| | Similar categories with all | PER with all | Similar categories | PER |
|----------------|-----------------------------|--------------|--------------------|-----------|
| 1 | 1.00 | 1.00000 | 1.00000 | 1.00000 |
| 2 | 0.930956 | 0.92755 | 0.924195 | 0.926502 |
| 3 | 0.511111 | 0.480658 | 0.589682 | 0.484003 |
| 4 | 0.312352 | 0.26111 | 0.393565 | 0.266244 |
| 5 | 0.19176 | 0.189493 | 0.240241 | 0.19042 |
| 6 | 0.095767 | 0.120565 | 0.130477 | 0.120447 |
| 7 | 0.125765 | 0.06027 | 0.123729 | 0.068036 |
| Path distances | 23.087669 | 26.08464 | 20.197252 | 25.794379 |
| | | | | |

Table 1

| Cross Validation Number | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | |
|-------------------------------|---|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-----------|
| Classify with | 1 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00 |
| similar products and | 2 | 0.92203 | 0.93051 | 0.94068 | 0.93898 | 0.92542 | 0.93718 | 0.92699 | 0.92869 | 0.93039 | 0.92869 | 0.930956 |
| included all samples | 3 | 0.48475 | 0.52203 | 0.51017 | 0.50678 | 0.52542 | 0.51952 | 0.51952 | 0.52462 | 0.48387 | 0.51443 | 0.511111 |
| oampieo | 4 | 0.30000 | 0.33107 | 0.30339 | 0.31186 | 0.33051 | 0.32937 | 0.31409 | 0.31749 | 0.29202 | 0.29372 | 0.312352 |
| | 5 | 0.18462 | 0.21062 | 0.19178 | 0.19145 | 0.20548 | 0.20654 | 0.18182 | 0.17607 | 0.18151 | 0.18771 | 0.19176 |
| | 6 | 0.09350 | 0.10559 | 0.10000 | 0.08108 | 0.10381 | 0.09434 | 0.09485 | 0.08384 | 0.09278 | 0.10788 | 0.095767 |
| | 7 | 0.15385 | 0.21429 | 0.05882 | 0.05882 | 0.05263 | 0.11111 | 0.13333 | 0.14286 | 0.11765 | 0.21429 | 0.125765 |
| | | 23.23599 | 22.49661 | 23.22034 | 23.35424 | 22.56102 | 22.56706 | 23.07131 | 23.41766 | 23.71647 | 23.23599 | 23.087669 |
| Classify with | 1 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 |
| PER and included all | 2 | 0.92699 | 0.92712 | 0.93729 | 0.93559 | 0.91864 | 0.93379 | 0.92190 | 0.92020 | 0.92699 | 0.92699 | 0.92755 |
| samples | 3 | 0.47708 | 0.49492 | 0.49661 | 0.47458 | 0.46610 | 0.49745 | 0.48048 | 0.47029 | 0.47199 | 0.47708 | 0.480658 |
| | 4 | 0.25637 | 0.27627 | 0.26949 | 0.25932 | 0.26271 | 0.28014 | 0.24788 | 0.24618 | 0.25637 | 0.25637 | 0.26111 |
| | 5 | 0.18771 | 0.19554 | 0.19761 | 0.19454 | 0.20684 | 0.20000 | 0.18027 | 0.17206 | 0.17265 | 0.18771 | 0.189493 |
| | 6 | 0.12522 | 0.12852 | 0.11478 | 0.10601 | 0.12698 | 0.12324 | 0.12090 | 0.11652 | 0.11826 | 0.12522 | 0.120565 |
| | 7 | 0.06667 | 0.06000 | 0.04878 | 0.04545 | 0.04545 | 0.05263 | 0.05455 | 0.06250 | 0.10000 | 0.06667 | 0.06027 |
| | | 26.20204 | 25.70339 | 25.74576 | 26.02881 | 25.99831 | 25.85739 | 26.50594 | 26.51443 | 26.08829 | 26.20204 | 26.08464 |
| Classify with | 1 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 |
| similar products | 2 | 0.92731 | 0.92952 | 0.94053 | 0.91189 | 0.91630 | 0.92070 | 0.92070 | 0.92511 | 0.93157 | 0.91832 | 0.924195 |
| with bad samples | 3 | 0.59251 | 0.61894 | 0.57930 | 0.59692 | 0.57489 | 0.59471 | 0.56828 | 0.61454 | 0.59382 | 0.56291 | 0.589682 |
| removed | 4 | 0.40529 | 0.41630 | 0.39207 | 0.37665 | 0.37885 | 0.38987 | 0.38106 | 0.40969 | 0.40839 | 0.37748 | 0.393565 |
| | 5 | 0.24722 | 0.25390 | 0.23490 | 0.23333 | 0.24161 | 0.22717 | 0.22148 | 0.26786 | 0.23991 | 0.23503 | 0.240241 |
| | 6 | 0.15850 | 0.12766 | 0.13239 | 0.12500 | 0.12798 | 0.12462 | 0.11143 | 0.12462 | 0.13393 | 0.13864 | 0.130477 |
| | 7 | 0.05263 | 0.04762 | 0.09091 | 0.11765 | 0.11765 | 0.14286 | 0.21429 | 0.10526 | 0.11765 | 0.23077 | 0.123729 |
| | | 20.18943 | 19.50220 | 20.88546 | 20.29295 | 20.29956 | 20.04626 | 20.94273 | 19.28855 | 19.99779 | 20.52759 | 20.197252 |
| | | | | | | | | | | | | |
| Classify with PER with | 1 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 | 1.00000 |
| bad samples | 2 | 0.92857 | 0.91837 | 0.93027 | 0.93197 | 0.92007 | 0.93197 | 0.93707 | 0.92687 | 0.91993 | 0.91993 | 0.926502 |
| removed | 3 | 0.48639 | 0.48469 | 0.48129 | 0.48980 | 0.47789 | 0.49490 | 0.49660 | 0.48980 | 0.46167 | 0.47700 | 0.484003 |
| | 4 | 0.26531 | 0.26020 | 0.26531 | 0.25510 | 0.26701 | 0.29592 | 0.27891 | 0.26361 | 0.25724 | 0.25383 | 0.266244 |
| | 5 | 0.17979 | 0.18259 | 0.20000 | 0.16894 | 0.19728 | 0.20000 | 0.19966 | 0.18664 | 0.19759 | 0.19171 | 0.19042 |
| | 6 | 0.11713 | 0.12195 | 0.11498 | 0.09532 | 0.13884 | 0.11964 | 0.13369 | 0.10545 | 0.13556 | 0.12191 | 0.120447 |
| | 7 | 0.07692 | 0.06977 | 0.06250 | 0.03636 | 0.07317 | 0.05000 | 0.08696 | 0.06977 | 0.06667 | 0.08824 | 0.068036 |
| | | 25.59694 | 26.08673 | 25.73299 | 26.69388 | 25.97279 | 25.30612 | 24.83503 | 25.76361 | 26.18228 | 25.77342 | 25.794379 |

Table 1

| Cross Validation Number | | | | 1 | | | 2 | | | 3 | | | 4 | | | 5 | | | 6 | | | 7 | | | 8 | | | 9 | | | 10 |
|-------------------------------|---|---------|-----|----------------|---------|-----|----------------|---------|-----|----------------|---------|-----|----------------|----------|-----|----------------|--------------|-----|----------------|---------|-----|----------------|---------|-----|----------------|---------|-----|----------------|---------|-----|----------|
| Classify with | 1 | 1.00000 | 590 | 590 | 1.00000 | 590 | 590 | 1.00000 | 590 | 590 | 1.00000 | 590 | 590 | 1.00000 | 590 | 590 | 1.00000 | 589 | 589 | 1.00000 | 589 | 589 | 1.00000 | 589 | 589 | 1.00000 | 589 | 589 | 1.00000 | 589 | 589 |
| similar products and | 2 | 0.92203 | 544 | 590 | 0.93051 | 549 | 590 | 0.94068 | 555 | 590 | 0.93898 | 554 | 590 | 0.92542 | 546 | 590 | 0.93718 | 552 | 589 | 0.92699 | 546 | 589 | 0.92869 | 547 | 589 | 0.93039 | 548 | 589 | 0.92869 | 547 | 589 |
| included all samples | 3 | 0.48475 | 286 | 590 | 0.52203 | 308 | 590 | 0.51017 | 301 | 590 | 0.50678 | 299 | 590 | 0.52542 | 310 | 590 | 0.51952 | 306 | 589 | 0.51952 | 306 | 589 | 0.52462 | 309 | 589 | 0.48387 | 285 | 589 | 0.51443 | 303 | 589 |
| | 4 | 0.30000 | 177 | 590 | 0.33107 | 195 | 589 | 0.30339 | 179 | 590 | 0.31186 | 184 | 590 | 0.33051 | 195 | 590 | 0.32937 | 194 | 589 | 0.31409 | 185 | 589 | 0.31749 | 187 | 589 | 0.29202 | 172 | 589 | 0.29372 | 173 | 589 |
| | 5 | 0.18462 | 108 | 585 | 0.21062 | 123 | 584 | 0.19178 | 112 | 584 | 0.19145 | 112 | 585 | 0.20548 | 120 | 584 | 0.20654 | 120 | 581 | 0.18182 | 106 | 583 | 0.17607 | 103 | 585 | 0.18151 | 106 | 584 | 0.18771 | 110 | 586 |
| | 6 | 0.09350 | 46 | 492 | 0.10559 | 51 | 483 | 0.10000 | 48 | 480 | 0.08108 | 39 | 481 | 0.10381 | 49 | 472 | 0.09434 | 45 | 477 | 0.09485 | 46 | 485 | 0.08384 | 41 | 489 | 0.09278 | 45 | 485 | 0.10788 | 52 | 482 |
| | 7 | 0.15385 | 2 | 13 | 0.21429 | 3 | 14 | 0.05882 | 1 | 17 | 0.05882 | 1 | 17 | 0.05263 | 1 | 19 | 0.11111 | 2 | 18 | 0.13333 | 2 | 15 | 0.14286 | 3 | 21 | 0.11765 | 2 | 17 | 0.21429 | 3 | 14 |
| | | | | 23.23599 | | | 22.49661 | | | 23.22034 | | | 23.35424 | | | 22.56102 | | | 22.56706 | | | 23.07131 | | | 23.41766 | | | 23.71647 | | | 23.23599 |
| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Classify with PER and | 1 | 1.00000 | 589 | 589 | 1.00000 | 590 | 590 | 1.00000 | 590 | 590 | 1.00000 | 590 | 590 | 1.00000 | 590 | 590 | 1.00000 | 589 | 589 | 1.00000 | 589 | 589 | 1.00000 | 589 | 589 | 1.00000 | 589 | 589 | 1.00000 | 589 | 589 |
| included all | 2 | 0.92699 | 546 | 589 | 0.92712 | 547 | 590 | 0.93729 | 553 | 590 | 0.93559 | 552 | 590 | 0.91864 | 542 | 590 | 0.93379 | 550 | 589 | 0.92190 | 543 | 589 | 0.92020 | 542 | 589 | 0.92699 | 546 | 589 | 0.92699 | 546 | 589 |
| samples | 3 | 0.47708 | 281 | 589 | 0.49492 | 292 | 590 | 0.49661 | 293 | 590 | 0.47458 | 280 | 590 | 0.46610 | 275 | 590 | 0.49745 | 293 | 589 | 0.48048 | 283 | 589 | 0.47029 | 277 | 589 | 0.47199 | 278 | 589 | 0.47708 | 281 | 589 |
| | 4 | 0.25637 | 151 | 589 | 0.27627 | 163 | 590 | 0.26949 | 159 | 590 | 0.25932 | 153 | 590 | 0.26271 | 155 | 590 | 0.28014 | 165 | 589 | 0.24788 | 146 | 589 | 0.24618 | 145 | 589 | 0.25637 | 151 | 589 | 0.25637 | 151 | 589 |
| | 5 | 0.18771 | 110 | 586 | 0.19554 | 114 | 583 | 0.19761 | 116 | 587 | 0.19454 | 114 | 586 | 0.20684 | 121 | 585 | 0.20000 | 117 | 585 | 0.18027 | 106 | 588 | 0.17206 | 101 | 587 | 0.17265 | 101 | 585 | 0.18771 | 110 | 586 |
| | 6 | 0.12522 | 72 | 575 | 0.12852 | 73 | 568 | 0.11478 | 66 | 575 | 0.10601 | 60 | 566 | 0.12698 | 72 | 567 | 0.12324 | 70 | 568 | 0.12090 | 70 | 579 | 0.11652 | 67 | 575 | 0.11826 | 68 | 575 | 0.12522 | 72 | 575 |
| | 7 | 0.06667 | 3 | 45 | 0.06000 | 3 | 50 | 0.04878 | 2 | 41 | 0.04545 | 2 | 44 | 0.04545 | 2 | 44 | 0.05263 | 3 | 57 | 0.05455 | 3 | 55 | 0.06250 | 3 | 48 | 0.10000 | 3 | 30 | 0.06667 | 3 | 45 |
| | | | | 26.20204 | | | 25.70339 | | | 25.74576 | | | 26.02881 | | | 25.99831 | | | 25.85739 | | | 26.50594 | | | 26.51443 | | | 26.08829 | | | 26.20204 |
| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Classify with similar | 1 | 1.00000 | 454 | 454 | 1.00000 | 454 | 454 | 1.00000 | 454 | 454 | 1.00000 | 454 | 454 | 1.00000 | 454 | 454 | 1.00000 | 454 | 454 | 1.00000 | 454 | 454 | 1.00000 | 454 | 454 | 1.00000 | 453 | 453 | 1.00000 | 453 | 453 |
| products with bad | 2 | 0.92731 | 421 | 454 | | 422 | 454 | 0.94053 | 427 | 454 | 0.91189 | 414 | 454 | 0.91630 | 416 | 454 | 0.92070 | 418 | 454 | 0.92070 | 418 | 454 | 0.92511 | 420 | 454 | 0.93157 | 422 | 453 | 0.91832 | 416 | 453 |
| samples | 3 | 0.59251 | 269 | 454 | | 281 | 454 | 0.57930 | 263 | 454 | 0.59692 | 271 | 454 | 0.57489 | 261 | 454 | 0.59471 | 270 | 454 | 0.56828 | 258 | 454 | 0.61454 | 279 | 454 | 0.59382 | 269 | 453 | 0.56291 | 255 | 453 |
| removed | 4 | 0.40529 | 184 | 454 | | 189 | 454 | 0.39207 | 178 | 454 | 0.37665 | 171 | 454 | 0.37885 | 172 | 454 | 0.38987 | 177 | 454 | 0.38106 | 173 | 454 | 0.40969 | 186 | 454 | 0.40839 | 185 | 453 | 0.37748 | 171 | 453 |
| _ | 5 | 0.24722 | 111 | 449 | | 114 | 449 | 0.23490 | 105 | 447 | 0.23333 | 105 | 450 | 0.24161 | 108 | 447 | 0.22717 | 102 | 449 | 0.22148 | 99 | 447 | 0.26786 | 120 | 448 | 0.23991 | 107 | 446 | 0.23503 | 106 | 451 |
| | 7 | 0.15850 | 55 | 347 | | 42 | 329 | 0.13239 | 47 | 355 | 0.12500 | 42 | 336 | 0.12798 | 43 | 336 17 | 0.12462 | 41 | 329 | 0.11143 | 39 | 350 | 0.12462 | 41 | 329 | 0.13393 | 45 | 336 17 | 0.13864 | 47 | 339 |
| - | 7 | 0.05263 | 1 | 20.18943 | | ı | 19.50220 | 0.09091 | 2 | 22 20.88546 | 0.11765 | 2 | 20.29295 | 0.11765 | 2 | 20.29956 | 0.14286 | 2 | 20.04626 | 0.21429 | 3 | 20.94273 | 0.10526 | 2 | 19 19.28855 | 0.11765 | 2 | 19.99779 | 0.23077 | 3 | 20.52759 |
| | | | | 20.16943 | | | 19.50220 | | | 20.00340 | | | 20.29295 | | | 20.29950 | | | 20.04020 | | | 20.94273 | | | 19.20000 | | | 19.99779 | | | 20.52759 |
| Classify with | 1 | 1.00000 | 588 | 588 | 1.00000 | 588 | 588 | 1.00000 | 588 | 588 | 1.00000 | 588 | 588 | 1.00000 | 588 | 588 | 1.00000 | 588 | 588 | 1.00000 | 588 | 588 | 1.00000 | 588 | 588 | 1.00000 | 587 | 587 | 1.00000 | 587 | 587 |
| PER with | 2 | 0.92857 | 546 | 588 | | 540 | 588 | 0.93027 | 547 | 588 | 0.93197 | 548 | 588 | 0.92007 | 541 | 588 | 0.93197 | 548 | 588 | 0.93707 | 551 | 588 | 0.92687 | 545 | 588 | 0.91993 | 540 | 587 | 0.91993 | 540 | 587 |
| bad samples removed | 2 | 0.48639 | 286 | 588 | | 285 | 588 | 0.48129 | 283 | 588 | 0.48980 | 288 | 588 | 0.47789 | 281 | 588 | 0.49490 | 291 | 588 | 0.49660 | 292 | 588 | 0.48980 | 288 | 588 | 0.46167 | 271 | 587 | 0.47700 | 280 | 587 |
| | 4 | 0.26531 | 156 | 588 | | 153 | 588 | 0.26531 | 156 | 588 | 0.25510 | 150 | 588 | 0.26701 | 157 | 588 | 0.29592 | 174 | 588 | 0.27891 | 164 | 588 | 0.26361 | 155 | 588 | 0.25724 | 151 | 587 | 0.25383 | 149 | 587 |
| _ | 5 | 0.17979 | 105 | 584 | 0.18259 | 107 | 586 | 0.20000 | 117 | 585 | 0.16894 | 99 | 586 | 0.19728 | 116 | 588 | 0.20000 | 117 | 585 | 0.19966 | 116 | 581 | 0.18664 | 109 | 584 | 0.19759 | 115 | 582 | 0.19171 | 111 | 579 |
| | 6 | 0.17979 | 67 | 572 | | 70 | 574 | 0.11498 | 66 | 574 | 0.10894 | 55 | 577 | 0.13884 | 79 | 569 | 0.20000 | 67 | 560 | 0.13369 | 75 | 561 | 0.10545 | 60 | 569 | 0.13556 | 77 | 568 | 0.19171 | 69 | 566 |
| | | 0.11710 | 57 | 312 | 0.12133 | 70 | 517 | 3.11730 | 00 | 57 4 | J.JJJJ2 | 55 | 511 | J. 10007 | 1 3 | 509 | J. 1 1 J U T | O1 | 300 | 3.10003 | 13 | 301 | 0.10070 | | 303 | 5.10000 | ,, | 300 | 0.12101 | 09 | 300 |
| | 7 | | 9 | 26 | 0 06977 | 2 | 43 | 0 06250 | 2 | 32 | 0 03636 | 2 | 55 | 0.07317 | 3 | 41 | 0.05000 | 2 | 40 | 0 08696 | 2 | 23 | 0 06977 | 3 | 43 | 0.06667 | વ | 45 | 0 08824 | વ | 34 |
| | 7 | 0.07692 | 2 | 26 25.59694 | 0.06977 | 3 | 43 26.08673 | 0.06250 | 2 | 32 25.73299 | 0.03636 | 2 | 55 26.69388 | 0.07317 | 3 | 41 25.97279 | 0.05000 | 2 | 40 25.30612 | 0.08696 | 2 | 23 24.83503 | 0.06977 | 3 | 43 25.76361 | 0.06667 | 3 | 45 26.18228 | 0.08824 | 3 | 25.77342 |