

The Random Effects in Multilevel Models: Getting Them Wrong and Getting Them Right

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Abstract

Many surveys of respondents from multiple countries or subnational regions have now been fielded on multiple occasions. Social scientists are regularly using multilevel models to analyse the data generated by such surveys, investigating variation across both space and time. We show, however, that such models are usually specified erroneously. They typically omit one or more relevant random effects, thereby ignoring important clustering in the data, which leads to downward biases in the standard errors. These biases occur even if the fixed effects are specified correctly; if the fixed effects are incorrect, erroneous specification of the random effects worsens biases in the coefficients. We illustrate these problems using Monte Carlo simulations and two empirical examples. Our recommendation to researchers fitting multilevel models to comparative longitudinal survey data is to include random effects at all potentially relevant levels, thereby avoiding any mismatch between the random and fixed parts of their models.

Introduction

Since 2001, the *European Sociological Review* (ESR) has published 17 papers fitting multilevel models to comparative longitudinal survey data—observations on survey respondents collected in multiple countries or other contexts, with these higher-level units each observed multiple times. Of these papers, 10 reported models fitted with random effect (RE) structures we show below to yield erroneous estimates; using the correct structure might well have changed results central to many of these papers' main conclusions.

The incorrect specification of the REs in such models is an important concern, given that multilevel models have become a prominent tool in the social sciences.¹ Used correctly, these models account for the contexts in which units of analysis are observed, a useful property

given that most social science theory speaks to the place of individuals in their social environments. More technically, compared with traditional single-level models, multilevel models account for dependencies in the data, thereby producing more appropriate inferences.²

Because of the increasing availability of comparative surveys collected over multiple waves (e.g. International Social Survey Programme, European Social Survey (ESS), World Values Survey), scholars have started to fit multilevel models not only to data from multiple countries but also to data that have been sampled at various time-points—survey data that are both comparative and, at the country level, longitudinal. While the nesting structure is obvious in the case of cross-sectional data (individuals observed at Level 1 and countries at Level 2), the correct structure is less obvious where countries

are each observed multiple times. In this article, we demonstrate that the choice of the nesting structure in analyses of such data has important consequences for the substantive inferences typically derived from such models. We discuss six different modelling approaches and show that those used in a majority of published studies are problematic. Specifically, common errors in the specification of the REs lead to downwards-biased standard errors (SEs) for fixed effects (FEs). Furthermore, if coefficients are biased because of misspecification of the FEs (e.g. an omitted variable), errors in the RE specification make such biases worse.

We show that the specification of the random part of a multilevel model must at least reflect the types of variables included in the fixed part. Failure to include REs at any level at which there are FEs can result in severely downwards-biased SEs and artificially inflated degrees of freedom for the coefficients on those FEs.³ In sum, the omission of relevant REs can severely increase the risk of making Type 1 errors. The two most common omissions in multilevel models of comparative longitudinal survey data are REs at the country and country-year levels. Omitting REs at the former level implies that respondents from Peru in 1990 and Peru in 1995 have no more in common, on average, than those from Peru in 1990 and Hungary in 1995. Omitting REs at the latter level implies that a respondent from Peru in 1990 has no more in common with another from Peru in 1990, on average, as with one from Peru in 1995. We believe these assumptions are unjustified.

The article is organized as follows: we first discuss six possible RE structures, identifying examples of published research using such structures. In the next section on ‘Six Types of Models and the Relation between FEs and REs’, we report the results of a simulation study which assesses the performance of the six specifications. Next, we present two empirical applications—one a replication of a published paper, and the other an original analysis. In the final section on ‘Summary and Conclusions’, we conclude with the relatively simple recommendation that researchers should include RE at all relevant levels. The costs of omitting a necessary RE substantially outweigh the costs of including a redundant RE, and the theoretically possible situations where there is any cost at all of including a redundant RE are few and unlikely to occur in practice.

For ease of presentation, we refer throughout the article to countries as the contextual-level units. But the arguments apply equally to data collected from different regions nested within single countries (cities, counties, etc.), or to organizations such as schools or firms, as the examples to which we refer make clear.

Six Types of Models and the Relation between FEs and REs

If the data to be analysed are drawn from multiple countries each observed on multiple occasions, a variety of potential RE specifications present themselves. REs can be included for countries, years, and combinations of countries and years (country-years). The range of possible model types, all but one of which has been used in existing studies, is presented in Table 1.⁴

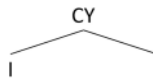
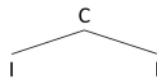
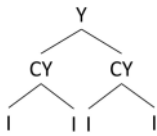
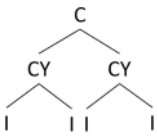
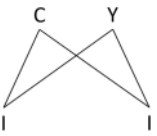
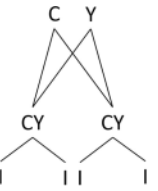
Models for comparative longitudinal survey data can incorporate covariates at each of these levels. Such covariates can be time-invariant country characteristics (e.g. common law legal tradition); characteristics which vary over time within countries (e.g. unemployment rate); or characteristics of years relevant for all countries (e.g. terrorist incidents globally). This final category of variables is likely to be relevant in few analyses of comparative longitudinal survey data; to the best of our knowledge, no cross-national studies have used such a year-level variable. However, among analyses of survey data drawn from multiple regions within a given country, there are some applications which estimate the effect of year-level variables; Schluter and Davidov (2013) for example include a measure of national media content, in their analysis of perceived group threat. More typically, models of comparative longitudinal survey data will include variables only at the country and country-year levels.

To explain the implications of the six models presented in Table 1, we refer to a hypothetical data set comprising respondents from 20 countries surveyed in five different years.

Model A has two levels and considers respondents to be nested within 100 country-years. This structure implicitly treats any time-invariant country-level variable as a time-varying one, and thus as having 100 unique values. Conversely, the model does not regard repeated observations on countries as nested within countries. Papers using such a structure include Huijts *et al.* (2010) and Semyonov *et al.* (2006). We replicate the former study below; the latter study, of anti-immigrant attitudes, rests on models of respondents nested in 12 countries each observed four times—which the authors describe as ‘48 (12×4) observations at the country level’ (p. 439).

Model B also has two levels, but this specification emphasizes the nesting of individuals within the 20 countries. For this model, any variable that is non-constant within a country—such as a national-level condition that varies over time but is constant for all respondents observed in a given country-year—will be

Table 1. A typology of random effects structures for multilevel models of comparative longitudinal survey data

Random effects	Model A	Model B	Model C	Model D	Model E	Model F
Country		✓		✓	✓	✓
Year			✓		✓	✓
Country-year	✓		✓	✓		✓
Structure						

Note: C=country-level RE, Y = year-level RE, CY = country-year-level RE, I = individual level.

taken as a property of individuals because there is no clustering below the country level. Eger (2010) uses such a model in studying support for the welfare state across Sweden’s 21 counties, where each county is observed four times. Several covariates she labels as county level are non-constant within counties.

Model C has three levels, with years taken as the highest level, and country-years nested within them. This model is similar to B, but recognizes that respondents within any given year—irrespective of where they are—have more in common than respondents from different years. The model has 5-year clusters at the highest level and 100 country-year clusters at the level below. We found no applications of models like this with international survey data, but some based on repeated cross-sections within countries (Andersen, Yang and Heath, 2006; Schlueter and Davidov, 2013). Andersen *et al.* (2006) examined British voters nested in 571 constituencies over eight elections, using models that ‘account for the clustering of individuals within constituencies, and constituencies within years’ (p. 218).

Model D, another three-level model, ignores the clustering of respondents from all places within years (unlike C), but (like B) recognizes that respondents from the same country are more similar than respondents from different countries. In addition to Model B, it recognizes that respondents observed in the same country in the same year have more in common than respondents observed in the same country but in a different year. This specification assumes that the 100 country-years at Level 2 are nested in 20 countries at Level 3. Fairbrother (2013) has used a specification of this type in studying the correlates of environmental concern.

Model E is a cross-classified model with both 20 countries and 5 years as the higher-level units. In contrast to Models C and D, this approach does not assume

hierarchical nesting. It recognizes that respondents observed within a given year are likely to be more similar than respondents from different years, and that respondents observed within a given country are likely to be more similar than respondents from different countries, but within a given year or country respondents are no more likely to be similar if they are observed in the same country or year, respectively. Lubbers and Scheepers (2001) have made use of cross-classified models of this type, in analysing voting for the extreme right across 17 regions in Germany.

Model F, finally, includes REs for (20) countries, (5) years, and (100) country-years. Model F treats country-years as cross-classified within countries and years, and individuals as strictly nested in country-years. We are not aware of any studies which have applied a model of type F to comparative longitudinal survey data.

Our presentation of this typology of models has not been innocent; the limitations of some RE structures should already be clear. Models A and C assume too much independence in taking the number of distinct values of country-level variables as 100 when it is 20, or alternatively in assuming independence of the five repeated observations of time-variant country-level variables. Structures B and E suffer from a different problem, if they include country-year-level variables (as did both studies we referenced). They do not take into account that country-year-level variables are themselves clustered; because country-year-level variables are not constant within countries, they are implicitly taken as individual-level variables, inflating the degrees of freedom and deflating the SEs. A cluster-level variable is defined by the fact that it is constant within clusters; a variable that is non-constant within clusters cannot by definition describe those clusters.

Structures A and B, and also D, suffer from the limitation that they ignore a potentially relevant level: years. If there is random variation between years, the model will yield biased SEs for any year-level variables. Finally, Model F is a full model, which should in principle control for any possible statistical dependence and includes a level for any kind of variable. As Model F is the most complex, it might face problems of convergence in cases where Model D is feasible because many applications will include no year-level variables, making Model D's one limitation inconsequential.

A Review of Published Research

To assess the prevalence of each of these specifications in applied research, we identified all relevant articles published in the ESR since 1985 and coded them according to our typology. We searched for the term 'multi-level' in the journal's online search engine, which returned 191 articles.⁵ In the first stage, we selected all those characterized by a multilevel structure, with individuals nested in contextual units observed on multiple occasions, and which estimate at least one contextual-level effect. This resulted in a set of 34 articles that could potentially use one of the model types we presented above. In the next stage, we excluded articles that used

individual-level panel data ($N = 14$) because the appropriate RE structure in these models would be even more complex—entailing an additional level of clustering.⁶ We furthermore excluded two papers for which we were not able to determine the type(s) of variables, and we excluded one paper which presented a model without any RE, thus falling outside our typology. This left us with a sample of 17 papers, which fitted multilevel models to comparative longitudinal survey data and included at least one contextual-level variable. Table 2 presents these papers.

We identified three papers using Model A, and 11 papers of type B. Six of the latter included only time-invariant country-level variables—which were in every case averages of time-varying variables. These models could have exploited variation over time in addition to variation across space, an issue we discuss further below. We also found two papers that used Model C, and one that used Model D. The results of our keyword search did not turn up any articles in ESR presenting models of type E. However, separately we identified one such paper, which we discussed earlier (Lubbers and Scheepers, 2001). A majority of the papers included analyses using RE structures which we show in 'A Simulation Study' led to downwards-biased SE. We should note that the authors of these papers may have

Table 2. A review of articles from the ESR

ID	FE			RE structure				Author(s)	Year
	Country	Year	Country-Year	Country	Year	Country-Year	Type		
76	✓		✓			✓	A	Gerlitz <i>et al.</i>	2012
86	✓		✓			✓	A	van der Lippe <i>et al.</i>	2011
116	✓		✓			✓	A	Huijts <i>et al.</i>	2010
30	✓			✓			B	Immerzeel and van Tubergen	2013
44	✓			✓			B	Dinesen	2013
62	✓			✓			B	Stegmueller <i>et al.</i>	2012
67	✓		✓	✓			B	Meulemann	2012
78	✓			✓			B	Engelhardt	2012
114	✓			✓			B	Kalmijn	2010
118			✓	✓			B	Eger	2010
149	✓			✓			B	Biedinger, Becker and Rohling	2008
158			✓	✓			B	Fekjær and Birkelund	2007
166			✓	✓			B	Kogan and Kalter	2006
176	✓	✓	✓	✓			B	Meulemann	2004
17		✓	✓		✓	✓	C	Schlueter and Davidov	2013
173			✓		✓	✓	C	Andersen <i>et al.</i>	2006
40	✓		✓	✓		✓	D	Fairbrother	2013

Note: This table displays only selected information from the full table with all coding results in the [Online Appendix A](#). ID corresponds to the full table of the [online appendix](#). Country-level variables are time invariant and describe the geographical higher-level units. Year-level variables vary only between years. Country-year-level variables are time varying and describe the geographical higher-level units. Model types correspond to [Table 1](#). Please see the [online appendix](#) for more information on our coding rules.

tested other RE specifications and not presented them, because the results were identical. In this sense, we do not know that the results from the reviewed papers are erroneous, but the results as presented, in the absence of results from fuller models, are highly questionable.

A Simulation Study

To investigate the consequences of using different RE structures, we now present a simulation study. We use 14 data-generating processes (DGPs). All of them include covariates at each of four levels (individual, country-year, country, year). Except where specified otherwise, all covariates are drawn from a normal distribution (with a mean of 0 and standard deviation of 1) and are uncorrelated with all REs.⁷ The residual error has a mean of 0 and a variance of 4. In the first eight DGPs, each simulated data set comprises 10 respondents observed in each of 5 years in each of 20 countries. In these DGPs, all covariates are uncorrelated with each other, and the estimated models are correctly specified, given the fixed part in the DGPs. What varies across these eight DGPs are the variances of the RE at each of the contextual levels, for the purpose of testing the implications of omitting a RE at a level with random error. Next, in DGPs 9, 10, and 11, we vary the N s at the individual and year level. In DGPs 12, 13, and 14, we analyse the impact of misspecifications in the fixed part. In 12 and 14, we simulate data with correlated covariates, omitting one in the estimation. In 13 and 14, the cross-sectional and longitudinal effects of a time-varying country-level covariate differ. The full R code used for the simulations, and for generating the graphics presented below, is included as [Online Appendix B](#). To ensure the robustness of the results, we ran two separate series of 10,000 simulations (starting with different seeds), inspected the chains visually, and verified that the results were substantially the same.

The N s we have chosen at some levels are not realistic, but keeping them modest allowed us to run more simulations, and below we briefly report the results of some tests of how our results varied depending on the N at each level. Particularly, given that some models have an N of 5 (years) at the highest level—too few for the reliable estimation of a RE variance—we experimented with the use of dummy variables rather than REs for years; this alternative approach yielded otherwise identical results. Note that Model D with the addition of year dummies is the same as Model F with year dummies in place of REs for years.

Consequences of Misspecifications in the Random Part

In this section, we discuss the first 11 DGPs, which can be written as follows:

$$y_{ijkl} = 1 \cdot X_{ijkl} + 1 \cdot Z_{jkl} + 1 \cdot Z_l + 1 \cdot Q_k + u_{jkl} + u_l + u_k + e_{ijkl}$$

The subscript i indicates individuals, j indicates country-years, l indicates countries, and k indicates years. X_{ijkl} is an individual-level and Q_k a year-level variable. Z varies at two levels, the country and the country-year level, with Z_l the between-country component and Z_{jkl} the within-country component. In DGPs 1–12, we set these two components to have the same effect.

To 10,000 data sets of each type, we fit two sets of six models. Each set of six includes the six RE structures discussed above. The first set includes separate country-year and country-level covariates (the fitted *fixed part* is $y_{ijkl} = \beta_0 + \beta_1 X_{ijkl} + \beta_2 Z_{jkl} + \beta_3 Z_l + \beta_4 Q_k$), while the second set forces these two covariates to share a single coefficient—as did all but one of the models in the applied work we discussed earlier. The fixed part of these models replaces the distinct within and between components with a single variable (the estimated *fixed part* is $y_{ijkl} = \beta_0 + \beta_1 X_{ijkl} + \beta_2 Z_{2,jkl} + \beta_3 Q_k$, where $Z_{2,jkl} = Z_l + Z_{jkl}$). Studies treating time-varying national characteristics like gross domestic product (GDP)/capita as country-year-level variables implicitly assume that cross-sectional differences among countries have the same relationship with y as longitudinal changes within them. In the DGPs 1–12, this assumption is true, and therefore, both sets of six yield unbiased coefficient estimates.

[Figure 1](#) presents the first key results of the simulation study: the implications of different RE structures for the SEs of FEs at different levels, across DGPs 1–8.

The optimism of the SEs is defined as the ratio of a coefficient's sampling variability across the 10,000 simulations to the variability as estimated by the SEs ([Shor et al., 2007](#)). In [Figure 1](#), we display the optimism on a log-scale, meaning that values >0 indicate downwards-biased and anti-conservative SEs and values <0 indicate upwards-biased, overly conservative SEs.

[Figure 1](#) shows that the SEs associated with country-year-level variables are too small where a fitted model excludes RE at the country-year level (B, E), assuming there is variance at that level (DGPs 1, 3, 5, 7). Even if there is no random error at the country-year level, if there is random error at the year level (DGPs 2, 6), the SEs for country-year-level covariates are too small using Model B, which excludes country-year REs. The country-year level in Model B reflects year-level error that is

Table 3. Data-generating processes

DGP	N_l	N_k	N_i	$\text{Var}(u_l)$	$\text{Var}(u_k)$	$\text{Var}(u_{jkl})$	Effect of Z_{jkl}	Correlated coefficient
1	20	5	10	1	1	1	1	N
2	20	5	10	1	1	0	1	N
3	20	5	10	1	0	1	1	N
4	20	5	10	1	0	0	1	N
5	20	5	10	0	1	1	1	N
6	20	5	10	0	1	0	1	N
7	20	5	10	0	0	1	1	N
8	20	5	10	0	0	0	1	N
9	20	5	50	1	1	1	1	N
10	20	2	10	1	1	1	1	N
11	20	20	10	1	1	1	1	N
12	20	5	10	1	1	1	1	Y
13	20	5	10	1	1	1	0.5	N
14	20	5	10	1	1	1	0.5	Y

Note: Index l indicates countries, k indicates years, i indicates individuals, and j indicates country-years. Correlated coefficient: N = no, Y = yes.

not allowed for by the RE structure. Whenever there are random differences across country-years—arising from random variance at the country-year and/or year levels—the SEs are biased at this level.

For year-level covariates, the SEs are too small if there is random error at the year level and the fitted model excludes REs at this level (DGPs 1, 2, 5, 6; Models A, B, D). Country-level covariates have downwards-biased SEs when there is random error at the country level (DGPs 1, 2, 3, 4), but the model does not include REs at that level (A, C). Finally, where a time-varying country-level variable is included but not decomposed into its country and country-year component (the bottom row), the bias in SEs is a combination of the biases found for each of the components.

Overall, then, only Model F avoids the problem of anti-conservative SEs for all FEs, no matter what random error is represented in the data. Model D also avoids the problem of anti-conservative SEs for all coefficients, except those on year-level variables because it includes no year-level RE. On the other hand, the SEs for some covariates as estimated by Model F and even more so Model D are, in a small number of exceptional circumstances, over-conservative. When a RE is estimated at a level where there is in fact no random error at all, the log-optimism of the SE for a covariate at that level can fall below 0 (see e.g. DPGs 5 and 6 under Models A and D in the top row). Nevertheless, the over-conservatism for all SEs as estimated by Model F is small, and in any event, it seems unlikely in the extreme for there to be precisely zero random error at any level in real-world data.

DGPs 9–11 vary the numbers of years and individuals. The results are presented in Figure OA1 in the [Online Appendix](#). In brief, the numbers of years and individuals have no influence in correctly specified models (F, and D if one is concerned only with country and country-year-level variables). In those models that take country-year-level variables as individual-level variables (B and E), an increase in the number of individuals makes the bias in SE worse. Please note that the simulated data sets contain only 10, respectively 50, respondents per country-year. In real data sets with about 1,000 respondents per country-year, this particular bias, which relates to the number of individuals, would be even higher. In models that treat repeated observations of time-constant country-level variables as distinct values (A and C), the bias in SE increases with the number of years.

Consequences of Misspecifications in the Random and Fixed Part

Now, we present the simulation results for DGPs 12–14, in which we investigate consequences of misspecifications in the random *and* fixed parts of a model. All models fitted to DGPs 1–11 had correctly specified fixed parts. However, for each DGP, we fitted two sets of models, one in which we estimated separate country- and country-year-level effects and one in which we forced them to share a coefficient, like all but one of the published papers we discussed earlier. This second set yielded unbiased coefficients because the two components were created with identical effects (Figure OA2 in [Online Appendix D](#) presents the FE coefficients for DGPs 1–8—all of them are unbiased).

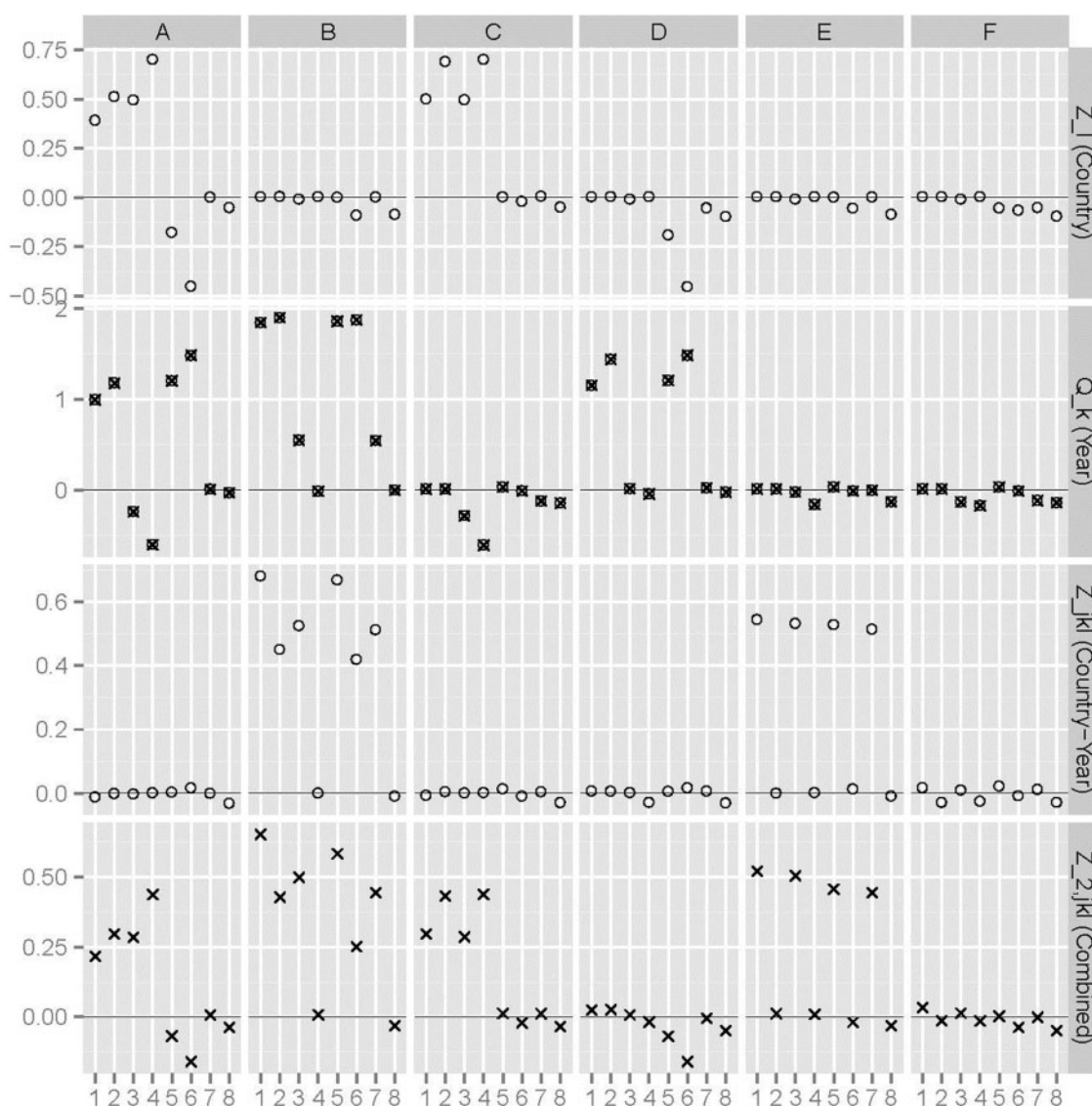


Figure 1. Log-optimism of the estimated SEs of four covariates—DGPs 1–8.

Note: See Table 3 for details about DGPs 1–8. O's indicate estimates from models including separate country- and country-year-level effects, and X's indicate estimates from models that include only the combined variable. Note then that the estimated coefficients differ: the second approach yields two estimates (for Q_k , a year-level covariate, and Z_{2jk} , a country-year-level covariate), whereas the first approach estimates fixed-effects coefficients for three covariates, including a covariate capturing the between-country effect (Z_1). The correct value of 0 is highlighted with a horizontal line. Given that our interest is in the contextual-level variables, we do not present the results for the intercept or the individual-level variable. Interested readers are welcome to replicate the simulation using the R code in [Online Appendix B](#).

Typically, such an assumption makes little sense in light of the usual results of [Hausman \(1978\)](#) tests, which regularly show that cross-sectional and longitudinal relationships are not equivalent ([Halaby, 2004](#): p. 527). Fortunately, such a misspecification is easy to avoid, the solution being to include the country means and the mean-differenced components of time-varying

country-level variables in the model. [Fairbrother \(2014\)](#) provides a detailed treatment of such models in the context of comparative longitudinal survey data, and we invite readers to look at this paper for more details. Not centring time-varying country-level variables by their country-means generates a single coefficient representing a weighted mean of the between and within effects

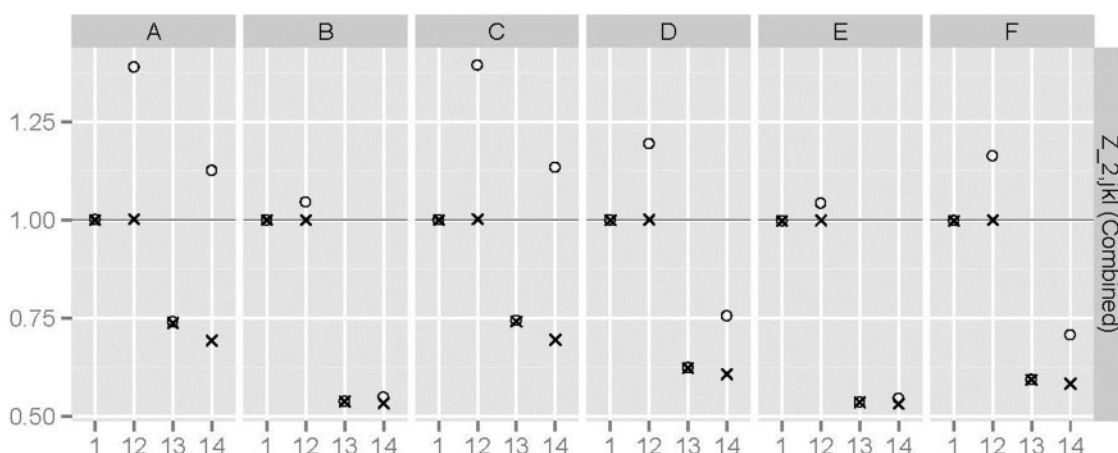


Figure 2. Fixed-effects estimates—DGPs 1, 12–14.

Note: Analogous to DGP 1, the random error variances in DGPs 12–14 are 1 at every level (compare Table 3, DGP 1). O's indicate estimates from models omitting the additional covariate, and X's indicate estimates from models that include the covariate. Note that in DGPs 1 and 13, there is no additional covariate correlated with Z , while there is in DGPs 12 and 14. In DGPs 13 and 14, the between and within effects are 1 and 0.5, respectively, whereas in DGPs 1 and 12, they are both 1. The value of 1 is highlighted with a horizontal line.

(Raudenbush and Bryk, 2002: pp. 134–149). This coefficient can be deeply misleading and/or difficult to interpret if the two effects are different (also see Te Grotenhuis *et al.*, 2015). Here, we investigate what happens if the between and within effects differ, by setting the effect size of Z_{jkl} to 0.5 instead of 1 in DGP 13.

To investigate the consequences of another common misspecification, the omission of a relevant variable, in DGP 12, we add two covariates (Z_{jkl}^{CC} and Z_l^{CC}): $y_{ijkl} = 1 \cdot X_{ijkl} + 1 \cdot Z_{jkl} + 1 \cdot Z_l + 1 \cdot Z_{jkl}^{CC} + 1 \cdot Z_l^{CC} + 1 \cdot Q_k + u_{ijkl} + u_l + u_k + e_{ijkl}$, where $\text{Corr}(Z_l, Z_l^{CC}) = 0.8$ and $\text{Corr}(Z_{jkl}, Z_{jkl}^{CC}) = 0$. To the data generated by DGP 12, we fit models that combine these two components. That is, we add one additional country-year-level covariate to the fitted models ($Z_{2,jkl}^{CC} = Z_{2,l}^{CC} + Z_{2,jkl}^{CC}$). The country-level component of this additional covariate is correlated with the first covariate (thus the superscript CC). Finally, in DGP 14, we combine these two characteristics by including the correlated covariate ($Z_{2,jkl}^{CC}$), as in DGP 12, and setting the effect of Z_{jkl} to 0.5, as in DGP 13. To these three DGPs we fit two sets of six models; the first set of six controls for the new covariate, while the second set of six omits it from the model. Both sets of six do not estimate separate country- and country-year-level effects but only the combined effect of Z . That is, the *fixed part* of the first set of six is $y_{ijkl} = \beta_0 + \beta_1 X_{ijkl} + \beta_2 Z_{2,jkl} + \beta_3 Z_{2,jkl}^{CC} + \beta_4 Q_k$ and the *fixed part* of the second set of six is $y_{ijkl} = \beta_0 + \beta_1 X_{ijkl} + \beta_2 Z_{2,jkl} + \beta_3 Q_k$. Figure 2 presents the mean FE coefficient across the 10,000 simulations.

The coefficient on the combined $Z_{2,jkl}$ is unbiased in DGP 12 if the correlated covariate is controlled for but biased if it is omitted from the model, and the severity of the bias depends on which of the six models is fitted. The bias is most severe for Models A and C, where the RE specification excludes the level at which the variables are correlated (the country level). In DGP 13, similarly, the coefficient estimate depends on which of the six models is estimated. In Models A and C, which do not recognize that there are fewer countries than country-years, the within and between components receive the same weight, which results in an estimate that is the average of the two components. In models that take the within-country component Z_{jkl} as an individual-level variable (B and E), the estimated effect for the combined variable $Z_{2,jkl}$ is heavily dominated by this within effect. In those models that do recognize the correct number of countries and country-years (D and E), the effect is slightly dominated by the within component. These results are in line with Raudenbush and Bryk (2002) who noted that the combined effects are a weighted average of the within and between components, where the weights depend (approximately) on the degrees of freedom at each level.

The results for DGP 14, which combines the key features of DGPs 12 and 13, show most dramatically of all how changing the RE structure alone can lead to a variety of different coefficient estimates, when the fixed part is misspecified.

The Empirical Relevance of Misspecifications

Here, we further illustrate the consequence of misspecified REs by first replicating a published study whose results change if we specify a different RE structure, and then presenting an original empirical example.

A Replication Study

We contacted the authors of several papers to ask for replication data sets. Though some in principle said they were willing, ultimately none provided us with access to their data. In some cases, this reticence was understandable: the authors committed to uphold data protection protocols. In other instances, the authors provided no clear explanation why they were unwilling to provide replication data.

We therefore replicate one paper published in the ESSR whose data were publicly available: 'Education, Educational Heterogamy, and Self-Assessed Health in Europe: A Multilevel Study of Spousal Effects in 29 European Countries' by Huijts *et al.* (2010). The authors provided the contextual-level data in the paper, which was a commendably transparent approach on their part. Their analysis is based on the first three rounds of the ESS.

The dependent variable is individual subjective health. The main interest is in the effect of educational heterogamy, a contextual-level variable that measures the share of couples with the same educational level. This variable is measured at the country-year level. As controls, the model includes one country-level variable (government health expenditures as percentage of all health expenditures) and a second country-year-level variable (logged GDP/capita in 1,000 US\$). The authors estimate Model A, treating each country-year as a single observation in a two-level model.

We are not able to replicate precisely the results because the ESS version to which we have access differs from the version that the authors had.⁸ Our analysis is based on three country-years less than the original study (Sweden 2002 and 2004, Iceland 2004). However, the estimates of our replication are sufficiently close to the original estimates to make our point. Table 4 presents the results of the original study (Huijts *et al.*, 2010: p. 270), our replication and our re-estimation of the model with the nesting structure of Model D.

In the original study, M0 is an empty model, and M1 a model containing all individual-level variables. In Model M2, the authors enter the degree of educational heterogamy (see Table 4). It has an effect of 0.011 and is significant at the 5 per cent level. In our replication, we

estimate a coefficient of 0.011 but with a slightly higher SE such that the effect is not significant; nevertheless, we are able to reproduce a nearly identical result. In the re-estimated model (termed Alternative), the effect becomes nowhere near significant, and the coefficient is dramatically different.

More interesting is Model M3 because it also contains a country-level variable (government health expenditure). The authors conclude from Model M3 that 'government share in health expenditure [...] is negatively related to self-assessed health: the larger the financial role of the government in the health system, the less healthy people feel. This may indicate that health systems in which the government covers a large share of health expenses are less successful in improving and maintaining people's health than health systems in which private funds play a more prominent role' (Huijts *et al.*, 2010: p. 270). This is clearly a far-reaching conclusion, and not an argument to be made lightly. Our replication of M3 with the inclusion of a country-level RE shows that this result is not robust. The absolute value of the coefficient on government health expenditure shrinks substantially, the SE expands slightly, and the effect turns non-significant. Is this estimate more defensible than the original? Given the simulations we reported earlier, it seems that Model A artificially expands the number of observations of country-level variables, downward biasing the SE. In this application, there are 29 independently observed values, but the model assumes the data contain 58. The re-estimated model takes the country level into account, and therefore reflects the correct number of independent observations. The estimated coefficient on GDP/capita, a country-year-level variable, also changes under the new specification. The effect size declines substantially, though it remains significant. The replication and re-estimation of the study therefore demonstrate the consequences of omitting relevant REs for the SEs of coefficients. Moreover, as demonstrated in the simulations, changes in the RE specification can have substantial impacts on the coefficient estimates. In the next sub-section on 'An Empirical Example with Real Survey Data', we present an empirical example that demonstrates even more clearly how substantial these impacts can be.

An Empirical Example with Real Survey Data

The analyses presented in Table 5 are based on five waves of the ESS (see European Social Survey, 2010, 2011). The dependent variable is respondent's support for income redistribution. The survey data have been merged with four country-year-level variables: GDP/capita, Gini

Table 4. Replication and re-estimation of Huijts *et al.* (2010)

Parameter	M2			M3		
	Original b/se	Replication b/se	Alternative b/se	Original b/se	Replication b/se	Alternative b/se
Constant	3.093** 0.197	3.100** 0.217	3.359** 0.153	2.229** 0.217	2.351** 0.227	2.832** 0.324
Individual characteristics						
Educational level						
Primary (ref.)						
Secondary	0.134** 0.009	0.135** 0.009	0.136** 0.009	0.135** 0.009	0.135** 0.009	0.136** 0.009
Tertiary	0.237** 0.010	0.247** 0.011	0.247** 0.011	0.238** 0.010	0.247** 0.011	0.247** 0.011
Educational level of partner						
Primary (ref.)						
Secondary	0.076** 0.009	0.087** 0.009	0.087** 0.009	0.076** 0.009	0.087** 0.009	0.087** 0.009
Tertiary	0.112** 0.010	0.129** 0.011	0.130** 0.011	0.112** 0.010	0.130** 0.011	0.129** 0.011
Father's occupation						
Manual and service (ref.)						
Technical and craft	0.018* 0.008	0.024* 0.010	0.023* 0.010	0.018* 0.008	0.023* 0.010	0.022* 0.010
Clerical and intermediate	0.041* 0.017	0.054* 0.021	0.052* 0.021	0.040* 0.017	0.053* 0.021	0.052* 0.021
Professional	0.045** 0.012	0.062** 0.015	0.060** 0.015	0.045** 0.012	0.061** 0.015	0.061** 0.015
Managers and administrators	0.037** 0.012	0.036* 0.014	0.034* 0.014	0.037** 0.012	0.035* 0.014	0.034* 0.014
No known occupation	-0.042** 0.010	-0.041** 0.012	-0.028* 0.011	-0.042** 0.010	-0.040** 0.012	-0.024* 0.012
Gender (female = 1)	-0.081** 0.006	-0.080** 0.007	-0.080** 0.007	-0.081** 0.006	-0.080** 0.007	-0.080** 0.007
Age	-0.018** 0.000	-0.018** 0.000	-0.018** 0.000	-0.018** 0.000	-0.018** 0.000	-0.018** 0.000
Country characteristics						
Educational heterogeneity	0.011* 0.005	0.011 0.006	0.003 0.004	-0.002 0.004	-0.004 0.004	-0.001 0.004
GDP/capita (logged)				0.577** 0.060	0.601** 0.061	0.277** 0.072
Government health expenditure				-0.007** 0.003	-0.009** 0.003	-0.003 0.004
Variance components						
Country-level variance	0.097** 0.016	0.095 0.018	0.092 0.025	0.033** 0.006	0.034 0.007	0.047 0.020
Country-year-level variance			0.002 0.001			0.003 0.001
Individual-level variance	0.596** 0.003	0.591 0.004	0.591 0.004	0.596** 0.003	0.591 0.004	0.591 0.004
N1 (country level)	58	55	27	58	55	27
N2 (country-year level)			55			55

Note: * $p < 0.05$, ** $p < 0.01$ (two-sided tests); our models are based on 56,712 individual observations; the models in the original study are based on 59,314 observations. The models are named M2 and M3 to fit the naming in the original study.

Source: ESS (2002–2006).

Table 5. Multilevel regressions with ESS data—Models A–F

	Model A	Model B	Model C	Model D	Model E	Model F
Parameter	b/se	b/se	b/se	b/se	b/se	b/se
Individual-level data						
Left–right	–0.0853*** (0.0012)	–0.0854*** (0.0012)	–0.0853*** (0.0012)	–0.0853*** (0.0012)	–0.0855*** (0.0012)	–0.0853*** (0.0012)
Gender (male = 1)	–0.1225*** (0.0054)	–0.1218*** (0.0054)	–0.1225*** (0.0054)	–0.1225*** (0.0054)	–0.1217*** (0.0054)	–0.1224*** (0.0054)
Age	0.0031*** (0.0002)	0.0030*** (0.0002)	0.0031*** (0.0002)	0.0031*** (0.0002)	0.003*** (0.0002)	0.0031*** (0.0002)
Household income	–0.0798*** (0.0022)	–0.0759*** (0.0022)	–0.0798*** (0.0022)	–0.0795*** (0.0022)	–0.0759*** (0.0022)	–0.0795*** (0.0022)
Employment status						
Employed	Ref.	Ref.	Ref.	Ref.	Ref.	Ref.
Unemployed	0.0868*** (0.0126)	0.0886*** (0.0127)	0.0867*** (0.0126)	0.0870*** (0.0126)	0.0876*** (0.0127)	0.0867*** (0.0126)
Not in labour force	–0.0224*** (0.0064)	–0.0201** (0.0064)	–0.0224*** (0.0064)	–0.0222*** (0.0064)	–0.0203** (0.0064)	–0.0223*** (0.0064)
Education						
ISCED 0–1	Ref.	Ref.	Ref.	Ref.	Ref.	Ref.
ISCED 2	0.0643*** (0.0104)	0.0628*** (0.0105)	0.0643*** (0.0104)	0.0651*** (0.0104)	0.0643*** (0.0105)	0.0652*** (0.0104)
ISCED 3	0.0188 (0.0101)	0.0155 (0.0101)	0.0188 (0.0101)	0.0198 (0.0101)	0.0147 (0.0101)	0.0196 (0.0101)
ISCED 4	–0.0595** (0.0216)	–0.0609** (0.0215)	–0.0595** (0.0216)	–0.0585** (0.0216)	–0.0573** (0.0215)	–0.0579** (0.0216)
ISCED 5–6	–0.1848*** (0.0106)	–0.1895*** (0.0106)	–0.1849*** (0.0106)	–0.1839*** (0.0106)	–0.1903*** (0.0106)	–0.1842*** (0.0106)
Bad health	0.0677*** (0.0063)	0.0704*** (0.0063)	0.0677*** (0.0063)	0.068*** (0.0063)	0.0705*** (0.0063)	0.068*** (0.0063)
Country-level data						
GDP/C (in 1,000\$)	–0.0059 (0.0031)	0.0053*** (0.0007)	–0.0064* (0.0031)	0.0042 (0.0022)	–0.0042** (0.0015)	–0.0043 (0.0031)
Gini index	0.0106 (0.0069)	0.0239*** (0.0022)	0.0104 (0.0069)	0.0257*** (0.0066)	0.0209*** (0.0023)	0.0200** (0.0064)
Social spending	–0.0166* (0.0067)	0.0095*** (0.0022)	–0.0163* (0.0067)	–0.0011 (0.0065)	–0.0069* (0.0031)	–0.0118 (0.0068)
Unemployment rate	0.0185* (0.0075)	–0.0021 (0.0017)	0.0179* (0.0075)	0.0034 (0.0052)	–0.0002 (0.0017)	0.0025 (0.0050)
Constant	4.5484*** (0.3056)	3.3754*** (0.1118)	4.5677*** (0.3044)	3.5723*** (0.2737)	4.1310*** (0.1410)	4.2582*** (0.2997)
Variance components						
Country		0.12430 (0.0345)		0.09380 (0.0296)	0.06403 (0.0180)	0.06088 (0.0180)
Year			0.00113 (0.0030)		0.00334 (0.0024)	0.00372 (0.0033)
Country-year	0.07030 (0.0098)		0.06921 (0.0099)	0.00733 (0.0014)		0.00694 (0.0013)
Individuals	0.93059 (0.0036)	0.93583 (0.0036)	0.93059 (0.0036)	0.93059 (0.0036)	0.93558 (0.0036)	0.93059 (0.0036)

Note: * $P < 0.05$, ** $P < 0.01$, *** $P < 0.001$. All models are based on 133,301 individual observations and data from 27 countries and 105 country-years. Models estimated with Stata's `xtmixed` command.

Source: ESS (2002–2010).

index, social spending as percentage of GDP, and the unemployment rate. The complete data set is taken from an article published elsewhere (Schmidt-Catran, 2014); readers should refer to this paper if they are interested in details about the data or the underlying theory. The main right-hand side variable of interest is income inequality (measured via the Gini index), with which there are theoretical reasons (derived from the median-voter hypothesis) to expect a positive correlation with demand for redistribution. GDP/capita, social spending, and unemployment rates are included as control variables.

While the replication study presented above demonstrated how the estimates of Model A change if Model D is estimated instead, Table 5 shows how the estimates can vary depending on which of all six models are estimated. The coefficients on the individual-level variables change to a small degree, but not substantially. The coefficients and SE for the country-year-level variables, however, change substantially. The coefficient on GDP/capita is positive and significant in Model B (0.0053***), while it turns significantly negative in Models C (−0.0064*) and E (−0.0042**). In Models A, D, and F, the effect is not significant. We observe a similar pattern for the effect of social spending: some models suggest a significant positive effect, while others suggest a significant negative effect. The other two contextual-level variables do not change so dramatically, but nonetheless vary and point to rather different conclusions. The effect of the Gini index is significantly positive in Models B, D, E, and F but not significantly different from zero in Models A and C. The effect of unemployment rates is significantly positive in Models A and C but not significant in all other models. Model F (as well as model D) supports the conclusion that inequality is positively related to demand for redistribution, while all other country-year-level variables have non-significant effects. For the purpose of our article, these results all show how a model with the same FE specification can lead to substantially different conclusions, if the random part changes.

In our discussion of the six model types, we pointed to the similarities of Models A and C which both ignore country-level REs. These similarities are reflected in the coefficient estimates. The simulation study showed that the SEs of country-year-level variables not centred by the country-mean are too optimistic, for multiple DGPs using all RE structures except D and F (see the bottom panel in Figure 1). This is also reflected in the estimates: while models D and F report only one significant effect, all other models show two or three significant effects. In the Table A1, we estimate the models from Table 5 but distinguish within- and between-country effects. This

analysis shows that the between effect of, for example, the Gini index is close to 0, but the within effect is positive (about 0.02). Consequently, Models A and C in Table 5 estimate a Gini effect that lies between 0 and 0.02, while Models B, D, E, and F provide estimates that are dominated by the within effect. Similar stories could be told about the other three variables. Generally, the additional analyses show that the changes in FE coefficients are much smaller than they were in the analysis without decomposition. There are no longer any instances where an effect changes substantially, which is analogous to the results of the simulation study, where correctly specified FEs are unaffected by the RE specification. The coefficients do still change slightly because—with this real survey data—there are certainly more misspecifications than just the missing decomposition into within and between effects (e.g. omitted variables: see Figure 2, DGP 14).

Summary and Conclusions

All of the above points to a single specific, but important, practical implication: it is safer to include REs at all potentially relevant levels. The first and general rule is to include REs at all levels at which there are FEs. A second rule however is: if there might be variation at a given level, even if there are no FEs included at that level, one should include REs at that level. This statement is particularly true for the level of geographical clusters (e.g. countries), as there will certainly be (unobserved) differences among these clusters that are stable over time. Observations on the same geographical clusters will likely not be independent of each other, and so omitting REs at this level will lead to downwards-biased SEs.

Our coding of relevant articles published in *ESR* shows that several papers did not include country REs (Model A), even though they included country-level FEs (violating rule 1). Some papers included country-year-level FEs and REs but no country-level REs (Model C). In this case, there is no mismatch between the random and the fixed part, but the assumption of independence of the repeated observations of geographical clusters, as implied by this RE structure, might also lead to downwards-biased SE (violating rule 2). Moreover, many (though not all) of the models of type B listed in Table 2 included FEs at the country-year and/or year levels, but did not include country-year or year REs. These models again suffer from a mismatch between the fixed and random parts (violating rule 1). Some models of type B included only time-invariant country-level variables, for which the SE should be unbiased, though they did not take advantage of the longitudinal properties of the data.

For practical reasons, different applied researchers may be thinking about this issue in different ways: some software requires users to specify the level of a variable, and provides a warning when variables are not constant within the relevant clusters. Other software, however, does not. Mplus and HLM require specifying the measurement level of each variable and thereby force users to become aware of this issue. Mplus even aborts estimation if cluster-level variables are not constant within clusters. MLwiN and HLM provide model equations, with subscripts indicating at which level the variables are assumed to be measured. In SPSS, Stata, R, and SAS, it is not necessary to specify the measurement levels. However, SPSS and SAS provide approximate degrees of freedom, which is indirect information about the measurement levels. [Online Appendix C](#) provides estimates from and some information about the most often used packages: MLwiN, Stata, R, HLM, SPSS, SAS, and Mplus.

Excluding relevant REs can lead to severely misleading inferences. Our recommendation to researchers is thus similar to Barr *et al.*'s (2013), in their recent demonstration of the importance of random slopes in multilevel models: 'keep it maximal'. If there is absolutely no random variation at a given level, our simulation study has shown that redundant REs may yield over-conservative SEs. But assuming that a given model converges, including a redundant RE should in practice do no harm, as there will always be some random error at any level.

Notes

- 1 Multilevel models are also known as random effects, mixed, or hierarchical models. We use the former term as it is the one most often used in the context of survey data analyses.
- 2 In this article we deal with RE models. There are alternative ways of accounting for clustered data, which we do not discuss here. Readers who are interested in this are referred to Bell and Jones (2014) for a comparison of random and fixed effects and to King and Roberts (2014) for a treatment of clustered standard errors.
- 3 For clarity, when we refer to fixed effects at a given level, we mean covariates measured at that level, not unit dummies intended to capture variance at that level.
- 4 There are two more logically possible combinations of RE—RE only at the year-level and no RE at all—but these are irrelevant in practice. The latter would not be a multilevel model, and the former would completely ignore the comparative character of the

data. In our coding, we found some studies fitting single-level models to multilevel data, in some but not all cases using clustered standard errors; but we do not address those here.

- 5 We performed the search on 27 March 2014. Detailed information on each stage of our coding process is included in [Online Appendix A](#).
- 6 However, 9 of 14 of these articles did not account for the clustering at the levels of geographical clusters at all. They estimated simple panel models but did not include REs for the geographical clusters.
- 7 Our simulation set-up implies that the variances of the covariates at the level of countries and country-years are of equal size. This condition might not be true in all real-life settings, where between-country variances often tend to be larger than variances at the country-year level, though the opposite can also be true. The bias that results from ignoring a level depends on the variance at this level.
- 8 The ESS data sets are continuously updated. We have not been able to determine precisely why, but some of the variables that were used in the study appear to have been problematic for some countries, and so have been removed from the available ESS data sets.

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Supplementary Data

[Supplementary data](#) are available at *ESR* online.

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Appendix

Table A1. Re-estimation of models from Table 5 with country-year-level variables decomposed into within- and between-country effects

	Model A	Model B	Model C	Model D	Model E	Model F
	b/se	b/se	b/se	b/se	b/se	b/se
Individual-level data						
Left-right	-0.0853*** (0.0012)	-0.0854*** (0.0012)	-0.0853*** (0.0012)	-0.0853*** (0.0012)	-0.0855*** (0.0012)	-0.0853*** (0.0012)
Gender (male = 1)	-0.1225*** (0.0054)	-0.1217*** (0.0054)	-0.1225*** (0.0054)	-0.1224*** (0.0054)	-0.1217*** (0.0054)	-0.1224*** (0.0054)
Age	0.0031*** (0.0002)	0.0030*** (0.0002)	0.0031*** (0.0002)	0.0031*** (0.0002)	0.0030*** (0.0002)	0.0031*** (0.0002)
Household income	-0.0799*** (0.0022)	-0.076*** (0.0022)	-0.0799*** (0.0022)	-0.0796*** (0.0022)	-0.0760*** (0.0022)	-0.0796*** (0.0022)
Employment status						
Employed	Ref.	Ref.	Ref.	Ref.	Ref.	Ref.
Unemployed	0.0866*** (0.0126)	0.0881*** (0.0127)	0.0866*** (0.0126)	0.0866*** (0.0126)	0.0876*** (0.0127)	0.0866*** (0.0126)
Not in labour force	-0.0225*** (0.0064)	-0.0202** (0.0064)	-0.0225*** (0.0064)	-0.0223*** (0.0064)	-0.0204** (0.0064)	-0.0223*** (0.0064)
Education						
ISCED 0–1	Ref.	Ref.	Ref.	Ref.	Ref.	Ref.
ISCED 2	0.0641*** (0.0104)	0.0625*** (0.0105)	0.0641*** (0.0104)	0.0648*** (0.0104)	0.0639*** (0.0105)	0.0648*** (0.0104)
ISCED 3	0.0184 (0.0101)	0.0150 (0.0101)	0.0185 (0.0101)	0.0194 (0.0101)	0.0146 (0.0101)	0.0194 (0.0101)
ISCED 4	-0.0597** (0.0216)	-0.0607** (0.0215)	-0.0597** (0.0216)	-0.0584** (0.0216)	-0.0575** (0.0215)	-0.0584** (0.0216)
ISCED 5–6	-0.1851*** (0.0106)	-0.1899*** (0.0106)	-0.1851*** (0.0106)	-0.1844*** (0.0106)	-0.1904*** (0.0106)	-0.1844*** (0.0106)
Bad health	0.0677*** (0.0063)	0.0704*** (0.0063)	0.0677*** (0.0063)	0.0679*** (0.0063)	0.0703*** (0.0063)	0.0679*** (0.0063)
Country-level data						
GDP/C (in 1,000\$) [BE]	-0.0092** (0.0033)	-0.0101 (0.0053)	-0.0092** (0.0033)	-0.0101 (0.0054)	-0.0093 (0.0053)	-0.0101 (0.0054)
GDP/C (in 1,000\$) [WE]	0.0084 (0.0066)	0.0055*** (0.0007)	0.0084 (0.0066)	0.0067** (0.0023)	-0.0022 (0.0017)	0.0067** (0.0023)
Gini index [BE]	0.0066 (0.0070)	0.0064 (0.0118)	0.0066 (0.0070)	0.0072 (0.0121)	0.0080 (0.0119)	0.0072 (0.0121)
Gini index [WE]	0.0220 (0.0209)	0.0237*** (0.0023)	0.0220 (0.0209)	0.0239*** (0.0073)	0.0213*** (0.0023)	0.0239*** (0.0073)
Social spending [BE]	-0.0149** (0.0070)	-0.0143 (0.0116)	-0.0149** (0.0070)	-0.0136 (0.0119)	-0.0137 (0.0117)	-0.0136 (0.0119)
Social spending [WE]	0.0098 (0.0211)	0.0107*** (0.0023)	0.0098 (0.0211)	0.0098 (0.0073)	-0.0034 (0.0034)	0.0098 (0.0073)
Unemployment rate [BE]	0.0208** (0.0082)	0.0158 (0.0151)	0.0208** (0.0082)	0.0161 (0.0154)	0.0157 (0.0153)	0.0161 (0.0154)
Unemployment rate [WE]	-0.0016 (0.0156)	-0.0028 (0.0017)	-0.0016 (0.0156)	-0.0022 (0.0054)	-0.0011 (0.0018)	-0.0022 (0.0054)
Constant	4.7050*** (0.3156)	4.7824*** (0.5390)	4.7050*** (0.3156)	4.7433*** (0.5506)	4.6995*** (0.5442)	4.7433*** (0.5507)

(continued)

Table A1. Continued

	Model A	Model B	Model C	Model D	Model E	Model F
	b/se	b/se	b/se	b/se	b/se	b/se
Variance components						
Country		0.0524437 (0.014329)		0.0525917 (0.014838)	0.0533606 (0.014593)	0.0526005 (0.014841)
Year			0.0000000 (0.000000)		0.0022625 (0.001781)	0.0000000 (0.000000)
Country-year	0.0634200 (0.008866)		0.0634276 (0.008868)	0.0068894 (0.001220)		0.0068889 (0.001222)
Individuals	0.9305877 (0.003610)	0.9358312 (0.003629)	0.9305876 (0.003610)	0.9305857 (0.003610)	0.9355842 (0.003629)	0.9305857 (0.003614)

Note: * $P < 0.05$, ** $P < 0.01$, *** $P < 0.001$; [BE] = between effect, [WE] = within effect. All models are based on 133,301 individual observations and data from 27 countries and 105 country-years. Models estimated with Stata's xtmixed command.

Source: ESS (2002–2010).