

Figure 1: Diagram showing the relations between true (black) and proxy (orange) metrics of lake geometry. Geometric depth calculated via Equation 1 requires a single distance and slope metric.

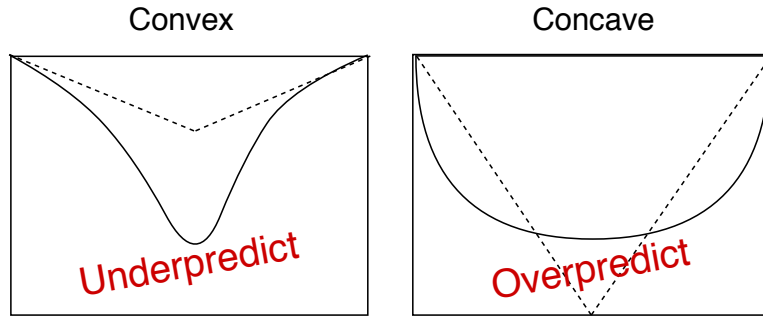


Figure 2: Diagram showing our expectation that slope-based models of lake depth will under predict true depth in convex lakes (left) and over predict true depth in concave lakes (right). Dashed lines represent extrapolated nearshore land slope while solid lines represent the lake bottom.

Variable	Median	Q25	Q75	n
Max depth (m)	8.2 (7)	4.6 (3.7)	14 (12)	4850 (17700)
Elevation (m)	300 (340)	180 (210)	400 (460)	4850 (17700)
Area (ha)	55 (33)	21 (11)	140 (100)	4850 (17700)
Island area (ha)	0 (0)	0 (0)	0.18 (0.076)	4850 (17700)
Perimeter (m)	4400 (3500)	2500 (1800)	8100 (7300)	4850 (17700)
Shoreline development	1.7 (1.7)	1.4 (1.4)	2.1 (2.2)	4850 (17700)
Watershed-lake ratio	7.8 (10)	3.9 (4.4)	17 (28)	4850 (17700)
Distance to deepest point (m)	180 (-)	110 (-)	290 (-)	4850 (-)
Distance to lake center (m)	240 (-)	160 (-)	380 (-)	4850 (-)
In-lake slope (m/m)	0.046 (-)	0.024 (-)	0.079 (-)	4850 (-)
Nearshore land slope (m/m)	0.077 (-)	0.051 (-)	0.11 (-)	4850 (-)

Table 1: Summary of lake characteristics for the present study (and for lakes in the contiguous United States from <LAGOSUS-Depth citation>). Predictor variables for computing random forest offsets (Eq 2) are printed in bold face. Dashes (-) indicate an identical sample size among this study and that of the contiguous United States.

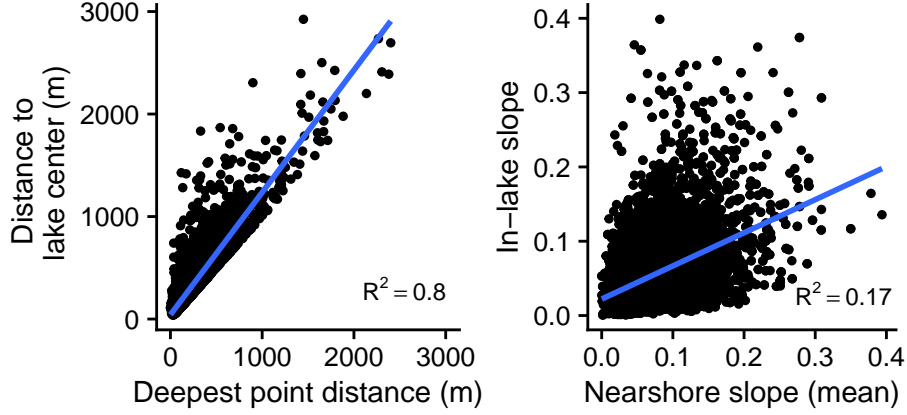


Figure 3: Comparison among proxy and true values of lake geometry for A) distance to deepest point versus distance distance to lake center and B) nearshore land slope versus in-lake slope. A best-fit line and coefficient of determination is shown to illustrate representativeness.

slope	distance	rmse	rsq
true	true	-	-
true	proxy	4.2 m	0.73
proxy	true	6.9 m	0.26
proxy	proxy	6.6 m	0.31

Table 2: Model fit and predictive accuracy metrics (RMSE = root mean square error, R2 = coefficient of determination) for all combinations of true (in-lake slope, distance to the deepest point of the lake) and proxy (nearshore land slope, distance to lake center) metrics.

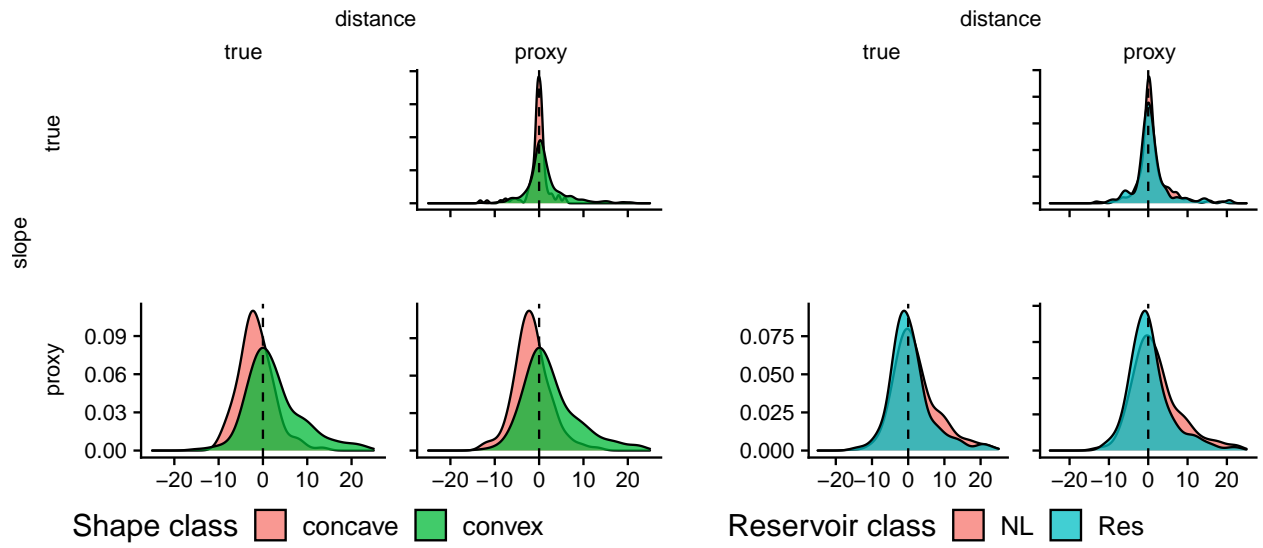


Figure 4: Depth model residuals (residual = observed - predicted) in meters by cross-section shape and reservoir class indicating overprediction of concave and reservoir lakes.

Supporting Information for "Geometric models overestimate lake depth due to imperfect slope measurement"

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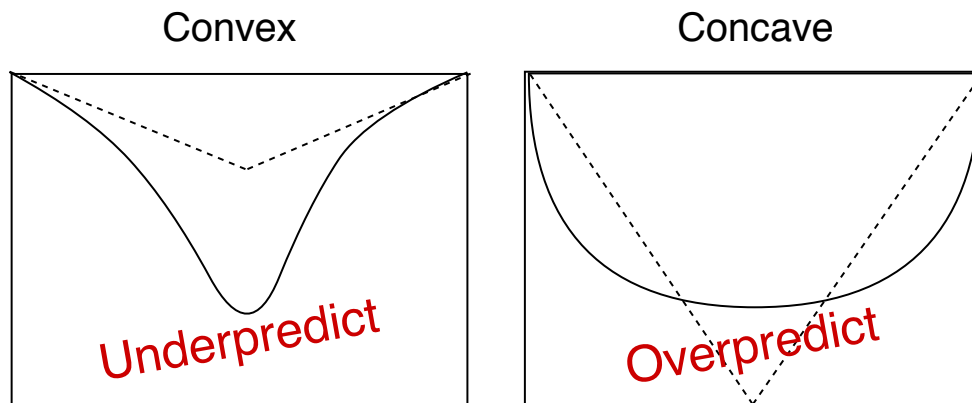


Figure S1. Diagram showing our expectation that slope-based models of lake depth will under predict true depth in convex lakes (left) and over predict true depth in concave lakes (right). Dashed lines represent extrapolated nearshore land slope while solid lines represent the lake bottom.

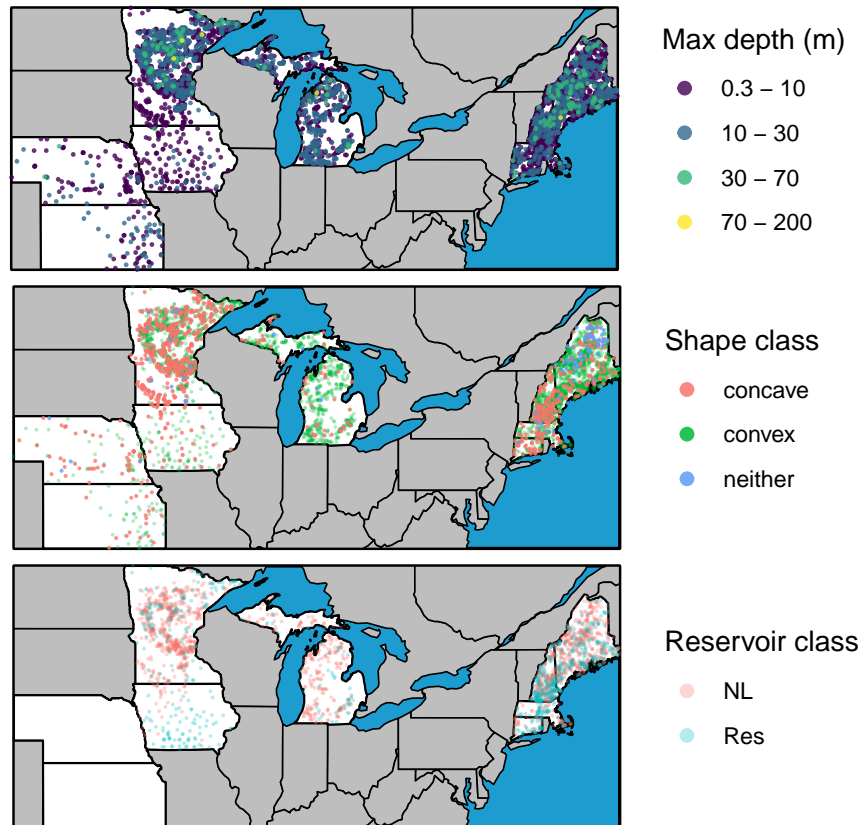


Figure S2. Map of study lakes showing A) lake maximum depth measurements, B) cross-section shape class, and C) reservoir classification.

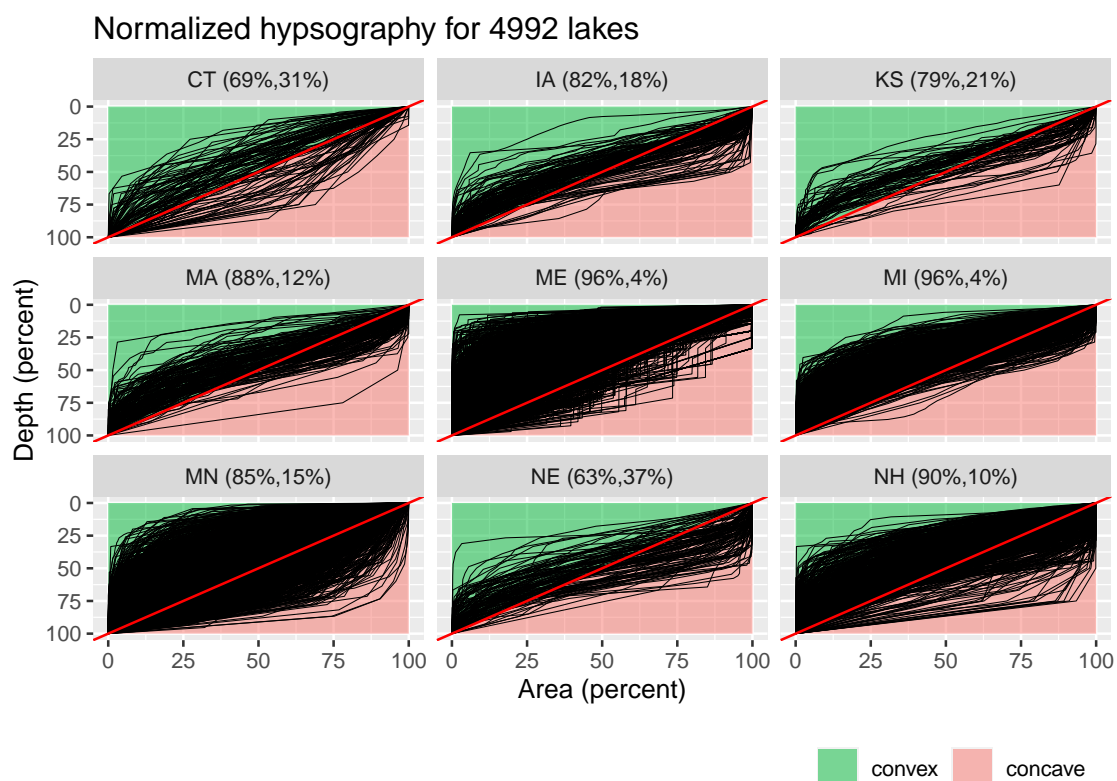


Figure S3. Hypsography classification by state. Numbers on panel labels indicate the percentage of lakes in each state with a convex versus a concave cross-section shape.

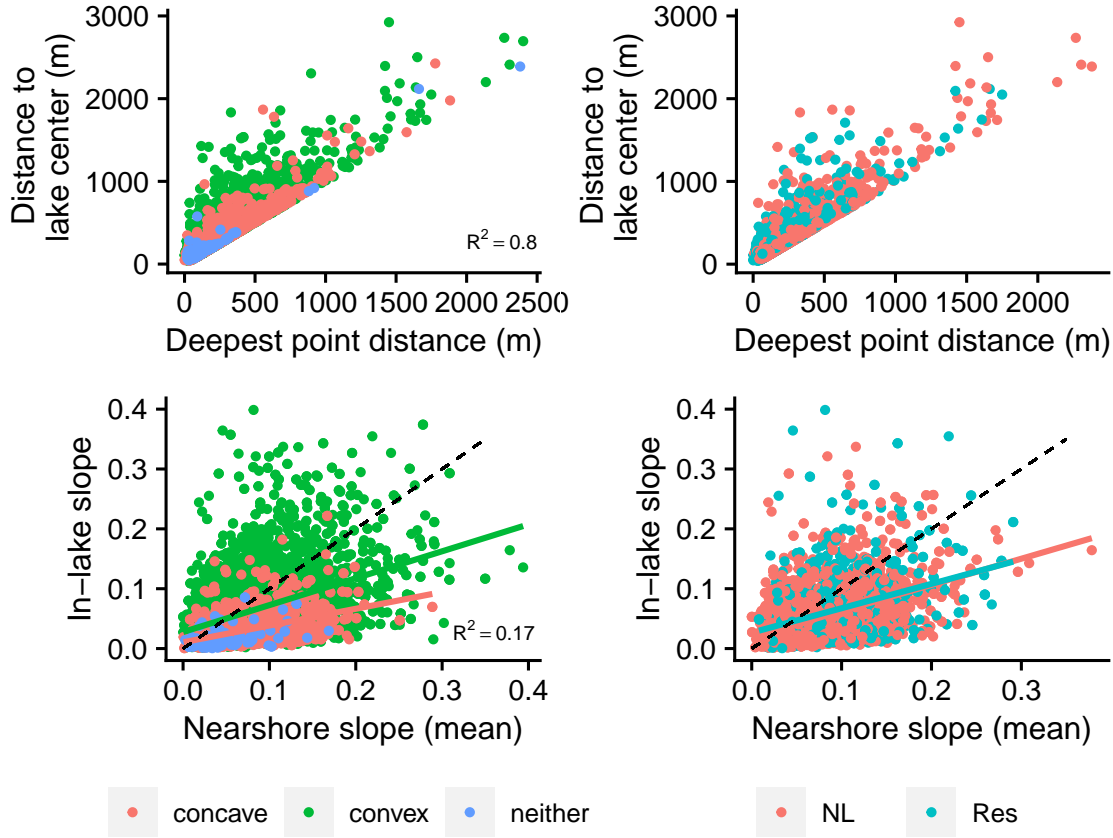


Figure S4. Comparison among lake shape and reservoir classes for A-B) distance to deepest point versus distance to lake visual center and C-D) nearshore slope versus inlake slope. A dashed 1:1 line is shown for comparison. Cross-section shape and reservoir class plots are not identical because not all lakes had a reservoir classification exceeding a 0.75 probability confidence level.

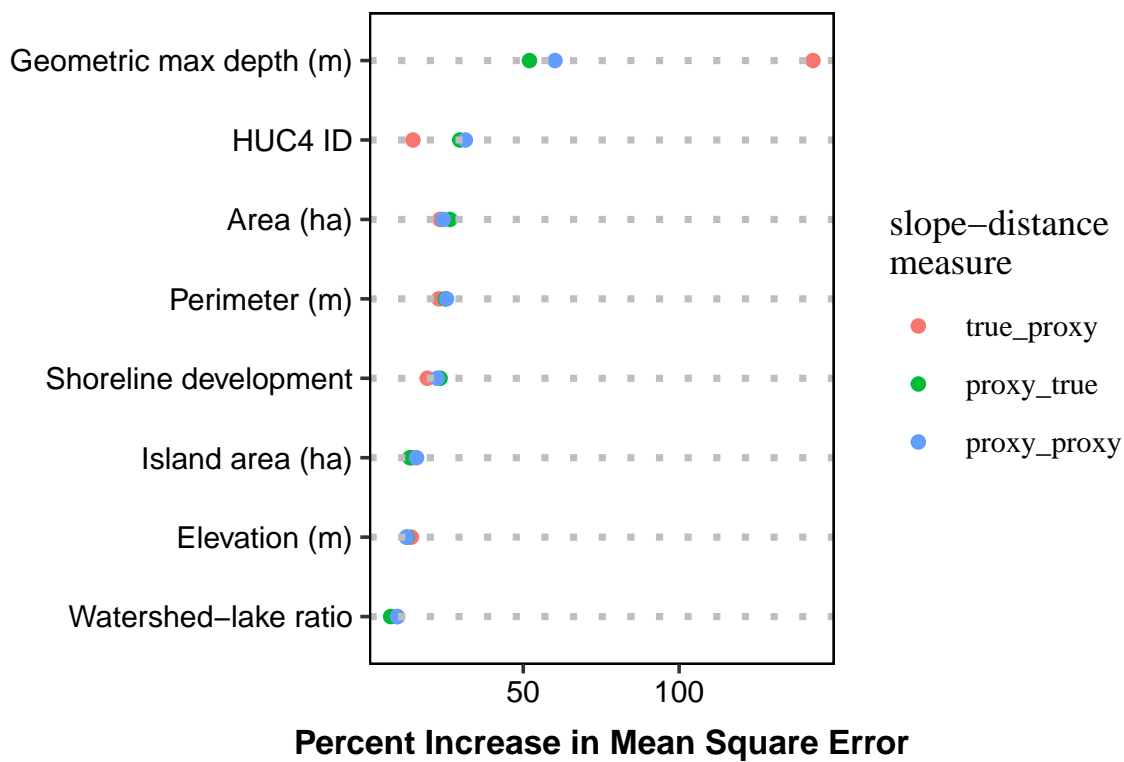


Figure S5. Importance plot for random forest variables showing increase in mean square error. Higher values indicate greater importance to model predictions. See Equation 1 for a definition of geometric max depth. HUC4 ID is a 'dummy' variable of geographic (hydrologic subbasin) location.

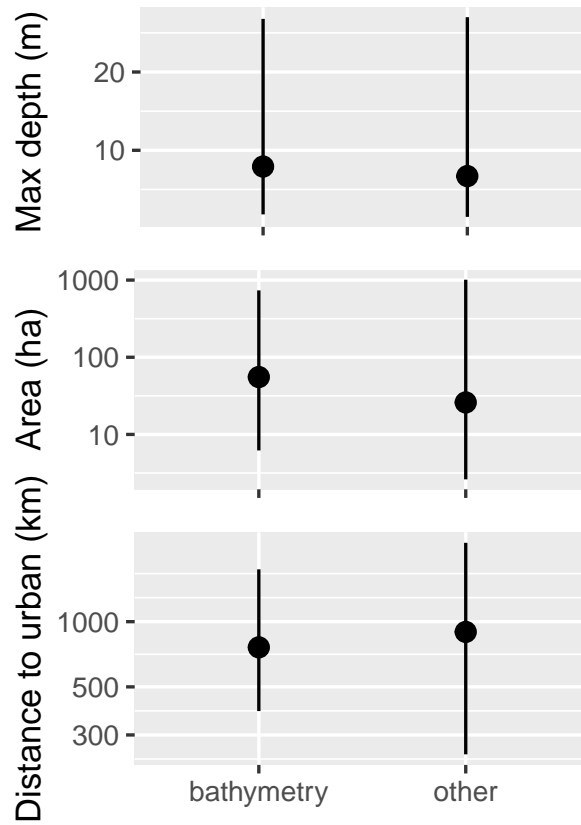


Figure S6. Comparison between characteristics of lakes with bathymetry data against lakes with depth from other sources in the LAGOSUS-Depth product. The distance to urban area metric is calculated using data from the 2018 US Census Urban and Rural Classification.

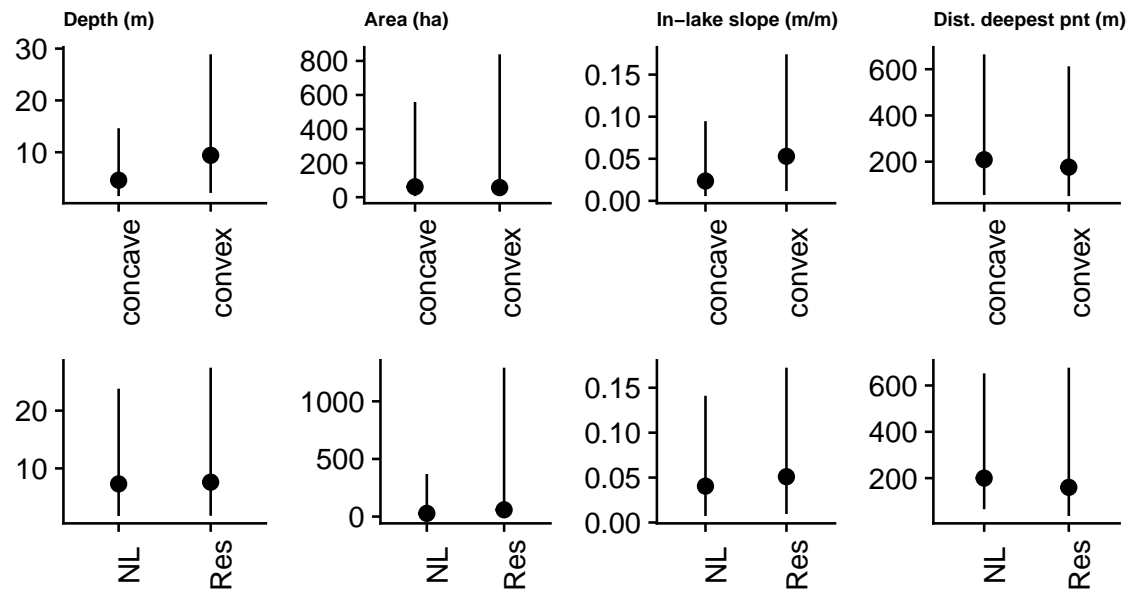


Figure S7. Comparison of lake characteristics according to differences in lake cross-section shape or reservoir status.

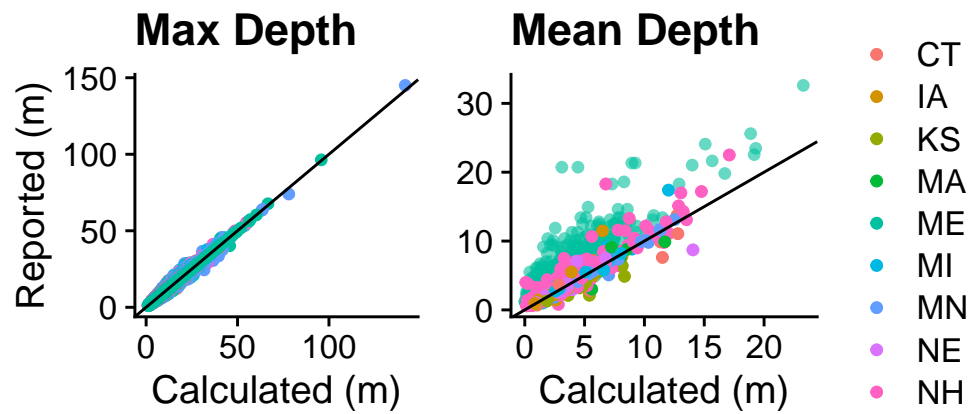


Figure S8. Comparison between reported depth and depth extracted from bathymetry surfaces by US State where reported depths come from the LAGOSUS-Depth product. For this figure, no reported depth values originated from the same source as its corresponding bathymetry-derived value.

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