

# Package ‘rddensity’

March 3, 2021

**Type** Package

**Title** Manipulation Testing Based on Density Discontinuity

**Description** Density discontinuity testing (a.k.a. manipulation testing) is commonly employed in regression discontinuity designs and other program evaluation settings to detect perfect self-selection (manipulation) around a cutoff where treatment/policy assignment changes. This package implements manipulation testing procedures using the local polynomial density estimators: `rddensity()` to construct test statistics and p-values given a prespecified cutoff, `rdbwdensity()` to perform data-driven bandwidth selection, and `rdplotdensity()` to construct density plots.

**Version** 2.2

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**Imports** ggplot2, lpdensity (>= 2.2)

**Depends** R (>= 3.1.0)

**License** GPL-2

**Encoding** UTF-8

**RoxygenNote** 7.1.1

## R topics documented:

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## Description

Density discontinuity testing (a.k.a. manipulation testing) is commonly employed in regression discontinuity designs and other program evaluation settings to detect perfect self-selection (manipulation) around a cutoff where treatment/policy assignment changes.

This package implements manipulation testing procedures using the local polynomial density estimators proposed in Cattaneo, Jansson and Ma (2020), and implements graphical procedures with valid confidence bands using the results in Cattaneo, Jansson and Ma (2021a,b). In addition, this package provides complementary manipulation testing based on finite sample exact binomial testing following the results in Cattaneo, Frandsen and Titiunik (2015) and Cattaneo, Frandsen and Vazquez-Bare (2017).

A companion Stata package is described in Cattaneo, Jansson and Ma (2018).

Commands: `rddensity` for manipulation (density discontinuity) testing. `rdbwdensity` for data-driven bandwidth selection, and `rdplottedensity` for density plots.

Related Stata and R packages useful for inference in regression discontinuity (RD) designs are described in the website: <https://rdpackages.github.io/>.

## Author(s)

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## References

- Calonico, S., M. D. Cattaneo, and M. H. Farrell. 2018. **On the Effect of Bias Estimation on Coverage Accuracy in Nonparametric Inference**. *Journal of the American Statistical Association* 113(522): 767-779.
- Calonico, S., M. D. Cattaneo, and M. H. Farrell. 2020. **Coverage Error Optimal Confidence Intervals for Local Polynomial Regression**. Working paper.
- Cattaneo, M. D., B. Frandsen, and R. Titiunik. 2015. **Randomization Inference in the Regression Discontinuity Design: An Application to the Study of Party Advantages in the U.S. Senate**. *Journal of Causal Inference* 3(1): 1-24.
- Cattaneo, M. D., M. Jansson, and X. Ma. 2018. **Manipulation Testing based on Density Discontinuity**. *Stata Journal* 18(1): 234-261.
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- Cattaneo, M. D., R. Titiunik and G. Vazquez-Bare. 2017. **Comparing Inference Approaches for RD Designs: A Reexamination of the Effect of Head Start on Child Mortality**. *Journal of Policy Analysis and Management* 36(3): 643-681.
- McCrary, J. 2008. Manipulation of the Running Variable in the Regression Discontinuity Design: A Density Test. *Journal of Econometrics* 142(2): 698-714. doi: [10.1016/j.jeconom.2007.05.005](https://doi.org/10.1016/j.jeconom.2007.05.005)

## Description

rdbwdensity implements several data-driven bandwidth selection methods useful to construct manipulation testing procedures using the local polynomial density estimators proposed in Cattaneo, Jansson and Ma (2020).

A companion Stata package is described in Cattaneo, Jansson and Ma (2018).

Companion command: `rddensity` for manipulation (density discontinuity) testing.

Related Stata and R packages useful for inference in regression discontinuity (RD) designs are described in the website: <https://rdpackages.github.io/>.

## Usage

```
rdbwdensity(
  X,
  c = 0,
  p = 2,
  fitselect = "",
  kernel = "",
  vce = "",
  massPoints = TRUE,
  regularize = TRUE,
  nLocalMin = NULL,
  nUniqueMin = NULL
)
```

## Arguments

<code>X</code>	Numeric vector or one dimensional matrix/data frame, the running variable.
<code>c</code>	Numeric, specifies the threshold or cutoff value in the support of <code>X</code> , which determines the two samples (e.g., control and treatment units in RD settings). Default is 0.
<code>p</code>	Nonnegative integer, specifies the local polynomial order used to construct the density estimators. Default is 2 (local quadratic approximation).
<code>fitselect</code>	String, specifies the density estimation method. "unrestricted" for density estimation without any restrictions (two-sample, unrestricted inference). This is the default option. "restricted" for density estimation assuming equal distribution function and higher-order derivatives.
<code>kernel</code>	String, specifies the kernel function used to construct the local polynomial estimators. "triangular": $K(u) = (1 -  u ) * ( u  \leq 1)$ . This is the default option. "epanechnikov": $K(u) = 0.75 * (1 - u^2) * ( u  \leq 1)$ . "uniform": $K(u) = 0.5 * ( u  \leq 1)$ .
<code>vce</code>	String, specifies the procedure used to compute the variance-covariance matrix estimator. "plugin" for asymptotic plug-in standard errors. "jackknife" for jackknife standard errors. This is the default option.
<code>massPoints</code>	TRUE (default) or FALSE, specifies whether to adjust for mass points in the data.

regularize	TRUE (default) or FALSE, specifies whether to conduct local sample size checking. When set to TRUE, the bandwidth is chosen such that the local region includes at least nLocalMin observations and at least nUniqueMin unique observations.
nLocalMin	Nonnegative integer, specifies the minimum number of observations in each local neighborhood. This option will be ignored if set to 0, or if regularize=FALSE is used. Default is $20+p+1$ .
nUniqueMin	Nonnegative integer, specifies the minimum number of unique observations in each local neighborhood. This option will be ignored if set to 0, or if regularize=FALSE is used. Default is $20+p+1$ .

### Value

h	Bandwidths for density discontinuity test, left and right to the cutoff, and asymptotic variance and bias.
N	full: full sample size; left/right: sample size to the left/right of the cutoff.
opt	Options passed to the function.
X_min	Smallest observations to the left and right of the cutoff.
X_max	Largest observations to the left and right of the cutoff.

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### References

Cattaneo, M. D., M. Jansson, and X. Ma. 2018. **Manipulation Testing based on Density Discontinuity**. *Stata Journal* 18(1): 234-261.

Cattaneo, M. D., M. Jansson, and X. Ma. 2020. **Simple Local Polynomial Density Estimators**. *Journal of the American Statistical Association*, 115(531): 1449-1455.

### See Also

[rddensity](#)

### Examples

```
# Generate a random sample
set.seed(42)
x <- rnorm(2000, mean = -0.5)

# Bandwidth selection
summary(rdbwdensity(X = x, vce="jackknife"))
```

## Description

rddensity implements manipulation testing procedures using the local polynomial density estimators proposed in Cattaneo, Jansson and Ma (2020), and implements graphical procedures with valid confidence bands using the results in Cattaneo, Jansson and Ma (2021a,b). In addition, the command provides complementary manipulation testing based on finite sample exact binomial testing following the results in Cattaneo, Frandsen and Titiunik (2015) and Cattaneo, Frandsen and Vazquez-Bare (2017). For an introduction to manipulation testing see McCrary (2008).

A companion Stata package is described in Cattaneo, Jansson and Ma (2018).

Companion commands: `rdbwdensity` for data-driven bandwidth selection, and `rdplotdensity` for density plots.

Related Stata and R packages useful for inference in regression discontinuity (RD) designs are described in the website: <https://rdpackages.github.io/>.

## Usage

```
rddensity(
  X,
  c = 0,
  p = 2,
  q = 0,
  fitselect = "",
  kernel = "",
  vce = "",
  massPoints = TRUE,
  h = c(),
  bwselect = "",
  all = FALSE,
  regularize = TRUE,
  nLocalMin = NULL,
  nUniqueMin = NULL,
  bino = TRUE,
  binoW = NULL,
  binoN = NULL,
  binoWStep = NULL,
  binoNStep = NULL,
  binoNW = 10,
  binoP = 0.5
)
```

## Arguments

- |   |  |
|---|--|
| X | Numeric vector or one dimensional matrix/data frame, the running variable.   |
| c | Numeric, specifies the threshold or cutoff value in the support of X, which determines the two samples (e.g., control and treatment units in RD settings). Default is 0. |

p	Nonnegative integer, specifies the local polynomial order used to construct the density estimators. Default is 2 (local quadratic approximation).
q	Nonnegative integer, specifies the local polynomial order used to construct the bias-corrected density estimators. Default is p+1 (local cubic approximation for default p=2).
fitselect	String, specifies the density estimation method. "unrestricted" for density estimation without any restrictions (two-sample, unrestricted inference). This is the default option. "restricted" for density estimation assuming equal distribution function and higher-order derivatives.
kernel	String, specifies the kernel function used to construct the local polynomial estimators. "triangular": $K(u) = (1 -  u ) * ( u  \leq 1)$ . This is the default option. "epanechnikov": $K(u) = 0.75 * (1 - u^2) * ( u  \leq 1)$ . "uniform": $K(u) = 0.5 * ( u  \leq 1)$ .
vce	String, specifies the procedure used to compute the variance-covariance matrix estimator. "plugin" for asymptotic plug-in standard errors. "jackknife" for jackknife standard errors. This is the default option.
massPoints	TRUE (default) or FALSE, specifies whether to adjust for mass points in the data.
h	Numeric, specifies the bandwidth used to construct the density estimators on the two sides of the cutoff. If not specified, the bandwidth h is computed by the companion command <a href="#">rdbwdensity</a> . If two bandwidths are specified, the first bandwidth is used for the data below the cutoff and the second bandwidth is used for the data above the cutoff.
bwselect	String, specifies the bandwidth selection procedure to be used. "each" based on MSE of each density estimator separately (two distinct bandwidths, h1 and hr). "diff" based on MSE of difference of two density estimators (one common bandwidth, h1=hr). "sum" based on MSE of sum of two density estimators (one common bandwidth, h1=hr). "comb" bandwidth is selected as a combination of the alternatives above. This is the default option. For fitselect="unrestricted", it selects median(each,diff,sum). For fitselect = "restricted", it selects min(diff,sum).
all	TRUE or FALSE (default), if specified, will report two testing procedures: conventional test statistic (not valid when using MSE-optimal bandwidth choice) and robust bias-corrected statistic.
regularize	TRUE (default) or FALSE, specifies whether to conduct local sample size checking. When set to TRUE, the bandwidth is chosen such that the local region includes at least nLocalMin observations and at least nUniqueMin unique observations.
nLocalMin	Nonnegative integer, specifies the minimum number of observations in each local neighborhood. This option will be ignored if set to 0, or if regularize=FALSE is used. Default is $20 + p + 1$ .
nUniqueMin	Nonnegative integer, specifies the minimum number of unique observations in each local neighborhood. This option will be ignored if set to 0, or if regularize=FALSE is used. Default is $20 + p + 1$ .
bino	TRUE (default) or FALSE, specifies whether to conduct binomial tests. By default, the initial (smallest) window contains 20 observations, and its length is also used as the increment for subsequent windows. This feature is based on the <a href="#">binom.test</a> function.
binoW	Numeric, specifies the half length(s) of the initial window. If two values are provided, they will be used for the data below and above the cutoff separately.

binon	Nonnegative integer, specifies the number of observations (closest to the cutoff) used for the binomial test. This option will be ignored if binow is provided.
binowStep	Numeric, specifies the increment in half length(s).
binonStep	Nonnegative integer, specifies the increment in sample size. This option will be ignored if binowStep is provided.
binonW	Nonnegative integer, specifies the total number of windows. Default is 10.
binonP	Numeric, specifies the null hypothesis of the binomial test. Default is 0.5.

**Value**

hat	left/right: density estimate to the left/right of cutoff; diff: difference in estimated densities on the two sides of cutoff.
sd_asy	left/right: standard error for the estimated density to the left/right of the cutoff; diff: standard error for the difference in estimated densities. (Based on asymptotic formula.)
sd_jk	left/right: standard error for the estimated density to the left/right of the cutoff; diff: standard error for the difference in estimated densities. (Based on the jackknife method.)
test	t_asy/t_jk: t-statistic for the density discontinuity test, with standard error based on asymptotic formula or the jackknife; p_asy/p_jk: p-value for the density discontinuity test, with standard error based on asymptotic formula or the jackknife.
hat_p	Same as hat, without bias correction (only available when all=TRUE).
sd_asy_p	Same as sd_asy, without bias correction (only available when all=TRUE).
sd_jk_p	Same as sd_jk, without bias correction (only available when all=TRUE).
test_p	Same as test, without bias correction (only available when all=TRUE).
N	full: full sample size; left/right: sample size to the left/right of the cutoff; eff_left/eff_right: effective sample size to the left/right of the cutoff (this depends on the bandwidth).
h	left/right: bandwidth used to the left/right of the cutoff.
opt	Options passed to the function.
binon	Binomial test results. leftWindow/rightWindow: window lengths. leftN/rightN: number of observations. pval: p-values.
X_min	left/right: the smallest observation to the left/right of the cutoff.
X_max	left/right: the largest observation to the left/right of the cutoff.

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## References

- Cattaneo, M. D., B. Frandsen, and R. Titiunik. 2015. **Randomization Inference in the Regression Discontinuity Design: An Application to the Study of Party Advantages in the U.S. Senate.** *Journal of Causal Inference* 3(1): 1-24.
- Cattaneo, M. D., M. Jansson, and X. Ma. 2018. **Manipulation Testing based on Density Discontinuity.** *Stata Journal* 18(1): 234-261.
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- Cattaneo, M. D., M. Jansson, and X. Ma. 2021b. **lpdensity: Local Polynomial Density Estimation and Inference.** *Journal of Statistical Software*, forthcoming.
- Cattaneo, M. D., R. Titiunik and G. Vazquez-Bare. 2017. **Comparing Inference Approaches for RD Designs: A Reexamination of the Effect of Head Start on Child Mortality.** *Journal of Policy Analysis and Management* 36(3): 643-681.
- McCrary, J. 2008. Manipulation of the Running Variable in the Regression Discontinuity Design: A Density Test. *Journal of Econometrics* 142(2): 698-714. doi: [10.1016/j.jeconom.2007.05.005](https://doi.org/10.1016/j.jeconom.2007.05.005)

## See Also

[rdbwdensity](#), [rdplotdensity](#)

## Examples

```
### Continuous Density
set.seed(42)
x <- rnorm(2000, mean = -0.5)
rdd <- rddensity(X = x, vce = "jackknife")
summary(rdd)

### Bandwidth selection using rdbwdensity()
rddbwd <- rdbwdensity(X = x, vce = "jackknife")
summary(rddbwd)

### Plotting using rdplotdensity()
# 1. From -2 to 2 with 25 evaluation points at each side
plot1 <- rdplotdensity(rdd, x, plotRange = c(-2, 2), plotN = 25)

# 2. Plotting a uniform confidence band
set.seed(42) # fix the seed for simulating critical values
plot2 <- rdplotdensity(rdd, x, plotRange = c(-2, 2), plotN = 25, CIuniform = TRUE)

### Density discontinuity at 0
x[x > 0] <- x[x > 0] * 2
rdd2 <- rddensity(X = x, vce = "jackknife")
summary(rdd2)
plot3 <- rdplotdensity(rdd2, x, plotRange = c(-2, 2), plotN = 25)
```



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rddensity_senate	<i>RD Senate Data</i>
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### Description

Extract of the dataset constructed by Cattaneo, Frandsen, and Titiunik (2015), which include measures of incumbency advantage in the U.S. Senate for the period 1914-2010.

### Format

Numeric vector containing 1390 observations:

**margin** Numeric vector. See Cattaneo, Frandsen and Titiunik (2015) regarding details about this dataset.

### Source

Cattaneo, M. D., B. Frandsen, and R. Titiunik. (2015). **Randomization Inference in the Regression Discontinuity Design: An Application to the Study of Party Advantages in the U.S. Senate**. *Journal of Causal Inference* 3(1): 1-24.

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rdplotdensity	<i>Density Plotting for Manipulation Testing</i>
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### Description

rdplotdensity constructs density plots. It is based on the local polynomial density estimator proposed in Cattaneo, Jansson and Ma (2020, 2021a). A companion Stata package is described in Cattaneo, Jansson and Ma (2018).

Companion command: **rddensity** for manipulation (density discontinuity) testing.

Related Stata and R packages useful for inference in regression discontinuity (RD) designs are described in the website: <https://rdpackages.github.io/>.

### Usage

```
rdplotdensity(
  rdd,
  X,
  plotRange = NULL,
  plotN = 10,
  plotGrid = c("es", "qs"),
  alpha = 0.05,
  type = NULL,
  lty = NULL,
  lwd = NULL,
  lcol = NULL,
  pty = NULL,
  pwd = NULL,
  pcol = NULL,
```

```

CItpe = NULL,
CIuniform = FALSE,
CIsimul = 2000,
Cishade = NULL,
Cicol = NULL,
bwselect = NULL,
hist = TRUE,
histBreaks = NULL,
histFillCol = 3,
histFillShade = 0.2,
histLineCol = "white",
title = "",
xlabel = "",
ylabel = "",
legendTitle = NULL,
legendGroups = NULL
)

```

### Arguments

rdd	Object returned by <a href="#">rddensity</a>
x	Numeric vector or one dimensional matrix/data frame, the running variable.
plotRange	Numeric, specifies the lower and upper bound of the plotting region. Default is <code>[c-3*hl, c+3*hr]</code> (three bandwidths around the cutoff).
plotN	Numeric, specifies the number of grid points used for plotting on the two sides of the cutoff. Default is <code>c(10, 10)</code> (i.e., 10 points are used on each side).
plotGrid	String, specifies how the grid points are positioned. Options are <code>es</code> (evenly spaced) and <code>qs</code> (quantile spaced).
alpha	Numeric scalar between 0 and 1, the significance level for plotting confidence regions. If more than one is provided, they will be applied to the two sides accordingly.
type	String, one of <code>"line"</code> (default), <code>"points"</code> or <code>"both"</code> , how the point estimates are plotted. If more than one is provided, they will be applied to the two sides accordingly.
lty	Line type for point estimates, only effective if type is <code>"line"</code> or <code>"both"</code> . 1 for solid line, 2 for dashed line, 3 for dotted line. For other options, see the instructions for <a href="#">ggplot2</a> or <a href="#">par</a> . If more than one is provided, they will be applied to the two sides accordingly.
lwd	Line width for point estimates, only effective if type is <code>"line"</code> or <code>"both"</code> . Should be strictly positive. For other options, see the instructions for <a href="#">ggplot2</a> or <a href="#">par</a> . If more than one is provided, they will be applied to the two sides accordingly.
lcol	Line color for point estimates, only effective if type is <code>"line"</code> or <code>"both"</code> . 1 for black, 2 for red, 3 for green, 4 for blue. For other options, see the instructions for <a href="#">ggplot2</a> or <a href="#">par</a> . If more than one is provided, they will be applied to the two sides accordingly.
pty	Scatter plot type for point estimates, only effective if type is <code>"points"</code> or <code>"both"</code> . For options, see the instructions for <a href="#">ggplot2</a> or <a href="#">par</a> . If more than one is provided, they will be applied to the two sides accordingly.

pwd	Scatter plot size for point estimates, only effective if type is "points" or "both". Should be strictly positive. If more than one is provided, they will be applied to the two sides accordingly.
pcol	Scatter plot color for point estimates, only effective if type is "points" or "both". 1 for black, 2 for red, 3 for green, 4 for blue. For other options, see the instructions for <a href="#">ggplot2</a> or <a href="#">par</a> . If more than one is provided, they will be applied to the two sides accordingly.
CIttype	String, one of "region" (shaded region, default), "line" (dashed lines), "ebar" (error bars), "all" (all of the previous) or "none" (no confidence region), how the confidence region should be plotted. If more than one is provided, they will be applied to the two sides accordingly.
CIuniform	TRUE or FALSE (default), plotting either pointwise confidence intervals (FALSE) or uniform confidence bands (TRUE).
CIsimul	Positive integer, the number of simulations used to construct critical values (default is 2000). This option is ignored if CIuniform=FALSE.
Cishade	Numeric, opaqueness of the confidence region, should be between 0 (transparent) and 1. Default is 0.2. If more than one is provided, they will be applied to the two sides accordingly.
CIcol	Color of the confidence region. 1 for black, 2 for red, 3 for green, 4 for blue. For other options, see the instructions for <a href="#">ggplot2</a> or <a href="#">par</a> . If more than one is provided, they will be applied to the two sides accordingly.
bwselect	String, the method for data-driven bandwidth selection. Available options are (1) "mse-dpi" (mean squared error-optimal bandwidth selected for each grid point); (2) "imse-dpi" (integrated MSE-optimal bandwidth, common for all grid points); (3) "mse-rot" (rule-of-thumb bandwidth with Gaussian reference model); and (4) "imse-rot" (integrated rule-of-thumb bandwidth with Gaussian reference model). If omitted, bandwidths returned by rddensity will be used.
hist	TRUE (default) or FALSE, whether adding a histogram to the background.
histBreaks	Numeric vector, giving the breakpoints between histogram cells.
histFillCol	Color of the histogram cells.
histFillShade	Opaqueness of the histogram cells, should be between 0 (transparent) and 1. Default is 0.2.
histLineCol	Color of the histogram lines.
title, xlabel, ylabel	Strings, title of the plot and labels for x- and y-axis.
legendTitle	String, title of legend.
legendGroups	String Vector, group names used in legend.

## Details

Bias correction is only used for the construction of confidence intervals/bands, but not for point estimation. The point estimates, denoted by  $f_p$ , are constructed using local polynomial estimates of order  $p$ , while the centering of the confidence intervals/bands, denoted by  $f_q$ , are constructed using local polynomial estimates of order  $q$ . The confidence intervals/bands take the form:  $[f_q - cv * SE(f_q), f_q + cv * SE(f_q)]$ , where  $cv$  denotes the appropriate critical value and  $SE(f_q)$  denotes a standard error estimate for the centering of the confidence interval/band. As a result, the confidence intervals/bands may not be centered at the point estimates because they have been

bias-corrected. Setting  $q$  and  $p$  to be equal results on centered at the point estimate confidence intervals/bands, but requires undersmoothing for valid inference (i.e., (I)MSE-optimal bandwidth for the density point estimator cannot be used). Hence the bandwidth would need to be specified manually when  $q=p$ , and the point estimates will not be (I)MSE optimal. See Cattaneo, Jansson and Ma (2021a,b) for details, and also Calonico, Cattaneo, and Farrell (2018, 2020) for robust bias correction methods.

Sometimes the density point estimates may lie outside of the confidence intervals/bands, which can happen if the underlying distribution exhibits high curvature at some evaluation point(s). One possible solution in this case is to increase the polynomial order  $p$  or to employ a smaller bandwidth.

### Value

Estl, Estr	Matrices containing estimation results: (1) grid (grid points), (2) bw (bandwidths), (3) nh (number of observations in each local neighborhood), (4) nhu (number of unique observations in each local neighborhood), (5) f_p (point estimates with $p$ -th order local polynomial), (6) f_q (point estimates with $q$ -th order local polynomial, only if option $q$ is nonzero), (7) se_p (standard error corresponding to f_p), and (8) se_q (standard error corresponding to f_q). Variance-covariance matrix corresponding to f_p. Variance-covariance matrix corresponding to f_q. A list containing options passed to the function.
Estplot	A standard ggplot object is returned, hence can be used for further customization.

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### References

- Calonico, S., M. D. Cattaneo, and M. H. Farrell. 2018. **On the Effect of Bias Estimation on Coverage Accuracy in Nonparametric Inference**. *Journal of the American Statistical Association* 113(522): 767-779.
- Calonico, S., M. D. Cattaneo, and M. H. Farrell. 2020. **Coverage Error Optimal Confidence Intervals for Local Polynomial Regression**. Working paper.
- Cattaneo, M. D., M. Jansson, and X. Ma. 2018. **Manipulation Testing based on Density Discontinuity**. *Stata Journal* 18(1): 234-261.
- Cattaneo, M. D., M. Jansson, and X. Ma. 2020. **Simple Local Polynomial Density Estimators**. *Journal of the American Statistical Association*, 115(531): 1449-1455.
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- Cattaneo, M. D., M. Jansson, and X. Ma. 2021b. **lpdensity: Local Polynomial Density Estimation and Inference**. *Journal of Statistical Software*, forthcoming.

### See Also

[rddensity](#)

**Examples**

```
# Generate a random sample with a density discontinuity at 0
set.seed(42)
x <- rnorm(2000, mean = -0.5)
x[x > 0] <- x[x > 0] * 2

# Estimation
rdd <- rddensity(X = x)
summary(rdd)

# Density plot (from -2 to 2 with 25 evaluation points at each side)
plot1 <- rdplotdensity(rdd, x, plotRange = c(-2, 2), plotN = 25)

# Plotting a uniform confidence band
set.seed(42) # fix the seed for simulating critical values
plot3 <- rdplotdensity(rdd, x, plotRange = c(-2, 2), plotN = 25, CIuniform = TRUE)
```

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