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# Lab 07

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## Prelab Q1

create the transfer function of the system (you should use the `tf()` function):

```
transBallDynamics = tf([30], [5 0 0])

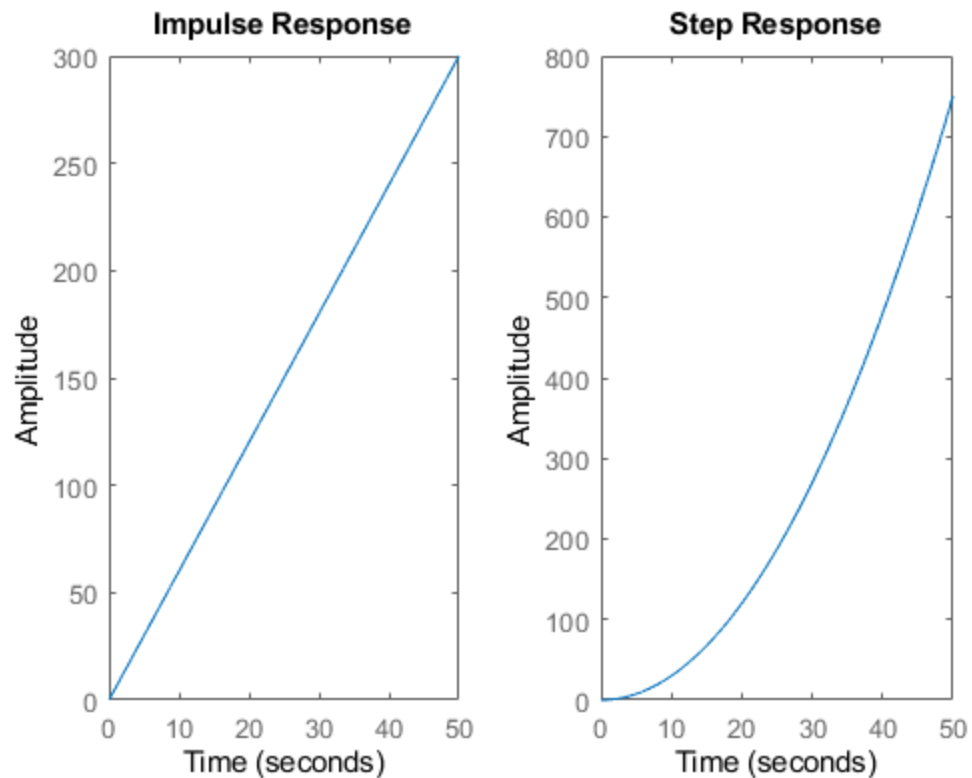
% set step options to have a step-size of 0.1 instead of 1 (standard),
% use
% stepDataOptions()
opt_StepAmplitude01 = stepDataOptions('StepAmplitude', 0.1);

% open loop impulse and step response in one figure (two subplots):
figure(1)
subplot(1,2,1)
impz(transBallDynamics)
subplot(1,2,2)
step(transBallDynamics, opt_StepAmplitude01)
```

*transBallDynamics =*

*30*  
*-----*  
*5 s^2*

*Continuous-time transfer function.*



## Prelab Q2

Controller Parameters:

```
K_P = 20;
K_I = 1;
K_D = 2;
K_D_ = 20;
```

```
% create the transfer function of the Controller:
```

```
transPID_Controller = tf([K_D_ K_P K_I], [1 0])
transForward = transPID_Controller * transBallDynamics;
```

```
% create the transfer function of the feedback loop
```

```
% trans_Q2_feedback = tf([6*K_D 6*K_P 6*K_I], [1 6*K_D 6*K_P 6*K_I]);
trans_Q2_feedback = feedback(transForward, 1)
```

```
% Plot the closed loop step response
```

```
figure(2)
step(trans_Q2_feedback, opt_StepAmplitude01)
% under damped using K_d = 2, and critically damped using K_d = 20;
```

```
transPID_Controller =
```

```
20 s^2 + 20 s + 1
```

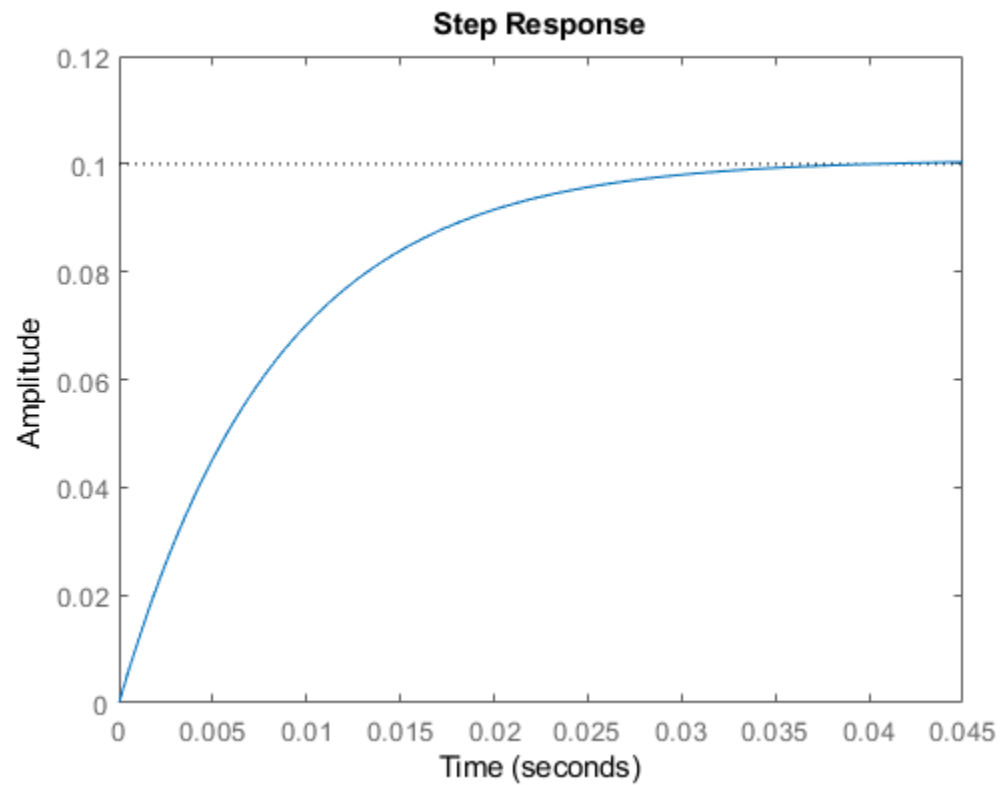
$$\frac{\quad}{s}$$

Continuous-time transfer function.

`trans_Q2_feedback =`

$$\frac{600 s^2 + 600 s + 30}{5 s^3 + 600 s^2 + 600 s + 30}$$

Continuous-time transfer function.



## Prelab Q3

controller constants:

```
Kp = 0.4;  
Ki = 0.05;  
Kd = 0.54;
```

```
% create the transfer function of the Controller  
transPID_ControllerDelay = tf([Kd Kp Ki], [1 0])
```

```
% Variables for delay:
DELAY=0.08; % 80ms
DELAY_=0.3; % 300ms

% create the transfer function of the delay in the system
% trans_Q3_delay = exp(-DELAY * s);
transDelay = tf(1, 1, 'InputDelay', DELAY_)

% create the transfer function of the feedback loop with delay
transForwardDelay = transPID_ControllerDelay * transBallDynamics;
transFeedbackDelay = feedback(transForwardDelay, transDelay)

% Plot the closed loop step response of the system with delay
y_top = 0.16;
y_bot = 0;
time_bot = 0;
time_top = 7;

figure(3)
step(transFeedbackDelay, opt_StepAmplitude01)
axis([time_bot time_top y_bot y_top])
yline(0.1+0.001)
yline(0.1-0.001)
% check design criteria for "steady state" error at 5 seconds
```

*transPID\_ControllerDelay =*

$$\frac{0.54 s^2 + 0.4 s + 0.05}{s}$$

*Continuous-time transfer function.*

*transDelay =*

$$\exp(-0.3s) * (1)$$

*Continuous-time transfer function.*

*transFeedbackDelay =*

$$A = \begin{array}{c|ccc} & x1 & x2 & x3 \\ \hline x1 & -3.24 & -2.4 & -0.3 \\ x2 & 1 & 0 & 0 \\ x3 & 0 & 1 & 0 \end{array}$$

$$B = \begin{array}{c|c} & u1 \\ \hline x1 & 2 \end{array}$$

```
x2    0
x3    0

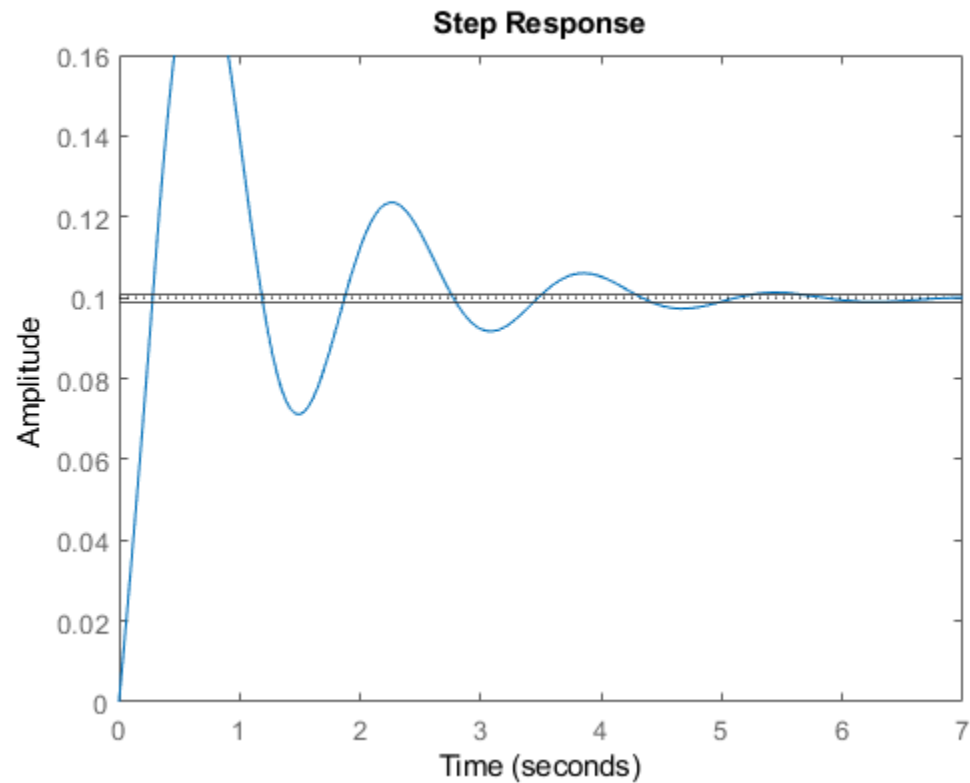
C =
      x1      x2      x3
y1  1.62    1.2    0.15

D =
      u1
y1    0

(values computed with all internal delays set to zero)

Internal delays (seconds): 0.3

Continuous-time state-space model.
```



## Prelab Q4

```
% Hint:
% - Make use of the linearized differential equations
GRAVITY = 9.81;

syms x(alpha)
equation = diff(x, alpha) == 3/5 * GRAVITY;
```

```
solution = dsolve(eqation);  
% - Filter out the first data points from the time delay to get rid of  
% the  
% incontinuity at the beginning of the sytem-response (otherwise the  
% derivative explodes)  
[x_output, t_output] = step(transFeedbackDelay, opt_StepAmplitude01);  
  
% - Make sure to use the right units (rad, degree, ...) --> check if  
% your  
% values make sense if you are not sure. E.g. a free-falling ball  
% has 9.81 m/s^2 acceleration
```

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