

Figure 1: A simplex is a generalization of a triangle to higher numbers of dimensions, but here the 2-dimensional simplex is illustrated and this is just a triangle. A simplex is not regular in general. In the description of the downhill simplex algorithm the vertices is ordered so  $f(\mathbf{x}_1) \leq f(\mathbf{x}_2) \leq \dots f(\mathbf{x}_{n+1})$ .

### 13 - downhill simplex

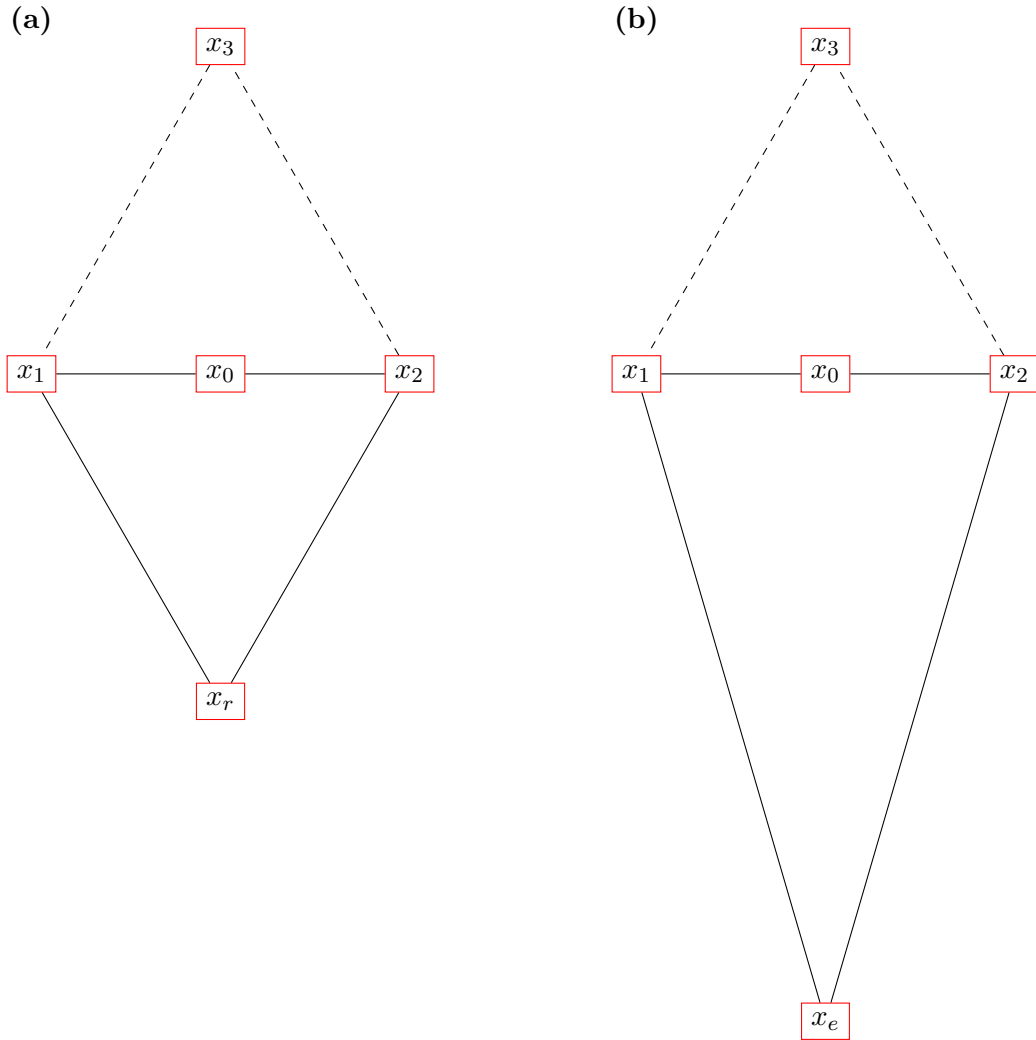


Figure 2: This illustrates reflection **(a)** and expansion **(b)**. In reflection the worst point is reflected through  $\mathbf{x}_0$ , the center of the remaining points to give a new point  $\mathbf{x}_r$ . Expansion goes from  $\mathbf{x}_0$  to  $\mathbf{x}_r$  and continues the same distance again in the same direction to give  $\mathbf{x}_e$

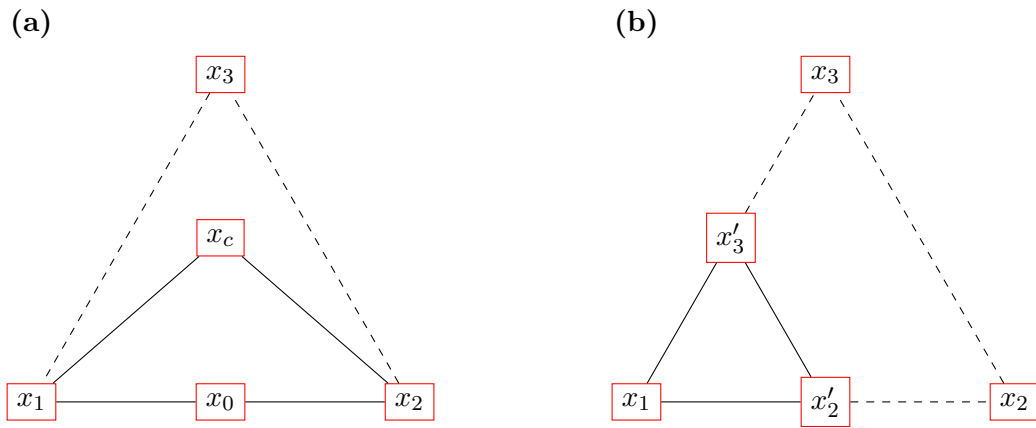


Figure 3: Contraction **(a)** and reduction **(b)**. In contraction a new point  $\mathbf{x}_c$  is chosen which is half way between the worst point  $\mathbf{x}_{n+1}$  and  $\mathbf{x}_0$ , the centre of the remaining points. In reduction the triangle is shrunk to half its size while keeping the best point.

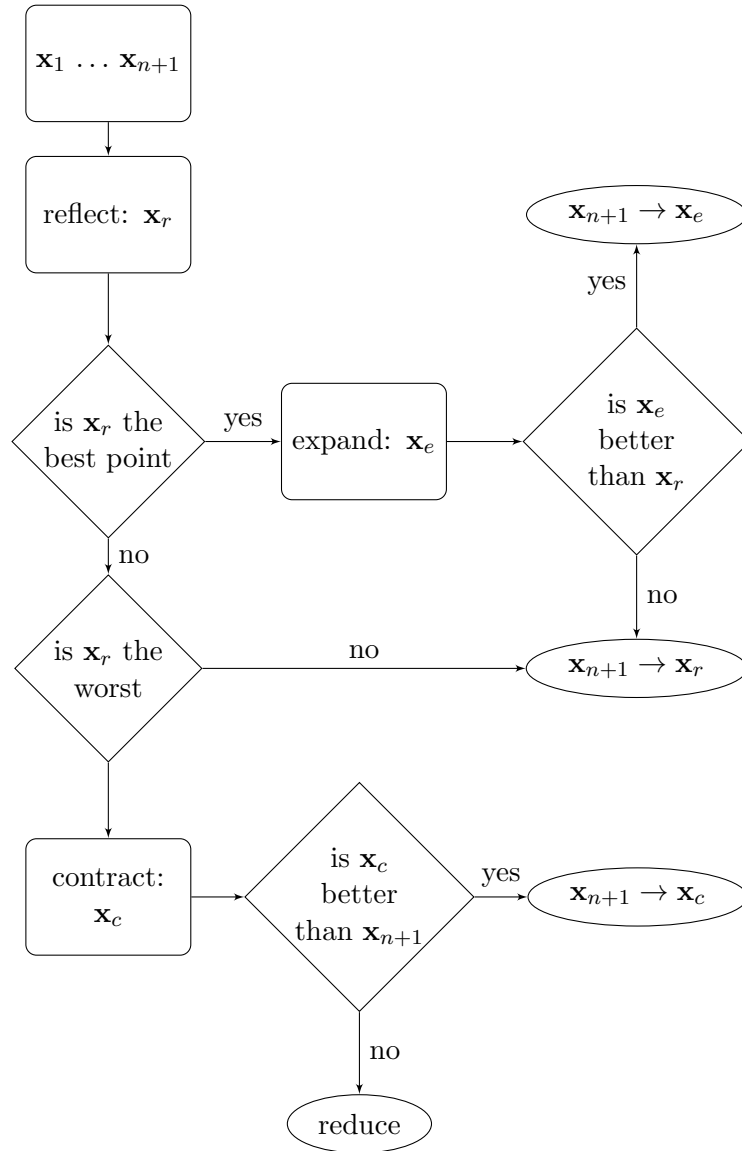


Figure 4: A flow chart for the downhill simplex algorithm. At the start, at the top, the points are put in order so that  $\mathbf{x}_{n+1}$  is the worst point and  $\mathbf{x}_1$  is the best. Next the reflected point is calculated to give  $\mathbf{x}_r$  and  $f(\mathbf{x}_r)$  is calculated. By comparing to the  $f(\mathbf{x}_i)$  it can be decided if  $\mathbf{x}_r$  is the best point, that is  $f(\mathbf{x}_r) < f(\mathbf{x}_1)$  and the flow chart has two branches depending on the answer. This carries out until an oval is reached, one or more points are changed and the process repeats.