

$$G_t - V(S_t) = \sum_{u=t}^{T-1} \gamma^{u-t} \cdot (R_{u+1} + \gamma \cdot V(S_{u+1}) - V(S_u))$$

$$G_t - V(S_t) =$$

$$G_t = \sum_{i=t+1}^{\infty} \gamma^{i-t-1} \cdot R_i = \sum_{i=t+1}^{T-1} \gamma^{i-t-1} \cdot R_i$$

$$= \sum_{i=t}^{T-1} \gamma^{i-t} R_{i+1}$$

$$G_t - V(S_t) = R_{t+1} + \gamma G_{t+1} - V(S_t)$$

$$= R_{t+1} + \gamma V(S_{t+1}) - \cancel{V(S_t)} + \gamma G_{t+1} - V(S_t)$$

$$= R_{t+1} + \gamma V(S_{t+1}) + \gamma (R_{t+2} + \gamma G_{t+2}) - V(S_t) - \gamma V(S_{t+1})$$

$$= \underbrace{R_{t+1} + \gamma V(S_{t+1}) - V(S_t)}_{\delta_t} + \gamma \underbrace{(R_{t+2} + \gamma V(S_{t+2}) - V(S_{t+1}))}_{\delta_{t+1}} + \gamma (\gamma G_{t+2} - \gamma V(S_{t+2}))$$

$$= \delta_t + \gamma \delta_{t+1} + \gamma^2 (G_{t+2} - V(S_{t+2}))$$

$$= \sum_{u=t}^{T-1} \gamma^{u-t} \delta_u$$

$$= \sum_{u=t}^{T-1} \gamma^{u-t} [R_{u+1} + \gamma V(S_{u+1}) - V(S_u)]$$

□