Multilevel Modellingcourse: DAY 3

University of Zurich PD Dr. Conrad Ziller conrad.ziller@uni-due.de https://conradziller.com

Schedule for Day 3

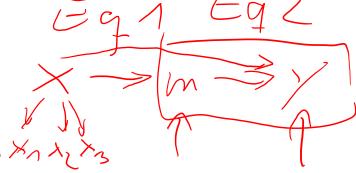
- Mediation
- Growth curve models
- Logit models (FYI)
- Your models your questions my advise

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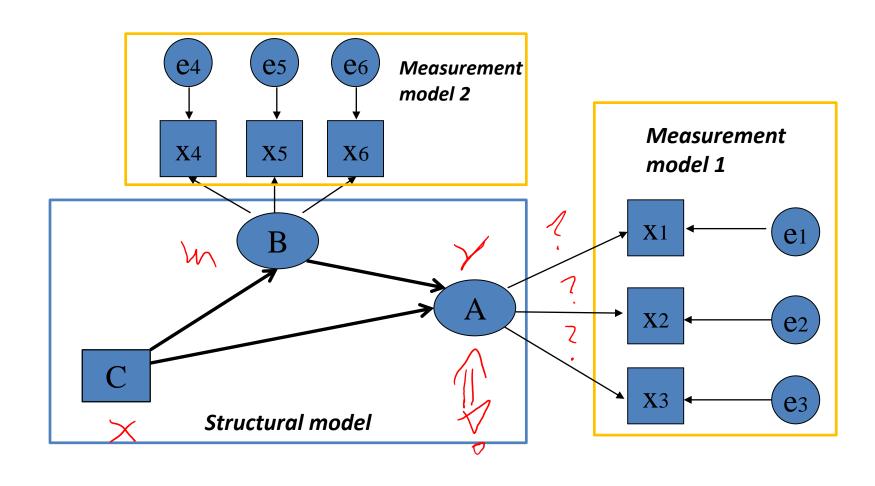
Structural Equation Models

Structural Equation Models (= SEM)

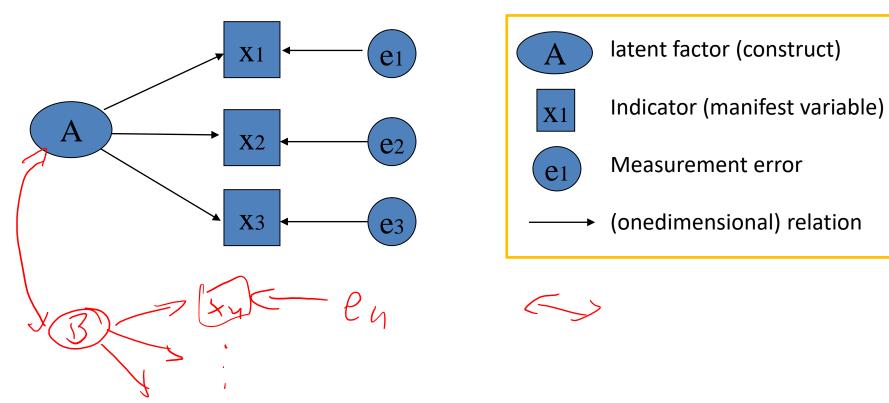


- consist of systems of equations > \(\lambda \lam
- can be divided into measurement models and structural models
- direct and indirect effects can be distinguished (mediation)
- distinguish between latent (non-measured) and manifest (measured) variables
- typical graphical representation of the models

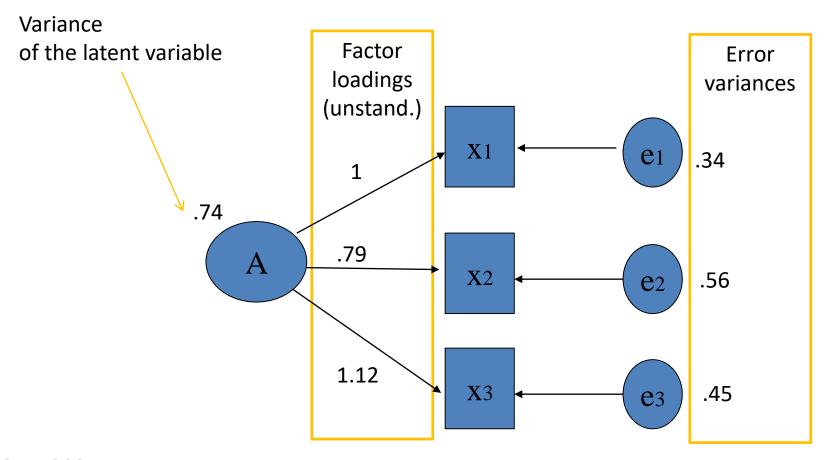
Structural Equation Models



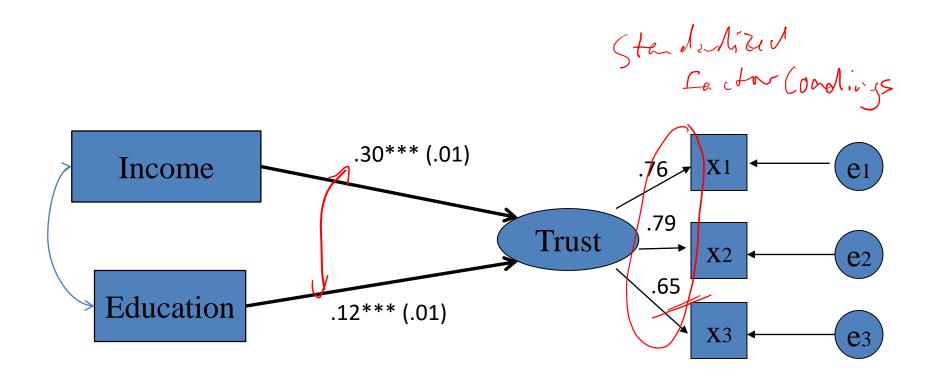
Measurement Model with one Factor



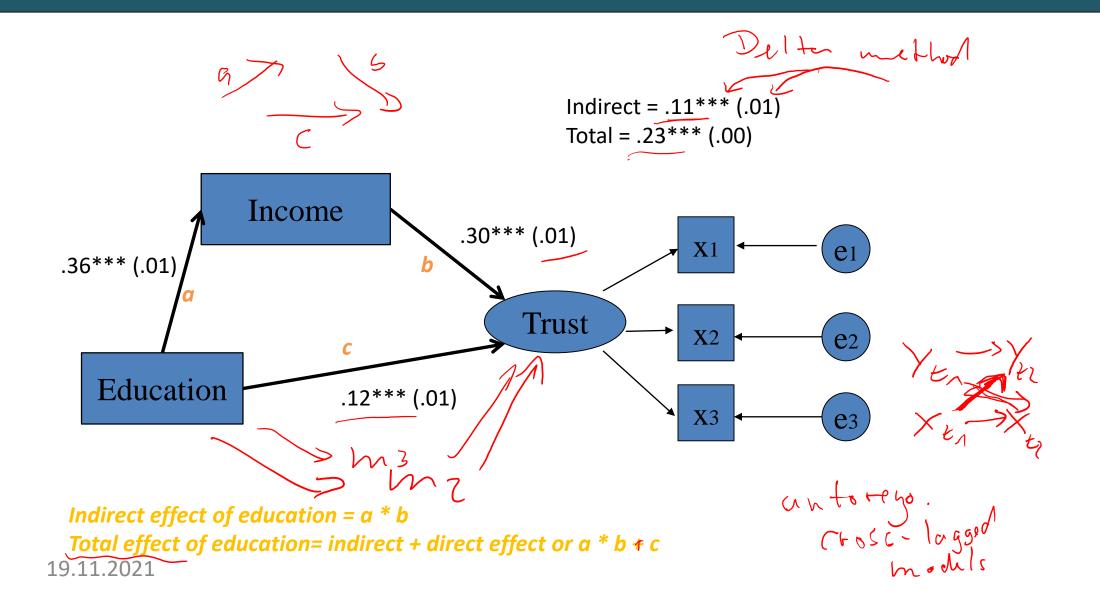
Measurement Model: Parameter (Loadings and variances)



Example 1: Social Trust



Example 2: Social Trust

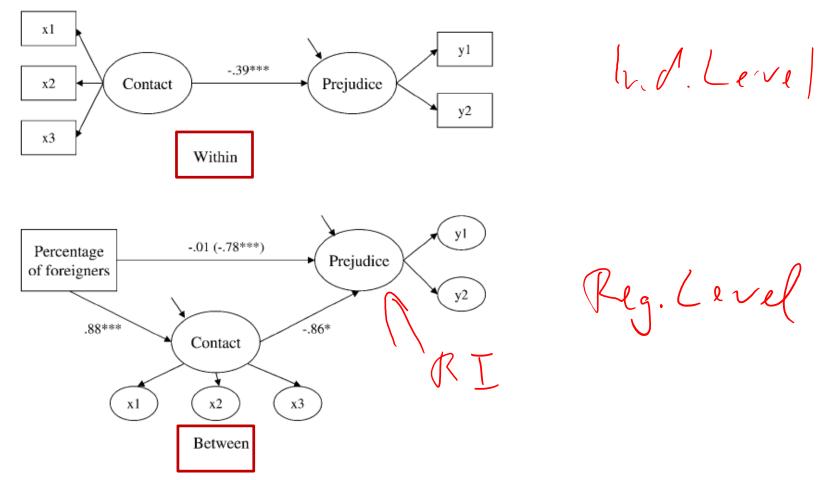


Stata

```
CKA
          * Example 1
sem (ppltrst pplfair pplhlp <- Trust) ///

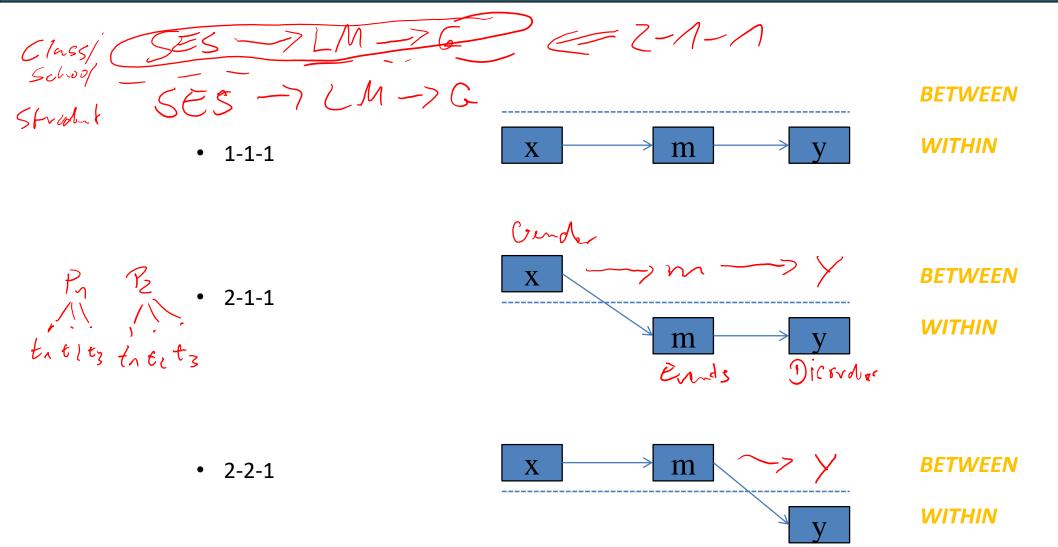
(Trust <- income educyears) , latent(Trust) stand
estat gof , stats(all) // shows fit-indices</pre>
           * Example 2
                                                CFA
           sem (ppltrst pplfair pplhlp <- Trust) ///
   5 ₹ \ (Trust <- income educyears) ///
     (income <- educyears) , latent(Trust) stand
      ____ estat teffects, stand //shows indirect effect
         estat gof , stats(all)
                                OF1 -7155
                                RMEA C 0.05
```

Example Multi-Level SEM



Wagner, U., Christ, O., Pettigrew, T.F., Stellmacher, J., & Wolf, C. (2006). Prejudice and minority proportion: Contact instead of threat effects. *Social Psychology Quarterly*, *69*, 380-390.

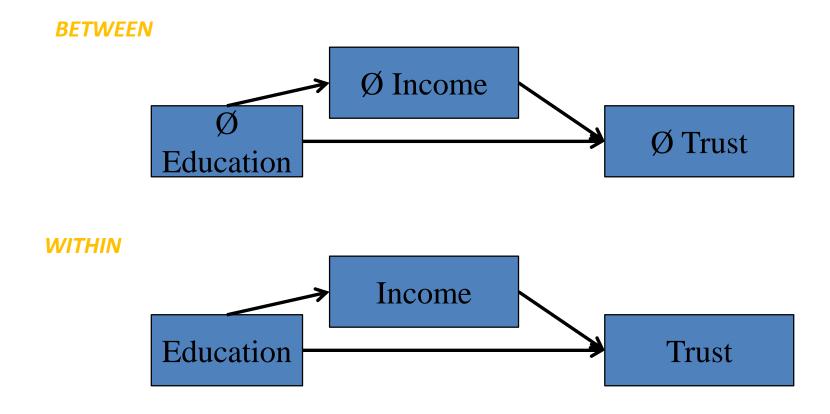
Typical Multi-Level SEM-Mediationmodel



Multi-Level SEM

- Without latent variables or mediation, multilevel regression and multilevel SEM produce equivalent results
- Latent measurement models (CFA) only reliable with large number of clusters (> 60)
- With multilevel mediation and level-2 involved, the between-level is one that is interpreted (Preacher et al. 2010)
- Mplus has enormous advantages over Stata in specifying ML-SEM models; Mplus syntax see http://www.quantpsy.org/pubs/syntax appendix 081311.pdf
- In R: lavaan package mimicks Mplus; Stata: gsem (slow and often does not converge)

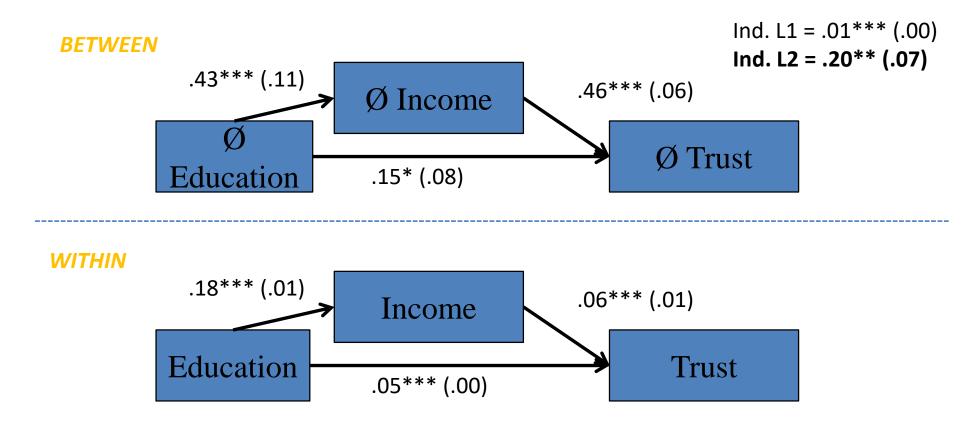
Example 3: Social Trust on Individual and Country-Level



Mplus – Output

MODEL RESULTS				
	Estimate	S.E.	Est./S.E.	Two-Tailed P-Value
Within Level				
TRUST ON INCOME EDUCYEARS	0.056 0.046	0.011	5.286 11.346	0.000
INCOME ON EDUCYEARS	0.177	0.009	20.568	0.000
Residual Variance TRUST INCOME	3.063 3.487	0.157 0.193	19.554 18.066	0.000
Between Level				
TRUST ON INCOME EDUCYEARS	0.458 0.148	0.062 0.076	7.443 1.960	0.000 0.050
INCOME ON EDUCYEARS	0.429	0.113	3.801	0.000
Intercepts TRUST INCOME	0.669 1.022	0.870 1.342	0.769 0.761	0.442 0.447
Residual Variance TRUST INCOME	0.212 1.646	0.048	4.462 2.681	0.000
New/Additional Pa	0.010 0.196	0.002 0.070	5.752 2.814	0.000

Example 3: Social Trust on Individual- and Country – Level



Group session

Come together in groups and find examples for all three types of multilevel mediation:

Predictor-Mediator-Outcome

L1-L1-L1

L2-L1-L1

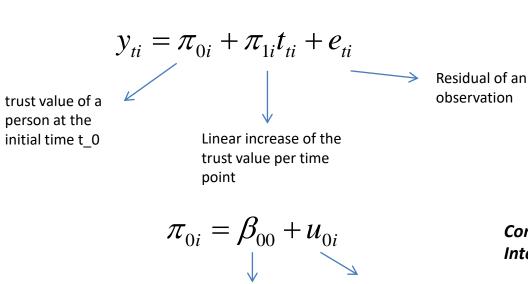
L2-L2-L1

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Questions (example DV: Social trust, period 2002-2006)

- 1. Can a change in social trust be observed in the period 2002-2006 and (b) is there variability in the change over time between respondents?
- 2. If there is significant variability in change over time, can this variability be explained by specific variables?
- Growth curve models can be estimated as ML regression models as well as ML-SEM models
- Complex, non-linear developments can be taken into account
- Particularly suitable for genuine panel data of individuals
- Attention: Both between- and within-variance are included in the estimates (no separation between the two)



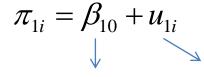


Basically a RIRS-model with repeated measurements nested in persons (random intercept) & with time as predictor and random slope

$$\pi_{0i} = \beta_{00} + u_{0i}$$

Overall average at baseline

Comparable with Random Intercept



Average linear increase per time point

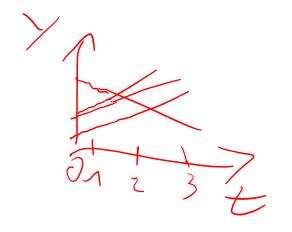
Deviation speed of increase/decrease

Deviations of single

for an individual

individuals

Comparable with Random Slope



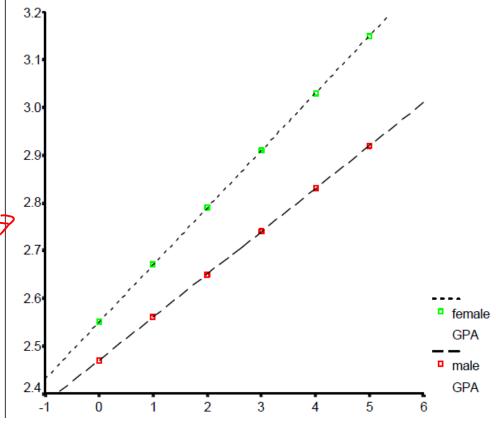
- Additional time-varying and time-constant covariates can be added
- In interaction with time, we want to explain different temporal trajectories with substantial variables (e.g., does gender (Z) explain the found variability in over-time development across individuals $(u_{1i}) \rightarrow$ cross-level interaction
- Polynomial curves can be added by including quadratic, cubic, ... time effects; even dummy variables for time are feasible
- Growth curve models allow for unbalanced panel data

What it

• Example Hox (2010: 90)

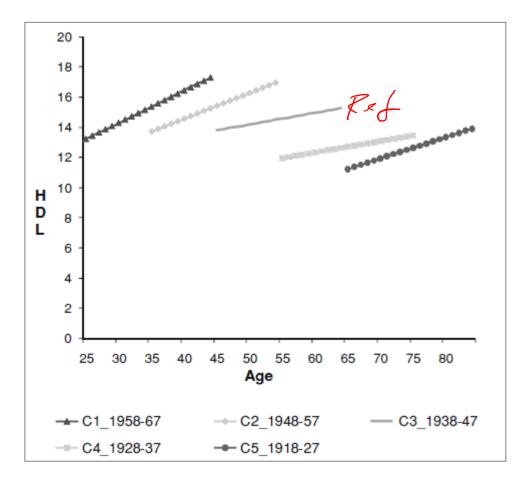
$$GPA_{ti} = \beta_{00} + \beta_{10}Time_{ti} + \beta_{20}Job_{ti} + \beta_{01}Sex_{i}$$
$$+ \beta_{11}Sex_{i}Time_{ti} + u_{1i}Time_{ti} + u_{0i} + \varepsilon_{ti}$$

	Fixed part	Coeff.	S.E.
fine-	Intercept	2.58	(0.09)
	Occasion	0.09	(0.01)
	Job status	-0.13	(0.02)
	GPA highschool	0.09	(0.03)
	Gender	0.08	(0.03)
	Occasion*Gender	0.03	(0.01)
	Random part		
	$\sigma^2(e)$	0.042	(0.002)
	σ²(u0)	0.038	(0.010)
	$\sigma^2(u1)$	0.004	(0.001)
	σ(u0 u1)	-0.002	(0.001)



Example: Brault, M.-C., Meuleman, B. & Bracke, P. (2012) Depressive symptoms in the Belgian population: disentangling age and cohort effects. *Journal of Social Psychiatry and Psychiatric Epidemiology*.

Fixed effects					
Initial status			Growth rate		
Intercept y ₀₀	13.65	***	Agec y_{10}	0.054	
C1 1958-1967	4.366	***	Agec2 y ₂₀		
C2 1948-1957	1.930	***	Agec \times C1_5867	0.165	***
C3 1938-1947	REF		Agec \times C2_4857	0.105	**
C4 1928–1937	-2.808	***	Agec \times C3_3847	REF	
C5 1918–1927	-5.489	***	Agec \times C4_2837	-0.003	
THE STATE OF THE S			Agec \times C5_1827	0.065	
Woman	3.360	***	Variance components (random effects)		
Education	-0.084	*	Level 1: within-person	30.315	***
Married	REF		Level 2: in initial status	43.739	***
Single/widowed	0.248		Level 2: in linear growth	0.087	***
Divorced/separated	0.349		Proportion of variance explained		
Partner	-1.042	**	Within-person	2.147	6.6%
Monthly income €	-0.163		In initial status	7.708	15.0%
Employed	-0.609	***	In linear growth	0.008	8.4%



Stata

(1) Lever)/cover

Growth curve modeling in R see https://rpsychologist.com/r-guide-longitudinal-lme-lmer

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Logistic Multilevel-Analysis

- Modelling dichotomous dependent variables as a function of individual and contextual explanatory factors $P(y_{ij} = 1 \mid x_{ij}, z_j)$
- Random Intercept Model
 - Logistic regression function for each country separately

$$\ln\left(\frac{p}{1-p}\right) = \beta_{0j} + \beta_{1j}x_{ij}$$
No error term!
Overall effect of x on the log(odds)

Average log(odds) in each group

Logistic Multilevel-Analysis

- Random Intercept Modell
 - Determination of the group-specific intercepts

$$\beta_{0j} = \gamma_{00} + u_{0j}$$

Average log(odds) across Difference in logged odds für group j all groups

$$\ln\left(\frac{p}{1-p}\right) = \gamma_{00} + \beta_{1j}x_{ij} + u_{0j}$$

Logistic Multilevel-Analysis

- Residual variance is fixed at Pi^2/3
- ICC is computed as

$$ICC = \frac{\sigma_{u0}^{2}}{\sigma_{u0}^{2} + \pi^{2}/3}$$

- Fixation leads to rescaling of coefficients in case of model changes; makes comparison of models difficult (calculate marginal effects!)
- Model fit as proportional reduction of variance

$$R_{MZ}^{2} = \frac{\sigma_{F}^{2}}{\sigma_{F}^{2} + \sigma_{u0}^{2} + \pi^{2}/3}$$

 σ_F^2 = Residual variance of a linear prediction of the estimated model parameters (see Snijders & Bosker 2012: 306)

Stata

```
//compute ICC
disp var(cons) / (var(cons) + pi^2 / 3)
//Random Intercept Modell
melogit DV IV1 IV2 ... ||id:
//Random Slope Modell
melogit DV IV1 IV2 ... ||id: IV1 , cov(un)
margins, dydx(*) predict(mu fixedonly)
In R: m_rs <- glmer(outcome ~ predictor1 + predictor2 + (1 | id), data = essdata, family = binomial)
Cf. https://stats.idre.ucla.edu/r/dae/mixed-effects-logistic-regression/
```

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|Assignment|

To successfully participate in the course:

- participants are required to conduct their own multilevel regression analysis and to describe their methodological approach and results (similar to the sections from typical journal articles)
- handed-in document of about 3-4 pages
- Please hand in DOCUMENT plus SYNTAX until Monday Dec 13th, 2021, sent to conrad.ziller@uni-due.de

Thank you for your Attention!