# Intro to Economic Analysis: Microeconomics EC 201 - Day 20 Slides

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Department of Economics - University of Oregon

1 December 2021

- ► Homework 8 due this Monday (Monday of finals week, Dec 6th at 11:59pm)
- ► Comprehensive final exam on December 9th at 2:45pm the exam will last for 2 hours

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- ► What should you do?
  - If you are just playing once and you value money, offer \$0 / always accept (unless maybe the offer is literally \$0, in which case it doesn't matter)
  - What actually happens? Do people care about spite? How does this change if people are expecting another round?

#### What is a Game?

Intro to Game Theory 000000000

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EC 201

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- How should I interact with this business on a regular basis in order to minimize costs, and keep me from getting screwed over?
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- What happens if your wife gets kidnapped? (Don't use game theory)

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# 2/3 Average

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- ► What's your guess?
- What's the best strategy?

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- ▶ Is this what we see?

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  - Even among economists, no

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  - ...So on and so forth

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  - ...So on and so forth
  - This seems silly, but game theorists have spent a great deal of time analyzing what happens when the  $n^{th}$  iteration of this thinking fails

- ► Today, we will mostly talk about games with 2 players and 2 strategies
- Players only play once, and they do not communicate before or during the game
- If our players are named A and B, the following is true:
  - A knows how to play the game, and B knows how to play the game
  - A knows that B knows how to play the game, and B knows that A knows how to play the game
  - A knows that B knows that A knows how to play the game, and B knows that A knows that B knows how to play the game
  - ...So on and so forth
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    - Here is an interesting application of this principle Green-Eyed Islander Puzzle

<sup>&</sup>lt;sup>3</sup>Note: this isn't the only way to represent a game

If these (and some other, subtler principles) are satisfied, we may write down what's called a Normal Form Game<sup>3</sup>

▶ Player  $A(P_A)$  can play Top or Bottom, while player B can play Left or Right

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- Players are trying to maximize their utility

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Connor Wiegand

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  - If both players snitch, then both go away for 10 years
- Here is the game in Normal Form:

		В	
		Q	S
Α	Q	-5, -5	-20, 0
	S	0, -20	-10, -10

п

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- Okay, but how do talk about this economically?
- Much like the 2/3 average game, we do so by iteratively thinking about what a rational person would do
  - Much of game theory is about assuming the other player is rational, narrowing down their rational decisions, and then seeing what another player would do, given what is rational for the first player

▶ Remember, the players cannot talk before or while the game В

 $<sup>^4</sup>$ They are only playing once. By "switch", I mean that we are thinking hypothetically. One might also say "she might instead play"

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  - Ariana now does not want to deviate from this strategy, so let's consider Byron
  - Given that Byron is "currently" playing Q, switching to S will have a better payoff (-10 vs -20) for him
    - o That is, given that he knows (...) that playing Q will mean Araiana plays S, he should play S

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$$\begin{array}{c|ccccc}
 & Q & S \\
\hline
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We could repeat that whole analysis starting with Byron instead of Ariana

$$\begin{array}{c|cccc} & & & & & & & & & \\ A & & & & & & & & \\ \hline A & & & & & & & & \\ S & & & & & & & & \\ \hline & & & & & & & & \\ \hline \end{array}$$

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- For the test, I want to be able to give you a prisoner's dilemma (with possibly varied notation), and show that you know that both players snitching is the solution

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  - Symbolically, given other players' strategies S as given, my payoff of playing s is better than (or at least as good as) any other strategy s', given S:

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- Definition: A Nash Equilibrium is a set of mutually best responses
  - In short, a Nash Equilibrium is "a set of strategies such that no player has the incentive to unilaterally (individually) deviate from their chosen strategy"
  - For the test, I want you to know what a Nash Equilibirum is

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# A Bigger Prisoner's Dilemma

► Recognize the following? It's just a prisoner's dilemma



Air To A Fortune, Mario Party Franchise

		Pedestrian		
		D	5	
Car	D	-25, -25	-10,40	
	S	20, -5	$-100, -\infty$	

Other Games •0000000

 $\blacktriangleright$  We see two NE here: (S, D) and (D, S)

#### Chicken

Yes, that chicken: car who can stay or dodge, driving at a person who can stay or dodge

Pedestrian 
$$D$$
  $S$  Car  $S$   $Car  $S$   $S$   $Car  $S$   $S$   $Car  $S$   $S$   $Car  $S$   $Car S$   $Car  $S$   $Car S$   $Car  $S$$ 

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- Some questions to think about:
  - How do we determine which is better?

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		D	S	
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- Some questions to think about:
  - How do we determine which is better?
  - Do we think one will happen more often than the other?

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  - Either player wants to individually deviate from (D, D), likewise with (S, S)
- Some questions to think about:
  - How do we determine which is better?
  - Do we think one will happen more often than the other?
  - What happens if the car randomly plays S half the time, and the pedestrian randomly plays S one third of the time? What happens if we play with these probabilities?

### BoS

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Other Games 0000000

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Other Games 0000000

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Again, we see two NE here, where we are both eating at the same restaurant

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#### BoS

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- Suppose I have the option that morning to burn a dollar in front of my girlfriend, changing my payoffs by a dollar if I did. How would this change the outcome of the game?

# Matching Pennies

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Other Games 00000000

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  - Fact: Every game with finite players and finite strategies has a solution

Pascal: don't use this to believe in God, but if you are truly on the fence completely, here is a nifty argument:

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		God Exists	God DNE	
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Other Games 00000000

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Other Games 00000000

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  - Hopefully you can see that decisions can still be structured as games, they can still be interesting, but they lose their quintessential interactive flavor

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  - What happens if the other prisoner knows you will shoot them when you get out?

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- ▶ JFK can threaten nuclear war in order to get missiles out of Cuba, but is that threat believable?5

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# Tying Oneself to the Mast

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Pedestrian 
$$\frac{D}{S}$$
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Other Games 00000000

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- ▶ Ulysses/Odysseus: tie me to the mast (and you all put wax in your ears), so that I can hear the song of the Sirens without jumping into the sea
- You may have done this when you asked your mom to say no to your friend staying the night

Other Games 0000000

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  - A game consists of (i) players, (ii) strategies/actions/moves, and (iii) payoffs

#### Summary

► Game theory is a whole discipline. It is hard to get through it all in one undergrad class, let alone a lecture. Hopefully I provided some thought-provoking intuition

- To summarize:
  - A game consists of (i) players, (ii) strategies/actions/moves, and (iii) pavoffs
  - Much of game theory is about assuming the other player is rational. narrowing down their rational decisions, and then seeing what another player would do, given what is rational for the first player

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Review

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- Ask questions if something is fair game or not for the exam

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