1488
                     \or \g@addto@macro{\sudaline}{3}
            1489
                     \or \g@addto@macro{\sudaline}{4}
                     \or \g@addto@macro{\sudaline}{5}
            1490
                     \or \g@addto@macro{\sudaline}{6}
            1491
                     \or \g@addto@macro{\sudaline}{7}
            1492
                     \or \g@addto@macro{\sudaline}{8}
            1493
            1494
                     \or \g@addto@macro{\sudaline}{9}
            1495
                     \else \g@addto@macro{\sudaline}{.}
            1496
                   \fi
            1497
                   \advance\s@dncol\@ne
            1498
                 \repeat
            1499
            1500 \egroup}
            1504
             \ variable \{\langle file \rangle\}\ reads a sudoku puzzle from the \langle file \rangle sudoku file, typesets
\sudokusolve
             the problem, does its best to solve it. It writes the solution to the \sudsolnfile
             file, then reads it back in again and typesets it.
            1505 \% Read in and typeset the problem, solve it, and typeset the answer
            1506 \newcommand{\sudokusolve}[1]{%
            1507
                 \begin{center}
                 \sudoku{#1}%
            1508
                 \end{center}
            1509
                 \getproblem{#1}%
            1510
            1511
                 \reduceallcells
                 \keepreducing
            1513
                 \writegame
                 \noindent\begin{minipage}{\linewidth}
            1514
                 THE ANSWER
            1515
            1516
                 \begin{center}
                 \cluefont\normalsize
            1517
            1518
                 \cellsize{1.5\baselineskip}
                 \sudoku{\sudsolnfile}
            1519
                 \end{center}
            1520
            1521
                 \end{minipage}}
            1522
                The end of the package.
            1523 (/solve)
```

3.4 The createsudoku package

The createsudoku package lets you automatically generate Sudoku puzzles. The package requires Donald Arseneau's random.tex and also the solvesudoku package, which in turn requires the printsudoku package.

```
1524 \langle *create \rangle
1525 \NeedsTeXFormat{LaTeX2e}
1526 \ProvidesPackage{createsudoku}[2006/02/16 v1.0 create sudoku puzzles]
1527 \input{random}
1528 \RequirePackage{solvesudoku}
```

\oldcommentary To avoid clutter it's a good idea to switch off solvesudoku's commentary. On the \commentary other hand it could be useful for this package to provide its own commentary.

```
\gencommentary_{1530} \let\oldcommentary\commentary
               1531 \let\commentary\@gobble
               1532 \newcommand*{\gencommentary}[1]{\typeout{#1}}
```

\genfile We need a file to write out the puxzzle to, and we also need two temporary files.

```
\prevfile_{1534} \newcommand*{\genfile}{gensud.sud}
\currfile 1535 \newcommand*{\prevfile}{genprev.sdx}
          1536 \newcommand*{\currfile}{gencurr.sdx}
          1537
```

\randomi This sets the seed for the random number generator. The default is setting it to \setsudrandom -1, which makes the seed depend on the date and time.

```
1538 \randomi\m@ne
1539 \newcommand*{\setsudrandom}[1]{%
     \randomi=#1\relax
1540
      \ifnum\randomi<\@ne\else
1541
        \nextrandom \nextrandom \nextrandom
1542
        \typeout{random initialised to #1}%
1543
1544
      \fi}
```

\generategrid \generategrid [$\langle file \rangle$] generates a new puzzle. If the sudoko file $\langle file \rangle$ is specified \printsudresults this is taken for the starting grid, otherwise a default one is used. The starting grid should be a complete solution.

> The pairs of rows, and pairs of columns, in the starting grid are exchanged in a random fashion (\swaps) and then the cell solutions are eliminated (\elimclus) until the puzzle is sufficiently complicated.

```
1546 \newcommand*{\generategrid}[1][\@empty]{%
      \ifx\@empty #1
1547
        \writestartgrid
1548
        \getproblem{\prevfile}
1549
1550
      \else
1551
        \getproblem{#1}
```

```
1552
                      \fi
                      \swaps
                1553
                      \elimclues
                1554
                      \printsudresults}
                1555
                1556 \newcommand*{\printsudresults}{%
                      \sudokusolve{\genfile}%
                1558
                      }
                1559
\writestartgrid Write out an initial fully solved grid to \prevfile.
                1560 \%\% the starting data
                1561 \newcommand*{\writestartgrid}{%
                1562
                      \immediate\closeout\s@dwrite
                      \immediate\openout\s@dwrite=\prevfile
                1563
                      \immediate\write\s@dwrite{123456789}
                1564
                      \immediate\write\s@dwrite{456789123}
                1565
                      \immediate\write\s@dwrite{789123456}
                1566
                      \immediate\write\s@dwrite{234567891}
                1567
                1568
                      \immediate\write\s@dwrite{567891234}
                      \immediate\write\s@dwrite{891234567}
                     \immediate\write\s@dwrite{345678912}
                1570
                      \immediate\write\s@dwrite{678912345}
                1571
                      \immediate\write\s@dwrite{912345678}
                1572
                      \immediate\closeout\s@dwrite}
                1573
                1574
                 \swaps randomly exchanges the contents of pairs of columns and pairs of rows.
                 In order to preserve the number uniqueness constraint for boxes, only pairs of
                 columns/rows that are in the same box may be exchanged.
                1575 \newcommand*{\swaps}{\bgroup
                      \setrannum{\maxrangectr}{36}{48}%
                1577 \gencommentary{number of swaps (36--48) = maxrangectr = \the\maxrangectr}
                      \s@dtemploopcnta\@ne
                1578
                1579
                      \loop
                1580
                        \ifnum\s@dtemploopcnta<\maxrangectr
                        \setrannum{\s@dtempcntb}{1}{18}%
                1582 %%\typeout{\space\space\space swap no \the\s@dtemploopcnta\space is \the\s@dtempcntb}
                        \ifcase\s@dtempcntb
                1583
                        \or \swapcolpair{1}{2}%
                1584
                        \or \swapcolpair{1}{3}%
                1585
                        \or \swapcolpair{2}{3}%
                1586
                1587
                        \or \swapcolpair{4}{5}%
                        \or \swapcolpair{4}{6}%
                1588
                        \or \swapcolpair{5}{6}%
                1589
                        \or \swapcolpair{7}{8}%
                1590
                        \or \swapcolpair{7}{9}%
                1591
                        \or \swapcolpair{8}{9}%
                1592
```

1593

1594

\or \swaprowpair{1}{10}%

\or \swaprowpair{1}{19}%

```
\or \swaprowpair{10}{19}%
              1595
                       \or \swaprowpair{28}{37}%
              1596
                       \or \swaprowpair{28}{46}%
              1597
                       \or \swaprowpair{37}{46}%
              1598
                       \or \swaprowpair{55}{64}%
              1599
                       \or \swaprowpair{55}{73}%
              1600
              1601
                       \or \swaprowpair{64}{73}%
              1602
              1603
                       \advance\s@dtemploopcnta\@ne
                    \repeat
              1604
              1605 \egroup}
              1606
\sum_{\text{swaprowpair}} \langle rowstartcell1 \rangle + \langle rowstartcell2 \rangle + \text{swaps} the contents of the two
               rows starting at \langle rowstartcell1 \rangle and \langle rowstartcell2 \rangle.
              1607 \% swap the data in rows starting at #1, and #2
              1608 \newcommand*{\swaprowpair}[2]{\bgroup
                    \s@dncol=#1\relax
              1609
                    \s@dcolpos=#2\relax
              1610
                    \s@dtemploopcnta\@ne
              1611
                    \maxrangectr=10\relax
              1612
                     \loop
              1613
                       \ifnum\s@dtemploopcnta<\maxrangectr
              1614
              1615
                       \s@dtempcnta=\useknt{s@lans\the\s@dncol}%
                       \global\useknt{s@lans\the\s@dncol}=\useknt{s@lans\the\s@dcolpos}%
              1616
              1617
                       \global\useknt{s@lans\the\s@dcolpos}=\s@dtempcnta
              1618
                       \advance\s@dncol\@ne
                       \advance\s@dcolpos\@ne
              1619
              1620
                       \advance\s@dtemploopcnta\@ne
              1621
                    \repeat
              1622 \egroup}
\space{2.5} swapcolpair {$\langle colstartcell1\rangle} {\langle colowstartcell2\rangle} swaps the contents of the two
               columns starting at \langle colstartcell1 \rangle and \langle colstartcell2 \rangle.
              1624 \%\% swap the data in cols starting #1 and #2
              1625 \newcommand*{\swapcolpair}[2]{\bgroup
                    \s@dnrow=#1\relax
              1626
                     \s@drowpos=#2\relax
              1627
                    \s@dtemploopcnta\@ne
              1628
                    \maxrangectr=10\relax
              1629
              1630
                    \loop
                       \ifnum\s@dtemploopcnta<\maxrangectr
              1631
                       \s@dtempcnta=\useknt{s@lans\the\s@dnrow}%
              1632
              1633
                       \global\useknt{s@lans\the\s@dnrow}=\useknt{s@lans\the\s@drowpos}%
              1634
                       \global\useknt{s@lans\the\s@drowpos}=\s@dtempcnta
                       \advance\s@dnrow 9\relax
              1635
              1636
                       \advance\s@drowpos 9\relax
              1637
                       \advance\s@dtemploopcnta\@ne
```

48 3 Code

```
\repeat
1638
1639 \egroup}
1640
```

\elimclues \elimclues first eliminates a set of clues from the (full) grid, writing the resulting puzzle to the two temporary files \prevfile and \currfile. It then eliminates clues one-by-one until the puzzle has been finally generated, the result having been written to the \prevfile, then writing it out to the file \genfile.

```
1641 \newcommand*{\elimclues}{\bgroup
      \initialelimination
1642
      \writestate{\prevfile}%
1643
1644
      \writestate{\currfile}%
1645
      \elimcluesonebyone
      \getproblem{\prevfile}
1646
      \writestate{\genfile}
1647
1648 \egroup}
1649
```

\elimseventeen \elimseventeen randomly eliminates the solutions for 17 cells in the grid (apparently if two numbers are completely eliminated as clues in a puzzle, then at best the solution is ambiguous).

```
1650 \newcommand*{\elimseventeen}{\bgroup
      \s@dtemploopcnta\@ne
1651
1652
      \maxrangectr 18\relax
      \loop
1653
        \ifnum\s@dtemploopcnta<\maxrangectr
1654
1655
        \setrannum{\s@dtempcnta}{1}{81}
1656
        \global\useknt{s@lans\the\s@dtempcnta}=111111111\relax
        \advance\s@dtemploopcnta\@ne
1658
      \repeat
1659 \egroup}
```

\elimcross Eliminate all solutions in column 5 and row 5.

```
1661 \% eliminates all clues in column 5 and row 5
1662 \newcommand*{\elimcross}{\bgroup
      \s@dtemploopcnta 5\relax
1663
      \loop
1664
        \ifnum\s@dtemploopcnta<78\relax%
                                              78 = 5 + 73
1665
        \global\useknt{s@lans\the\s@dtemploopcnta}=111111111\relax
1666
        \advance\s@dtemploopcnta 9\relax
1667
1668
      \repeat
      \s@dtemploopcnta 37\relax
1669
1670
      \loop
1671
        \ifnum\s@dtemploopcnta<46\relax%
                                              46 = 37 + 9
1672
        \global\useknt{s@lans\the\s@dtemploopcnta}=111111111\relax
        \advance\s@dtemploopcnta \@ne
1673
1674
      \repeat
1675 \egroup}
```

1676 \elimnum \elimnum $\{\langle num \rangle\}\$ (0 < num < 10) eliminates all instances of the $\langle num \rangle$ solution from the grid. 1677 \newcommand*{\elimnum}[1]{\bgroup 1678 \s@dtemploopcnta\@ne 1679 \loop 1680 \ifnum\s@dtemploopcnta<82\relax 1681 \ifnum\useknt{s@lans\the\s@dtemploopcnta}=-#1\relax \global\useknt{s@lans\the\s@dtemploopcnta}=111111111\relax 1682 1683 \advance\s@dtemploopcnta \@ne 1684 \repeat 1685 1686 \egroup} 1687 \elimcrossandnines Eliminate all 9's and the solutions in column 5 and row 5. 1688 \newcommand*{\elimcrossandnines}{\bgroup 1689 \elimcross \s@dtemploopcnta\@ne 1690 \loop 1691 \ifnum\s@dtemploopcnta<82\relax 1692 1693 \ifnum\useknt{s@lans\the\s@dtemploopcnta}=-9\relax \global\useknt{s@lans\the\s@dtemploopcnta}=111111111\relax 1694 1695 \advance\s@dtemploopcnta \@ne 1696 \repeat 1697 1698 \egroup} 1699 \elimex Eliminate all solutions on the diagonals of the grid. 1700 \newcommand*{\elimex}{\bgroup \s@dtemploopcnta\@ne 1701 1702 \loop \ifnum\s@dtemploopcnta<82\relax 1703 \global\useknt{s@lans\the\s@dtemploopcnta}=111111111\relax 1704 \advance\s@dtemploopcnta 10\relax 1705 1706 \repeat \s@dtemploopcnta=9\relax 1707 \loop 1708 1709 \ifnum\s@dtemploopcnta<81\relax \global\useknt{s@lans\the\s@dtemploopcnta}=111111111\relax 1710 1711 \advance\s@dtemploopcnta 8\relax

\elimcrossandex Eliminate all solutions in column 5 and row 5 and on the diagonals.

1715 \newcommand*{\elimcrossandex}{\bgroup

1712

1714

\repeat 1713 \egroup}

50 3 Code

```
\elimcross
1716
      \elimex
1717
1718 \egroup}
```

\elimcrossandexandnines Eliminate all solutions in column 5 and row 5 and on the diagonals, and all 9's.

```
1720 \newcommand*{\elimcrossandexandnines}{\bgroup
```

\elimcross 1721 1722 \elimex 1723 \elimnum{9} 1724 \egroup} 1725

\initialelimination \initialelimination eliminates an initial set of solutions from the grid. Several predefined sets are provided.

> 1726 \let\initialelimination\elimseventeen 1727 \let\initialelimination\elimcross 1728 \let\initialelimination\elimcrossandnines 1729 \let\initialelimination\elimcrossandex 1730 \let\initialelimination\elimcrossandexandnines

\toomanyloops \elimcluesonebyone

Eliminate solutions from the grid one-by-one until the puzzle cannot be solved. Then reinstate the last solution deleted to produce the final puzzle. I'm not sure if this is needed, but just in case the process stops after 81 attempts to remove solutions (highly unlikely but the random number generator could keep producing numbers corresponding to clueless cells).

We use the \currfile and \prevfile to hold the current state of affairs and the previous state.

```
1732 \newcount\toomanyloops
1733 \newcommand*{\elimcluesonebyone}{\bgroup
1734 %%%\typeout{***elimcluesonebyone}
1735 \toomanyloops\z@
1736
      \s@dtempcntb=81\relax
1737
      \loop
1738
        \ifnum\s@dtempcntb>80\relax
1739 \advance\toomanyloops\@ne
```

Read the current puzzle from \currfile and try to solve it.

```
1740
        \getproblem{\currfile}
1741
        \trysolution
1742
        \ifnum\solcnt=81\relax
                                     % can delete another clue
```

The puzzle was solvable so try deleting another clue. Read the (unsolved) puzzle again from \currfile and write its state to \prevfile.

```
\getproblem{\currfile}
1743
1744
          \writestate{\prevfile}
```

Now delete a clue, writing the resultant puzzle to \currfile, and go round the loop again.

```
1745
                              \deleteaclue
                              \writestate{\currfile}%
                   1746
                              \s@dtempcntb=81\relax
                   1747
                            \else % done
                   1748
                     The puzzle was not solvable, and the state before the last clue deletion is in file
                     \prevfile.
                              \typeout{Solver failed, solcnt = \the\solcnt}
                   1749
                   1750
                              \s@dtempcntb=\@ne
                   1751
                            \ifnum\toomanyloops>80\relax
                   1752
                              \typeout{Too much looping}
                   1753
                              \s@dtempcntb=\@ne
                   1754
                   1755
                            \fi
                          \repeat
                   1756
                   1757 \egroup}
                   1758
\ifacluenotdeleted Keep calling the random number generator until it returns a cell that has a solu-
                    tion, then delete the solution.
      \deleteaclue
                   1759 \newif\ifacluenotdeleted
                   1760 \newcommand*{\deleteaclue}{\bgroup
                          \acluenotdeletedtrue
                   1762
                            \ifacluenotdeleted
                   1763
                   1764
                            \setrannum{\s@dtempcnta}{1}{81}%
                              \ifnum\useknt{s@lans\the\s@dtempcnta}<\z@% found a clue
                   1765
                                \gencommentary{Deleting clue for cell \the\s@dtempcnta}%
                   1766
                                \global\useknt{s@lans\the\s@dtempcnta}=111111111\relax
                   1767
                                \acluenotdeletedfalse
                   1768
                   1769
                   1770
                          \repeat
                   1771 \egroup}
                   1772
      \trysolution \trysolution attempts to solve the current puzzle state.
                   1773 \newcommand*{\trysolution}{\bgroup
                          \reduceallcells
                   1774
                          \keepreducing
                   1775
                   1776 \egroup}
       \writestate \writestate\{\langle file \rangle\} writes the current state (clues and blanks) to the sudoku file
                   1778 %% \writestate{<outputfile>}
                   1779 \newcommand*{\writestate}[1]{\bgroup
                   1780
                          \immediate\closeout\s@dwrite
                          \immediate\openout\s@dwrite=#1
                   1781
                   1782
                          \s@dnrow\@ne
                          \loop
                   1783
```

```
1784 \ifnum\s@dnrow<81\relax
1785 \gatherline{\the\s@dnrow}%
1786 \immediate\write\s@dwrite{\sudaline}%
1787 \advance\s@dnrow 9\relax
1788 \repeat
1789 \immediate\closeout\s@dwrite
1790 \egroup}
1791

The end of the package.
1792 \( / \create \)
```

4 Example sudoku puzzles

LaTeXing the following file will provide you with a selection of Sudoku puzzles. You can try solving them yourself and/or get Latex to do it for you. The solvesudoku package is able to solve most, but not all of the puzzles.

```
1793 (*examples)
1794 \documentclass[twoside]{article}
1795 \usepackage{comment}
1796 \usepackage{url}
1797 \usepackage{printsudoku}
1798 \mbox{newcommand} {\Lpack}[1]{\textsf{#1}}
1799 \title{Example Sudoku Puzzles}
1800 \author{Peter Wilson}
1801 \date{16 February 2006}
1802 \raggedbottom
1803 \begin{document}
1804 \maketitle
1805
        A Sudoku puzzle consists of a 9 by 9 array of squares, some of which have
1807 numbers in them, the numbers ranging from 1 through 9. The problem is to
1808 fill in all the squares such that each row, column, and 3 by 3 box includes
1809 the numbers 1 through 9 with no repetitions.
1810
        This is a collection of some 54 Sudoku puzzles which I have culled
1812 from various places. The sources include, among others:
1813 the \mbox{emph{Sudoku Solver}^{cite{SSBL}}} website (labelled SE, SM, SH and SVH),
1814 \emph{The Daily Telegraph}~\cite{DT2} (labelled TG, TM, and TT),
1815 \emph{The Seattle Times} (labelled ST),
1816 and some automatically generated by the \Lpack{createsudoku}
1817 package~\cite{SUDOKUBUNDLE} (labelled CS).
1819 You can try solving them yourself and/or get
1820 \; {\tt LaTeX} \; {\tt to} \; {\tt do} \; {\tt it} \; {\tt for}
1821 you. The \Lpack{solvesudoku} package~\cite{SUDOKUBUNDLE} is able to solve
1822 most, but not all of the puzzles. Other LaTeX packages may do better or worse.
1823
```

```
The puzzles are presented in approximately increasing order of difficulty.
1824
1825 Each source, though, has its own set of categories which don't necessarily
1826 agree with each other (and sometimes not within one source). I have included
1827 an indication of the difficulty as stated by the relevant source.
1828
1829 The parameters for the puzzles created via \Lpack{createsudoku} are given in
1830 the table.
1831
1832 \begin{table}[hbp]
1833 \centering
1834 \begin{tabular}{lll} \hline
1835 Number & Seed & \verb?initialelimination? \\ \hline
           & 1505263462 & \verb?\elimcrossandexandnines? \\
1837 CS2
           & 1495929734 & \verb?\elimcrossandex? \\
1838 CS3
          & 1487762722 & \verb?\elimcrossandexandnines? \\
1839 CS4
          & 1508763610 & \verb?\elimcrossandex? \\
1840 CS5
           & 839068723 & \verb?\elimseventeen? \
1841 CS6
           & 833235143 & \verb?\elimcrossandexandnines? \\ \hline
1842 \end{tabular}
1843 \end{table}
1844
1845 \cleardoublepage
1846
1847 \land \text{LARGE}
1848 \cellsize{2.25\baselineskip}
1849
1850 \markboth{EASY}{EASY}
1851 \pagestyle{headings}
1852
1853 \renewcommand*{\puzzlefile}{se5.sud}
1854 \writepuzzle%
1855 {.2...5863}{56.2.3.9.}{.3...7251}%
1856 { . . . 975 . . . . } { . . . 6 . . . 47 . 9} { . . 7 . . . 286 . . } %
1857 {6.58...7.}{8....1..6}{3.7.6..4.}%
1858 [SSBL easy 5]
1859 \vfill
1860 \begin{minipage}{0.95\linewidth}\begin{center}
1861 SE5 (easy) \\
1862 \sudoku{se5.sud}
1863 \end{center}\end{minipage}
1865 \renewcommand*{\puzzlefile}{se10.sud}
1866 \writepuzzle%
1867 { . . 6 . 497 . . } { . . 82 . 1 . 6 . . } { 79 . . 8 . 145 } %
1868 {649.5.27.}{..7.6..5.}{.3..72.96}%
1869 {.2....81.}{.7..28...}{.....5.7}%
1870 [SSBL easy 10]
1871 \vfill
1872 \begin{minipage}{0.95\linewidth}\begin{center}
1873 SE10 (easy) \\
```

```
1874 \sudoku{se10.sud}
1875 \end{center}\end{minipage}
1876
1877 \renewcommand*{\puzzlefile}{se15.sud}
1878 \writepuzzle%
1879 {4.67.39.2}{..16.84..}{.7...4..1}%
1880 {5...4.21.}{.2....6.}{.68.7...9}%
1881 {6..5...9.}{..24.93..}{9.53.17.4}%
1882 [SSBL easy 15]
1883 \vfill
1884 \begin{minipage}{0.95\linewidth}\begin{center}
1885 SE15 (easy) \\
1886 \sudoku{se15.sud}
1887 \end{center}\end{minipage}
1889 \renewcommand*{\puzzlefile}{se20.sud}
1890 \writepuzzle%
1891 {36.9..5..}{...54.8.2.}{.....78.9}%
1892 {2....3.68}{.83.9....}{.4.7..2.3}%
1893 {6.71..3..}{13.8.59.2}{..9.7..56}%
1894 [SSBL easy 20]
1895 \vfill
1896 \begin{minipage}{0.95\linewidth}\begin{center}
1897 SE20 (easy) \\
1898 \slashed se20.sud
1899 \end{center}\end{minipage}
1901 \renewcommand*{\puzzlefile}{se25.sud}
1902 \writepuzzle%
1903 {....63.5.}{6.5.1.839}{...1...2..}%
1904 {823...7...}{.5...7....}{.64.9...1}%
1905 {4.25796.3}{.9.1.65.8}{.1...89.7}%
1906 [SSBL easy 25]
1907 \vfill
1908 \begin{minipage}{0.95\linewidth}\begin{center}
1909 SE25 (easy) \\
1910 \sudoku{se25.sud}
1911 \end{center}\end{minipage}
1913 \renewcommand*{\puzzlefile}{se30.sud}
1914 \verb|\writepuzzle||%
1915 { . 3 . 12 . . . . } { 1 . 87 . . 4 . 6} { . . . 98 . . . . 1} %
1916 {5....7.3.}{.73.9.2.4}{.92..65..}%
1917 { .4...8.5. } {3...7...8 } {2..4.596. } %
1918 [SSBL easy 30]
1919 \vfill
1920 \begin{minipage}{0.95\linewidth}\begin{center}
1921 SE30 (easy) \\
1922 \sudoku{se30.sud}
1923 \end{center}\end{minipage}
```

```
1925 \renewcommand*{\puzzlefile}{tg5.sud}
1926 \writepuzzle%
1927 {.6.1.9.8.}{.19...74.}{2.....1}%
1928 {...79.26...}{..3.....2.}{...14.35...}%
1929 {1......5}{.75...23.}{.9.5.6.7.}%
1930 [DT2 gentle 5]
1931 \vfill
1932 \begin{minipage}{0.95\linewidth}\begin{center}
1933 TG5 (gentle) \\
1934 \sudoku{tg5.sud}
1935 \end{center}\end{minipage}
1937 \renewcommand*{\puzzlefile}{tg10.sud}
1938 \writepuzzle%
1939 {....96..4}{..1....2}{56...8...}%
1940 {2.8....9.}{9.63.52.7}{.3....4.6}%
1941 {...9...58}{7.....9..}{8..45....}%
1942 [DT2 gentle 10]
1943 \vfill
1944 \begin{minipage}{0.95\linewidth}\begin{center}
1945 TG10 (gentle) \\
1946 \sudoku{tg10.sud}
1947 \end{center}\end{minipage}
1948
1949 \renewcommand*{\puzzlefile}{tg15.sud}
1950 \writepuzzle%
1951 {...1.8...}{.57...18.}{98.....26}%
1952 {...67419...}{.......}{...42536...}%
1953 {72.....94}{..19....73.}{....3.9....}%
1954 [DT2 gentle 15]
1955 \vfill
1956 \begin{minipage}{0.95\linewidth}\begin{center}
1957 TG15 (gentle) \\
1958 \sudoku{tg15.sud}
1959 \end{center}\end{minipage}
1960
1961 \renewcommand*{\puzzlefile}{tg20.sud}
1962 \writepuzzle%
1963 {...7.9...}{.8.3.6.5.}{7.9...6.8}%
1964 { . . 42 . 18 . . } { . . . . . 4 . } { . . . 35 . 41 . . } %
1965 {9.2...5.7}{.4.8.7.1.}{...1.2...}%
1966 [DT2 gentle 20]
1967 \vfill
1968 \begin{minipage}{0.95\linewidth}\begin{center}
1969 TG20 (gentle) \\
1970 \sudoku{tg20.sud}
1971 \end{center}\end{minipage}
1972
1973 \renewcommand*{\puzzlefile}{tg25.sud}
```

```
1974 \writepuzzle%
1975 {7..4..5..}{.61..5.7.}{.9.7.1..6}%
1976 {8...27...}{......}{....34...1}%
1977 {1..8.2.3.}{.7.1..62.}{..3..9..7}%
1978 [DT2 gentle 25]
1979 \vfill
1980 \begin{minipage}{0.95\linewidth}\begin{center}
1981 TG25 (gentle) \\
1982 \sudoku{tg25.sud}
1983 \end{center}\end{minipage}
1985 \renewcommand*{\puzzlefile}{tg30.sud}
1986 \writepuzzle%
1987 {37.4....}{9....61.4}{....23...}%
1988 {.4.1..9..}{.12...79.}{..5..7.4.}%
1989 {....36.....}{4.32....6}{.....9.57}%
1990 [DT2 gentle 30]
1991 \vfill
1992 \begin{minipage}{0.95\linewidth}\begin{center}
1993 TG30 (gentle) \\
1994 \sudoku{tg30.sud}
1995 \end{center}\end{minipage}
1997 \renewcommand*{\puzzlefile}{st1226.sud}
1998 \writepuzzle%
1999 {9....4.31}{7452.....}{.8..674..}%
2000 { .26.4 . . . 5}{5 . . 6.9 . . 8}{4 . . . 2 . 37 . }%
2001 {...759...6.}{.....1823}{21.3....7}%
2002 [Seattle Times 2005/12/26 1 star]
2003 \vfill
2004 \begin{minipage}{0.95\linewidth}\begin{center}
2005 ST1226 (1 star) \\
2006 \sudoku{st1226.sud}
2007 \end{center}\end{minipage}
2009 \renewcommand*{\puzzlefile}{st0206.sud}
2010 \writepuzzle%
2011 {17.42...5}{..2.1..96}{849..3...}%
2012 {....718..}{.25...67.}{..826....}%
2013 {...5..749}{53..9.1..}{6...48.23}%
2014 [Seattle Times 2005/02/06 1 star]
2015 \vfill
2016 \begin{minipage}{0.95\linewidth}\begin{center}
2017 ST0206 (1 star) \\
2018 \sudoku{st0206.sud}
2019 \end{center}\end{minipage}
2021 \renewcommand*{\puzzlefile}{st0213.sud}
2022 \writepuzzle%
2023 {.94.2...7}{.36...1.5}{28.35....}%
```

```
2024 { . . 92 . . . 5 . } { 6 . 21 . 49 . 8 } { . . . . . 63 . . } %
2025 {....13.46}{1.5...78.}{8...4.29.}%
2026 [Seattle Times 2006/02/13 1 star]
2027 \vfill
2028 \begin{minipage}{0.95}\linewidth}\begin{center}
2029 ST0213 (1 star) \\
2030 \sudoku{st0213.sud}
2031 \end{center}\end{minipage}
2032
2033 \renewcommand*{\puzzlefile}{cs1.sud}
2034 \writepuzzle%
2035 {.46..731.}{2.36.4...}{87.3.1.45}%
2036 {657...423}{......}{.81...756}%
2037 {43.8.6..1}{7..2..5.4}{..25.386.}%
2038 [CreateSudoku 1 (level 2)]
2039 \vfill
2040 \begin{minipage}{0.95\linewidth}\begin{center}
2041 CS1 (level 2) \\
2042 \sudoku{cs1.sud}
2043 \end{center}\end{minipage}
2045 \renewcommand*{\puzzlefile}{cs2.sud}
2046 \writepuzzle%
2047 { .7.3.265. } { ...6..9.7 } { 64.9.8.2. } %
2048 {...9....765}{........}{756...4.2}%
2049 {29.5...76}{...2.15.3}{...4..7.1.}%
2050 [CreateSudoku 2 (level 2)]
2051 \vfill
2052 \begin{minipage}{0.95\linewidth}\begin{center}
2053 CS2 (level 2) \\
2054 \sudoku{cs2.sud}
2055 \end{center}\end{minipage}
2057 \renewcommand*{\puzzlefile}{cs3.sud}
2058 \writepuzzle%
2059 {.5.8.71..}{..35.....}{78.2.1.56}%
2060 {.34...8.1}{......}{8.1...56.}%
2061 {.4.7.6.12}{...4.36.8}{.781..34.}%
2062 [CreateSudoku 3 (level 2)]
2063 \vfill
2064 \begin{minipage}{0.95\linewidth}\begin{center}
2065 CS3 (level 2) \\
2066 \sudoku{cs3.sud}
2067 \end{center}\end{minipage}
2069 %%%%%%%%%%%%%%%%%%%%%%%%%%% moderate
2070
2071 \clearpage
2072 \markboth{MODERATE}{MODERATE}
2073
```

```
2074 \renewcommand*{\puzzlefile}{sm5.sud}
2075 \text{ writepuzzle}\%
2076 {...76...24.}{..46.....9.}{92...85...}%
2077 {8....29..}{...3...4..}{...49....6}%
2078 {...73..24}{.5....86.}{.32..67..}%
2079 [SSBL medium 5]
2080 \vfill
2081 \begin{minipage}{0.95\linewidth}\begin{center}
2082 \text{ SM5 (medium) } \setminus
2083 \sudoku{sm5.sud}
2084 \end{center}\end{minipage}
2086 \renewcommand*{\puzzlefile}{sm10.sud}
2087 \writepuzzle%
2088 {...57.82...}{4.......6}{..7...6...8.}%
2089 {52.9.4.31}{......}{86.1.7.54}%
2090 { .9..3..6. }{7......5}{..24.61..}%
2091 [SSBL medium 10]
2092 \vfill
2093 \begin{minipage}{0.95\linewidth}\begin{center}
2094 SM10 (medium) \\
2095 \sudoku{sm10.sud}
2096 \end{center}\end{minipage}
2097
2098 \renewcommand*{\puzzlefile}{sm15.sud}
2099 \writepuzzle%
2100 {85...4..2}{4...2.9..}{...8...7.}%
2101 { . . 6 . . . . . 1} { . . 4 . . 8 . . 3 . } { 2 . . . . 5 . . } %
2102 { .34 . .7 . . .}{ .87 .9 . . .6}{6 . .1 . . .47}%
2103 [SSBL medium 15]
2104 \vfill
2105 \begin{minipage}{0.95\linewidth}\begin{center}
2106 SM15 (medium) \\
2107 \sudoku{sm15.sud}
2108 \end{center}\end{minipage}
2110 \renewcommand*{\puzzlefile}{sm20.sud}
2111 \writepuzzle%
2112 { . . 34 . 2 . 97} { . . . 4 . . . . 2 . } { . 7 . 6 . . . . . 8} %
2113 {....9....}{.38...47.}{....1....}%
2114 {4....5.1.}{.5....6..}{72.3.19..}%
2115 [SSBL medium 20]
2116 \vfill
2117 \begin{minipage}{0.95\linewidth}\begin{center}
2118 SM20 (medium) \\
2119 \sudoku{sm20.sud}
2120 \end{center}\end{minipage}
2122 \renewcommand*{\puzzlefile}{sm25.sud}
2123 \writepuzzle%
```

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2124 { . . . 4 . 79 . . } { 7 . 6 . . . 2 . . } { . . 5 . . 83 . 6 } %
2125 {56..298..}{..8..1...}{.3.7....5}%
2126 {......38} {....93...} {.4.5....}
2127 [SSBL medium 25]
2128 \vfill
2129 \begin{minipage}{0.95\linewidth}\begin{center}
2130 SM25 (medium) \\
2131 \sudoku{sm25.sud}
2132 \end{center}\end{minipage}
2133
2134 \renewcommand*{\puzzlefile}{sm30.sud}
2135 \writepuzzle%
2136 {...58.....}{....79...}{...461..7.}%
2137 {.5.3....4}{.23...65.}{9....8.3.}%
2138 {.3..572..}{....42....}{.....61..}%
2139 [SSBL medium 30]
2140 \vfill
2141 \begin{minipage}{0.95\linewidth}\begin{center}
2142 SM30 (medium) \\
2143 \sudoku{sm30.sud}
2144 \end{center}\end{minipage}
2145
2146 \renewcommand*{\puzzlefile}{tm35.sud}
2147 \writepuzzle%
2148 {5..3.8..6}{..4.5.8..}{2.8...1.5}%
2149 { . . 62 . 74 . . } { . . . . . . . . } { . . . 94 . 32 . . } %
2150 {9.5...6.4}{...2.1.9...}{1...8.9...2}%
2151 [DT2 moderate 35]
2152 \vfill
2153 \begin{minipage}{0.95\linewidth}\begin{center}
2154 TM35 (moderate) \\
2155 \sudoku{tm35.sud}
2156 \end{center}\end{minipage}
2157
2158 \renewcommand*{\puzzlefile}{tm40.sud}
2159 \writepuzzle%
2160 {...1...92}{9...7..36}{3....2...}%
2161 {.3....7.9}{.8.9.5.6.}{4.5....8.}%
2162 {...8....5}{54..2...7}{12...3...}%
2163 [DT2 moderate 40]
2164 \vfill
2165 \begin{minipage}{0.95\linewidth}\begin{center}
2166 \text{ TM40} \text{ (moderate) } \setminus
2167 \sudoku{tm40.sud}
2168 \end{center}\end{minipage}
2170 \renewcommand*{\puzzlefile}{tm45.sud}
2171 \writepuzzle%
2172 { .1.2.8.3. } { ...87.94.. } { 9 . . . . . . 6 } %
2173 {...9.8.5..}{6......3}{...3.5.6..}%
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2174 {2......7}{...73.51...}{..6.4.7.9.}%
2175 [DT2 moderate 45]
2176 \vfill
2177 \begin{minipage}{0.95\linewidth}\begin{center}
2178 \text{ TM45} \text{ (moderate) } \setminus
2179 \sudoku{tm45.sud}
2180 \end{center}\end{minipage}
2182 \renewcommand*{\puzzlefile}{tm50.sud}
2183 \text{ \writepuzzle\%}
2184 {...9.2..4}{4..3.5...}{3.....7.6}%
2185 {6..8..3..}{1.3...9.7}{...9..7..2}%
2186 {9.5....8}{...2.9..1}{2..7.4...}%
2187 [DT2 moderate 50]
2188 \vfill
2189 \begin{minipage}{0.95\linewidth}\begin{center}
2190 TM50 (moderate) \\
2191 \sudoku{tm50.sud}
2192 \end{center}\end{minipage}
2194 \renewcommand*{\puzzlefile}{tm55.sud}
2195 \writepuzzle%
2196 {7......}{24.1.8...}{.6..72..3}%
2197 { . . 4 . 29 . 8 . } { . 7 . . . . . 6 . } { . 9 . 46 . 7 . . } %
2198 {1...68...3.}{....3.7.91}{........6}%
2199 [DT2 moderate 55]
2200 \vfill
2201 \begin{minipage}{0.95\linewidth}\begin{center}
2202 TM55 (moderate) \\
2203 \sudoku{tm55.sud}
2204 \verb|\end{center}\end{minipage}
2205
2206 \renewcommand*{\puzzlefile}{tm60.sud}
2207 \writepuzzle%
2208 {724.9.5..}{.5..2...8}{.8.5.7...}%
2209 {...7..64.}{....8....}{.79..6...}%
2210\ \{\dots 8.5.2.\} \{6\dots 4\dots 8.\} \{\dots 8.3.174\} \%
2211 [DT2 moderate 60]
2212 \vfill
2213 \begin{minipage}{0.95\linewidth}\begin{center}
2214 TM60 (moderate) \\
2215 \sudoku{tm60.sud}
2216 \end{center}\end{minipage}
2218 \renewcommand*{\puzzlefile}{st0914.sud}
2219 \writepuzzle%
2220 { .6.29 . .8 . } { . . . . . . 3 . } { .1 . . . . . } %
2221 {.217.9..8}{6......3}{7..6.492.}%
2222 {...12..4.}{.7....3..}{.5..86.7.}%
2223 [Seattle Times 2005/09/14 2 stars]
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2224 \vfill
2225 \begin{minipage}{0.95\linewidth}\begin{center}
2226 ST0914 (2 stars) \\
2227 \sudoku{st0914.sud}
2228 \end{center}\end{minipage}
2230 \renewcommand*{\puzzlefile}{st0207.sud}
2231 \writepuzzle%
2232 {......46}{5..8.9.73}{...6..5.1}%
2233 {.592..1..}{6...1...7}{..3..785.}%
2234 {2.5..6...}{19.7.5..8}{34.....}%
2235 [Seattle Times 2005/02/07 2 stars]
2236 \vfill
2237 \begin{minipage}{0.95\linewidth}\begin{center}
2238 ST0207 (2 stars) \\
2239 \sudoku{st0207.sud}
2240 \end{center}\end{minipage}
2241
2242 \renewcommand*{\puzzlefile}{cs4.sud}
2243 \writepuzzle%
2244 { . . . 4 . 597 . } { . . . 67 . 83 . 2 } { 78 . 1 . 2 . 45 } %
2245 {891...75.}{......}{567...423}%
2246 {.1...4.67}{...89.15..}{.4....29.}%
2247 [CreateSudoku 4 (level 8)]
2248 \vfill
2249 \begin{minipage}{0.95\linewidth}\begin{center}
2250 CS4 (level 4) \\
2251 \sudoku{cs4.sud}
2252 \end{center}\end{minipage}
2253
2254 \renewcommand*{\puzzlefile}{cs5.sud}
2255 \writepuzzle%
2256 {...6..978}{...498...2}{..97.21...}%
2258 {7.6..95..}{...87...1}{.2..4.867}%
2259 [CreateSudoku 5 (level 4)]
2260 \vfill
2261 \begin{minipage}{0.95\linewidth}\begin{center}
2262 CS5 (level 4) \\
2263 \sudoku{cs5.sud}
2264 \end{center}\end{minipage}
2266 \renewcommand*{\puzzlefile}{cs6.sud}
2267 \writepuzzle%
2268 {.126.4.7.}{6.5..73.2}{.7.3.1.4.}%
2269 {756...423}{......}{18.....6}%
2270 { .3.8.6..1} { 2.1.....7} { ... 72...3.} %
2271 [CreateSudoku 6 (level 4)]
2272 \vfill
2273 \begin{minipage}{0.95\linewidth}\begin{center}
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2274 CS6 (level 4) \\
2275 \sudoku{cs6.sud}
2276 \end{center}\end{minipage}
2277
2279
2280 \clearpage
2281 \markboth{HARD}{HARD}
2283 \text{ renewcommand*{\puzzlefile}{sh5.sud}}
2284 \writepuzzle%
2285 {..9..5...}{47...2...}{.836.4.1.}%
2286 { .15 . . . . 8 . } { . . . . 3 . 7 . . . } { . 2 . . . . 74 . } %
2287 {.4.5.187.}{...7...52}{...2..1..}%
2288 [SSBL hard 5]
2289 \vfill
2290 \begin{minipage}{0.95\linewidth}\begin{center}
2291 SH5 (hard) \\
2292 \sudoku{sh5.sud}
2293 \end{center}\end{minipage}
2295 \renewcommand*{\puzzlefile}{sh10.sud}
2296 \writepuzzle%
2297 {.3.921..5}{15.83....}{.......}%
2298 {59.....4}{37.....81}{6.....53}%
2299 {......}{....19.26}{9..574.1.}%
2300 [SSBL hard 10]
2301 \vfill
2302 \begin{minipage}{0.95\linewidth}\begin{center}
2303 SH10 (hard) \\
2304 \sudoku{sh10.sud}
2305 \end{center}\end{minipage}
2307 \renewcommand*{\puzzlefile}{sh15.sud}
2308 \writepuzzle%
2309 {2..9....}{.7..6..59}{...4...61}%
2310 {7.1..2..4}{....4....}{8..1..9.6}%
2311 {12...3...}{53..2..7.}{.....9..2}%
2312 [SSBL hard 15]
2313 \vfill
2314 \begin{minipage}{0.95\linewidth}\begin{center}
2315 SH15 (hard) \\
2316 \sudoku{sh15.sud}
2317 \end{center}\end{minipage}
2319 \renewcommand*{\puzzlefile}{sh20.sud}
2320 \writepuzzle%
2321 { .6.2...3. } {9...3...1} { ....9.2.. } %
2322 {1..7....}{.32...46.}{....4..2}%
2323 {..7.4....}{2...5...8}{.4...6.5.}%
```

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2324 [SSBL hard 20]
2325 \vfill
2326 \begin{minipage}{0.95\linewidth}\begin{center}
2327 SH20 (hard) \\
2328 \sudoku{sh20.sud}
2329 \end{center}\end{minipage}
2331 \renewcommand*{\puzzlefile}{sh25.sud}
2332 \writepuzzle%
2333 {4....1..8}{...7.3845.}{...24....1.}%
2334 {28.9....}{..4...5..}{.....4.86}%
2335 {.4...92..}{.2134.8..}{9..6....1}%
2336 [SSBL hard 25]
2337 \vfill
2338 \begin{minipage}{0.95\linewidth}\begin{center}
2339 SH25 (hard) \\
2340 \slashed {sh25.sud}
2341 \end{center}\end{minipage}
2343 \renewcommand*{\puzzlefile}{sh30.sud}
2344 \writepuzzle%
2345 {....5..9.}{.53..78..}{78.4....}%
2346 {3....9.2.}{.72...38.}{.1.3....4}%
2347 {.....1.35}{...58..41.}{.2..3....}%
2348 [SSBL hard 30]
2349 \vfill
2350 \begin{minipage}{0.95\linewidth}\begin{center}
2351 SH30 (hard) \\
2352 \sudoku{sh30.sud}
2353 \end{center}\end{minipage}
2354
2355 \renewcommand*{\puzzlefile}{tt100.sud}
2356 \writepuzzle%
2357 {...896..7}{...23.5...}{...8...5.1}%
2358 {15...9...}{3......9}{...6...54}%
2359 {8.1...7..}{...9.18..}{6..428...}%
2360 [DT2 tough 100]
2361 \vfill
2362 \begin{minipage}{0.95\linewidth}\begin{center}
2363 TT100 (tough) \\
2364 \sudoku{tt100.sud}
2365 \end{center}\end{minipage}
2366
2367 \renewcommand*{\puzzlefile}{tt105.sud}
2368 \writepuzzle%
2369 {..5.7..46}{6..25....}{.3...6...}%
2370 {2..7....}{.78...35.}{....1..7}%
2371 {...8...2.}{....97..5}{81..2.9..}%
2372 [DT2 tough 105]
2373 \vfill
```

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2374 \begin{minipage}{0.95\linewidth}\begin{center}
2375 TT105 (tough) \\
2376 \sudoku{tt105.sud}
2377 \end{center}\end{minipage}
2378
2379 \renewcommand*{\puzzlefile}{tt110.sud}
2380 \writepuzzle%
2381 {.79.1....}{.4.5....7}{1..6.....}%
2382 {9368..1..}{..4...9..}{..7..4632}%
2383 \{ \dots .8..1 \} \{ 5 \dots 6.9. \} \{ \dots 4.82. \} \%
2384 [DT2 tough 110]
2385 \vfill
2386 \begin{minipage}{0.95\linewidth}\begin{center}
2387 TT110 (tough) \\
2388 \sudoku{tt110.sud}
2389 \end{center}\end{minipage}
2391 \renewcommand*{\puzzlefile}{tt115.sud}
2392 \writepuzzle%
2393 {432.5....}{.....3...}{75.1.....}%
2394 { . . 5 . 823 . . } { . . 6 . 5 . 1 . 4 . } { . . 193 . 2 . . } %
2395 {.....6.58}{....3.....}{....2.934}%
2396 [DT2 tough 115]
2397 \vfill
2398 \begin{minipage}{0.95\linewidth}\begin{center}
2399 TT115 (tough) \\
2400 \slashed{115.sud}
2401 \end{center}\end{minipage}
2402
2403 \renewcommand*{\puzzlefile}{tt120.sud}
2404 \writepuzzle%
2405 { . . 8 . 1 . 7 . . } { . . 4 . 67 . 8 . . } { . . . 2 . . . 461 . } %
2406 { .9 . . . . 1 . 8 } { . . . . . . . } { 2 . 1 . . . . 9 . } %
2407 { .759 . . 4 . . } { . . 4 . 52 . 6 . } { . . 9 . 3 . 5 . . } %
2408 [DT2 tough 120]
2409 \vfill
2410 \begin{minipage}{0.95\linewidth}\begin{center}
2411 TT120 (tough) \\
2412 \sudoku{tt120.sud}
2413 \end{center}\end{minipage}
2415 \renewcommand*{\puzzlefile}{st1130.sud}
2416 \writepuzzle%
2417 {8...356...}{5....4.1.}{34......}%
2418 \{7.156..2.\} \{.6....7.\} \{.2..796.5\} \%
2419 {......32}{.9.4....8}{...682..9}%
2420 [Seattle Times 2005/11/30 3 stars]
2421 \vfill
2422 \begin{minipage}{0.95\linewidth}\begin{center}
2423 ST1130 (3 stars) \\
```

```
2424 \sudoku{st1130.sud}
2425 \end{center}\end{minipage}
2426
2427 \renewcommand*{\puzzlefile}{st1207.sud}
2428 \writepuzzle%
2429 {...483..6}{.....57.2}{.....38.}%
2430 { . . 8 . . 16 . . } { . . 26 . 5 . 17 . } { . . . 57 . . . 2 . . } %
2431 {.82.....}{9.18.....}{4..527...}%
2432 [Seattle Times 2005/12/07 3 stars]
2433 \vfill
2434 \begin{minipage}{0.95}\linewidth}\begin{center}
2435 ST1207 (3 stars) \\
2436 \sudoku{st1207.sud}
2437 \end{center}\end{minipage}
2438
2439 \renewcommand*{\puzzlefile}{st1209.sud}
2440 \writepuzzle%
2441 {...6.....}{.4..8..5.}{.519..2.8}%
2442 \{...729...3\} \{.9....1.\} \{4...679..\}%
2443 {6.8..957.}{.7..2..9.}{....4...}%
2444 [Seattle Times 2005/12/09 5 stars]
2445 \vfill
2446 \ensuremath{\verb|\degin{minipage}{0.95}| linewidth}\ensuremath{\verb|\degin{center}|}
2447 ST1209 (5 stars) \\
2448 \sudoku{st1209.sud}
2449 \end{center}\end{minipage}
2451 \renewcommand*{\puzzlefile}{st1221.sud}
2452 \writepuzzle%
2453 {.....392.}{4....5.7.}{29.4...63}%
2454 {..4....5.}{...2.1...}{.5....3..}%
2455 {74...2.96}{.6.5....7}{.217.....}%
2456 [Seattle Times 2005/12/21 3 stars]
2457 \vfill
2458 \begin{minipage}{0.95\linewidth}\begin{center}
2459 ST1221 (3 stars) \\
2460 \sudoku{st1221.sud}
2461 \end{center}\end{minipage}
2463 \renewcommand*{\puzzlefile}{st1228.sud}
2464 \writepuzzle%
2465 {6..1..5..}{.....379}{.942....}%
2466 {...5....8.3}{.4.....9.}{9.7...6..}%
2467 {.....623.}{138......}{..6..8..7}%
2468 [Seattle Times 2005/12/28 3 stars]
2469 \vfill
2470 \begin{minipage}{0.95\linewidth}\begin{center}
2471 ST1228 (3 stars) \\
2472 \sudoku{st1228.sud}
2473 \end{center}\end{minipage}
```

```
2475 \renewcommand*{\puzzlefile}{st0126.sud}
2476 \writepuzzle%
2477 {...36....7.}{1....352..}{...4......}%
2478 {..6....29}{7......4}{32....5..}%
2479 {.....1..}{...824...5}{..4...93..}%
2480 [Seattle Times 2006/01/26 4 stars]
2481 \vfill
2482 \begin{minipage}{0.95\linewidth}\begin{center}
2483 ST0126 (4 stars) \\
2484 \sudoku{st0126.sud}
2485 \end{center}\end{minipage}
2487 \renewcommand*{\puzzlefile}{st0127.sud}
2488 \writepuzzle%
2489 \{25.8....\}\{....9.8.2\}\{9..4.7...\}\%
2490 {64.....9.}{.9.1.3.4.}{.7.....21}%
2491 {...5.4..7}{7.6.8....}{....1.83}%
2492 [Seattle Times 2006/01/27 5 stars]
2494 \begin{minipage}{0.95\linewidth}\begin{center}
2495 ST0127 (5 stars) \\
2496 \sudoku{st0127.sud}
2497 \end{center}\end{minipage}
2499 \renewcommand*{\puzzlefile}{st0204.sud}
2500 \writepuzzle%
2501 {.5..2.8.6}{.....6..3}{.6..132..}%
2502 \{.7....96.\} \{4.....1\} \{.16....3.\}\%
2503 {...723...8.}{6...7.....}{2.4.9...7.}%
2504 [Seattle Times 2006/02/04 6 stars]
2505 \vfill
2506 \begin{minipage}{0.95\linewidth}\begin{center}
2507 ST0204 (6 stars) \\
2508 \sudoku{st0204.sud}
2509 \end{center}\end{minipage}
2511 \renewcommand*{\puzzlefile}{st0208.sud}
2512 \writepuzzle%
2513 {21.9....7}{5.9..421.}{..7.....}%
2514 { . . . 875 . . . . } { 3 . 14 . 95 . 8 } { . . . . . 361 . . } %
2515 {.....4..}{.325..9.1}{1....8.25}%
2516 [Seattle Times 2005/02/08 3 stars]
2517 \vfill
2518 \begin{minipage}{0.95\linewidth}\begin{center}
2519 ST0208 (3 stars) \\
2520 \sudoku{st0208.sud}
2521 \end{center}\end{minipage}
2523 \renewcommand*{\puzzlefile}{st0209.sud}
```

```
2524 \writepuzzle%
2525 {...9......}{.523.1...}{8.12.6...}%
2526 {..4....1.}{97..2..84}{.2....9..}%
2527 {...8.41.5}{...6.524.}{....8..}%
2528 [Seattle Times 2005/02/09 4 stars]
2529 \vfill
2530 \begin{minipage}{0.95\linewidth}\begin{center}
2531 ST0209 (4 stars) \\
2532 \sudoku{st0209.sud}
2533 \end{center}\end{minipage}
2534
2535 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% answers
2536
2537 \clearpage
2538 \pagestyle{empty}
2539 \cleardoublepage
2540 \pagestyle{myheadings}
2541 \markboth{SOLUTIONS}{SOLUTIONS}
2543 \cluefont{\normalsize}
2544 \cellsize{1.5\baselineskip}
2545
2546 \renewcommand*{\puzzlefile}{se5.ans}
2547 \writepuzzle%
2548\ \{724195863\}\{561283497\}\{938647251\}\%
2549 {189756324} {256314789} {473928615} %
2550 {645839172}{892471536}{317562948}%
2551 [SSBL easy 5 solution]
2552 \renewcommand*{\puzzlefile}{se10.ans}
2553 \writepuzzle%
2554 {156349782}{482715639}{793286145}%
2555 {649853271}{217964358}{835172496}%
2556 {524697813}{371528964}{968431527}%
2557 [SSBL easy 10 solution]
2558 \vfill
2559 \verb|\noindent\begin{minipage}{0.47} linewidth} \verb|\begin{center}|
2560 SE5 (easy solution) \\
2561 \sudoku{se5.ans}
2562 \end{center}\end{minipage}
2563 \hfill
2564 \begin{minipage}{0.47\linewidth}\begin{center}
2565 SE10 (easy solution) \\
2566 \sudoku{se10.ans}
2567 \end{center}\end{minipage}
2569 \renewcommand*{\puzzlefile}{se15.ans}
2570 \writepuzzle%
2571 {456713982}{231698475}{879254631}%
2572 {597846213}{124935867}{368172549}%
2573 {643527198}{712489356}{985361724}%
```

```
2574 [SSBL easy 15 solution]
2575 \renewcommand*{\puzzlefile}{se20.ans}
2576 \writepuzzle%
2577 {368912547}{975438621}{412657839}%
2578 {291543768}{783296414}{546781293}%
2579 {657129384}{134865972}{829374156}%
2580 [SSBL easy 20 solution]
2581 \vfill
2582 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
2583 SE15 (easy solution) \\
2584 \sudoku{se15.ans}
2585 \end{center}\end{minipage}
2586 \hfill
2587 \begin{minipage}{0.47\linewidth}\begin{center}
2588 SE20 (easy solution) \\
2589 \sudoku{se20.ans}
2590 \end{center}\end{minipage}
2592 \renewcommand*{\puzzlefile}{se25.ans}
2593 \writepuzzle%
2594 {278963154}{645712839}{931854276}%
2595 {823641795}{159387462}{764295381}%
2596 {482579613}{397126548}{516438927}%
2597 [SSBL easy 25 solution]
2598 \renewcommand*{\puzzlefile}{se30.ans}
2599 \writepuzzle%
2600 {436129875}{128753496}{759864321}%
2601 {514287639}{673591284}{892346517}%
2602 {941638752}{365972148}{287415963}%
2603 [SSBL easy 30 solution]
2604 \vfill
2605 \noindent\begin{minipage}\{0.47\linewidth\}\begin{center}
2606 SE25 (easy solution) \\
2607 \setminus sudoku\{se25.ans\}
2608 \end{center}\end{minipage}
2609 \hfill
2610 \begin{minipage}{0.47\linewidth}\begin{center}
2611 SE30 (easy solution) \\
2612 \sudoku{se30.ans}
2613 \end{center}\end{minipage}
2615 \renewcommand*{\puzzlefile}{tg5.ans}
2616 \writepuzzle%
2617 {764159382}{519238746}{823674951}%
2618 {457982613}{936715428}{281463597}%
2619 {142397865}{675841239}{398526174}%
2620 [DT2 gentle 5 solution]
2621 \renewcommand*{\puzzlefile}{tg10.ans}
2622 \verb|\writepuzzle||%
2623\ \{382196574\}\{491573862\}\{567248139\}\%
```

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2624 {278614395}{946385217}{135729486}%
2625 {624931758}{753862941}{819457623}%
2626 [DT2 gentle 10 solution]
2627 \vfill
2628 \noindent\begin{minipage}{0.47}\linewidth}\begin{center}
2629 TG5 (gentle solution) \\
2630 \sudoku{tg5.ans}
2631 \end{center}\end{minipage}
2632 \hfill
2633 \begin{minipage}{0.47\linewidth}\begin{center}
2634 TG10 (gentle solution) \\
2635 \sudoku{tg10.ans}
2636 \end{center}\end{minipage}
2638 \renewcommand*{\puzzlefile}{tg15.ans}
2639 \writepuzzle%
2640 {462198573}{357462189}{981537426}%
2641 {236741958}{175986342}{894253617}%
2642 {723615894}{619824735}{548379261}%
2643 [DT2 gentle 15 solution]
2644 \renewcommand*{\puzzlefile}{tg20.ans}
2645 \writepuzzle%
2646 {256789431}{481326759}{739415628}%
2647 {594261873}{167938245}{823574196}%
2648 {912643587}{645897312}{378152964}%
2649 [DT2 gentle 20 solution]
2650 \vfill
2651 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
2652 TG15 (gentle solution) \\
2653 \sudoku{tg15.ans}
2654 \end{center}\end{minipage}
2655 \hfill
2656 \begin{minipage}{0.47\linewidth}\begin{center}
2657 TG20 (gentle solution) \\
2658 \sudoku{tg20.ans}
2659 \end{center}\end{minipage}
2660
2661 \renewcommand*{\puzzlefile}{tg25.ans}
2662 \writepuzzle%
2663 {782463519}{461295378}{395781246}%
2664 {819527463}{634918752}{527346891}%
2665 {256872934}{978134625}{243659187}%
2666 [DT2 gentle 25 solution]
2667 \renewcommand*{\puzzlefile}{tg30.ans}
2668 \writepuzzle%
2669 {376418529}{928756134}{154923678}%
2670 {749132865}{612584793}{835697241}%
2671 {597361482}{483275916}{261849357}%
2672 [DT2 gentle 30 solution]
2673 \vfill
```

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2674 \rightarrow \frac{minipage}{0.47} inewidth} \eqni{center}
2675 TG25 (gentle solution) \\
2676 \slashed {tg25.ans}
2677 \end{center}\end{minipage}
2678 \hfill
2679 \begin{minipage}{0.47\linewidth}\begin{center}
2680 TG30 (gentle solution) \\
2681 \sudoku{tg30.ans}
2682 \end{center}\end{minipage}
2684 \renewcommand*{\puzzlefile}{st1226.ans}
2685 \writepuzzle%
2686 {962854731}{745213689}{183967452}%
2687 {326748915}{571639248}{498125376}%
2688 {837592164}{659471823}{214386597}%
2689 [Seattle Times 2005/12/26 1 star solution]
2690 \renewcommand*{\puzzlefile}{st0206.ans}
2691 \writepuzzle%
2692\ \{176429385\}\{352817496\}\{849653217\}\%
2693 {463971852}{925384671}{718265934}%
2694 {281536749}{534792168}{697148523}%
2695 [Seattle Times 2005/02/06 1 star solution]
2696 \vfill
2697 \verb|\noindent\begin{minipage}{0.47} linewidth} \verb|\begin{center}|
2698 ST1226 (1 star solution) \
2699 \sudoku{st1226.ans}
2700 \end{center}\end{minipage}
2701 \hfill
2702 \ensuremath{\verb| begin{minipage}{0.47} linewidth}\ensuremath{\verb| begin{center}|}
2703\;\text{STO2O6} (1 star solution) \\
2704 \sudoku{st0206.ans}
2705 \end{center}\end{minipage}
2707 \renewcommand*{\puzzlefile}{st0123.ans}
2708 \writepuzzle%
2709 {594621837}{736489125}{281357469}%
2710 {319278654}{652134978}{478596312}%
2711 {927813546}{145962783}{863745291}%
2712 [Seattle Times 2006/01/23 1 star solution]
2713 \renewcommand*{\puzzlefile}{cs1.ans}
2714 \writepuzzle%
2715 {546987312}{213654978}{879321645}%
2716 {657198423}{324765189}{981432756}%
2717 {435876291}{768219534}{192543867}%
2718 [CreateSudoku 1 (level 2) solution]
2719 \vfill
2720 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
2721 ST0123 (1 star solution) \\
2722 \sudoku{st0123.ans}
2723 \end{center}\end{minipage}
```

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2724 \hfill
2725 \begin{minipage}{0.47\linewidth}\begin{center}
2726 CS1 (level 2 solution) \\
2727 \sudoku{cs1.ans}
2728 \end{center}\end{minipage}
2729
2730 \renewcommand*{\puzzlefile}{cs2.ans}
2731 \writepuzzle%
2732 {978312654}{312645987}{645978321}%
2733 {189423765}{423756198}{756189432}%
2734 {291534876}{867291543}{534867219}%
2735 [CreateSudoku 2 (level 2) solution]
2736 \renewcommand*{\puzzlefile}{cs3.ans}
2737 \writepuzzle%
2738 {456897123}{123564789}{789231456}%
2739 {234675891}{567918234}{891342567}%
2740 {345786912}{912453678}{678129345}%
2741 [CreateSudoku 3 (level 2) solution]
2742 \vfill
2743 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
2744 CS2 (level 2 solution) \\
2745 \sudoku{cs2.ans}
2746 \end{center}\end{minipage}
2747 \hfill
2748 \begin{minipage}{0.47\linewidth}\begin{center}
2749 CS3 (level 2 solution) \\
2750 \sudoku{cs3.ans}
2751 \end{center}\end{minipage}
2752
2753 %%%%%%%%%%%%%%%%%%%%%%%%%%%% medium
2754
2755 \renewcommand*{\puzzlefile}{sm5.ans}
2756 \writepuzzle%
2757 {387691245}{546273198}{921485637}%
2758 {865342971}{193567482}{274918356}%
2759 {618739524}{759124863}{432856719}%
2760 [SSBL medium 5 solution]
2761 \renewcommand*{\puzzlefile}{sm10.ans}
2762 \writepuzzle%
2763 {635748219}{418392576}{279561483}%
2764 {527984631}{941653827}{863127954}%
2765 {194835762}{786219345}{352476198}%
2766 [SSBL medium 10 solution]
2767 \vfill
2768 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
2769 SM5 (medium solution) \\
2770 \sudoku{sm5.ans}
2771 \end{center}\end{minipage}
2772 \hfill
2773 \begin{minipage}{0.47\linewidth}\begin{center}
```

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2774 \text{ SM10} \text{ (medium solution) } 
2775 \sudoku{sm10.ans}
2776 \end{center}\end{minipage}
2778 \mbox{renewcommand}*{\puzzlefile}{sm15.ans}
2779 \writepuzzle%
2780 {853974612}{471326958}{962815473}%
2781 {396542781}{745681239}{218739564}%
2782 {134267895}{587493126}{629158347}%
2783 [SSBL medium 15 solution]
2784 \renewcommand*{\puzzlefile}{sm20.ans}
2785 \writepuzzle%
2786 {863452197}{594178326}{172639548}%
2787 {617894235}{938526471}{234713869}%
2788 {489265713}{351947682}{726381954}%
2789 [SSBL medium 20 solution]
2790 \vfill
2791 \noindent\begin{minipage}\{0.47\ \begin{center}
2792 SM15 (medium solution) \\
2793 \sudoku{sm15.ans}
2794 \end{center}\end{minipage}
2796 \ensuremath{\verb|\document|} 196 \ensuremath{\document|} 196 \ensuremath{\docu
2797\;\mathrm{SM20} (medium solution) \\
2798 \sudoku{sm20.ans}
2799 \end{center}\end{minipage}
2801 \renewcommand*{\puzzlefile}{sm25.ans}
2802 \writepuzzle%
2803 \ \{382467951\} \{716935284\} \{495218376\} \%
2804 {564329817}{278651493}{139784625}%
2805 {927146538}{651893742}{843572169}%
2806 [SSBL medium 25 solution]
2807 \renewcommand*{\puzzlefile}{sm30.ans}
2808 \writepuzzle%
2809 {765834921}{318279465}{294615378}%
2810 {657392814}{823741659}{941568732}%
2811 {439157286}{186423597}{572986143}%
2812 [SSBL medium 30 solution]
2813 \vfill
2814 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
2815 SM25 (medium solution) \\
2816 \setminus sudoku\{sm25.ans\}
2817 \end{center}\end{minipage}
2819 \begin{minipage}{0.47\linewidth}\begin{center}
2820 SM30 (medium solution) \\
2821 \sudoku{sm30.ans}
2822 \end{center}\end{minipage}
2823
```

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2824 \renewcommand*{\puzzlefile}{tm35.ans}
2825 \writepuzzle%
2826 {591328746}{674951823}{238674195}%
2827 {356297481}{427185369}{819463257}%
2828 {985732614}{742516938}{163849572}%
2829 [DT2 moderate 35 solution]
2830 \renewcommand*{\puzzlefile}{tm40.ans}
2831 \writepuzzle%
2832 {874136592}{952478136}{316592874}%
2833 {631284759}{287915463}{495367281}%
2834 {763841925}{548629317}{129753648}%
2835 [DT2 moderate 40 solution]
2836 \vfill
2837 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
2838 TM35 (moderate solution) \\
2839 \sudoku{tm35.ans}
2840 \end{center}\end{minipage}
2841 \hfill
2842 \begin{minipage}{0.47\linewidth}\begin{center}
2843 TM40 (moderate solution) \\
2844 \sudoku{tm40.ans}
2845 \end{center}\end{minipage}
2846
2847 \mbox{renewcommand}*{\puzzlefile}{tm45.ans}
2848 \writepuzzle%
2849 {716248935}{538769421}{924531786}%
2850 {179683542}{652974813}{483152679}%
2851 {241896357}{897325164}{365417298}%
2852 [DT2 moderate 45 solution]
2853 \renewcommand*{\puzzlefile}{tm50.ans}
2854 \writepuzzle%
2855 {751962834}{468375219}{392148756}%
2856 {627891345}{143526987}{589437162}%
2857 {975613428}{834259671}{216784593}%
2858 [DT2 moderate 50 solution]
2859 \vfill
2860 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
2861 TM45 (moderate solution) \\
2862 \sudoku{tm45.ans}
2863 \end{center}\end{minipage}
2864 \hfill
2865 \begin{minipage}{0.47\linewidth}\begin{center}
2866 \text{ TM50} (moderate solution) \\
2867 \sudoku{tm50.ans}
2868 \end{center}\end{minipage}
2870 \renewcommand*{\puzzlefile}{tm55.ans}
2871 \writepuzzle%
2872 {731946528}{245138679}{968572143}%
2873 {614729385}{572813964}{893465712}%
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2874 {159684237}{426357891}{387291456}%
2875 [DT2 moderate 55 solution]
2876 \renewcommand*{\puzzlefile}{tm60.ans}
2877 \writepuzzle%
2878 {734198562}{156324798}{982567431}%
2879 {813752649}{465983217}{279416853}%
2880 {341875926}{697241385}{528639174}%
2881 [DT2 moderate 60 solution]
2882 \vfill
2883 \noindent\begin{minipage}{0.47}\newidth}\begin{center}
2884 \text{ TM55} (moderate solution) \\
2885 \sudoku{tm55.ans}
2886 \end{center}\end{minipage}
2888 \begin{minipage}{0.47\linewidth}\begin{center}
2889 TM60 (moderate solution) \\
2890 \setminus \text{sudoku}\{\text{tm}60.\text{ans}\}
2891 \end{center}\end{minipage}
2893 \renewcommand*{\puzzlefile}{st0914.ans}
2894 \writepuzzle%
2895 {567293184}{298461537}{413578692}%
2896 {321759468}{649812753}{785634921}%
2897 {936127845}{872945316}{154386279}%
2898 [Seattle Times 2005/09/14 2 star solution]
2899 \renewcommand*{\puzzlefile}{st0207.ans}
2900 \writepuzzle%
2901 {872351946}{561849273}{934672581}%
2902 {759283164}{628514397}{413967852}%
2903 {285436719}{196725438}{347198625}%
2904 [Seattle Times 2005/02/07 2 star solution]
2905 \vfill
2906 \noindent\begin{minipage}\{0.47\linewidth\}\begin{center}
2907 ST0914 (2 star solution) \\
2908 \sudoku{st0914.ans}
2909 \end{center}\end{minipage}
2910 \hfill
2911 \begin{minipage}{0.47\linewidth}\begin{center}
2912 ST0207 (2 star solution) \\
2913 \sudoku{st0207.ans}
2914 \end{center}\end{minipage}
2916 \renewcommand*{\puzzlefile}{cs4.ans}
2917 \writepuzzle%
2918 {123465978}{456798312}{789132645}%
2919 {891243756}{234576189}{567819423}%
2920 {912354867}{678921534}{345687291}%
2921 [CreateSudoku 4 (level 4) solution]
2922 \renewcommand*{\puzzlefile}{cs5.ans}
2923 \writepuzzle%
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2924 {231654978}{564987312}{897321645}%
2925 {918432756}{675198423}{342765189}%
2926 {786219534}{453876291}{129543867}%
2927 [CreateSudoku 5 (level 4) solution]
2928 \vfill
2929 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
2930 CS4 (level 8 solution) \\
2931 \sudoku{cs4.ans}
2932 \end{center}\end{minipage}
2933 \hfill
2934 \begin{minipage}{0.47\linewidth}\begin{center}
2935 CS5 (level 8 solution) \\
2936 \sudoku{cs5.ans}
2937 \end{center}\end{minipage}
2938
2939 \renewcommand*{\puzzlefile}{cs6.ans}
2940 \writepuzzle%
2941 {312654978}{645987312}{978321645}%
2942 {756198423}{423765189}{189432756}%
2943 {534876291}{291543867}{867219534}%
2944 [CreateSudoku 6 (level 4) solution]
2945 \renewcommand*{\puzzlefile}{sh5.ans}
2946 \writepuzzle%
2947 {269175438} {471832965} {583694217} %
2948 {715426389}{894317526}{326958741}%
2949 {942561873}{138749652}{657283194}%
2950 [SSBL hard 5 solution]
2951 \vfill
2952 \verb|\noindent\begin{minipage}{0.47} linewidth} \verb|\begin{center}{}
2953 CS6 (level 4 solution) \\
2954 \sudoku{cs6.ans}
2955 \end{center}\end{minipage}
2957 \begin{minipage}{0.47\linewidth}\begin{center}
2958 SH5 (hard solution) \\
2959 \sudoku{sh5.ans}
2960 \end{center}\end{minipage}
2962 \renewcommand*{\puzzlefile}{sh10.ans}
2963 \writepuzzle%
2964 {437921865}{156837492}{289456137}%
2965 {598163274}{374295681}{621748953}%
2966 {713682549}{845319726}{962574318}%
2967 [SSBL hard 10 solution]
2968 \renewcommand*{\puzzlefile}{sh15.ans}
2969 \writepuzzle%
2970 {216935847} {478261359} {395478261} %
2971 {761392584}{952846713}{843157926}%
2972 {124783695}{539624178}{687519432}%
2973 [SSBL hard 15 solution]
```

```
2974 \vfill
2975 \verb|\noindent\begin{minipage}{0.47} linewidth} \verb|\begin{center}|
2976 SH10 (hard solution) \\
2977 \slashed{sh10.ans}
2978 \end{center}\end{minipage}
2979 \hfill
2980 \begin{minipage}{0.47\linewidth}\begin{center}
2981 SH15 (hard solution) \\
2982 \sudoku{sh15.ans}
2983 \end{center}\end{minipage}
2985 \renewcommand*{\puzzlefile}{sh20.ans}
2986 \writepuzzle%
2987 {468271935}{925438671}{713695284}%
2988 {154762893}{832519467}{679384512}%
2989 {587943126}{296157348}{341826759}%
2990 [SSBL hard 20 solution]
2991 \renewcommand*{\puzzlefile}{sh25.ans}
2992 \writepuzzle%
2993 {439561728}{167238459}{852497613}%
2994 {286953174}{794816532}{513724986}%
2995\ \{348179265\}\{621345897\}\{975682341\}\%
2996 [SSBL hard 25 solution]
2997 \vfill
2998 \noindent\begin{minipage}\{0.47\linewidth\}\
2999 SH20 (hard solution) \\
3000 \sudoku{sh20.ans}
3001 \end{center}\end{minipage}
3002 \hfill
3003 \begin{minipage}{0.47\linewidth}\begin{center}
3004 SH25 (hard solution) \\
3005 \sudoku{sh25.ans}
3006 \end{center}\end{minipage}
3008 \renewcommand*{\puzzlefile}{sh30.ans}
3009 \writepuzzle%
3010 {461258793}{253917846}{789463152}%
3011 {346789521}{572146389}{918325674}%
3012 {894671235}{635892417}{127534968}%
3013 [SSBL hard 30 solution]
3014 \renewcommand*{\puzzlefile}{tt100.ans}
3015 \writepuzzle%
3016 {513896427}{742315698}{968742531}%
3017 {154289376}{376154289}{289637154}%
3018 {891563742}{425971863}{637428915}%
3019 [DT2 tough 100 solution]
3020 \vfill
3021 \noindent\left( \min_{minipage} \{0.47 \le dh \} \right)
3022 SH30 (hard solution) \\
3023 \sudoku{sh30.ans}
```

```
3024 \end{center}\end{minipage}
3025 \hfill
3026 \end{figure} \{0.47 \end{figure} \end{figure} \label{fig:conter}
3027 TT100 (tough solution) \\
3028 \sudoku{tt100.ans}
3029 \end{center}\end{minipage}
3031 \renewcommand*{\puzzlefile}{tt105.ans}
3032 \writepuzzle%
3033 {925378146}{681254793}{734916582}%
3034 {256739418}{178462359}{349581267}%
3035 {597843621}{462197835}{813625974}%
3036 [DT2 tough 105 solution]
3037 \renewcommand*{\puzzlefile}{tt110.ans}
3038 \writepuzzle%
3039 {379412586}{648539217}{125687349}%
3040 {936825174}{214763958}{857194632}%
3041 {492358761}{581276493}{763941825}%
3042 [DT2 tough 110 solution]
3043 \vfill
3044 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
3045 TT105 (tough solution) \\
3046 \sudoku{tt105.ans}
3047 \end{center}\end{minipage}
3048 \hfill
3049 \begin{minipage}{0.47\linewidth}\begin{center}
3050 TT110 (tough solution) \\
3051 \sudoku{tt110.ans}
3052 \end{center}\end{minipage}
3053
3054 \renewcommand*{\puzzlefile}{tt115.ans}
3055 \writepuzzle%
3056 {432758196}{196243587}{758169423}%
3057 {945682371}{263571849}{871934265}%
3058 {329416758}{584397612}{617825934}%
3059 [DT2 tough 115 solution]
3060 \renewcommand*{\puzzlefile}{tt120.ans}
3061 \writepuzzle%
3062 {968215734}{143679852}{752384619}%
3063 {496523178}{537198246}{281746395}%
3064 {875961423}{314852967}{629437581}%
3065 [DT2 tough 120 solution]
3066 \vfill
3067 \verb|\noindent\begin{minipage}{0.47} linewidth} \verb|\begin{center}{}
3068 TT115 (tough solution) \\
3069 \sudoku{tt115.ans}
3070 \end{center}\end{minipage}
3071 \hfill
3072 \begin{minipage}{0.47\linewidth}\begin{center}
3073 TT120 (tough solution) \\
```

```
3074 \sudoku{tt120.ans}
3075 \end{center}\end{minipage}
3076
3077 \renewcommand*{\puzzlefile}{st1130.ans}
3078 \writepuzzle%
3079 {819356247}{576924813}{342817596}%
3080 {781563924}{965248371}{423179685}%
3081 {658791432}{297435168}{134682759}
3082 [Seattle Times 2005/11/30 3 star solution]
3083 \renewcommand*{\puzzlefile}{st1207.ans}
3084 \writepuzzle%
3085 {217483956}{834695712}{659172384}%
3086 {798231645}{326954178}{145768239}%
3087 {582319467}{971846523}{463527891}%
3088 [Seattle Times 2005/12/07 3 star solution]
3089 \vfill
3090 \noindent\begin{minipage}{0.47}\newidth}\begin{center}
3091 ST1130 (3 star solution) \\
3092 \sudoku{st1130.ans}
3093 \end{center}\end{minipage}
3095 \begin{minipage}{0.47\linewidth}\begin{center}
3096 ST1207 (3 star solution) \\
3097 \sudoku{st1207.ans}
3098 \end{center}\end{minipage}
3100 \renewcommand*{\puzzlefile}{st1209.ans}
3101 \writepuzzle%
3102 {839652147}{246781359}{751943268}%
3103\ \{167295483\}\{592438716\}\{483167925\}\%
3104 {628319574}{374526891}{915874632}%
3105 [Seattle Times 2005/12/09 5 star solution]
3106 \renewcommand*{\puzzlefile}{st1221.ans}
3107 \writepuzzle%
3108 {517863924}{436925178}{298417563}%
3109 {174389652}{683251749}{952674381}%
3110 {745132896}{369548217}{821796435}%
3111 [Seattle Times 2005/12/21 3 star solution]
3112 \vfill
3113 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
3114 ST1209 (5 star solution) \\
3115 \sudoku{st1209.ans}
3116 \end{center}\end{minipage}
3117 \hfill
3118 \begin{minipage}{0.47\linewidth}\begin{center}
3119 ST1221 (3 star solution) \\
3120 \sudoku{st1221.ans}
3121 \end{center}\end{minipage}
3123 \renewcommand*{\puzzlefile}{st1228.ans}
```

```
3124 \writepuzzle%
3125 {673189524}{812654379}{594273186}%
3126 {265791843}{341865792}{987342651}%
3127 {795416238}{138927465}{426538917}%
3128 [Seattle Times 2005/12/28 3 star solution]
3129 \renewcommand*{\puzzlefile}{st0126.ans}
3130 \writepuzzle%
3131 {253698471}{197435286}{864127953}%
3132 {416573829}{785912634}{329864517}%
3133 {972356148}{638241795}{541789362}%
3134 [Seattle Times 2006/01/26 4 star solution]
3135 \vfill
3136 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
3137 ST1228 (3 star solution) \\
3138 \sudoku{st1228.ans}
3139 \end{center}\end{minipage}
3140 \hfill
3141 \begin{minipage}{0.47\linewidth}\begin{center}
3142 ST0126 (4 star solution) \\
3143 \sudoku{st0126.ans}
3144 \end{center}\end{minipage}
3145
3146 \renewcommand*{\puzzlefile}{st0127.ans}
3147 \writepuzzle%
3148 {253816479}{467395812}{918427536}%
3149 {641752398}{892163745}{375948621}%
3150 {189534267}{736289154}{524671983}%
3151 [Seattle Times 2006/01/27 5 star solution]
3152 \renewcommand*{\puzzlefile}{st0204.ans}
3153 \writepuzzle%
3154 {153427896}{742986513}{869513247}%
3155 {375142968}{428369751}{916875432}%
3156 {597321684}{681754329}{234698175}%
3157 [Seattle Times 2006/02/04 6 star solution]
3158 \vfill
3159 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
3160 ST0127 (5 star solution) \\
3161 \sudoku{st0127.ans}
3162 \end{center}\end{minipage}
3163 \hfill
3164 \begin{minipage}{0.47\linewidth}\begin{center}
3165 ST0204 (6 star solution) \\
3166 \sudoku{st0204.ans}
3167 \end{center}\end{minipage}
3169 \renewcommand*{\puzzlefile}{st0208.ans}
3170 \writepuzzle%
3171 {213985647}{589674213}{647213859}%
3172 {928751364}{361429578}{754836192}%
3173 {875192436}{432567981}{196348725}%
```

```
3174 [Seattle Times 2005/02/08 3 star solution]
3175 \renewcommand*{\puzzlefile}{st0209.ans}
3176 \writepuzzle%
3177 {639587421}{752341698}{841296753}%
3178 {584769312}{976123584}{123458976}%
3179 {297834165}{318675249}{465912837}%
3180 [Seattle Times 2005/02/09 4 star solution]
3181 \vfill
3182 \noindent\begin{minipage}{0.47\linewidth}\begin{center}
3183 ST0208 (3 star solution) \\
3184 \sudoku{st0208.ans}
3185 \end{center}\end{minipage}
3186 \hfill
3187 \begin{minipage}{0.47\linewidth}\begin{center}
3188 ST0209 (4 star solution) \\
3189 \sudoku{st0209.ans}
3190 \end{center}\end{minipage}
3191
3192
3194 \cleardoublepage
3196 \bibliographystyle{alpha}
3197 \begingroup
3198 \raggedright
3199 \begin{thebibliography}{GMSN94A}
3201 \bibitem[Mep05]{DT2}
3202 Michael Mepham.
3203 \emph{The Daily Telegraph Sudoku 2}.
3204 \newblock Pan Books, 2005.
3205 \newblock ISBN 0-330-44203-3.
3207 \bibitem[Wil06] {SUDOKUBUNDLE}
3208 Peter Wilson.
3209 \emph{The sudoku bundle for displaying, solving and generating
         Sudoku puzzles}.
3211 \newblock February 2006.
3212 \newblock (Available from CTAN in \url{macros/latex/contrib/sudokubundle}).
3214 \bibitem[SOL] {SOL}
3215 \emph{Sudoku Online: Home of the Sudokulist}.
3216 \newblock \url{http://www.sudoku.org.uk}
3218 \bibitem[SSBL]{SSBL}
3219 \emph{Sudoku Solver ... by logic}.
3220 \newblock \url{http://www.sudokusolver.co.uk}
3222 \end{thebibliography}
3223 \endgroup
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[Ars95]	Donald Arseneau. Generating random numbers in T _E X. 1995. (Available from CTAN in macros/generic/random.tex)
[MG04]	Frank Mittelbach and Michel Goossens. The LaTeX Companion. Second edition. Addison-Wesley Publishing Company, 2004. ISBN 0-201-36299-6.
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[SOL]	Sudoku Online: Home of the Sudokulist. http://www.sudoku.org.uk
[SSBL]	Sudoku Solver by logic. http://www.sudokusolver.co.uk

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