# M4L2 Homework Assignment

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### 1 M4L2 Homework Assignment

R studio was configured with the following parameters before beginning the project:

```
# clears the console in RStudio
cat("\014")

# clears environment
rm(list = ls())

# Load required packages
require(ggplot2)
require(cluster)
require(amap)
require(useful)
```

#### 1.1 Load Data.

I opened the Wholesale customers Data Set using read.csv2 and downloaded it directly from the UC Irvine Machine Learning Repository.

To format the data, the data is separated by ',', stringsAsFactors = FALSE so that the strings in a data frame will be treated as plain strings and not as factor variables. I set na strings for missing data. Once the data was loaded I added the column names and changed the data types to numeric and finally removed the text data type.

Below is my R code:

```
# Some csv files are really big and take a while to open. This command checks to
# see if it is already opened, if it is, it does not open it again.
# I also omitted the first column
if (!exists("dfWCD")) {
dfWCD <-
  read.csv2("Wholesale customers data.csv",
    sep = ",",
    stringsAsFactors = FALSE,
    na.strings=c("","NA")
 )
# Add a column so I know which study the data is refereing to
study <- sprintf("study %s", seq(1:440))
dfWCD$study<-study</pre>
}
# Download directly from site (unreliable from Ecuador)
# if (!exists("dfWCD")) {
# dfWCD <-
#
    read.csv2(
#
      url(
#
        "https://archive.ics.uci.edu/ml/machine-learning-databases/00292/Wholesale customers data.csv"
#
      ),
#
      sep = ",",
#
      stringsAsFactors = FALSE,
#
      na.strings=c("","NA")
#
# # Add a column so I know which study the data is refereing to
```

```
# study <- sprintf("study_%s", seq(1:440))
# dfWCD$study<-study
# }
# change 2 to 24 to numeric
dfWCD[1:8] <- sapply(dfWCD[1:8], as.numeric)</pre>
# Print first lines
str(dfWCD)
  'data.frame':
                    440 obs. of 9 variables:
   $ Channel
##
                             2 2 2 1 2 2 2 2 1 2 ...
                      : num
##
   $ Region
                      : num
                             3 3 3 3 3 3 3 3 3 . . .
##
   $ Fresh
                             12669 7057 6353 13265 22615 ...
                      : num
##
   $ Milk
                             9656 9810 8808 1196 5410 ...
                      : num
##
  $ Grocery
                      : num
                           7561 9568 7684 4221 7198 ...
##
   $ Frozen
                             214 1762 2405 6404 3915 ...
                      : num
##
   $ Detergents_Paper: num
                             2674 3293 3516 507 1777 ...
   $ Delicassen
                      : num
                             1338 1776 7844 1788 5185 ...
                             "study_1" "study_2" "study_3" "study_4" ...
  $ study
                      : chr
# Select the first 8 lines for plotting
dfWCD2<-dfWCD[1:8]
# Print first lines
str(dfWCD2)
  'data.frame':
                    440 obs. of 8 variables:
##
   $ Channel
                             2 2 2 1 2 2 2 2 1 2 ...
                      : num
##
   $ Region
                             3 3 3 3 3 3 3 3 3 . . .
                      : num
##
   $ Fresh
                             12669 7057 6353 13265 22615 ...
                      : num
                      : num 9656 9810 8808 1196 5410 ...
##
   $ Milk
  $ Grocery
##
                      : num 7561 9568 7684 4221 7198 ...
##
                      : num
                             214 1762 2405 6404 3915 ...
                             2674 3293 3516 507 1777 ...
##
   $ Detergents_Paper: num
   $ Delicassen
                     : num
                             1338 1776 7844 1788 5185 ...
```

#### 1.2 Clustering

Clustering is grouping like with like such that:

- 1. Similar objects are close to one another within the same cluster.
- 2. Dissimilar to the objects in other clusters.

#### 1.2.1 Understanding the data

The data set refers to clients of a wholesale distributor in Portugal. It includes the annual spending in monetary units (m.u.) on diverse product categories. The data has the following attribute information:

- 1. FRESH: annual spending (m.u.) on fresh products (Continuous);
- 2. MILK: annual spending (m.u.) on milk products (Continuous);
- 3. GROCERY: annual spending (m.u.) on grocery products (Continuous);
- 4. FROZEN: annual spending (m.u.) on frozen products (Continuous)
- 5. DETERGENTS\_PAPER: annual spending (m.u.) on detergents and paper products (Continuous)

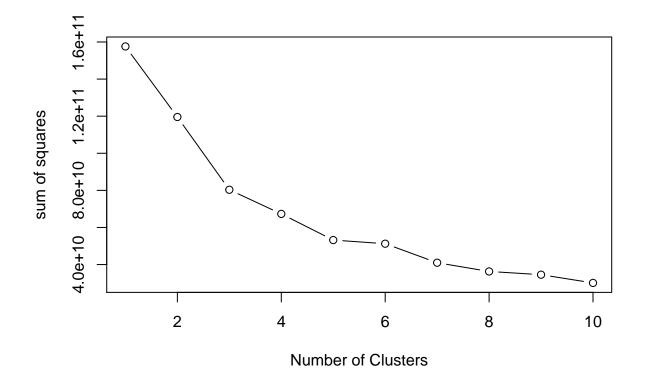
- 6. DELICATESSEN: annual spending (m.u.) on and delicatessen products (Continuous);
- 7. CHANNEL: customer channel 1 = Horeca (Hotel/Restaurant/Cafe) or 2 = Retail channel (Nominal) 2 = Oporto or 3 = Other (Nominal)

#### 1.2.2 Number of Clusters

Before I can begin clustering analysis, I need to determine the number of clusters. For determining "the right number of clusters", for this analysis I will use the averaged Silhouette width and Gap statistic and Hartigan's rule.

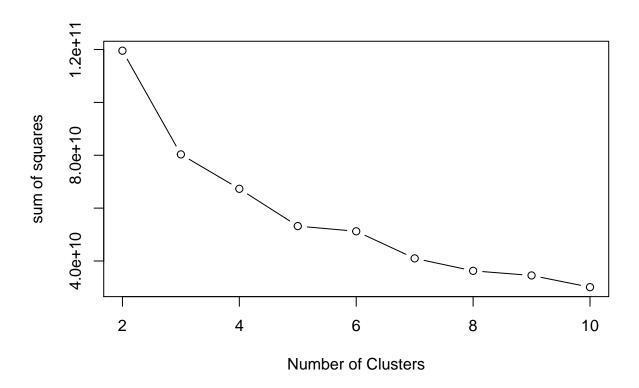
#### 1.2.2.1 Averaged Silhouette Width and Gap Statistic

```
# Determining number of clusters
sos <- (nrow(dfWCD2) - 1) * sum(apply(dfWCD2, 2, var))
for (i in 2:10)
    sos[i] <- sum(kmeans(dfWCD2, centers = i)$withinss)
plot(1:10,
        sos,
        type = "b",
        xlab = "Number of Clusters",
        ylab = "sum of squares")</pre>
```



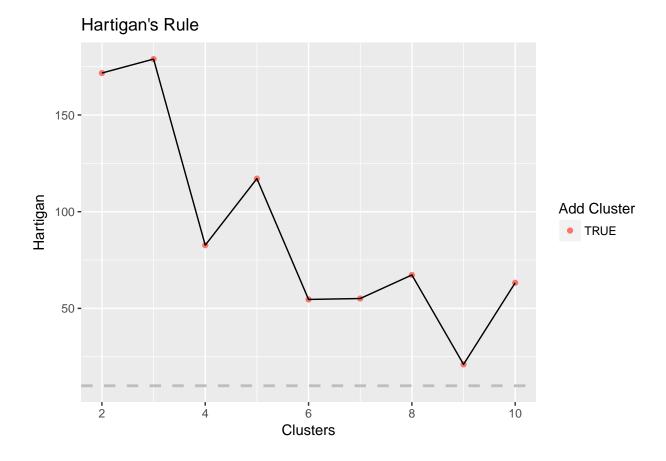
```
plot(2:10,
    sos[c(2:10)],
    type = "b",
```

```
xlab = "Number of Clusters",
ylab = "sum of squares")
```



### 1.2.2.2 Hartigan's rule

```
# Hartigans's rule FitKMean (similarity)
# require(useful)
best<-FitKMeans(dfWCD2,max.clusters=10, seed=111)
PlotHartigan(best)</pre>
```



#### 1.2.2.3 Number of Clusters Results

Based off of the graphs above it looks like I should perform clustering with 3 to 5 clusters. The analysis looks better with 4 after some trial and error.

#### 1.2.3 Partitioning-based clustering

Partitioning algorithms construct various partitions and then evaluate them by some criterion Hierarchy algorithms, two examples are k-means and k-mediods algorithms.

#### 1.2.3.1 k-means

k-means clustering is a method of vector quantization, originally from signal processing. k-means clustering aims to partition n observations into k clusters in which each observation belongs to the cluster with the nearest mean, serving as a prototype of the cluster. This results in a partitioning of the data space into Voronoi cells.

Below I apply the k-means algorithm:

```
# Clustering with 4 clusters
k <- 4
dfWCD2.4.cluster <- kmeans(dfWCD2,k)
dfWCD2.4.cluster</pre>
```

```
## K-means clustering with 4 clusters of sizes 95, 11, 58, 276 ##
```

```
## Cluster means:
##
   Channel
          Region
                 Fresh
                        Milk
                            Grocery
                                   Frozen
## 1 1.863158 2.536842 4808.842 10525.011 16909.789 1462.589
## 2 1.909091 2.545455 19888.273 36142.364 45517.455 6328.909
## 3 1.137931 2.586207 36144.483 5471.466 6128.793 6298.655
## 4 1.152174 2.536232 9087.464 3027.428 3753.514 2817.986
   Detergents Paper Delicassen
## 1
        7302.400
               1650.884
## 2
       21417.091
               8414.000
## 3
        1064.000
               2316.724
## 4
        1003.004
               1040.525
##
## Clustering vector:
   ## [36] 1 3 1 1 3 3 4 1 1 4 1 1 2 4 1 4 4 3 1 3 4 1 1 4 4 4 2 4 1 4 2 4 4 4 4
  [71] 4 1 4 4 4 4 4 4 1 4 4 4 1 1 4 4 2 2 3 4 3 4 4 2 4 1 4 4 4 4 4 1 1 4 3 4
## [176] 1 3 4 4 4 4 3 1 2 4 4 4 1 1 1 4 4 4 1 4 4 3 1 4 4 1 1 3 4 4 1 4 4 4 1
## [316] 1 4 4 4 1 4 4 4 4 3 3 4 4 4 4 4 1 4 2 4 3 4 4 4 4 1 1 4 1 4 4 1 3 4 1
## [421] 1 4 3 4 4 4 1 3 4 4 1 4 4 4 3 3 1 4 4
##
## Within cluster sum of squares by cluster:
## [1] 10434501446 14680550155 20922612384 18817881861
## (between_SS / total_SS = 58.8 %)
##
## Available components:
##
                       "totss"
## [1] "cluster"
              "centers"
                                 "withinss"
## [5] "tot.withinss" "betweenss"
                       "size"
                                 "iter"
## [9] "ifault"
```

This calculation makes the k-means calculation more stable, it performs this analysis 1000 times and takes the ones with the least error:

```
# Clustering with 4 clusters
k < -4
trails<-1000
dfWCD2.4.cluster <- kmeans(dfWCD2,k, nstart = trails)</pre>
dfWCD2.4.cluster
## K-means clustering with 4 clusters of sizes 93, 281, 59, 7
## Cluster means:
      Channel
               Region
                           Fresh
                                      Milk
                                             Grocery
## 1 1.881720 2.505376 5121.527 11293.570 17686.441 1545.806
## 2 1.160142 2.544484 9004.922 3103.815 3861.922 2804.562
## 3 1.135593 2.593220 36156.390 6123.644 6366.780 6811.119
## 4 2.000000 2.571429 20031.286 38084.000 56126.143 2564.571
   Detergents_Paper Delicassen
```

```
## 1
         7702.699
                1886.527
## 2
         1053.534
                1051.053
## 3
         1050.017
                3090.051
## 4
        27644.571
                2548.143
## Clustering vector:
   [36] 1 3 1 1 3 3 2 1 1 2 1 1 4 2 1 2 2 3 1 3 2 1 1 2 2 2 4 2 1 2 4 2 2 2 2
## [71] 2 1 2 2 2 2 2 1 2 2 2 1 1 2 2 4 4 3 2 3 2 2 1 2 1 2 2 2 2 2 1 1 2 3 2
## [176] 1 3 2 2 2 2 3 1 3 2 2 2 2 1 1 2 2 2 1 2 2 3 1 2 2 1 1 3 2 2 1 2 2 2 1
## [316] 1 2 2 2 1 2 2 2 2 3 3 2 2 2 2 2 1 2 4 2 3 2 2 2 2 1 1 2 1 2 2 1 3 2 1
## [421] 1 2 3 2 2 2 1 3 2 2 1 2 2 2 3 3 1 2 2
##
## Within cluster sum of squares by cluster:
## [1] 12568477117 19299314618 25518237851 7469349068
  (between_SS / total_SS = 58.8 %)
##
##
## Available components:
## [1] "cluster"
               "centers"
                          "totss"
                                    "withinss"
## [5] "tot.withinss" "betweenss"
                          "size"
                                    "iter"
## [9] "ifault"
There is 1 cluster that I need to look at with a value 7. Below is a table looking at all of the information
# Clustering with 5 clusters
cm<-table(dfWCD$study,dfWCD2.4.cluster$cluster)</pre>
head(cm)
##
##
          1 2 3 4
          0 1 0 0
##
   study_1
##
   study_10 1 0 0 0
##
   study_100 0 1 0 0
##
   study 101 1 0 0 0
##
   study_102 1 0 0 0
   study_103 0 1 0 0
# Get cluster of 7
# clusterOf7<-cm[,4][cm[,4]>0]
# clusterOf7
# Look at the group of 7
dfSeven <- dfWCD[c(212, 334, 48, 62, 66, 86, 87), ]
dfSeven
    Channel Region Fresh Milk Grocery Frozen Detergents_Paper Delicassen
## 212
         2
             1 12119 28326
                         39694
                              4736
                                          19410
```

```
## 334
             2
                     2 8565 4980
                                      67298
                                               131
                                                               38102
                                                                            1215
## 48
             2
                     3 44466 54259
                                              7782
                                                               24171
                                                                            6465
                                      55571
                                                               26701
## 62
             2
                     3 35942 38369
                                      59598
                                              3254
                                                                            2017
                          85 20959
                                                                            1423
## 66
             2
                     3
                                      45828
                                                36
                                                               24231
## 86
             2
                     3 16117 46197
                                      92780
                                              1026
                                                               40827
                                                                            2944
## 87
             2
                     3 22925 73498
                                      32114
                                               987
                                                               20070
                                                                             903
##
           study
## 212 study 212
## 334 study 334
        study_48
## 48
## 62
        study_62
## 66
        study_66
## 86
        study_86
## 87
        study_87
```

I cannot make too much sense of this data and will review the centroid plot.

#### 1.2.3.1.1 Evaluating model performance

```
# Evaluating model performance
# look at the size of the clusters
dfWCD2.4.cluster$size
## [1] 93 281 59 7
# look at the cluster centers
dfWCD2.4.cluster$centers
      Channel
                Region
                           Fresh
                                      Milk
                                              Grocery
                                                        Frozen
## 1 1.881720 2.505376 5121.527 11293.570 17686.441 1545.806
## 2 1.160142 2.544484 9004.922 3103.815 3861.922 2804.562
## 3 1.135593 2.593220 36156.390 6123.644 6366.780 6811.119
## 4 2.000000 2.571429 20031.286 38084.000 56126.143 2564.571
    Detergents_Paper Delicassen
## 1
            7702.699
                        1886.527
## 2
             1053.534
                        1051.053
## 3
             1050.017
                        3090.051
## 4
            27644.571
                        2548.143
names(dfWCD2)
## [1] "Channel"
                          "Region"
                                              "Fresh"
## [4] "Milk"
                          "Grocery"
                                              "Frozen"
## [7] "Detergents_Paper" "Delicassen"
# mean of 'Fresh' by cluster
Fresh <- aggregate (data = dfWCD2, Fresh ~ dfWCD2.4.cluster$cluster, mean)
Fresh
    dfWCD2.4.cluster$cluster
##
                                  Fresh
## 1
                            1 5121.527
## 2
                            2 9004.922
## 3
                            3 36156.390
                            4 20031.286
# mean of 'Milk' by cluster
Milk<-aggregate(data = dfWCD2, Milk ~ dfWCD2.4.cluster$cluster, mean)</pre>
Milk
```

```
dfWCD2.4.cluster$cluster
## 1
                             1 11293.570
## 2
                             2 3103.815
## 3
                             3 6123.644
## 4
                             4 38084.000
# mean of 'Grocery' by cluster
Grocery<-aggregate(data = dfWCD2, Grocery ~ dfWCD2.4.cluster$cluster, mean)</pre>
Grocery
##
     dfWCD2.4.cluster$cluster
                                 Grocery
## 1
                             1 17686.441
## 2
                             2 3861.922
## 3
                             3 6366.780
## 4
                             4 56126.143
# mean 'Detergents_Paper' by cluster
DP<-aggregate(data = dfWCD2, Detergents_Paper ~ dfWCD2.4.cluster$cluster, mean)
DP
##
     dfWCD2.4.cluster$cluster Detergents_Paper
## 1
## 2
                             2
                                       1053.534
## 3
                             3
                                       1050.017
## 4
                             4
                                      27644.571
# mean 'Delicassen' by cluster
Delicassen - aggregate(data = dfWCD2, Delicassen - dfWCD2.4.cluster$cluster, mean)
Delicassen
##
     dfWCD2.4.cluster$cluster Delicassen
## 1
                                 1886.527
## 2
                             2
                                 1051.053
## 3
                             3
                                 3090.051
## 4
                             4
                                 2548.143
```

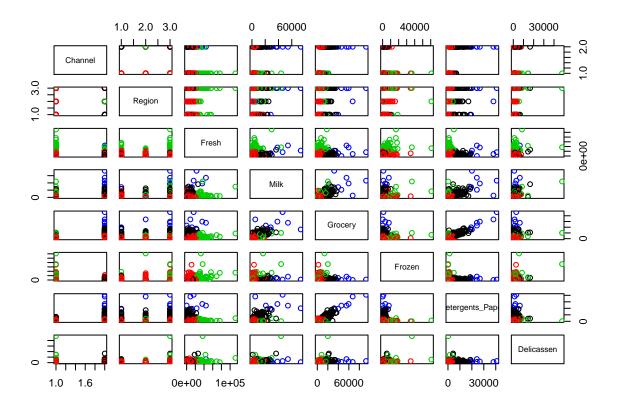
### 1.2.3.1.2 Multidimensional scaling (MDS)

Multidimensional scaling (MDS) is a means of visualizing the level of similarity of individual cases of a high-dimensional dataset.

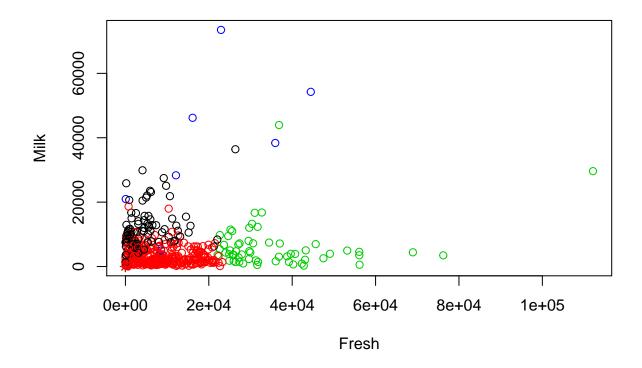
MDS attempts to find an embedding from the I objects into  $\mathbb{R}^N$  such that distances are preserved.

Below are some MDS plots:

```
plot(dfWCD2,col=dfWCD2.4.cluster$cluster) # Plot Clusters
```

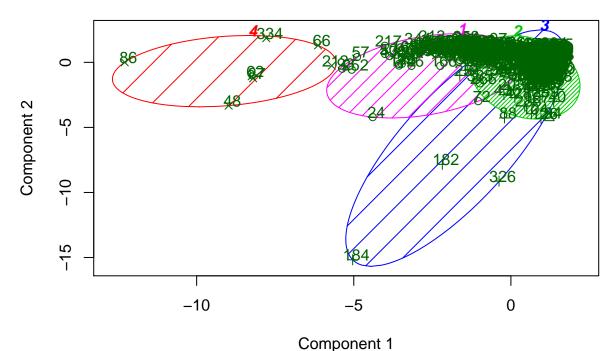


```
# Plot drinks and mcv
plot(dfWCD2[c("Fresh","Milk")],col=dfWCD2.4.cluster$cluster)
points(dfWCD2.4.cluster$centers, col = 1:2, pch = 8)
```



# Centroid Plot against 1st two discriminant functions
clusplot(dfWCD2, dfWCD2.4.cluster\$cluster, color=TRUE, shade=TRUE, labels=2, lines=0)

### CLUSPLOT( dfWCD2 )



These two components explain 61.12 % of the point variability.

```
# library(fpc)
# plotcluster(dfWCD2, dfWCD2.4. cluster$cluster)
```

The plots look good, the data is clustered as expected. The centroid plot looks ok. I can see the small cluster is grouped ok, however, there is some overlaping with a couple of clusters in the corner, it seems like there is a lot going on in the upper right corner, but I do not think this is an issue.

#### 1.2.3.2 K-medoids clustering in R

The K-medoids or Partitioning Around Medoids (PAM) algorithm is related to the k-means algorithm and but uses medoid shifts rather than reassigning points based on Euclidean distance. Each cluster is represented by one of the objects (i.e. points) in the cluster A medoid is a point in a cluster whose dissimilarity to all the points in the cluster is minimal. Medoids are similar in concept to means or centroids, but medoids are always members of the data set. That is, in 2D Cartesian space a centroid can be any valid x.y coordinate. Whereas a medoid must be one of the data points.

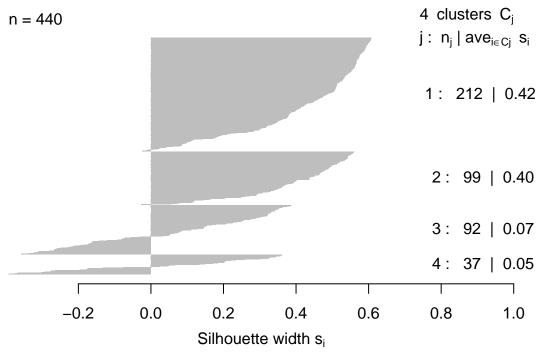
Below I use R to apply the k-medoids algorithm:

```
# PAM
k<-4
dfWCD2.pam.4.clust<- pam(dfWCD2,k, keep.diss = TRUE, keep.data = TRUE)
dfWCD2.pam.4.clust
## Medoids:
##
         ID Channel Region Fresh Milk Grocery Frozen Detergents_Paper
## [1,] 292
                  1
                          3
                            6022
                                   3354
                                            3261
                                                   2507
                                                                      212
## [2,] 297
                  1
                          2 19087
                                   1304
                                            3643
                                                   3045
                                                                      710
## [3,]
                  2
                          3
                             6006 11093
                                          18881
                                                                     7425
         10
                                                   1159
```

```
## [4,] 371
                                                       523
              2
                    3 39679 3944
                                  4955
                                        1364
      Delicassen
##
## [1,]
            686
## [2,]
            898
## [3,]
           2098
## [4,]
           2235
## Clustering vector:
    [1] \ 1 \ 1 \ 1 \ 2 \ 2 \ 1 \ 1 \ 1 \ 1 \ 3 \ 3 \ 2 \ 4 \ 2 \ 2 \ 1 \ 3 \ 1 \ 2 \ 1 \ 2 \ 1 \ 4 \ 3 \ 2 \ 2 \ 1 \ 2 \ 3 \ 4 \ 2 \ 1 \ 2 \ 4 \ 1
   [36] 1 4 3 3 4 2 2 3 3 1 3 3 3 1 3 1 1 4 3 2 1 3 3 2 1 1 3 1 3 1 3 1 2 1 1
##
  [71] 2 3 1 2 1 2 1 3 1 1 1 3 3 2 1 3 3 4 1 2 1 2 3 1 3 1 1 1 1 1 3 3 1 4 2
## [176] 3 4 1 1 1 1 4 3 4 1 1 1 1 3 3 2 2 1 3 1 2 4 1 1 1 3 3 2 1 1 3 1 1 1 3
## [246] 3 1 2 2 1 1 3 1 4 1 4 1 1 4 4 1 1 2 1 3 3 3 2 3 2 1 1 1 4 1 1 2 1 1 2
## [281] 1 1 4 2 4 4 1 2 2 4 1 1 1 3 2 1 2 1 1 1 2 3 1 3 3 3 3 2 1 3 1 4 3 1 1
## [316] 3 1 1 1 3 1 1 2 2 2 4 1 1 2 1 1 3 2 3 2 2 2 1 1 1 1 3 1 3 1 1 3 2 1 3
## [351] 1 3 1 3 2 1 2 3 1 1 2 1 1 1 1 1 1 1 2 1 4 2 1 2 1 1 3 4 1 1 2 2 4 1 3
## [421] 3 2 2 2 2 1 3 4 1 1 3 1 2 1 2 4 4 3 1 1
## Objective function:
     build
             swap
## 9285.399 8863.968
##
## Available components:
   [1] "medoids"
                 "id.med"
                            "clustering"
                                      "objective"
                                                  "isolation"
  [6] "clusinfo"
                                       "call"
##
                 "silinfo"
                            "diss"
                                                  "data"
plot(dfWCD2.pam.4.clust, which.plots = 2)
```

## Silhouette plot of pam(x = dfWCD2, k = k, keep.diss = TRUE, k

DA5030

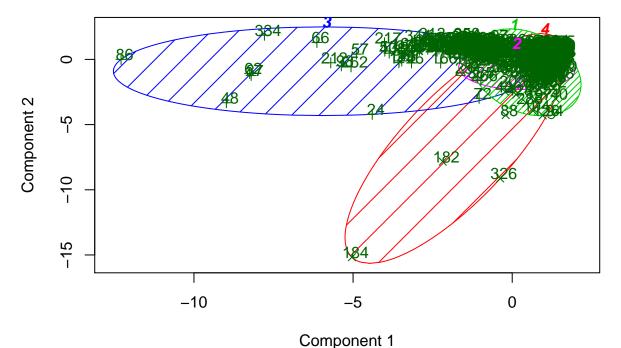


Average silhouette width: 0.31

```
# long lines good - means greater within cluster similarity
```

# Centroid Plot against 1st two discriminant functions clusplot(dfWCD2.pam.4.clust, color=TRUE, shade=TRUE, labels=2, lines=0)

## clusplot(pam(x = dfWCD2, k = k, keep.diss = TRUE, keep.data = TRUI



These two components explain 61.12 % of the point variability.

The silhouette plot dosn't loof too good, long lines are good, short ones are not. It appears that there are more short lines.

The centroid plot looks good, but there seems to be a little overlap with the clusters

#### 1.3 Confusion Plots

confusion plot is a plot of the confusion matrix. A confusion matrix, also known as a contingency table or an error matrix. A confusion matrix is a 2x2 table with counts of the following in each of its quadrents. true positive (TP) eqv. with hit true negative (TN) eqv. with correct rejection false positive (FP) eqv. with false alarm, Type I error false negative (FN) eqv. with miss, Type II error

To make a confusion plot I am going to make data with 2 clusters and compare how many times milk was purchased above the mean (above 5796.27) and how many times grocery was purchased above the mean (above 7951.28) for both k-means and pam.

Below is the R code:

```
# Clustering with 2 clusters
k <- 2
trails<-1000

# k-means
dfWCD2.2.cluster <- kmeans(dfWCD2,k, nstart = trails)

# Confusion matrix of Milk
cmMilk<-table(dfWCD2$Milk>5796.27,dfWCD2.2.cluster$cluster)
```

```
cmMilk

##

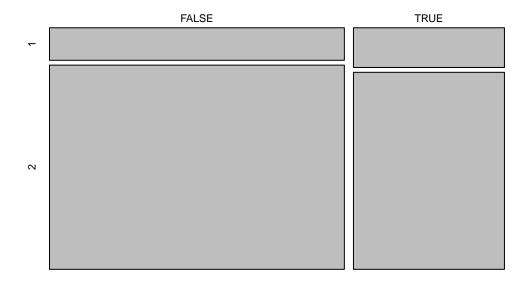
## 1 2

## FALSE 40 251

## TRUE 25 124

plot(cmMilk)
```

### **cmMilk**



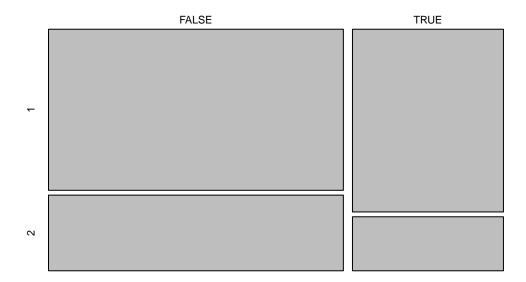
```
# pam
dfWCD2.pam.2.clust<- pam(dfWCD2,k, keep.diss = TRUE, keep.data = TRUE)

# Confusion matrix of Milk
cmMilkP<-table(dfWCD2$Milk>5796.27,dfWCD2.pam.2.clust$cluster)
cmMilkP

##
##
##
1 2
## FALSE 198 93
## TRUE 115 34

plot(cmMilkP)
```

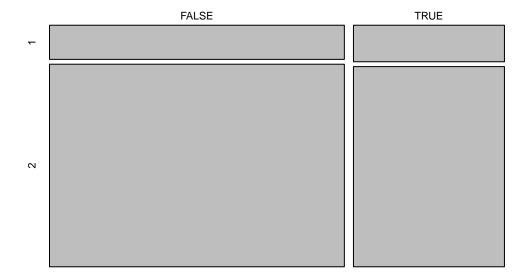
### cmMilkP



For the milk data, both the k-means and pam data show me that most of the data is about 50/50 for both groups, as I would expect.

```
# Clustering with 2 clusters
k < -2
trails<-1000
\# k-means
dfWCD2.2.cluster <- kmeans(dfWCD2,k, nstart = trails)</pre>
# Confusion matrix of grocery
cmGrocery<-table(dfWCD2$Grocery>7951.28,dfWCD2.2.cluster$cluster)
cmGrocery
##
##
                 2
             1
##
     FALSE 42 249
     TRUE
            23 126
plot(cmGrocery)
```

## cmGrocery

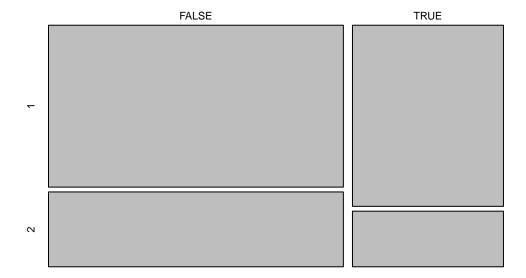


```
# pam
dfWCD2.pam.2.clust<- pam(dfWCD2,k, keep.diss = TRUE, keep.data = TRUE)

# Confusion matrix of Grocery
cmGroceryP<-table(dfWCD2$Grocery>7951.28,dfWCD2.pam.2.clust$cluster)
cmGroceryP

##
## 1 2
## FALSE 199 92
## TRUE 114 35
plot(cmGroceryP)
```

## cmGroceryP



The grocery data is a little different, the larger group is almost 60/40 (false/true), but the smaller group has 2/3 false to true.

### 1.4 Gap statistic

clusGap() calculates a goodness of clustering measure, the â gapâ statistic. For each number of clusters k, it compares  $\log(W(k))$  with  $E^*[\log(W(k))]$  where the latter is defined via bootstrapping, i.e. simulating from a reference distribution.

 $\max SE(f, SE.f)$  determines the location of the maximum of f, taking a  $\hat{a}$  1-SE rule $\hat{a}$  into account for the SE methods. The default method "firstSEmax" looks for the smallest k such that its value f(k) is not more than 1 standard error away from the first local maximum. This is similar but not the same as "Tibs2001SEmax", Tibshirani et al's recommendation of determining the number of clusters from the gap statistics and their standard deviations.

```
gap <- clusGap(dfWCD2, FUNcluster = pam, K.max = 10) # Bootstrapping
gap$Tab</pre>
```

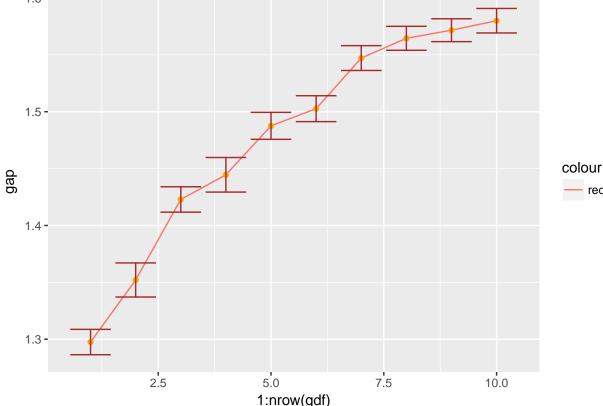
```
##
             logW
                                        SE.sim
                    E.logW
                                gap
    [1,] 14.64325 15.94079 1.297536 0.01114409
##
##
    [2,] 14.44108 15.79317 1.352091 0.01498568
##
   [3,] 14.25248 15.67539 1.422905 0.01117061
   [4,] 14.15140 15.59598 1.444578 0.01520112
##
   [5,] 14.06726 15.55488 1.487619 0.01185845
##
   [6,] 14.01411 15.51682 1.502710 0.01137696
##
   [7,] 13.93610 15.48332 1.547213 0.01091849
   [8,] 13.88909 15.45366 1.564568 0.01053377
```

x = 1:nrow(gdf),

```
## [9,] 13.85404 15.42574 1.571702 0.01005508
## [10,] 13.81975 15.39979 1.580041 0.01077285
gdf <- as.data.frame(gap$Tab)</pre>
head(gdf)
##
         logW
               E.logW
                             gap
## 1 14.64325 15.94079 1.297536 0.01114409
## 2 14.44108 15.79317 1.352091 0.01498568
## 3 14.25248 15.67539 1.422905 0.01117061
## 4 14.15140 15.59598 1.444578 0.01520112
## 5 14.06726 15.55488 1.487619 0.01185845
## 6 14.01411 15.51682 1.502710 0.01137696
 x = 1:nrow(gdf),
  y = logW,
 data = gdf,
  geom = "line",
  color = "red"
  geom_point(aes(y = logW), color = "orange") +
  geom_line(aes(y = E.logW), color = "blue") +
  geom_point(aes(y = E.logW), color = "purple")
    16.0 -
    15.5 -
    15.0 -
                                                                                     colour
                                                                                     - red
    14.5 -
    14.0 -
                      2.5
                                        5.0
                                                          7.5
                                                                            10.0
                                       1:nrow(gdf)
# Gap statistic
qplot(
```

```
y = gap,
data = gdf,
geom = "line",
color = "red"
) +
geom_point(aes(y = gap), color = "orange") +
geom_errorbar(aes(ymin = gap - SE.sim, ymax = gap + SE.sim), color = "brown")

1.6-
```



It looks like around 3 or 4, the gap increases at a higher slope, so I think a k of 4 is good.

### 1.5 Hierarchical clustering in R

In hierarchical clustering the idea is to group data objects (i.e. points) into a tree of clusters. That is, hierarchical clustering is a method of cluster analysis which seeks to build a hierarchy of clusters.

These trees (hierarchies) generally fall into two types:

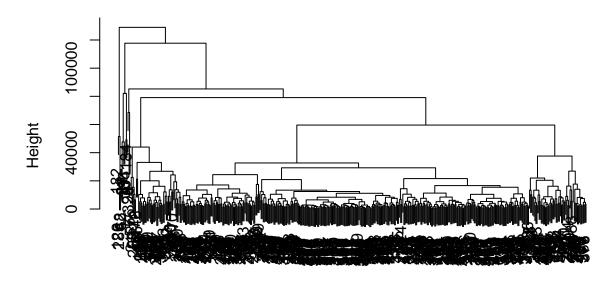
- 1. Agglomerative hierarchical clustering: Initially each data object (i.e. point) in its own cluster. Iteratively the clusters are merged together from the "bottom-up." The two most similar/closest objects are aggreated in to the same cluster/data object. Then the next two, until there is just one cluster/data object. This agglomerative approach result in "straggly" (long and thin) clusters due to a chaining effect. It is also sensitive to noise.
- 2. Divisive hierarchical clustering: in divisive hierarchical clustering all data objects (i.e. points) are initially in one cluster. These clusters are successively divided recursivley in a "top-down" manner. The cluster is broken in to two clusters that are most dissimilar. Then each of those clusters is broken in to two cluster that are most dissimilar. This continues until each cluster is a single data object

```
(i.e. point).
```

Below is my analysis using Hierarchical clustering:

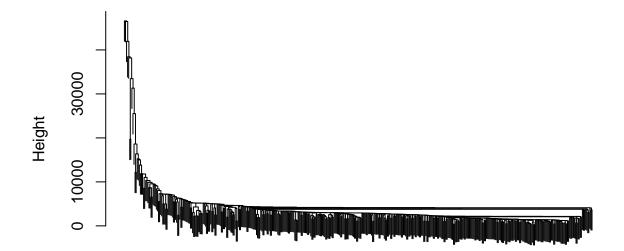
```
dfWCD2.h.clust<- hclust(d=dist(dfWCD2))
plot(dfWCD2.h.clust)</pre>
```

### **Cluster Dendrogram**



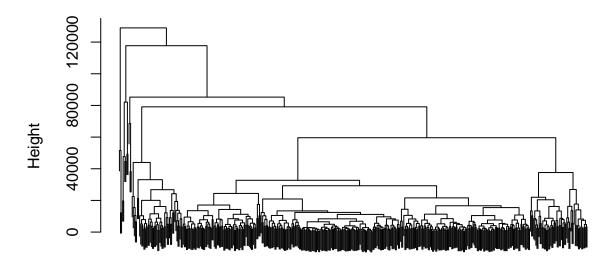
### dist(dfWCD2) hclust (\*, "complete")

```
dfWCD2.h.clust.si<- hclust(dist(dfWCD2), method = "single")
dfWCD2.h.clust.co<- hclust(dist(dfWCD2), method = "complete")
dfWCD2.h.clust.av<- hclust(dist(dfWCD2), method = "average")
dfWCD2.h.clust.ce<- hclust(dist(dfWCD2), method = "centroid")
dfWCD2.h.clust.me<- hclust(dist(dfWCD2), method = "ward.D")
plot(dfWCD2.h.clust.si, labels = FALSE)</pre>
```



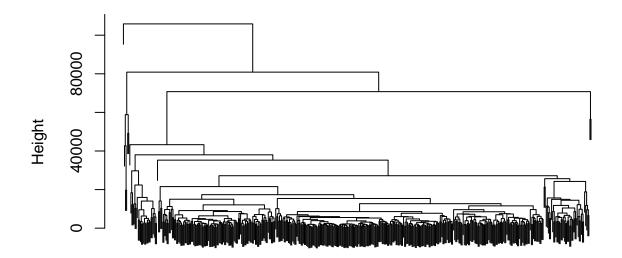
dist(dfWCD2) hclust (\*, "single")

plot(dfWCD2.h.clust.co, labels = FALSE)



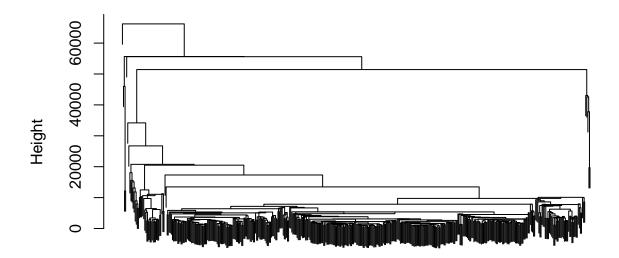
dist(dfWCD2) hclust (\*, "complete")

plot(dfWCD2.h.clust.av, labels = FALSE)



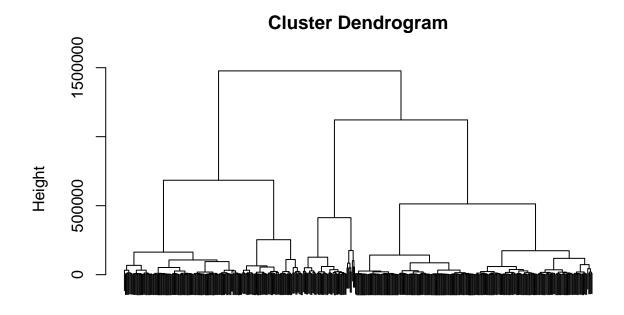
dist(dfWCD2) hclust (\*, "average")

plot(dfWCD2.h.clust.ce, labels = FALSE)



dist(dfWCD2) hclust (\*, "centroid")

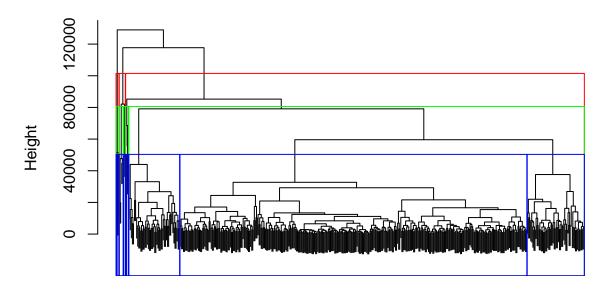
plot(dfWCD2.h.clust.me, labels = FALSE)



dist(dfWCD2) hclust (\*, "ward.D")

#### 1.5.1 Plotting to deterimine the cluster level.

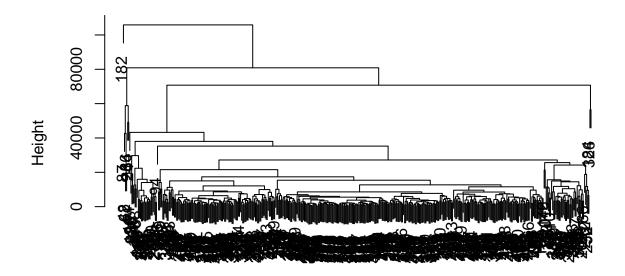
```
plot(dfWCD2.h.clust, labels = FALSE)
rect.hclust(dfWCD2.h.clust, k=3, border="red")
rect.hclust(dfWCD2.h.clust, k=5, border="green")
rect.hclust(dfWCD2.h.clust, k=9, border="blue")
```



dist(dfWCD2)
hclust (\*, "complete")

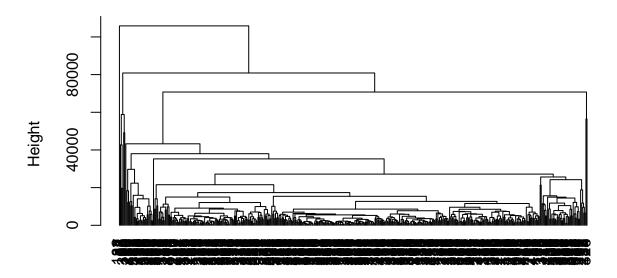
### 1.5.2 Hierarchical clustering using centroid clustering and squared Euclidean distance

```
h_c <- hcluster(dfWCD2,link = "ave") # require(amap)
plot(h_c)</pre>
```



dfWCD2 hcluster (\*, "average")

 $plot(h_c, hang = -1)$ 



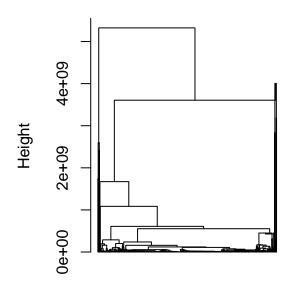
### dfWCD2 hcluster (\*, "average")

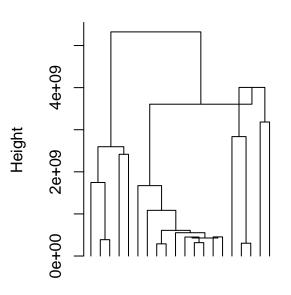
```
### centroid clustering and squared Euclidean distance
h_c<- hclust(dist(dfWCD2)^2, "cen")

### Cutting the tree into 20 clusters and reconstruct upper part of the tree from cluster center
memb <- cutree(h_c, k = 20)
cent <- NULL
for(k in 1:20){
    cent <- rbind(cent, colMeans(dfWCD2[,-1][memb == k, , drop = FALSE]))
}
h_c1 <- hclust(dist(cent)^2, method = "cen", members = table(memb))
opar <- par(mfrow = c(1, 2))
plot(h_c, labels = FALSE, hang = -1, main = "Original Tree")
plot(h_c1, labels = FALSE, hang = -1, main = "Re-start from 20 clusters")</pre>
```

## **Original Tree**

## Re-start from 20 clusters

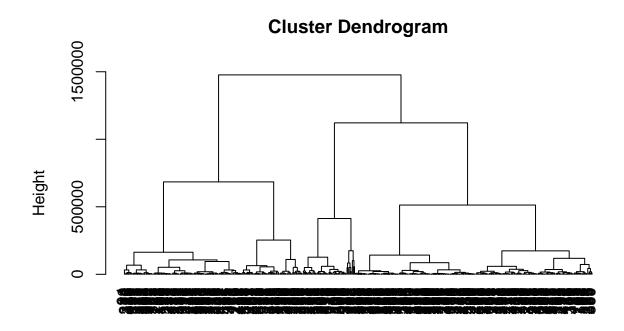




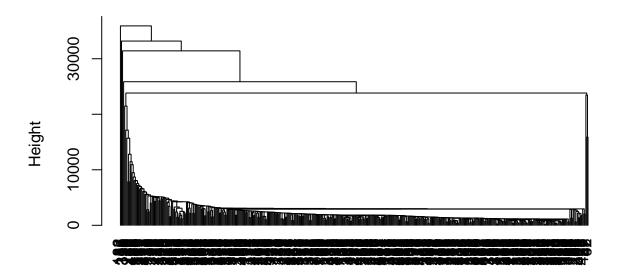
dist(dfWCD2)^2 hclust (\*, "centroid") dist(cent)^2 hclust (\*, "centroid")

par(opar)

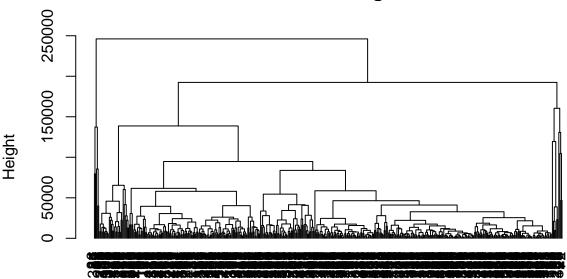
### 1.5.3 Other combinations



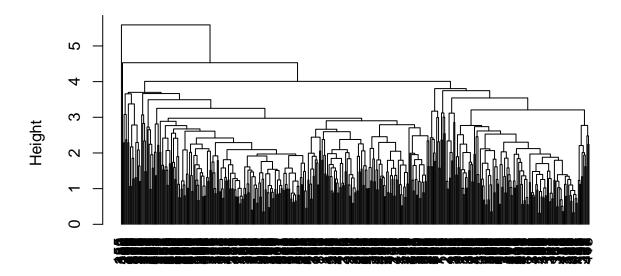
### dfWCD2 hcluster (\*, "ward")



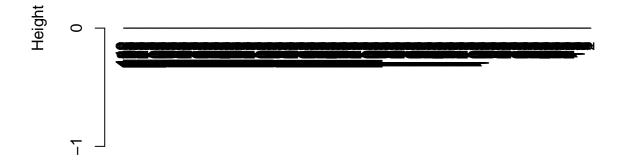
### dfWCD2 hcluster (\*, "single")



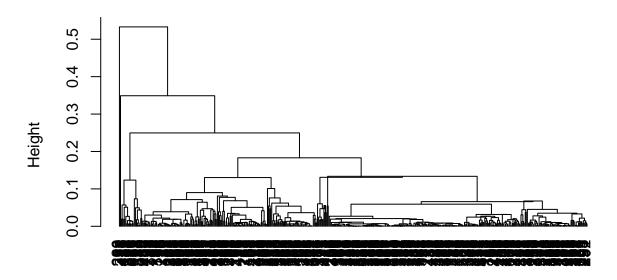
### dfWCD2 hcluster (\*, "complete")



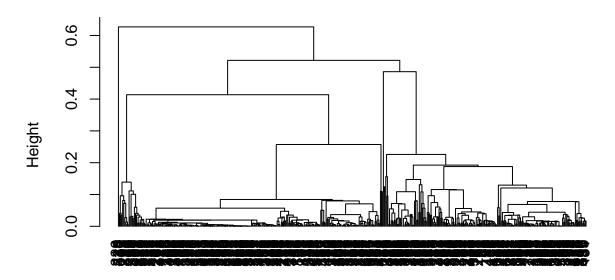
### dfWCD2 hcluster (\*, "average")



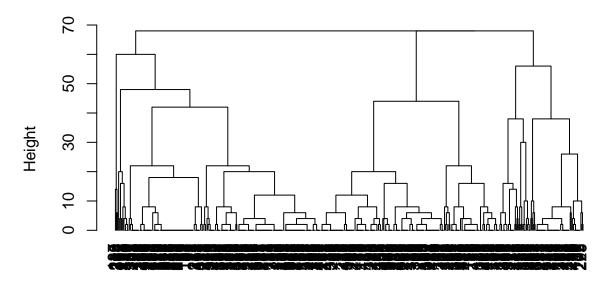
### dfWCD2 hcluster (\*, "mcquitty")



### dfWCD2 hcluster (\*, "median")



### dfWCD2 hcluster (\*, "centroid")



dfWCD2 hcluster (\*, "complete")

### 1.6 Questions

- 1. How did you choose a k for k-means? I used a mixture of the averaged Silhouette width and Gap statistic, Hartigan's rule, gap analysis, and trial and error. I eventually settled with 4 after reviewing the gap analysis.
- 2. Evaluate the model performance. How do the clustering approaches compare on the same data? K-means clustering with 4 clusters of sizes 93, 281, 59, 7. The cluster of seven looked low, but after analysis it seemed ok. I started by analyzing the raw data, but I could not make much sense of the data until it was in the centroid plot, then it looked like it fit, the seven all clustered together nicely. Overall the plots look good too, in the individual plots I can see clustering and the clustering looks acceptable.
- 3. Generate and plot confusion matrices for the k-means and PAM. What do they tell you? I plotted four different confusion plots, two for milk and two for grocery for k-means and pam. For the milk data, both the k-means and pam data show me that most of the data is about 50/50 for both groups, as I would expect. The grocery data is a little different, the larger group is almost 60/40 (false/true), but the smaller group has 2/3 false to true.
- 4. Generate centroid plots against the 1st two discriminant functions for k-means and PAM. What do they tell you? For k-means, the centroid plot looks good. I can see that the small cluster is grouped ok, however, there is some overlapping with a couple of clusters, but I do not think this is an issue. The pam plot is similar, but there seems to be a little overlap with the clusters
- 5. Generate silhouette plots for PAM. What do they tell you? The silhouette plot doesn't look too good. A good plot should have a lot of long lines, it appears that there are more short lines with this data.
- 6. For the hierarchical clustering use all linkage methods (Single Link, Complete Link, Average

Link, Centroid and Minimum energy clustering) and generate dendograms. How do they compare on the same data? They all look different. The single is hard to read, the complete looks ok, the average and centroid have a couple clads going off to nowhere, and the ward plot looks the best, it is organized nicely.

- 7. For the hierarchical clustering use both agglomerative and divisive clustering with a linkage method of your choice and generate dendograms. How do they compare on the same data? In section 1.5.3 I ran many different combinations to generate dendograms and they all look different. The mcquitty plot doesn't look like anything.
- 8. For the hierarchical clustering use centroid clustering and squared Euclidean distance and generate dendograms. How do they compare on the same data? The original tree is hard to read, especially toward the bottom. The re-start from 20 clusters looks great and it is easy to read.