

### **Title**

rdbwdensity — Bandwidth Selection for Manipulation Testing Using Local Polynomial Density Estimation.

#### Syntax

### **Description**

- rdbwdensity implements several data-driven bandwidth selection methods useful to
   construct manipulation testing procedures using the local polynomial density
   estimators proposed in <u>Cattaneo, Jansson and Ma (2020)</u>.
- A detailed introduction to this Stata command is given in <u>Cattaneo</u>, <u>Jansson and Ma (2018)</u>.

  Companion <u>R</u> functions are also available <u>here</u>.
- Companion function is  $\underline{rddensity}$ . See also the  $\underline{lpdensity}$  package for other related bandwidth selection methods.
- Related Stata and R packages useful for inference in regression discontinuity (RD) designs are described in the following website:

https://rdpackages.github.io/

Local Sample Size Checking

#### Options

```
Bandwidth Selection
\mathbf{c} (#) specifies the threshold or cutoff value in the support of Var, which
    determines the two samples (e.g., control and treatment units in RD settings).
    Default is c(0).
p(#) specifies the local polynomial order used to construct the density
    estimators. Default is \mathbf{p}(2) (local quadratic approximation).
<u>fit</u>select (FitMethod) specifies the density estimation method.
    unrestricted for density estimation without any restrictions (two-sample,
        unrestricted inference). This is the default option.
    restricted for density estimation assuming equal distribution function and
        higher-order derivatives.
kernel (KernelFn) specifies the kernel function used to construct the local
    polynomial estimators.
    triangular K(u) = (1 - |u|) * (|u| \le 1). This is the default option.
    epanechnikov K(u) = 0.75 * (1 - u^2) * (|u| <= 1).
                 K(u) = 0.5 * (|u| <= 1).
    uniform
vce(VceMethod) specifies the procedure used to compute the variance-covariance
    matrix estimator.
              for asymptotic plug-in standard errors.
    jackknife for jackknife standard errors. This is the default option.
nomasspoints will not adjust for mass points in the data.
```

nlocalmin(#) specifies the minimum number of observations in each local
 neighborhood. This option will be ignored if set to 0, or if noregularize is
 used. The default value is 20+p(#)+1.

nuniquemin(#) specifies the minimum number of unique observations in each local
neighborhood. This option will be ignored if set to 0, or if noregularize is
used. The default value is 20+p(#)+1.

noregularize suppresses the local sample size checking feature.

### Example: Cattaneo, Frandsen and Titiunik (2015) Incumbency Data.

```
Load dataset (cutoff is 0 in this dataset):
    . use rddensity_senate.dta
```

Bandwidth selection for manipulation test using default options:

. rdbwdensity margin

Bandwidth selection for manipulation test using plug-in standard errors:

. rdbwdensity margin, vce(plugin)

# Saved results

rddensity saves the following in e():

```
Macros
                        cutoff value
  e(c)
  e (p)
                       order of the polynomial used for density estimation
                      sample size to the left of the cutoff sample size to the right of the cutoff
  e(N_1)
  e(N_r)
                      matrix of estimated bandwidth (including underlying
  e (h)
                        estimated constants)
  e(runningvar)
                      running variable used
                    kernel used
  e(kernel)
  e(fitmethod)
                      model used
  e (vce)
                       standard errors estimator used
```

#### References

- Cattaneo, M. D., B. Frandsen, and R. Titiunik. 2015. Randomization Inference in the Regression Discontinuity Design: An Application to the Study of Party Advantages in the U.S. Senate.

  Journal of Causal Inference 3(1): 1-24.
- Cattaneo, M. D., M. Jansson, and X. Ma. 2018. <u>Manipulation Testing based on Density Discontinuity</u>.

  Stata Journal 18(1): 234-261.
- Cattaneo, M. D., M. Jansson, and X. Ma. 2020. <u>Simple Local Polynomial Density Estimators</u>.

  Journal of the American Statistical Association 115(531): 1449-1455.

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