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Knowledge representation : ( Markov logic networks )

A set of first-order logic rules can be represented as a Markov logic network

$$f_1: A \wedge B \Rightarrow Y \quad \Leftrightarrow \neg A \vee \neg B \vee Y$$

Predicate set  $X = (X_1, X_2, \dots, X_n) \in \mathcal{X}$

Energy-based model : ( Markov logic Networks )

$$P(X=x) = \frac{1}{Z} \exp \left\{ \sum_{f \in |F|} w_f f_f(x) \right\}$$

where  $f_f(x)$  is logic-informed feature.

(KDD) - draft

$K = (C, \mathcal{X}, D)$   
(knowledge base)       $\downarrow$  entity       $\downarrow$  relation       $\downarrow$  facts

(ICML 2024)

$C = \{c_1, c_2, \dots, c_n\}$ . entity set

( in our case. we can only consider one entity. i.e. focus on individual patient )

Consider a set of  $N$  predicates ( properties or relations )

( e.g. measurements, Treatments, ... )

$X = \{x_1, \dots, x_N\}$

$X(\cdot) : C \rightarrow \{0, 1\}$  logic variable

each grounded predicate  $\equiv$  a binary random variable  
by data

$O = \{o_1, \dots, o_L\}$ , where each observation is a true value  $\{0, 1\}$ .  
assigned to a grounded predicate.

Knowledge base  $F = \{f_1, \dots, f_K\}$

$f() :$   $\in \{0, 1\}$ . logic formula.

$f() :$   $A \wedge B \Rightarrow Y$  (Horn rule)

$A(c) \wedge B(c) \Rightarrow Y(c)$  if-then  
 $\Rightarrow$   $\downarrow$   $\downarrow$   $\downarrow$

Given De Morgan's law.

a disjunctive form



$$f() : \neg A(c) \vee \neg B(c) \vee Y(c)$$

General form :

$$f_x = \left( \bigvee_{x \in X^+} x \right) \vee \left( \bigvee_{x \in X^-} \neg x \right) \quad \star$$

Given Markov logic networks

Any  $f_i$  can be evaluated by  $\star$ .

$$P(X=x) = \frac{1}{Z} \exp \left( \sum_{j \in |F|} w_j \underbrace{f_j(x_{\{j\}})} \right)$$

$\uparrow$



For an AI algorithm (no information processing limit)

↓ if  $|D|x|$  (symptoms part) is fully observed. Reasoning only requires one-step.

For a real human, however, her

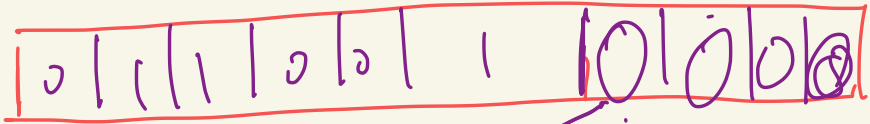
↓ information processing ability is limited.

A snapshot can only focus on some segments of information.

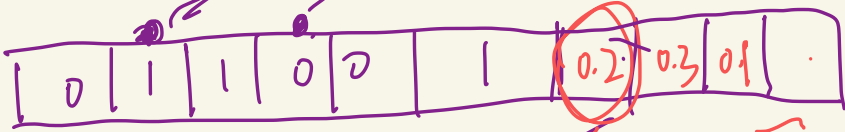
forward reasoning  
↑

200

$0^3_{|x|}$



$0^2_{|x|}$



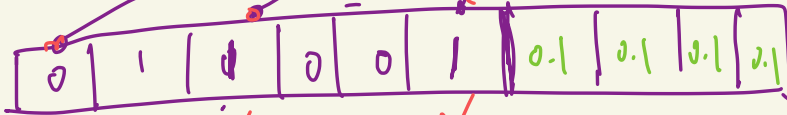
reasoning

query  
↑

apply attention mask

rule

$0^1_{|x|}$

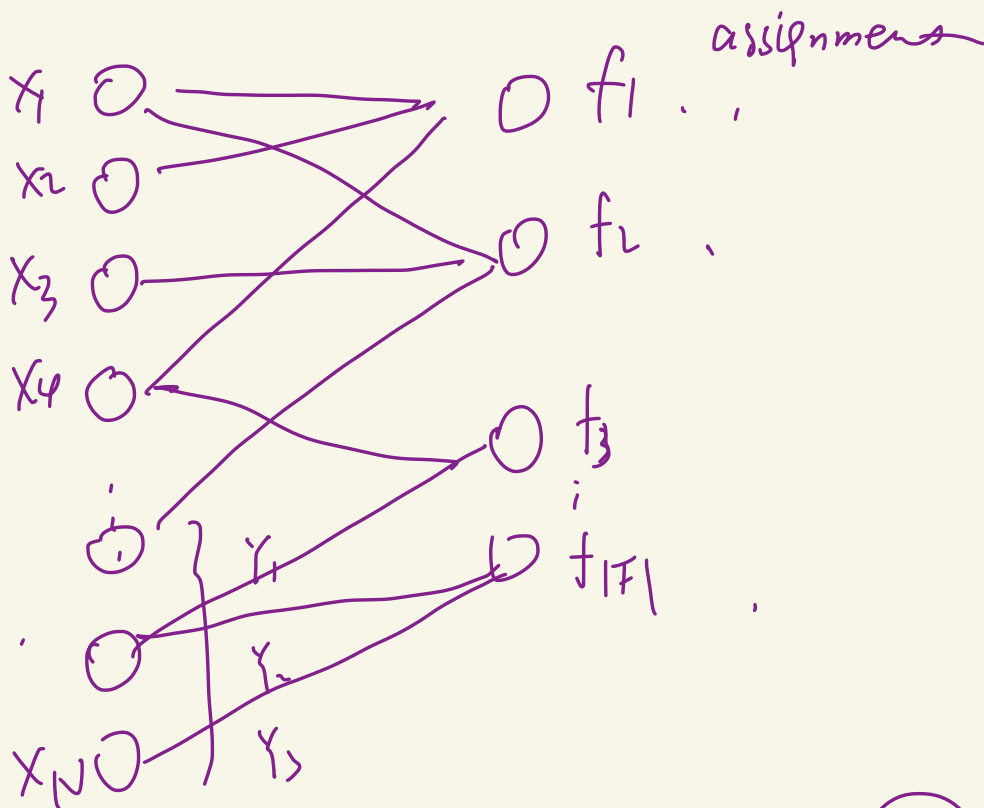


random initialization

attention is used to select information  
from all the observations

Modelling : ① how to compute the  
current reasoning results  
given information in the  
memory . ( increasing )

( ICML 2024 paper results )



rw



Forward reasoning : ( ICLR : KB )  
chaining ( always from evidence  
to goals ) ✓

Given  $\{ X_1, X_3, X_5 \}$  in the memory.

trigger  $\{ f_1, f_2, f_4, f_6 \}$  ✓  
( determine neighborhood )