Adv. Optimization HW #1

Problem 1

133 AV 4H
 Conner Reinhardt HIW #IMM Optimization) 9/2 P31 To Original Standard Form $min x_1 + 2xz$ $st, x_1 + x_2 = 10$ $2x_1 + 5x_2 = 40$ $x_1 \ge 0$ $x_2 \ge 0$ $x_2 \ge 0$
Sh max X1-x2 min + X1+X2 St X1+x2 = 4 241+5x2 = 30 X1 = 0 X2 = 0

Adv. Optimization HW #1

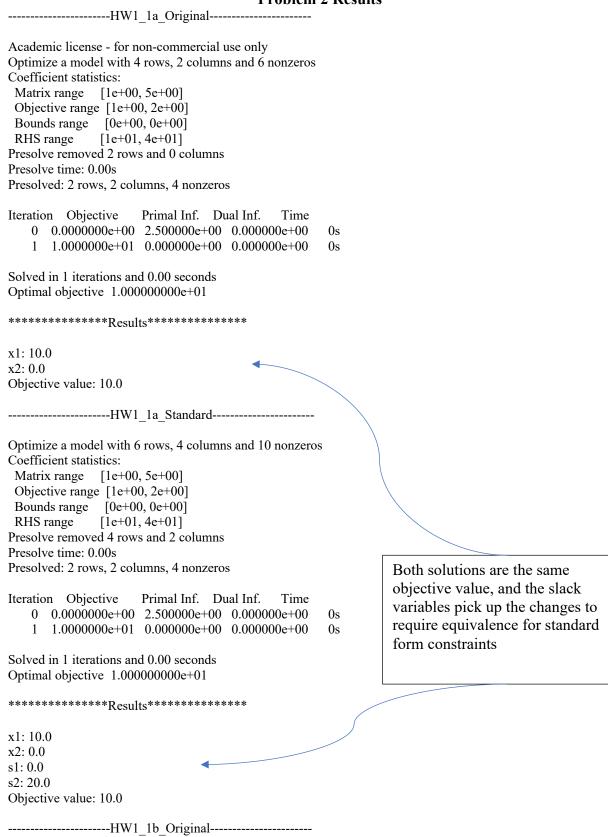
Problem 2 Code

```
#!/usr/bin/env python3
Created on Mon Aug 26 17:16:49 2019
@author: connerreinhardt
from gurobipy import *
print("\n-----\n")
m = Model("1a Original")
x1 = m.addVar(vtype=GRB.CONTINUOUS, name="x1")
x2 = m.addVar(vtype=GRB.CONTINUOUS, name="x2")
m.setObjective(x1+2*x2, GRB.MINIMIZE)
m.addConstr(x1 + x2 >= 10)
m.addConstr(2*x1 + 5*x2 <= 40)
m.addConstr(x1 >= 0)
m.addConstr(x2 >= 0)
m.optimize()
print("\n************Results***********\n")
for v in m.getVars():
  print(v.varName + ":", v.X)
print("Objective value: " + str(m.objVal))
print("\n-----\n")
m = Model("1a_Standard")
x1 = m.addVar(vtype=GRB.CONTINUOUS, name="x1")
x2 = m.addVar(vtype=GRB.CONTINUOUS, name="x2")
s1 = m.addVar(vtype=GRB.CONTINUOUS, name="s1")
s2 = m.addVar(vtype=GRB.CONTINUOUS, name="s2")
m.setObjective(x1+2*x2, GRB.MINIMIZE)
m.addConstr(x1 + x2 -s1 == 10)
m.addConstr(2*x1 + 5*x2 +s2 == 40)
```

```
m.addConstr(x1 >= 0)
m.addConstr(x2 >= 0)
m.addConstr(s1 >= 0)
m.addConstr(s2 >= 0)
m.optimize()
print("\n************Results***********\n")
for v in m.getVars():
  print(v.varName + ":", v.X)
print("Objective value: " + str(m.objVal))
print("\n-----\n")
m = Model("1b_Original")
x1 = m.addVar(vtype=GRB.CONTINUOUS, lb=-GRB.INFINITY, name="x1") #can be allowed to go
below 0
x2 = m.addVar(vtype=GRB.CONTINUOUS, name="x2")
m.setObjective(x1-x2, GRB.MAXIMIZE)
m.addConstr(x1 + x2 <= 4)
m.addConstr(2*x1 + 5*x2 == 30)
m.addConstr(x1 <= 0)</pre>
m.addConstr(x2 >= 0)
m.optimize()
print("\n************Results***********\n")
for v in m.getVars():
  print(v.varName + ":", v.X)
print("Objective value: " + str(m.objVal))
print("\n-----\n")
m = Model("1b_Standard")
x1 = m.addVar(vtype=GRB.CONTINUOUS, name="x1")
x2 = m.addVar(vtype=GRB.CONTINUOUS, name="x2")
s1 = m.addVar(vtype=GRB.CONTINUOUS, name="s1")
```

Adv. Optimization HW #1

Problem 2 Results



Adv. Optimization HW #1

Optimize a model with 4 rows, 2 columns and 6 nonzeros Coefficient statistics: Matrix range [1e+00, 5e+00] Objective range [1e+00, 1e+00] Bounds range [0e+00, 0e+00] RHS range [4e+00, 3e+01] Presolve removed 4 rows and 2 columns Presolve time: 0.00s Presolve: All rows and columns removed Iteration Objective Primal Inf. Dual Inf. Time 0 -1.0666667e+01 0.000000e+00 0.000000e+00 0sSolved in 0 iterations and 0.00 seconds Optimal objective -1.066666667e+01 *************Results********* x1: -3.33333333333333333 x2: 7.3333333333333334 Objective value: -10.6666666666668 -----HW1_1b_Standard-----Optimize a model with 5 rows, 3 columns and 8 nonzeros Coefficient statistics: Matrix range [1e+00, 5e+00] Objective range [1e+00, 1e+00] Bounds range [0e+00, 0e+00] RHS range [4e+00, 3e+01]Presolve removed 5 rows and 3 columns Presolve time: 0.00s Presolve: All rows and columns removed Iteration Objective Primal Inf. Dual Inf. Time 0 1.0666667e+01 0.000000e+00 0.000000e+00 0s

Both solutions are the same absolute value, except the sign is switched as it was rewritten to be a minimization instead of maximization problem in standard form

Solved in 0 iterations and 0.00 seconds Optimal objective 1.066666667e+01

*************Results*********

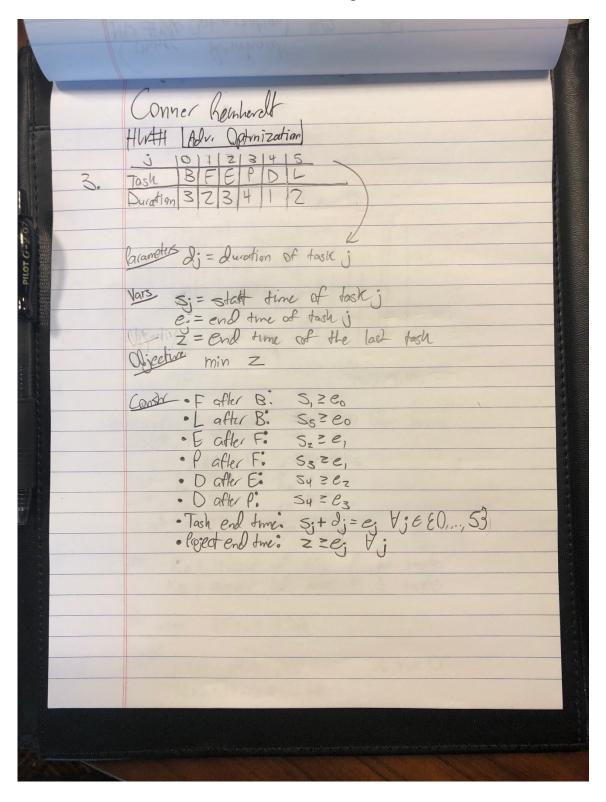
x1: 3.333333333333333 x2: 7.3333333333333334

s1: 0.0

Objective value: 10.6666666666668

Adv. Optimization HW #1

Problem 3 Setup



Adv. Optimization HW #1

Problem 3 Code

```
#!/usr/bin/env python3
Created on Mon Aug 26 17:16:49 2019
@author: connerreinhardt
from gurobipy import *
print("\n-----hw1 3-----\n")
m = Model("Pr3")
#--Params
d = [3,2,3,4,1,2] #durations of tasks
taskname = ["B","F","E","P","D","L"]
#--Vars
s = m.addVars(len(d),vtype=GRB.INTEGER, name="s") #start time of task j
e = m.addVars(len(d),vtype=GRB.INTEGER, name="e")                            #end time of task j
z = m.addVar(vtype=GRB.INTEGER) #end time of project
#--Objective
m.setObjective(z, GRB.MINIMIZE)
#--Constr
for i in range(len(d)):
   m.addConstr(e[i]==s[i]+d[i]) #task end time
   m.addConstr(z>=e[i]) #project end time
m.addConstr(s[1]>=e[0]) #Prereq: F after B
m.addConstr(s[5]>=e[0]) #Prereq: L after B
m.addConstr(s[2]>=e[1]) #Prereq: E after F
m.addConstr(s[3]>=e[1]) #Prereq: P after F
m.addConstr(s[4]>=e[2]) #Prereq: D after E
m.addConstr(s[4]>=e[3]) #Prereq: D after P
m.optimize()
print("\n************Results***********\n")
for v in m.getVars():
   print(v.varName + ":", v.X)
print("\n0bjective value: " + str(m.objVal) + "\n")
for i in range(len(d)):
   print(taskname[i] + " Started: " + str(s[i].x))
   print(taskname[i] + " Ended: " + str(e[i].x))
   print("\n")
```

Adv. Optimization HW #1

Problem 3 Output

```
-----HW1 3-----
Optimize a model with 18 rows, 13 columns and 36 nonzeros
Variable types: 0 continuous, 13 integer (0 binary)
Coefficient statistics:
Matrix range [1e+00, 1e+00]
 Objective range [1e+00, 1e+00]
 Bounds range [0e+00, 0e+00]
               [1e+00, 4e+00]
RHS range
Found heuristic solution: objective 10.0000000
Presolve removed 18 rows and 13 columns
Presolve time: 0.01s
Presolve: All rows and columns removed
Explored 0 nodes (0 simplex iterations) in 0.02 seconds
Thread count was 1 (of 4 available processors)
Solution count 1: 10
Optimal solution found (tolerance 1.00e-04)
Best objective 1.000000000000e+01, best bound 1.00000000000e+01, gap 0.0000%
s[0]: 0.0
s[1]: 3.0
s[2]: 5.0
s[3]: 5.0
s[4]: 9.0
s[5]: 3.0
e[0]: 3.0
e[1]: 5.0
e[2]: 8.0
e[3]: 9.0
e[4]: 10.0
e[5]: 5.0
C12: 10.0
Objective value: 10.0
B Started: 0.0
B Ended: 3.0
F Started: 3.0
F Ended: 5.0
E Started: 5.0
E Ended: 8.0
P Started: 5.0
P Ended: 9.0
D Started: 9.0
D Ended: 10.0
L Started: 3.0
L Ended: 5.0
```

(base) lawn-128-61-55-191:~ connerreinhardt\$

Adv. Optimization HW #1

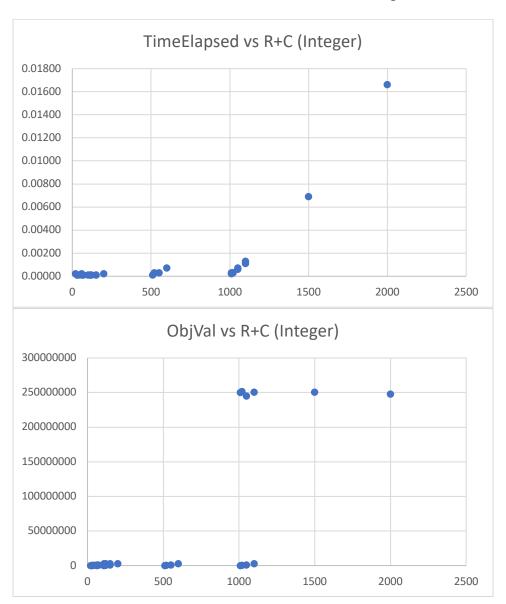
Problem 4 Code

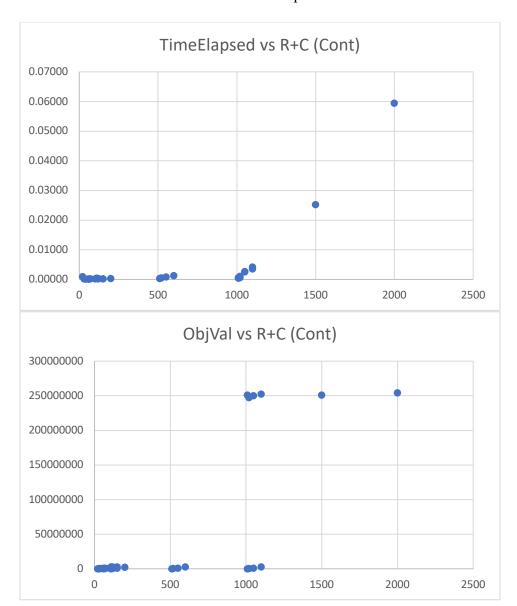
```
from gurobipy import *
import numpy as np
#X: 0 1 2 3 4 5 6
M = [10, 20, 50, 100, 500, 1000] #removed entries for simplicity
#Y: 0 1 2 3
N = [10, 20, 50, 100, 1000] #removed entries for simplicity
total_time_elapsed = 0.0
times_elapsed = []
objVals = []
matrix\_array = [np.random.rand(M[x],N[y]) for x in range(0,len(M)) for y in
range(0,len(N))]
times_elapsed_avg_dict = {}
times_elapsed_dict = {}
objVals avg dict = {}
objVals_dict = {}
for r in range(0,len(M)*len(N)):
    for c in range(0,5): #changed from 10-> 5 to run fast
       matrix = matrix_array[r]
       X = list(range(len(matrix[0]))) #full MxN matrix
       B = np.random.rand(len(matrix),1)*1000
       C = np.random.rand(len(matrix[0]),1)*1000 #cost matrix
       itnM = len(matrix)
       itnN = len(matrix[0])
       print("")
       print("M : " + str(itnM))
       print("N : " + str(itnN))
       print("")
       print(str(len(matrix)) + "x" + str(len(matrix[0])) + " iteration " + str(c+1))
       m = Model("Pr4")
       x = m.addVars(X, vtype=GRB.CONTINUOUS, name = "x")
       m.addConstrs(quicksum(matrix[r][c]*x[c] for c in range(len(matrix[0]))) >=
B[r] for r in range(len(matrix)))
```

```
m.setObjective(quicksum(X[c] * C[c] for c in range(len(matrix[0]))),
GRB.MINIMIZE)
        m.optimize()
        states =
{1:'LOADED',2:'OPTIMAL',3:'INFEASIBLE',4:'INF_OR_UNBD',5:'UNBOUNDED',6:'CUTOFF',7:'ITE
RATION_LIMIT',8:'NODE_LIMIT',9:'TIME_LIMIT',10:'SOLUTION_LIMIT',11:'INTERRUPTED',12:'N
UMERIC',13:'SUBOPTIMAL',14:'INPROGRESS',15:'USER_OBJ_LIMIT'}
        state = m.status
        total_time_elapsed += m.RunTime
        times_elapsed.append(m.RunTime)
        objVals.append(m.objVal)
        if c == 9: #after 10 iterations
            times_elapsed_avg_dict["Avg Time Elapsed " + str(itnM) + "x" + str(itnN)]
= (str(round((total_time_elapsed/20),4)) + " sec")
            times_elapsed_dict["Time Elapsed " + str(itnM) + "x" + str(itnN)] =
times_elapsed
            objVals_avg_dict["Avg Obj Vals " + str(itnM) + "x" + str(itnN)] =
np.mean(objVals)
            objVals_dict["Obj Vals " + str(itnM) + "x" + str(itnN)] = objVals
            total_time_elapsed = 0.0
            times_elapsed = []
            objVals = []
print(times_elapsed_avg_dict)
print(objVals_avg_dict)
print("\n\n\n")
print(times_elapsed_dict)
print(objVals_dict)
```

Adv. Optimization HW #1

Problem 4 Results Output



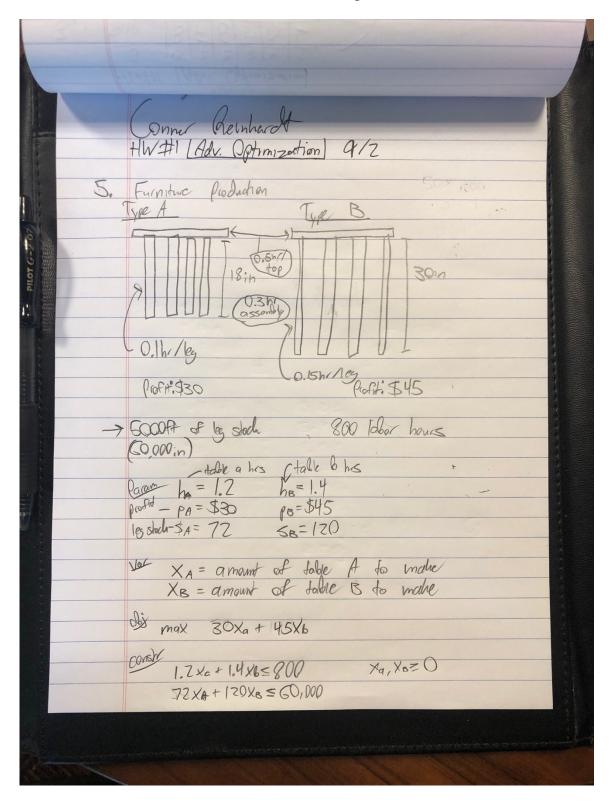


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R+C	TimeElapsedInteger	ObjValInteger	TimeElapsedCont	ObjValCont
20	0.00020	19130.65301	0.00090	16947.5095
30	0.00010	100177.484	0.00020	97319.4993
60	0.00020	594420.8247	0.00020	609696.816
110	0.00010	2459155.626	0.00040	2447240.93
1010	0.00030	250011430.9	0.00040	250943664
30	0.00010	26070.8719	0.00020	20212.5073
40	0.00010	100984.7585	0.00010	81400.8732
70	0.00010	614841.6963	0.00020	603429.927
120	0.00010	2374668.267	0.00030	2452462.34
1020	0.00030	251480838.8	0.00060	247288484
60	0.00010	20783.21142	0.00010	20270.1772
70	0.00010	93020.0766	0.00020	104106.782
100	0.00010	633781.3294	0.00020	620541.01
150	0.00010	2485494.245	0.00020	2519222.97
1050	0.00060	245036272.7	0.00260	249768366
110	0.00010	25229.46292	0.00030	18749.6161
120	0.00010	86901.41445	0.00020	97888.8527
150	0.00010	632228.4174	0.00020	607450.129
200	0.00020	2556493.744	0.00030	2354128.92
1100	0.00110	250259564.3	0.00420	252452799
510	0.00010	25371.81362	0.00030	24422.43
520	0.00030	98470.0105	0.00050	98449.9862
550	0.00030	627874.7089	0.00080	584015.574
600	0.00070	2554302.244	0.00120	2421317.3
1500	0.00690	250611174.9	0.02520	250834764
1010	0.00020	26437.97634	0.00060	24688.2605
1020	0.00030	84974.4461	0.00100	98718.8959
1050	0.00070	624568.5946	0.00250	611778.516
1100	0.00130	2538445.521	0.00350	2476213.14
2000	0.01660	247762271.1	0.05940	253938003

Adv. Optimization HW #1

Problem 5 Setup



Adv. Optimization HW #1

Problem 5 Code

```
Created on Mon Aug 26 17:16:49 2019
@author: connerreinhardt
from gurobipy import *
m = Model("Pr5")
#--Vars
xa = m.addVar(vtype=GRB.CONTINUOUS, name="xa") #amount of table A to make
xb = m.addVar(vtype=GRB.CONTINUOUS, name="xb") #amount of table B to make
#--Objective
m.setObjective(30*xa + 45*xb, GRB.MAXIMIZE)
#--Constr
m.addConstr(1.2*xa+1.4*xb<=800) #hours to create table</pre>
m.addConstr(72*xa+120*xb<=60000) #inches of legs available
m.addConstr(xa>=0)
m.addConstr(xb>=0)
m.optimize()
print("\n************Results***********\n")
for v in m.getVars():
    print(v.varName + ":", v.X)
print("\n0bjective value: " + str(m.objVal) + "\n")
```

Adv. Optimization HW #1

Problem 5 Output

lawn-128-61-55-191:~ connerreinhardt\$ source /Users/connerreinhardt/miniconda3/bin/activate (base) lawn-128-61-55-191:~ connerreinhardt\$ conda activate base (base) lawn-128-61-55-191:~ connerreinhardt\$ /Users/connerreinhardt/miniconda3/bin/python "/Users/connerreinhardt/Google Drive/Advanced Optimization/HW1/#5.py"

Warning: your license will expire in 2 days

Academic license - for non-commercial use only
Optimize a model with 4 rows, 2 columns and 6 nonzeros
Coefficient statistics:

Matrix range [1e+00, 1e+02]
Objective range [3e+01, 4e+01]
Bounds range [0e+00, 0e+00]
RHS range [8e+02, 6e+04]
Presolve removed 2 rows and 0 columns

Presolve time: 0.00s

Presolved: 2 rows, 2 columns, 4 nonzeros

Iteration Objective Primal Inf. Dual Inf. Time
0 2.5714286e+04 2.048561e+02 0.000000e+00 0s
2 2.3333333e+04 0.000000e+00 0.000000e+00 0s

Solved in 2 iterations and 0.00 seconds Optimal objective 2.33333333e+04

*************Results********

xa: 277.7777777778 xb: 333.33333333333333

Objective value: 23333.333333333336

(base) lawn-128-61-55-191:~ connerreinhardt\$