

Game-Theoryst

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Overview

Full Example

```
#nfg(
  players: ([A\ Joe], [Bas Pro]),
  s1: ([$x$], [a]),
  s2: ("x", "aaaa", [$a$]),
  pad: ("x": 12pt, "y": 10pt),
  eliminations: ("s11", "s21", "s22"),
  ejust: (
    s11: (x: (0pt, 36pt), y: (-3pt, -3.5pt)),
    s22: (x: (-10pt, -12pt), y: (-10pt, 10pt)),
    s21: (x: (-3pt, -9pt), y: (-10pt, 10pt)),
  ),
  mixings: (hmix: ($p$, $1-p$), vmix: ($q$, $r$, $1-q-r$)),
  custom-fills: (hp: maroon, vp: navy, hm: purple, vm: fuchsia, he: gray, ve:
gray),
  [$0,vul(1000000000)$], [$0,1$], [$0,0$],
  [$hul(1),1$], [$0, -1$], table.cell(fill: yellow.lighten(30%),
[$hful(0),vful(0)$])
)
```

		Bas Pro		
		$[q]$ x	$[r]$ aaaa	$[1 - q - r]$ a
A Joe	$[p]$ x	0, <u>1000000000</u>	0, 1	0, 0
	$[1 - p]$ a	<u>1</u> , 1	0, -1	<u>0</u> , <u>0</u>

Importing

Simply insert the following into your Typst code: (Coming soon)

```
#import "@preview/game-theoryst:0.1.0": *
```

This imports the `nfg()` function as well as the underlining methods. If you want to tweak the helper functions for generating an `nfg`, import them explicitly through the `utils/` directory. The package's repository is located at <https://github.com/connortwiegand/game-theoryst>.

Example

The main function to make strategic (or **normal**) form games is `nfg`. For a basic 2x2 game, you can do

```
#nfg(
  players: ("Jack", "Diane"),
  s1: ($C$, $D$),
  s2: ($C$, $D$),
  [$10,10$], [$2,20$],
  [$20,2$], [$5,5$],
)
```

		Diane	
		C	D
Jack	C	10, 10	2, 20
	D	20, 2	5, 5

All of `<players>`, `<s1>`, and `<s2>` have defaults for convenience sake. Payoffs (table entries) are provided via unnamed arguments after all other payoff matrix options have been set.

Color

By default, player names, mixed-strategy parameters (called *mixings*), and elimination lines are shown in color. These colors can be turned off at the method-level by passing `bw: true`, or at the document level by running the state helper-function `#colorless()`.

`nfg` accepts custom colors for all of the aforementioned parameters by passing a dictionary of colors to the `custom-fills` arg. The keys for this dictionary are as follows (`<defaults>`):

- `hp` – “horizontal player” (**red**)
- `vp` – “vertical player” (**blue**)
- `hm` – “hor. mixing” (**#e64173**)
- `vm` – “ver. mixing” (**eastern**)
- `he` – “hor. elimination” line (**orange**)
- `ve` – “ver. elimination” line (**olive**)

Cell Customization

Since the payoffs are implemented as argument sinks (`.args`) which are passed directly to Typst’s `#table()`, underlining of non-math can be accomplished via the standard `#underline()` command. Similarly, any of the payoff cells can be customized by using `table.cell()` directly. For instance, `table.cell(fill: yellow.lighten(30%), [$1,1$])` can be used to highlight a specific cell.

Padding

There are edge cases where the default padding may be off. These can be mended by passing the optional `pad` argument to `nfg()`. This should represent how much **additional** padding you want. The `pad` arg. is interpreted as follows:

- If a `length` is provided, it assumes you want that much length added to all cell walls
- If an array of the form `(L1, L2)` is provided, it assumes you want padding a horizontal (`x`) padding of `L1` and a vertical padding (`y`) of `L2`

- If a `dictionary` is provided, it operates identically to that of the array, but you must specify the `x / y` keys yourself

Automatic Cell Sizing

Cells are automatically sized to equal heights/widths according to the longest/tallest content. If you want to avoid this behavior, pass `lazy-cells: true` to `nfg`. This behavior can be combined with the custom `padding` argument.

Semantic Game Styling

Underlining

The package imports a small set of underlining utility functions.

The primary functions for underlining are

- `hul()` – *Horizontal Underline*
- `vul()` – *Vertical Underline*
- `bul()` – *Black Underline*

These can be wrapped around values in math-mode (`$. . $`) within the payoff matrix. The underlines for `hul` and `vul` are colored by default according to the default colors for names, but they accept an optional `col` parameter for changing the color of the underline. `bul()` produces a black underline.

```
#nfg(
  players: ("Jack", "Diane"),
  s2: ($x$, $y$, $z$),
  s1: ($a$, $b$),
  [$hul(0), $vul(0)$], [$1,1$], [$2,2$],
  [$3,3$], [$4,4$], [$5,5$],
)
```

		Diane		
		<i>x</i>	<i>y</i>	<i>z</i>
Jack	<i>a</i>	<u>0</u> , <u>0</u>	1, 1	2, 2
	<i>b</i>	3, 3	4, 4	5, 5

By default, these commands leave the numbers themselves black, but boldface them. *Full Color* versions of `hul` and `vul`, which color the numbers and under-lines identically, are available via `hful()` and `vful()`. Like their counterparts, they accept an optional `col` command for the color.

Both of the colors can be modified individually via the general `cul()` command, which takes in content (`cont`), an underline color (`ucl`), and the color for the text value (`tccl`). For instance,

```
#let new-ul(cont, col: olive, tccl: fuchsia) = { cul(cont, col, tccl) }
```

will define a new command which underlines in olive and sets the text (math) color to fuchsia.

Mixed Strategies

You can optionally mark mixed strategies that a player will in a `nfg` using the `mixing` argument. This can be a dictionary with `hmix` and `vmix` keys, or an array, interpreted as a dictionary with the aforementioned keys in the `(hmix, vmix)` order. The values/entries here should be arrays which mimic `s1` and `s2` in size, with some parameter denoting the proportion of time the relevant player uses that strategy. If you would like to omit a strategy from this markup, pass `[]` in it's place.

For example, in a 2x3 game, the following dictionary would add mixing parameters to both of player 1's strategies and player 2's first and third strategies:

```
(hmix: (p$, 1-p$), vmix: (q$, [], 1-q$))
```

Example

```
#nfg(
  players: ("Chet", "North"),
  s1: (["F$"], ["G$"], ["H$"]),
  s2: (["X$"], ["Y$"]),
  mixings: (
    hmix: (p$, 1-p$),
    vmix: (q$, [], 1-q$)),
  ["7,3$"], ["2,4$"],
  ["5,2$"], ["6,1$"],
  ["6,1$"], ["5,4$"]
)
```

		North	
		$[q]$ X	$[1 - q]$ Y
Chet	$[p]$ F	7, 3	2, 4
	G	5, 2	6, 1
	$[1 - p]$ H	6, 1	5, 4

Iterated Deletion (Elimination) of Dominated Strategies

You can use the `pinit` package to cross out lines, semantically eliminating strategies. `pinit` comes pre-imported with `game-theoryst` by default.

```
#let directions = (["N$"], ["S$"], ["E$"], ["W$"])
#let elements = (["W$"], ["E$"], ["F$"], ["A$"])
#let domd = ("s12", "s13", "s14", "s21", "s22", "s23")
```

```
#nfg(
  players: ("A", "B"),
  s1: directions,
  s2: elements,
  eliminations: domd,
  ejust:(
    "s12": (x: (0pt, 10pt), y: (-3pt, -3pt)),
    "s13": (x: (0pt, 10pt), y: (-3pt, -3pt)),
    "s14": (x: (0pt, 10pt), y: (-3pt, -3pt)),
    "s21": (x: (-6pt, -8pt), y: (3pt, 8pt)),
    "s22": (x: (-4pt, -8pt), y: (3pt, 8pt)),
    "s23": (x: (-4pt, -8pt), y: (3pt, 8pt)),
  ),
  [$6,4$], [$7,3$], [$5,5$], [$6,6$],
  [$7,3$], [$2,7$], [$4,6$], [$5,5$],
  [$8,2$], [$6,4$], [$3,7$], [$2,8$],
  [$3,7$], [$5,5$], [$4,6$], [$5,5$],
)
```

B

	W	E	F	A
N	6,4	7,3	5,5	6,6
S	7,3	2,7	4,6	5,5
E	8,2	6,4	3,7	2,8
W	3,7	5,5	4,6	5,5

A

You can tell `nfg` which strategies to eliminate with the `eliminations` argument and the corresponding `ejust` helper-argument. The `eliminations` argument is simply an array of strings of the form "`s<i><j>`", where `<i>` is the player – 1 or 2 – and `<j>` is player `i`'s `<j>`th strategy (in left-to-right / top-to-bottom order *starting from 1*). These strategy strings represent the rows/columns which you want to eliminate. For instance, ("`s12`", "`s21`") denotes an elimination of player 1's second strategy as well as player 2's first strategy.

Due to `context` dependence, the lines typically need manual adjustments, which can be done via the `ejust` arg. `ejust` needs to be a dictionary with keys of matching those strings present in `eliminations` (`s11`, `s21`, etc.). The values of one of these dictionary entries is itself a dictionary: one with `x` and `y` keys. Each of these keys needs an array consisting of 2 lengths, corresponding to the starting/ending `dx/dy` adjustments from `pinit-line`.

Example

Here is the previous game with no `ejust` options included. As you can see, even similar lines may need different adjustments.

B

	W	E	F	A
N	6,4	7,3	5,5	6,6
S	7,3	2,7	4,6	5,5
E	8,2	6,4	3,7	2,8
W	3,7	5,5	4,6	5,5

A

For example, one such `ejust` argument could be `("s12": (x: (5pt, -5pt), y: (-10pt, 3pt)))`. This says to adjust the “s12” elimination line by `5pt` in the x direction and `-10pt` in the y direction for the starting (strategy-) side of the line, and adjust by `-5pt` in x and `3pt` in y on the ending (payoff-) side of the line.

Pin modifications

If you would like to modify the pins and/or lines in any way, there are easy-to-follow naming conventions for the pins. The name of every pin is

`<prefix-id>-s<i><j>--<start/end suffix>`.

Prefix ID

To prevent confusion of `pinit-lines` across games within a document, there is a counter called `_nfg-counter` which steps every time `nfg` is called. The counter begins from 0. By default, this counter is used to define the start of every pin; if the value of `_nfg-counter` is `<c>`, then the start of the pin label is “nfg-”.

You may change the starting prefix of the elims within a game by passing a `string` to the `gid` argument of `nfg`. *No additional - will be added*. Note that the `_nfg-counter` will still increment for every game in the document.

Strategy

The strategy portion of the pin name is identical to the strategy being crossed out; see above for explanation.

Start/End Suffix

For the suffix, the rule is as follows:

- The starting pin – e.g., strategy-side pin – is labelled with the suffix `--start`
- The ending pin – e.g., payoff-side pin – is labelled with the suffix `--end`

For example, consider an elimination line in the 1st game within a document which eliminates player 2’s 1st strategy. This `pinit-line` would connect the pins `nfg0-s21--start` with `nfg0-s22--end`.

Debugging

If you want to see all of the lines for the table, including the ones for a players, strategies, and mixings, set the following at the top of your document.

```
#set table.cell(stroke: (thickness: auto))
```

Note that cells are always present for mixings, they just have 0 width/height when no mixings of a specific variety are provided.