# SGN-12007 Introduction to Image and Video Processing

## **EXERCISE 6**

### 13.11.2019 - 15.11.2019

The tasks should be completed and presented to TA during the lab session. **Do not forget to upload your solutions to Moodle!** Questions about exercises should be addressed to the TA personally, through Moodle messages or via email, which can be found on the Moodle page of the course.

### 1. Signal Creation

Create the following 128 x 128 gray-scale images:

- a) Constant value 0.5 for whole image;
- b) 20x20 white square in the middle;
- c) Ramp from 0 to 1 in horizontal axis, constant in vertical axis.
- d) Delta function at the center of the image;
- e) Cosine signal having four periods in both directions; (help meshgrid)

All the images should be created using the full range of double precision from 0 to 1, and without using any for or while loops.

#### 2. DFT

- a) Perform the 2D Fourier transform on all the images in task 1. Take a look at *Ex6\_DFT.pdf* for instruction of DFT in MATLAB. (help fftshift, fft2, log)
- b) Explain what information you get from Fourier transform of an image.
- c) Consider DFT images from task 1. Where is the energy concentrated and why?

### 3. Filtering in the Frequency Domain

Butterworth filters can be defined as follows:

(a) Butterworth low-pass filter: 
$$H(u, v) = \frac{1}{1 + \left(\frac{D(u, v)}{D_0}\right)^{2n}}$$

(b) Butterworth high-pass filter: 
$$H(u, v) = 1 - \frac{1}{1 + \left(\frac{D(u, v)}{D_0}\right)^{2n}}$$

where  $D_0$  is the so-called cut-off frequency distance.  $D(u, v) = \sqrt{(u - M/2)^2 + (v - N/2)^2}$ , where  $M \times N$  is the size of the image.

Use the given Butterworth low-pass filter (BWLPfilter.m), set the values  $D_0=20$ , n=2 and filter the image *cameraman.tif* with both (a) and (b) filters. Show images of the filters and the final filtered images.