

# GMAT Maths Grinds

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## 1 The Prologue

I<sup>1</sup> am just going to outline the rules and formulae which are needed for the GMAT Mathematics test.

## 2 Topics

The topics covered

- Geometry - Area and Perimeter of shapes, and Surface Area and Volume.
- Algebra - solve equations, factoring, inequalities
- Arithmetic - working out the results
- Problem Solving - word problems

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## 3 Prerequisites and Definitions

### 3.1 Numbers

- **Natural Number** - a number which occurs in nature, an integer, a positive whole number e.g. 1,2,3,4,511 etc.
- **Real Number** - any number which can be plotted on a line  
e.g.  $3, 2/3, -0.2, \sqrt{3}$
- **Imaginary Number** - a number which can not be calculated e.g.  $\sqrt{-5}$
- **Rational Number** - a number which can be written as a fraction e.g.  $4(4/1), 2/3$
- **Irrational Number** - a number which can not be written as a fraction  
e.g.  $\sqrt{2}, \pi, 0.271271271271\dots$

### 3.2 Multiplying Signed Numbers

$$\begin{aligned} +a * +b &= +ab \\ +a * -b &= -ab \\ -a * +b &= -ab \\ -a * -b &= +ab \end{aligned}$$

### 3.3 Exponents or Indices

Exponents are the 'power' of a number, so the number of times a number is multiplied by itself e.g.

$$x^3 = x * x * x$$

A Negative exponent equates to 1 divided by that number multiplied by itself e.g.

$$x^{-4} = \frac{1}{(x * x * x * x)}$$

$$10^{-3} = \frac{1}{1000} = 0.001$$

Multiplying numbers with exponents you add the exponents

$$a^2 * a^3 = a^{2+3} = a^5$$

Dividing numbers with exponents you subtract the exponents of the divisor number from the number

$$a^3/a^2 = a^{3-2} = a^1 = a$$

$$a^2/a^3 = a^{2-3} = a^{-1} = 1/a$$

$$a^x * b^x = ab^x$$

$$(a/b)^x = a^x/b^x$$

$$(a^x)^y = (a^y)^x = a^{xy}$$

Zero to the power of a number is zero

$$0^x = 0 \quad \text{e.g.} \quad 0^1 = 0$$

A number to the power of zero is one

$$x^0 = 1 \quad \text{e.g.} \quad x^{0=1}$$

Multiplying across by a number  $a^2 + a = a(a + 1)$

$$a^3 + a^2 + 2a = a(a^2 + a + 2)$$

$$\log_2 8 = 3 \text{ i.e. ; } 2^3 = 8$$

### 3.4 Ratio

The Ratio of A to B is written as  $A/B$  or  $A : B$

### 3.5 Percentage

To get a percentage of a fraction your multiply by 100 so  $(3/4) * 100 = 75\%$

### 3.6 Absolute Value

The *Absolute Value* of a number is the square root of a number squared, so it is always a positive value.

The *absolute value* of a number 'a' is written as  $|a|$ .

$$|a| = \sqrt{a^2}$$

The absolute value of a number is often used to get its value, ignoring the sign e.g. the length of a line, where the sign is the direction,

## 4 Geometry

- Lines
- Four-sided figures
- Triangles
- Pythagoras
- Circles
- Volume and Surface Area
- Polygons

### 4.1 Lines

A Line is said to be 180°, so if you know the angle one makes intersecting a line you know the other side

### 4.2 Intersecting Lines

The opposite angles in intersecting lines are equal.

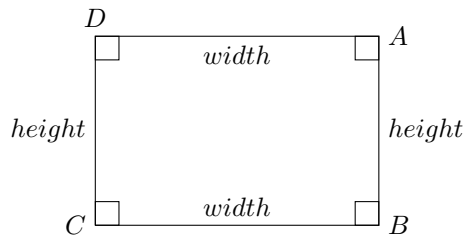
### 4.3 Line intersecting Parallel Lines

Parallel lines the angles are preserved, i.e. the angles made by the intersecting lines are the same

#### 4.4 Four-sided figures

1. Rectangles
2. Squares
3. Parallelograms
4. Other foursided figures

##### 4.4.1 Area of a Rectangle



Area of a rectangle is the length of the sides multiplied together.

$$Area_{rectangle} = width * height \quad (1)$$

##### 4.4.2 Perimeter of a Rectangle

Is the sum of the 4 sides

$$\begin{aligned} Perimeter_{Rectangle} &= 2\ width + 2\ height \\ Perimeter_{rectangle} &= 2(width + height) \end{aligned} \quad (2)$$

##### 4.4.3 Square

Well a square is just a rectangle where all the sides are the same size, so all the rules apply but just are simpler.

##### 4.4.4 Parallelogram

A parallelogram is a four-sided figure where the the sides are parallel, opposite sides are equal and opposite angles are equal. The only property which changes is the area

$$\begin{aligned} Area_{Parallelogram} &= base * perpendicular - height \\ Sum\ of\ the\ Angles\ in\ a\ Parallelogram &= 360^\circ \end{aligned}$$

## 4.5 Triangles

1. Perimeter of a Triangle equals sum of 3 sides
2. Area of a Triangle equals half the base by perpendicular height
3. The sum of the angles of a triangle equal  $180^\circ$
4. Equilateral Triangle - all the angles are  $60^\circ$ , and all sides are the same length
5. Isosceles Triangle - 2 angles are the same and 2 sides are the same length

### 4.5.1 Perimeter of a Triangle

Perimeter of a triangle is the sum of the 3 sides so  $\text{Perimeter} = \text{Side A} + \text{Side B} + \text{Side C}$

### 4.5.2 Area of a Triangle

$$\text{Area}_{\text{Triangle}} = \text{base} * \text{PerpendicularHeight} / 2 \quad (3)$$

### 4.5.3 Angles in a Triangle

The angles in a triangle equal  $180^\circ$  So if you have two angles you always can deduct the third.



## 4.6 Pythagoras Theorem

The most important theorem In a Right angle triangle(one angle =  $90^\circ$ ), the square on the hypoteneuse (longest side) is equal to the sum of the squares on the other two sides



$$h^2 = a^2 + b^2 \quad (4)$$

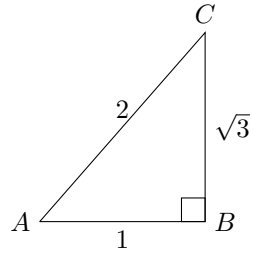
so  $h = \sqrt{a^2 + b^2}$

### 4.6.1 Also works for the Circle on the Hypoteneuse

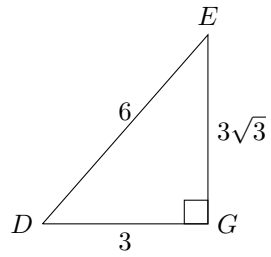
As a result the circle on the hypoteneuse is equal to the sum of the circle of the other two sides.

$$\pi(h/2)^2 = \pi(a/2)^2 + \pi(b/2)^2 \quad (5)$$

You will find that often the numbers used in examples are triangles with sides 5, 4 and 3, 10, 8 and 6 or 50, 40 and 30 which all neatly square etc.

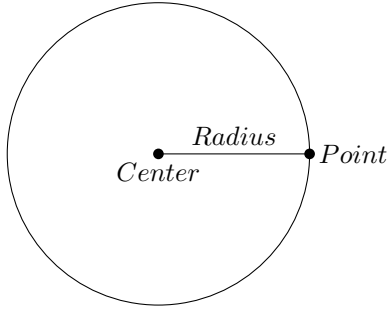
**Example 30 60 90 degree triangle**

$$\begin{aligned}
 ac^2 &= ab^2 + bc^2 \\
 2^2 &= 1^2 + bc^2 \\
 2^2 - 1^2 &= bc^2 \\
 4 - 1 &= bc^2 \\
 3 &= bc^2 \\
 \sqrt{3} &= bc
 \end{aligned}$$



$$\begin{aligned}
 de^2 &= dg^2 + ge^2 \\
 6^2 &= 3^2 + ge^2 \\
 6^2 - 3^2 &= ge^2 \\
 (3 * 2)^2 - (3 * 2)^2 &= ge^2 \\
 bc &= 3 * ge \\
 3\sqrt{3} &= 3bc
 \end{aligned}$$

### 4.7 Circles



#### 4.7.1 Area of a Circle

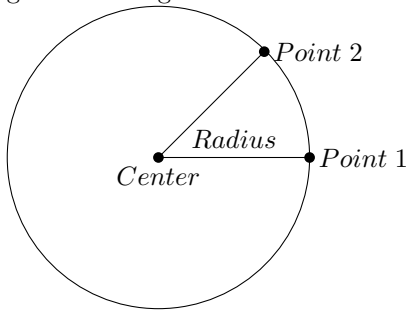
$$Area_{Circle} = \pi r^2 \quad (6)$$

#### 4.7.2 Circumference of a Circle

$$Circumference_{Circle} = 2\pi r \quad (7)$$

### 4.8 Sectors of a Circle

A sector of a Circle is a portion of a circle like a slice of pizza or tart with two straight lines from the centre of the circle out to the edge. The Angle is the angle between the two straight lines from the centre of the circle.



#### 4.8.1 Area of a Sector of a Circle

$$Area_{Sector\ of\ a\ Circle} = \left(\frac{Angle}{360}\right)\pi r^2 \quad (8)$$

#### 4.8.2 Circumference of a Sector of a Circle

$$Circumference_{Sector\ of\ a\ Circle} = \left(\frac{Angle}{360}\right)2\pi r \quad (9)$$

## 4.9 Polygons

### 4.9.1 Area of a Polygon

To get a polygons area, you *break it up into triangles* or triangles and rectangles, you may need to use pythagoras.

### 4.9.2 Perimeter of a Polygon

The sum of the lengths of its sides

### 4.9.3 Sum of angles of a polygon

Sum of the triangles which meet the points of the polygon - i.e. multiples of 180 Or triangle is 180, rectangle 360, adding another side will always be adding another triangle so pentagon is 540, hexagon is 720 and heptagon is 900 and octagon 1060 and so on...

## 4.10 Volume and Surface Area

### 4.10.1 Rectangular Box

- Volume of a Rectangular Box - Length by Breath by Height
- Surface Area, is six rectangle, two breath by depth plus two breath by height plus two height by depth

$$Volume = width * height * depth \quad (10)$$

$$Surface Area = 2(width * height) + 2(width * depth) + 2(height * depth) \quad (11)$$

### 4.10.2 Cylinder

- Volume of a Cylinder is area of the base by the height
- Surface area is 2 circles and a rectangle (from the rolled out tube of the cylinder) height by circumference of the circle

$$Volume_{Cylinder} = h\pi r^2 \quad (12)$$

$$Surface Area_{Cylinder} = 2\pi rh + 2(\pi r^2) \quad (13)$$

### 4.10.3 Sphere

A sphere is an object like a ball, where the distance from the centre of the object to the edge is the radius. For GMAT your supposed to know what a sphere is but not required to know how to get its volume or surface area. However if you're curious

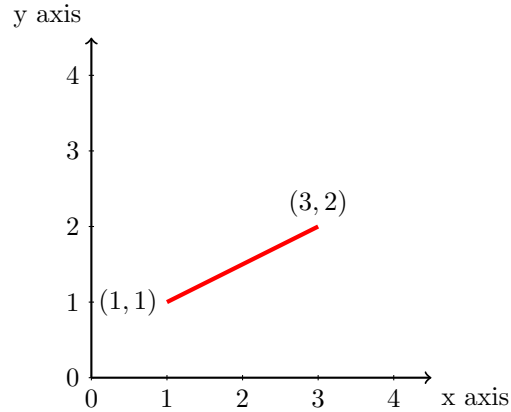
$$Volume_{Sphere} = \frac{4}{3}\pi r^3 \quad (14)$$

$$Surface Area_{Sphere} = 4\pi r^2 \quad (15)$$

## 4.11 Coordinate Geometry

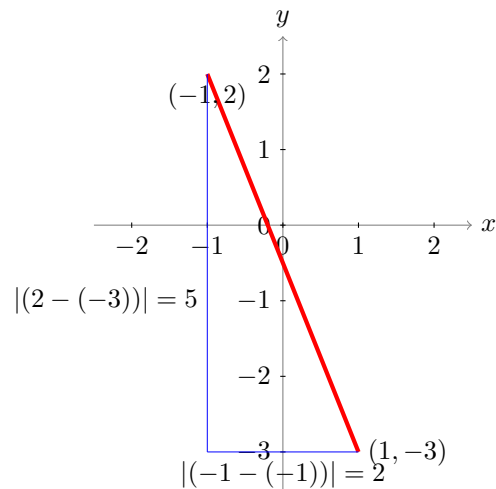
### 4.11.1 Plotting a line

To plot a line on the x-y axis if you have two points with co-ordinates  $a = (1, 1)$  and  $b = (3, 2)$  you plot the two points on the axis and draw a line between them.



### 4.11.2 Length of a line between two points on the plane

Finding the length of a line on a plane, involves plotting it on an  $xy$  axis. The length of a line can be worked out by using Pythagoras. So the length of a line from  $a = (1, -3)$  and  $b = (-1, 2)$  is  $\sqrt{2^2 + (-5)^2}$ .



$x$	$x^2 - 6 = f(x)$	$(x, f(x))$
-2	$-2^2 - 6 = -2$	$(-2, -2)$
-1	$-1^2 - 6 = -5$	$(-1, -6)$
0	$0^2 - 6 = -6$	$(0, -6)$
1	$1^2 - 6 = -6$	$(1, -6)$
2	$2^2 - 6 = -2$	$(2, -2)$
3	$3^2 - 6 = 3$	$(3, -3)$
4	$4^2 - 6 = 10$	$(4, 10)$

Table 1:

#### 4.11.3 Slope of a Line

There are two ways which get you the slope of a line one is with the co-ordinates the other with an equation which you resolve to look like  $y = mx + b$  where  $m$  is the slope of the line

##### Using the Equation

$$y = mx + B \quad (16)$$

##### Using Co-ordinates

With co-ordinates  $(x_1, y_1)$  and  $(x_2, y_2)$

$$m = \frac{(y_2 - y_1)}{(x_2 - x_1)} \quad (17)$$

*Caveat if the slope of a line  $m$  is positive the line goes upwards from left to right, and if the slope is negative then it goes downwards.*

#### 4.11.4 Functions

A *function* relates an input to an output, often the output is expressed as an expression/equation. e.g.  $f(x) = x^2 - 6$  is a function which you can plot on an x-y axes, where each point will  $(x, f(x))$ .

## 5 Algebra

### 5.1 Solve an Equation one Variable

In this case you just manipulate the equation so as the variable is on one side on its own and what it equals is on the other.

$$2x - 9 = 1$$

$$2x = 1 + 9$$

$$2x = 10$$

$$x = 10/2 \text{ so } x = 5$$

#### 5.1.1 Two Equations with Two Variables

Solved by getting what one variable is as an expression of the other then plug it in

$$2x - 3y = 1$$

$$x + 2y = 11$$

$$x = 11 - 2y$$

$$22 - 4y - 3y = 1$$

$$22 - 7y = 1$$

$$-7y = 1 - 22$$

$$-7y = -21$$

$$7y = 21$$

$$y = 21/7 \text{ so } y = 3$$

So since you now know  $y$  you can work out  $x$

$$x + 3(3) = 11 \quad x = 11 - 9 = 2$$



## 5.2 Quadratic Equations

A *Quadratic Equation* is an equation of the form  $ax^2 + bx + c = 0$  (Quadratic just means the function contains a squared variable).

- Factoring
- Using Quadratic Formula
- Completing the Square

### 5.2.1 Factoring

Solve an equation by simplifying and factoring, factoring is finding out what is multiplied that gives you the quadratic equation

Often the key is recognising patterns and knowing how combinations of factors multiply you can work out what the factors are

$$a^2 + 2ab + b^2 = (a + b)(a + b) = (a + b)^2$$

$$a^2 - 2ab + b^2 = (a - b)(a - b) = (a - b)^2$$

$$a^2 - b^2 = (a + b)(a - b)$$

Multiplying across

$$2a^3 - 4a^2b + 2ab^2 = 2a(a^2 - 2ab + b^2) = 2a(a - b)^2$$

To solve an equation by factoring you move all the elements to one side so as it equals to 0, then you try and reduced the equation to what it will. Ultimately you are find what are the possible values for the variable.

### 5.2.2 Quadratic Formula

Solve the equation by using the *Quadratic Formula* So for  $ax^2 + bx + c = 0$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad (18)$$

**For Example** Solve  $5x^2 + 6x + 1 = 0$

$$a = 5 ; b = 6 ; c = 1 ;$$

Put into formula

$$\begin{aligned} & \frac{-6 \pm \sqrt{6^2 - 4(5)(1)}}{2(5)} \\ & \frac{-6 \pm \sqrt{36 - 20}}{10} \\ & \frac{-6 \pm \sqrt{16}}{10} \\ & \frac{-6 \pm 4}{10} \\ & x = -\frac{1}{5} \text{ or } -1 \end{aligned}$$

### 5.2.3 Completing the Square

$$2x^2 - 12x - 9 = 0$$

$$2x^2 - 12x = 9$$

$$x^2 - 6x = \frac{9}{2}$$

Make the left hand side look like a factor-able function in this case by adding 9 to both sides.

$$x^2 - 6x + 9 = \frac{9}{2} + 9$$

$$(x - 3)(x - 3) = \frac{9}{2} + 9$$

$$(x - 3)^2 = \frac{9}{2} + \frac{18}{2} = \frac{27}{2}$$

$$x - 3 = \pm \sqrt{\frac{27}{2}}$$

$$x = \pm \sqrt{\frac{27}{2}} + 3$$

$$x = 3 \pm \sqrt{\frac{9 \cdot 3}{2}}$$

$$x = 3 \pm 3\sqrt{\frac{3}{2}} = 3 \pm 3\sqrt{\frac{6}{4}}$$

$$x = 3 \pm 3\frac{\sqrt{6}}{\sqrt{4}}$$

$$x = 3 \pm 3\frac{\sqrt{6}}{2} \text{ So you have two solutions.}$$

## 5.3 Inequalities

### 5.3.1 Symbols

<i>Symbol</i>	<i>Meaning</i>	<i>Usage</i>
$<$	<i>Less than</i>	$5 < 10$
$>$	<i>Greater than</i>	$51 > 49$
$\leq$	<i>Less than or equal to</i>	$p \leq 10$
$\geq$	<i>Greater than or equal to</i>	$\text{Age} \geq 18$

## 6 Arithmetic

### 6.1 Statistics

#### 6.1.1 Average/Mean

In Statistics the *Mean* is the average of the sequence numbers (sometimes referred to as the *arithmetic mean*).

$$Mean = \frac{A+B+C+D+\dots}{Number\ of\ Numbers}$$

#### 6.1.2 Median

Roughly is the middle number of a sequence, it is either the middle number or the average of the 2 middle numbers.

#### 6.1.3 Range

The *range* is the span from the lowest number to the highest number.

#### 6.1.4 Mode

The *Mode* of a list of numbers is the most frequently occurring number or numbers.

#### 6.1.5 Standard Deviation

*List* = 0, 7, 8, 10, 10

*Number of numbers in the sequence* = 5

$$Mean = \frac{0+7+8+10+10}{5} = 7$$

$x$	$(x - 7)$	$(x - 7)^2$
0	-7	49
7	0	0
8	1	1
10	3	9
10	3	9
Total	is	68

Table 2: Calculating the Standard Deviation.

$$Standard\ Deviation\ \sigma = \sqrt{\frac{68}{5}}$$

## 6.2 Counting Systems

### 6.2.1 Factorials

A factorial of a number is the product of all the positive integers less than or equal to that number. Notation  $n!$

$$2! = 2 * 1 = 2$$

$$5! = 5 * 4 * 3 * 2 * 1 = 120$$

$$10! = 10 * 9 * 8 * 7 * 6 * 5 * 4 * 3 * 2 * 1 = 3,628,800$$

$$\text{Caveat } 0! = 1$$

### 6.2.2 Simplifying Factorials

$$\left( \frac{10!}{5!2!} \right) = \left( \frac{10*9*8*7*6*5*4*3*2*1}{(5*4*3*2*1)(2*1)} \right)$$

$$\left( \frac{10*9*8*7*6*5*4*3*2*1}{(5*4*3*2*1)(2*1)} \right) = \frac{10*9*8*7*6}{2} = 15120$$

### 6.2.3 Permutations

Permutations order does matter.  $\binom{n}{k} = \frac{n!}{(n-k)!}$  If the number being selected is the same as the number of items i.e.  $n = k$  then the formula is just the factorial so  $n!$ .

### 6.2.4 Combinations

Combinations order does not matter  $\binom{n}{k} = \frac{n!}{k!(n-k)!}$

### 6.3 Probability

Probability of an event is the number of results over the total number of possible results.

$$P(E) = \frac{\text{Number of outcomes}}{\text{Total number of possible}} \quad (19)$$

**e.g** If you throw a dice twice what are the chances (probability) of 1 side being shown.

$$P(E) = \frac{2}{6} = \frac{1}{3}$$

This often described as a 1 in 3 chance of occurring.

#### 6.3.1 Probability Arithmetic

Rule of thumb in combining probability is if you have two events, and you want to know the probability of

- Probability of Event A **AND** Event B =  $P(A) * P(B)$
- Probability of Event A **OR** Event B =  $P(A) + P(B)$
- Probability of an Event E **NOT** occurring  $P(NOTE) = P(\bar{E}) = 1 - P(E)$

**e.g** If you throw two dice (Dice A and Dice B) at the same time, what are the chances (probability) of the number 6 been shown on (1) both the dice A AND dice B, (2) Probability of either dice A OR dice B being the number 6 and (3) chances of the number 6 NOT landing on both dice A AND dice B.

(1)

$$P(A \text{ AND } B) = P(A) * P(B)$$

$$P(A \text{ AND } B) = \frac{1}{6} * \frac{1}{6}$$

$$P(A \text{ AND } B) = \frac{1*1}{6*6} = \frac{1}{36}$$

(2)

$$P(A \text{ OR } B) = P(A) + P(B)$$

$$P(A \text{ OR } B) = \frac{1}{6} + \frac{1}{6}$$

$$P(A \text{ OR } B) = \frac{1+1}{6} = \frac{2}{6} = \frac{1}{3}$$

(3)

$$NOT (P(A \text{ AND } B)) = 1 - (P(A) * P(B))$$

$$NOT P(A \text{ AND } B) = 1 - (\frac{1}{6} * \frac{1}{6})$$

$$NOT P(A \text{ AND } B) = 1 - (\frac{1*1}{6*6}) = 1 - (\frac{1}{36}) = \frac{36-1}{36} = \frac{35}{36}$$

## 6.4 Sets

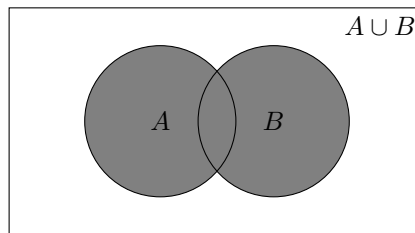
A Set is a collection of objects, in mathematics it is generally a collection of numbers but could be other objects.

- **Union** A Union B is all the contents of sets A and B -  $A \cup B$
- **Intersection** A intersection B is the contents which are common to A and B -  $A \cap B$

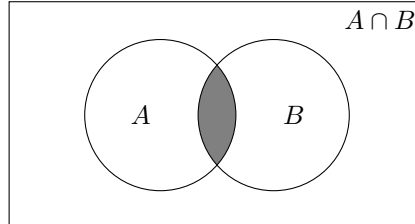
### 6.4.1 Venn Diagram

Sets can be represented diagrammatically using Venn Diagrams.

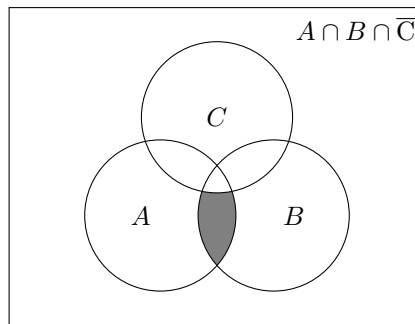
**A Union B**



**A Intersection B**



**A Intersection B NOT C**



## 7 Colophon

Wouldn't have been possible without Mr Euclid and Mr Pythagoras (and maybe Mr Archimedes).

This document was written created using L<sup>A</sup>T<sub>E</sub>X.

Initially it was word-processed using text editor [www.vim.org](http://www.vim.org) and then rendered into pdf using pdf<sub>l</sub>at<sub>e</sub>x. Latterly TexMaker (The Universal L<sup>A</sup>T<sub>E</sub>X editor) was used.

The amendments from the original version were made using Version 2.4 of MiKTeX([www.miktex.org](http://www.miktex.org)) However since using the macbook a lot of late I use T<sub>E</sub>X Live ( [www.tug.org/texlive/](http://www.tug.org/texlive/)).

K.A. Stroud[4] was my go to book in college for mathematics as well as the *Red Notes*[1], and as many in the irish education system Holland and Madden books taught me maths[2] in school.

There are many helpful websites online one I found was *Maths is Fun*[3].

## References

- [1] Maynooth Maths Dept. *Mathematics Red Notes*. MUP, Maynooth, 1990.
- [2] F.J. Holland and A.D. Madden. *Mathematics 4-7*. The Educational Company of Ireland, Dublin, 1977.
- [3] Rod Pierce. Maths is fun - math resources.
- [4] K.A. Stroud. *Engineering Mathematics*. Macmillian, 3rd edition, 1987.

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