

# Fast and Efficient Creation of an Universal Quantum Gate Set Using Reinforcement Learning Methods

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# Agenda

- ① Introduction
- ② Overview: QM and QC
- ③ Overview: RL
- ④ Implementation
- ⑤ Results
- ⑥ Summary
- ⑦ Conclusions

# Introduction

# Introduction

This master thesis presentation explores the use of reinforcement learning (RL) methods to efficiently construct a set of universal quantum gates comprising:

- Hadamard (H)
- $\pi/4$  phase shift (T)
- Controlled NOT (CNOT)

These gates, recognized for their minimality and universality, serve as essential building blocks for arbitrary quantum operations.

Specifically, this work seeks to:

- Formulate quantum gate control as a reinforcement learning problem.
- Deploy and compare the performance of various RL agents for optimizing quantum control.
- Validate the proposed methods through numerical simulations, compare them to optimal control methods, and analyze their scalability to multi-qubit systems.

$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \quad T = \begin{pmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{pmatrix}$$

$$\text{CNOT} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$

The Reinforcement Learning frameworks deployed are:

- Double Dueling Deep Q-Network (DDDQN)
- Proximal Policy Optimization (PPO)
- Group Relative Policy Optimization (GRPO)
- Twin Delayed Deep Deterministic Policy Gradient (TD3)

# Quantum Mechanics and Control

Quantum gates operate on qubits and are represented by unitary matrices. For example:

- the Hadamard Gate (H) creates a superposition from a basis state,
- the T Gate (T) introduces a  $\pi/4$  phase shift and
- the Controlled-NOT Gate (CNOT) acts on two qubits, flipping the second qubit if the first is  $|1\rangle$ .

Quantum control is the process of manipulating quantum systems to achieve specific objectives, such as implementing gates with high fidelity. Control is achieved by tuning the system parameters.

The evolution of a quantum system is governed by the Schrödinger equation expressed as follows:

$$i \frac{\partial}{\partial t} |\psi(t)\rangle = \hat{H} |\psi(t)\rangle$$

where  $\hat{H}$  is the Hamiltonian operator that dictates the system's dynamics.

The Hamiltonian will be determined by the control parameters

$$\hat{H} = f(\Omega, \Delta, J)$$

$\Omega$  : Rabi Frequency

$\Delta$  : Detuning

$J$  : Coupling Strength

# Challenges in Quantum Control

Quantum systems are sensitive to interactions with their environment.

Precise control of the  $\Omega$ ,  $\Delta$ ,  $\phi$  or  $J$  pulses is required to realize unitary transformations.

Longer gate times increase the likelihood of decoherence, which requires optimization to reduce execution time.

$$\hat{U}(t) = e^{-i\hat{H}t}$$

*Time is just a parameter in quantum mechanics, not an operator.*  
— Sakurai & Napolitano

# Single Qubit Hamiltonian

$$\hat{H}_{\text{RWA}}(t) = \frac{1}{2} \left( \Delta \hat{\sigma}_z + \Omega(t) e^{i\phi} \hat{\sigma}_+ + \Omega(t) e^{-i\phi} \hat{\sigma}_- \right)$$

$$\hat{\sigma}_{\pm} = \frac{1}{2} (\hat{\sigma}_x \pm i \hat{\sigma}_y)$$

$$\hat{\sigma}_x = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \quad \hat{\sigma}_y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}, \quad \hat{\sigma}_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}.$$

$$\hat{\sigma}_+ = \frac{1}{2} \left( \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} + i \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} \right) = \frac{1}{2} \left( \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} + \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} \right) = \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix}$$

$$\hat{\sigma}_- = \frac{1}{2} \left( \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} - i \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} \right) = \frac{1}{2} \left( \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} - \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} \right) = \begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix}$$

# Two Qubits Hamiltonian

A general two-qubit Hamiltonian can be written as

$$H = \sum_{\alpha, \beta \in \{0, x, y, z\}} c_{\alpha\beta} \sigma_\alpha \otimes \sigma_\beta,$$

Expanded explicitly, the Hamiltonian becomes

$$\begin{aligned} H = & c_{00} I \otimes I + \Omega_{0x} I \otimes \sigma_x + \Omega_{0y} I \otimes \sigma_y + \Delta_{0z} I \otimes \sigma_z + \\ & \Omega_{x0} \sigma_x \otimes I + J_{xx} \sigma_x \otimes \sigma_x + J_{xy} \sigma_x \otimes \sigma_y + J_{xz} \sigma_x \otimes \sigma_z + \\ & \Omega_{y0} \sigma_y \otimes I + J_{yx} \sigma_y \otimes \sigma_x + J_{yy} \sigma_y \otimes \sigma_y + J_{yz} \sigma_y \otimes \sigma_z + \\ & \Delta_{z0} \sigma_z \otimes I + J_{zx} \sigma_z \otimes \sigma_x + J_{zy} \sigma_z \otimes \sigma_y + J_{zz} \sigma_z \otimes \sigma_z. \end{aligned}$$

- $J_{zx} \hat{\sigma}_z^{(c)} \otimes \hat{\sigma}_x^{(t)}$  : Flips the target qubit
- $J_{xz} \hat{\sigma}_x^{(c)} \otimes \hat{\sigma}_z^{(t)}$  : Phase-shifts the target qubit
- $J_{xy} \hat{\sigma}_x^{(c)} \otimes \hat{\sigma}_y^{(t)}$  : Combines bit and phase flip on the target
- $J_{yx} \hat{\sigma}_y^{(c)} \otimes \hat{\sigma}_x^{(t)}$  : Yields a phase-dependent flip on the target
- $J_{xx} \hat{\sigma}_x^{(c)} \otimes \hat{\sigma}_x^{(t)}$  : Promotes simultaneous bit flips
- $J_{yy} \hat{\sigma}_y^{(c)} \otimes \hat{\sigma}_y^{(t)}$  : Yields correlated phase rotations
- $J_{yz} \hat{\sigma}_y^{(c)} \otimes \hat{\sigma}_z^{(t)}$  : Modulates target's detuning via control's phase
- $J_{zy} \hat{\sigma}_z^{(c)} \otimes \hat{\sigma}_y^{(t)}$  : Phase-dependent modulation of the target's state
- $J_{zz} \hat{\sigma}_z^{(c)} \otimes \hat{\sigma}_z^{(t)}$  : Both qubits interact via their detuning

$$\sigma_x \otimes \sigma_x = \begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix} \quad \sigma_x \otimes \sigma_y = \begin{pmatrix} 0 & 0 & 0 & -i \\ 0 & 0 & i & 0 \\ 0 & -i & 0 & 0 \\ i & 0 & 0 & 0 \end{pmatrix} \quad \sigma_x \otimes \sigma_z = \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \\ 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \end{pmatrix}$$

$$\sigma_y \otimes \sigma_x = \begin{pmatrix} 0 & 0 & 0 & -i \\ 0 & 0 & -i & 0 \\ 0 & i & 0 & 0 \\ i & 0 & 0 & 0 \end{pmatrix} \quad \sigma_y \otimes \sigma_y = \begin{pmatrix} 0 & 0 & 0 & -1 \\ 0 & 0 & 1 & 0 \\ 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix} \quad \sigma_y \otimes \sigma_z = \begin{pmatrix} 0 & 0 & -i & 0 \\ 0 & 0 & 0 & i \\ i & 0 & 0 & 0 \\ 0 & -i & 0 & 0 \end{pmatrix}$$

$$\sigma_z \otimes \sigma_x = \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \end{pmatrix} \quad \sigma_z \otimes \sigma_y = \begin{pmatrix} 0 & -i & 0 & 0 \\ i & 0 & 0 & 0 \\ 0 & 0 & 0 & i \\ 0 & 0 & -i & 0 \end{pmatrix} \quad \sigma_z \otimes \sigma_z = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$H = \frac{1}{2} \left( \Delta_c \hat{\sigma}_z^{(c)} + \Delta_t \hat{\sigma}_z^{(t)} + \Omega_c e^{i\phi} \hat{\sigma}_x^{(c)} + \Omega_t e^{i\phi} \hat{\sigma}_x^{(t)} + J_{zx} \hat{\sigma}_z^{(c)} \otimes \hat{\sigma}_x^{(t)} \right)$$

# Hadamard Gate Evolution

A common strategy:

$$\hat{n} = \frac{1}{\sqrt{2}}(\hat{x} + \hat{z})$$

Hamiltonian of one qubit:

$$H = \frac{1}{2}(\Delta \sigma_z + \Omega_x \sigma_x)$$

One often chooses

$$\Omega_x = \Delta = -1$$

so that

$$H = -\frac{1}{2}(\sigma_z + \sigma_x)$$

# Hadamard Gate Evolution

The corresponding time evolution operator is

$$U(t) = e^{-i(-\frac{1}{2}(\sigma_z + \sigma_x))t}$$

A calculation shows that if the pulse duration is set to

$$t = \frac{\pi}{\sqrt{2}}$$

the resulting operator is (up to a global phase) equivalent to the Hadamard gate. In other words,

$$e^{-i(-\frac{1}{2}(\sigma_z + \sigma_x))\frac{\pi}{\sqrt{2}}} \propto H$$

# T Gate Evolution

$$H = \frac{1}{2}\sigma_z$$

$$U(t) = e^{-iHt} = e^{-i\frac{t}{2}\sigma_z} = \begin{pmatrix} e^{-it/2} & 0 \\ 0 & e^{it/2} \end{pmatrix}$$

Removing  $e^{-it/2}$

$$U(t) \propto \begin{pmatrix} 1 & 0 \\ 0 & e^{it} \end{pmatrix}$$

To generate the T gate we need the relative phase to be  $\pi/4$ , so we set

$$t = \frac{\pi}{4}$$

# T Gate Evolution

Thus,

$$e^{-i\frac{\pi}{8}\sigma_z} \propto T$$

More precisely, one obtains

$$U\left(\frac{\pi}{4}\right) = e^{-i\frac{\pi}{8}\sigma_z} = e^{-i\pi/8} \begin{pmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{pmatrix}$$

which implements the T gate up to a global phase.

# CNOT Gate Evolution

$$\text{CNOT} = |0\rangle\langle 0| \otimes I + |1\rangle\langle 1| \otimes X$$

A standard approach:

$$H_{\text{int}} = g |1\rangle\langle 1| \otimes u$$

so that the time evolution operator becomes

$$U(t) = e^{-iH_{\text{int}}t} = |0\rangle\langle 0| \otimes I + |1\rangle\langle 1| \otimes e^{-iut}$$

To implement the CNOT gate, choose

$$u = \frac{\pi}{2}X$$

and set the evolution time  $t = 1$  (with  $g = 1$  in dimensionless units).

# CNOT Gate Evolution

Then,

$$U = e^{-i(|1\rangle\langle 1| \otimes \frac{\pi}{2}X)} = |0\rangle\langle 0| \otimes I + g|1\rangle\langle 1| \otimes e^{-i\frac{\pi}{2}X}$$

Since

$$e^{-i\frac{\pi}{2}X} = -iX$$

(up to a phase), we have

$$U \propto |0\rangle\langle 0| \otimes I + |1\rangle\langle 1| \otimes X$$

which is the CNOT gate (ignoring the phase factor).

Our problem is to find the control parameters that yield these quantum gates. We set the overall time

$$T = 1$$

and we discretize the operator as:

$$U(t) = (e^{-iH(\Omega, \Delta, J)\Delta t})^N U(0)$$

where

$$\Delta t = T/N = 1/N$$

$$U(0) = \mathbb{I}$$

The fidelity of the implemented gate is defined as

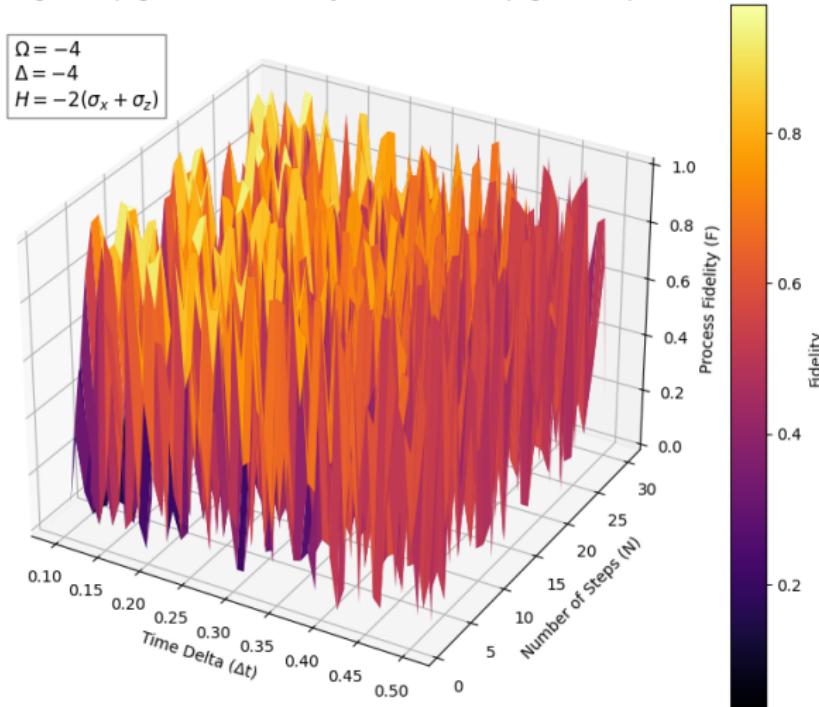
$$F(U, T) = \frac{1}{d^2} \left| \text{Tr}(T^\dagger U) \right|^2$$

where  $T$  is the target gate,  $U$  is the realized gate,  $d$  is the dimension of the Hilbert space. A fidelity close to **1** indicates a high gate accuracy.

While the gate fidelity measures how well a specific unitary transformation is achieved, a more robust measure is the average fidelity of the process, which quantifies the precision of the gate implemented across all possible input states. The average process fidelity  $\bar{F}$  is given by:

$$\bar{F} = \frac{d + F(U, T)d}{d + 1}$$

### H gate-Propagator Process Fidelity vs. Time and Propagation Steps



# Reinforcement Learning

# Markov Decision Process

The optimization of quantum gates can be formulated as a Markov Decision Process (MDP), where the goal is to maximize the fidelity of a quantum operation.

An MDP is represented as a tuple  $(\mathcal{S}, \mathcal{A}, \mathcal{P}, R, \gamma)$

The agent's objective is to find an optimal policy  $\pi^*$  that maps states to actions, maximizing the expected cumulative reward

$$J(\pi) = \mathbb{E} \left[ \sum_{t=0}^{\infty} \gamma^t R_t \right]$$

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## Algorithm General

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**Require:** Initial model parameters  $\theta$

- 1: **for** episode = 1, 2, ..., EPISODES **do**
- 2:   Reset the quantum environment state
- 3:   **for**  $k = 1, 2, \dots, N$  **do**
- 4:     Choose first action to define the pulse
- 5:     Evolve the unitary by the pulse and time
- 6:     Compute the step reward based on fidelity
- 7:     Estimate the next unitary
- 8:     Choose next action according to the agent strategy
- 9:     Store trajectory  $(s_{k-1}, a_{k-1}, s_k, r_k, d_k)$
- 10:   **end for**
- 11:   Calculate Discounted Rewards
- 12:   Calculate Loss Function
- 13:   Update the model parameters  $\theta$
- 14: **end for**

Monte Carlo (MC) methods estimate action or state values by averaging sampled returns from episodes.

In quantum control, they can be used to optimize pulse sequences for gate implementation:

$$V(s) = \mathbb{E}[G_t \mid S_t = s] \quad (1)$$

where  $G_t = \sum_{k=0}^{\infty} \gamma^k R_{t+k}$  is the return.

# Temporal Difference

Temporal Difference (TD) methods combine Monte Carlo sampling with bootstrapping to estimate value functions.

$$V(s) \leftarrow V(s) + \alpha [R_{t+1} + \gamma V(S_{t+1}) - V(S_t)]$$

# Temporal Difference Methods

## Q-Learning

$$Q(S_t, A_t) \leftarrow Q(S_t, A_t) + \alpha \left[ R_{t+1} + \gamma \max_a Q(S_{t+1}, a) - Q(S_t, A_t) \right]$$

## SARSA

$$Q(S_t, A_t) \leftarrow Q(S_t, A_t) + \alpha [R_{t+1} + \gamma Q(S_{t+1}, A_{t+1}) - Q(S_t, A_t)]$$

## Deep Q-Network

$$\mathcal{L}(\theta) = \mathbb{E}_{(s,a,r,s')} \left[ \left( R_{t+1} + \gamma \max_a Q(s', a; \theta^-) - Q(s, a; \theta) \right)^2 \right]$$

# Temporal Difference Methods

Double Deep Q-Networks (DDQN) Double Deep Q-Network

$$\mathcal{L}(\theta) = \mathbb{E}_{(s,a,r,s')} \left[ \left( R_{t+1} + \gamma Q(s', \arg \max_a Q(s', a; \theta); \theta^-) - Q(s, a; \theta) \right)^2 \right]$$

Double Dueling Deep Q-Network (DDDQN)

$$Q(s, a) = V(s) + A(s, a) - \frac{1}{|\mathcal{A}|} \sum_{a'} A(s, a')$$

Policy gradient methods directly optimize the policy  $\pi_\theta(a | s)$  by maximizing the expected return:

$$\nabla_\theta J(\pi_\theta) = \mathbb{E}_{\pi_\theta} [\nabla_\theta \log \pi_\theta(a | s) G_t]$$

# Policy Gradient Methods

REINFORCE:

$$\Delta\theta \propto \nabla_\theta \log \pi_\theta(a | s) G_t.$$

REINFORCE with Baseline: To reduce variance, a baseline  $b(s)$  is introduced

$$\Delta\theta \propto \nabla_\theta \log \pi_\theta(a | s) [G_t - b(s)].$$

# Policy Gradient Methods

DDPG is designed for continuous action spaces and leverages a deterministic policy:

$$a = \mu_\theta(s)$$

The critic evaluates the Q-value  $Q(s, a)$ , and both the actor and the critic are updated using neural networks

TD3 improves DDPG by addressing its sensitivity to overestimation and instability. Key modifications include:

- Double Critics: Two critic networks are used, and the smaller Q-value is chosen during updates:

$$y = R + \gamma \min_{i=1,2} Q_i(s', \mu(s'))$$

- Delayed Policy Update The actor is updated less frequently than the critics to improve stability.
- Target Policy Smoothing: Adds noise to the target actions to prevent the use of sharp Q-value spikes.

# Policy Gradient Methods

PPO simplifies trust-region policy optimization by clipping the policy ratio:

$$L^{CLIP}(\theta) = \mathbb{E}_t \left[ \min \left( r_t(\theta) \hat{A}_t, \text{clip}(r_t(\theta), 1 - \epsilon, 1 + \epsilon) \hat{A}_t \right) \right]$$

where  $r_t(\theta)$  is the probability ratio and  $\hat{A}_t$  is the advantage estimate.

GRPO is built on top of PPO and is a critic-free model.

# Implementation

To optimize the gate control process, four reinforcement learning algorithms were implemented:

DDDQN: Discrete - Deterministic

TD3: Continuous - Deterministic

PPO: Both - Stochastic

GRPO: Both - Stochastic

# Reward Shaping

$$F = \frac{1}{d^2} \left| \text{Tr}(T^\dagger U) \right|^2$$

$$L = \log_{10}(1 - F)$$

$$R = -L \left( 1 - \frac{t}{T_{\max}} \right)$$

The episode terminates if:

$$t = T_{\max} | F \geq F_{\text{threshold}}$$

At the final time step, an additional reward scaling factor is introduced:

$$R \leftarrow R \times 5, \quad \text{if } F \geq F_{\text{threshold}}$$

where  $F_{\text{threshold}}$  is the predefined fidelity threshold.

# State Representation

$$U = \begin{bmatrix} a + ib & c + id \\ e + if & g + ih \end{bmatrix}$$

$$\mathcal{S} = [a, b, c, d, e, f, g, h]$$

## Hadamard Gate ( $H$ ) and T Gate

- Control Parameters: Rabi frequency  $\Omega_x(t)$ , and detuning  $\Delta(t)$ .
- Actions:
  - Adjust  $\Omega_x$  for qubit rotations.
  - Control  $\Delta$  to maintain resonance.
  - Values for a discrete set:  $\{-4, 0, 4\}$  for both parameters.

## CNOT Gate

- Control Parameters: Coupling strength  $J_{zx}$ ; target qubit Rabi frequency  $\Omega_x^t$  and detuning  $\Delta_t$ ; and control qubit Rabi frequency  $\Omega_x^c$  and detuning  $\Delta_c$ .
- Actions:
  - Tune  $J_{zx}$  for entangling operations.
  - Adjust  $\Omega_x^c$ ,  $\Omega_x^t$  for qubit rotations.
  - Control  $\Delta_c$ ,  $\Delta_t$  to maintain resonance.
  - Values for a discrete set:  $\{-4, 0, 4\}$  for single-qubit parameters and  $\{-4, -2, 2, 4\}$  for the coupling strength.

# Unitary Evolution

$$i\hbar \frac{d}{dt} U(t) = \hat{H}(t)U(t)$$

$$U(t + \Delta t) = e^{-i\hat{H}(t)\Delta t} U(t)$$

$$U(0) = \mathbb{I}$$

$$U_{n+1} = e^{-i\hat{H}_n\Delta t} U_n$$

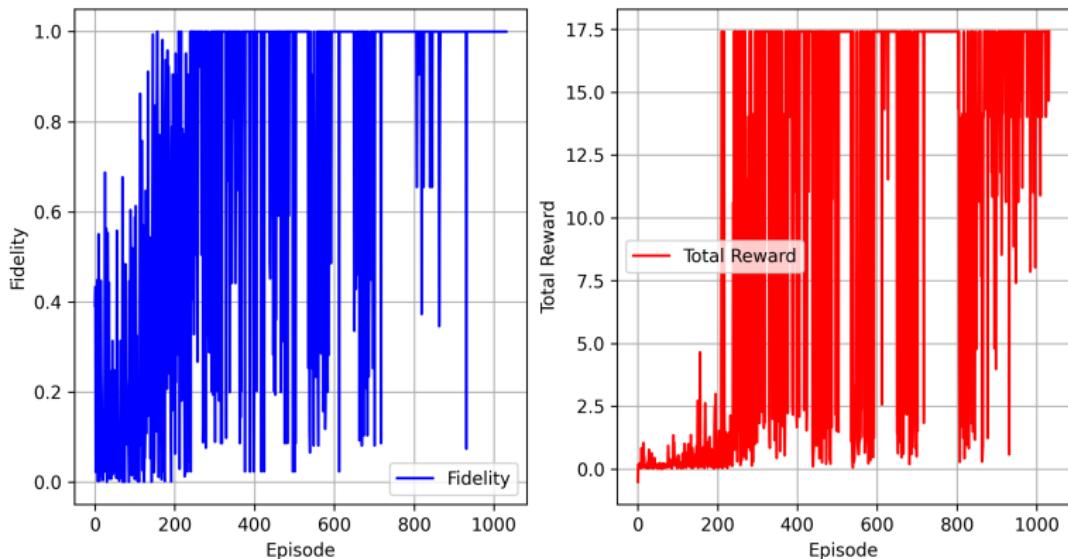
# System Configuration

- Operating system: Linux Kernel 6.11.5-1-liquorix-amd64
- Processor: x86\_64, 64-bit architecture
- CPU Cores: 6 physical cores, 12 logical threads
- CPU Frequency: 2601.00 MHz
- Total RAM: 31.00 GB
- Python Version: 3.12.7
- PyTorch Version 2.6.0+cu124
- CUDA Version: 12.6
- cuDNN Version: 9.0.1
- NVIDIA Compiler (nvcc): CUDA 12.6
- GPU Model: NVIDIA GeForce GTX 1650 Ti
- Driver Version: 560.35.03
- GPU Memory: 4 GB
- CUDA Cores: GTX 1650 Ti features 1024 CUDA cores.

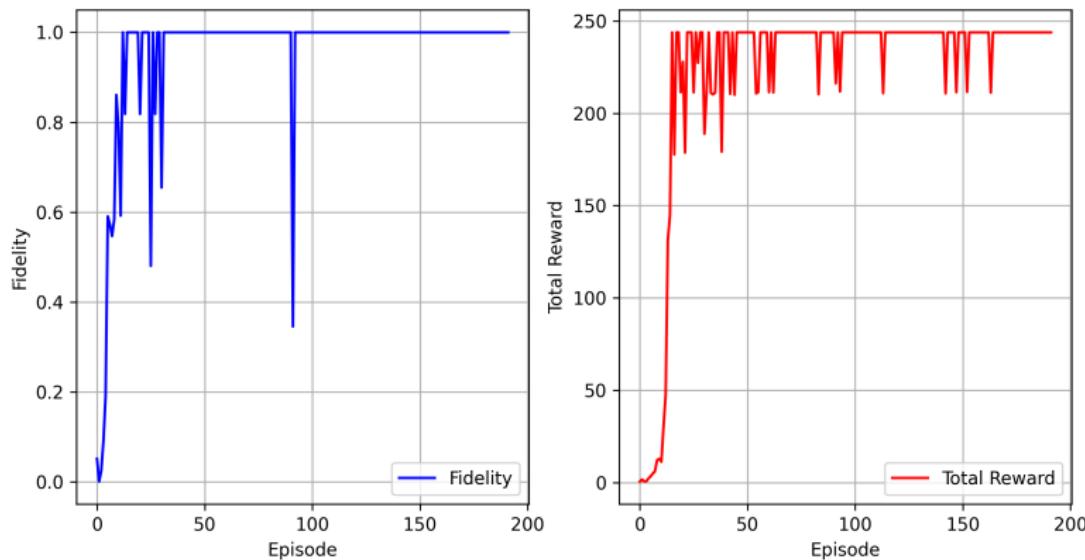
# Results

# H Gate Training

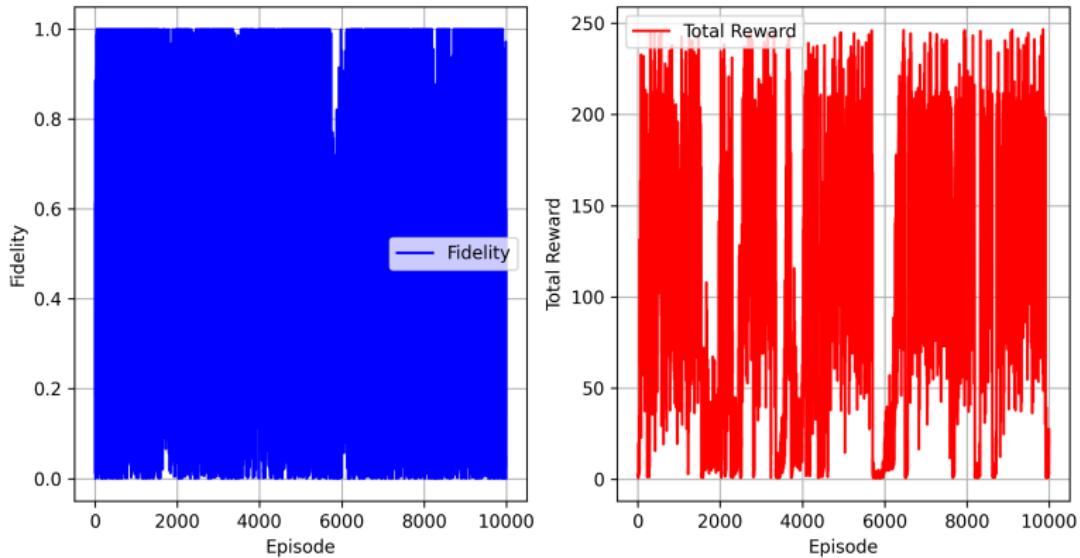
DDDQN H-Gate Training



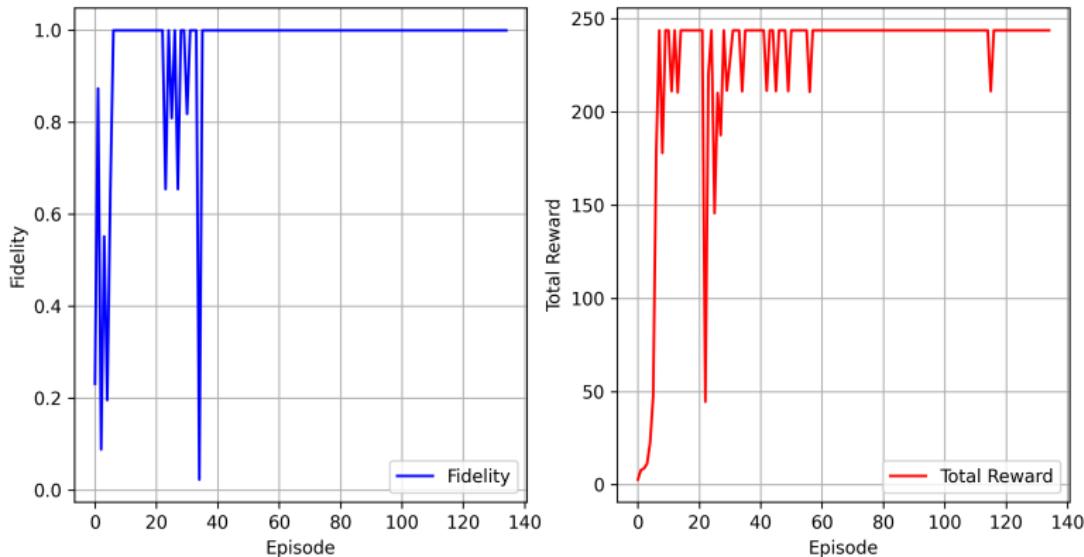
### DPPO H-Gate Training



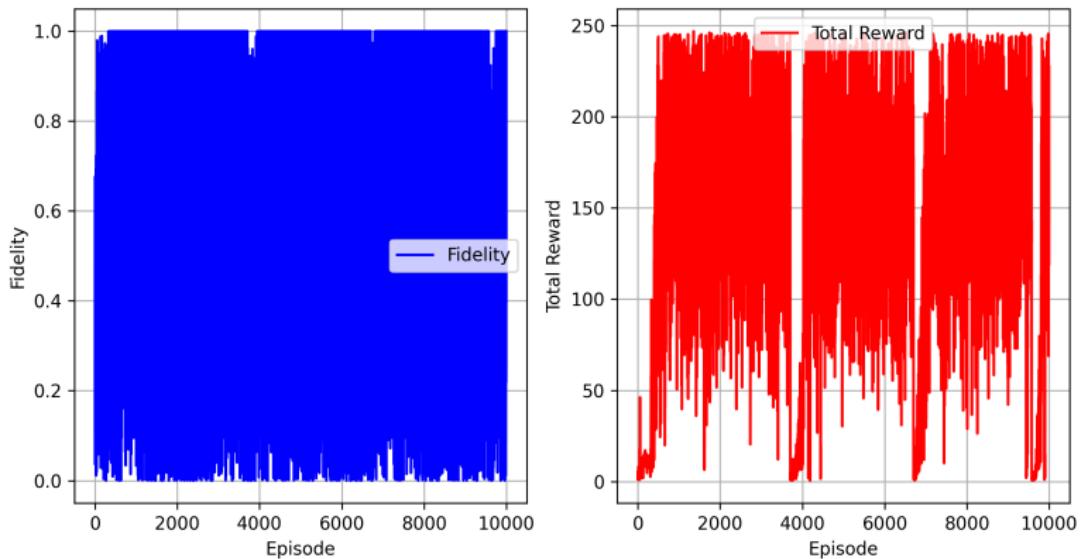
### CPPO H-Gate Training



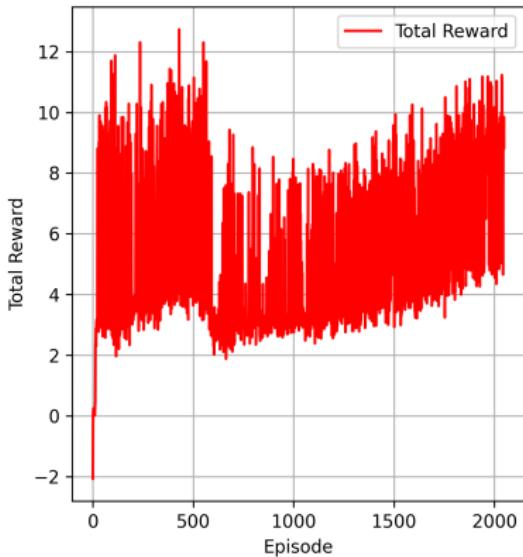
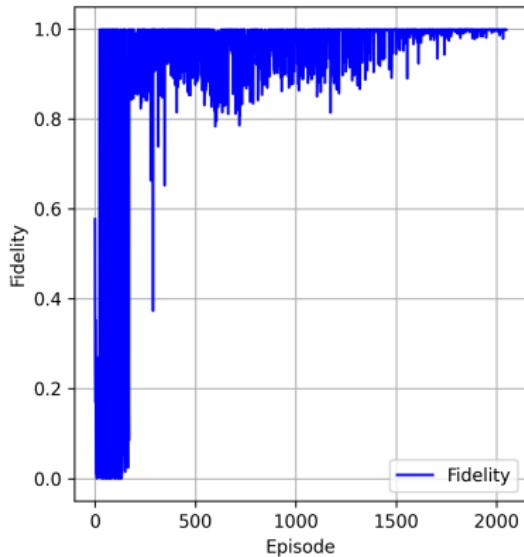
### DGRPO H-Gate Training



### CGRPO H-Gate Training



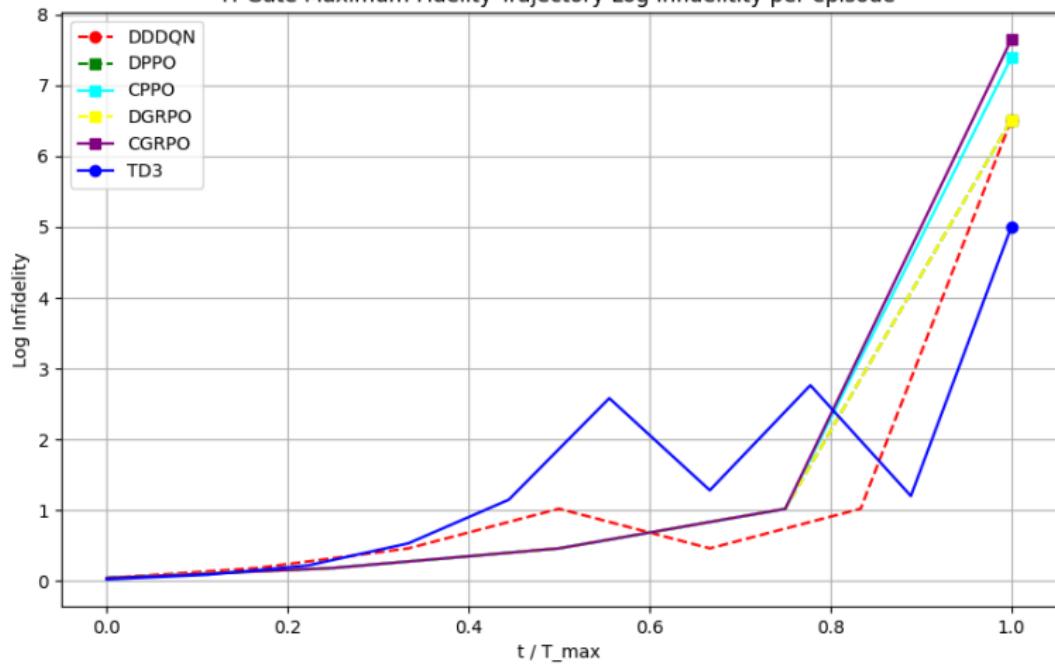
### TD3 H-Gate Training



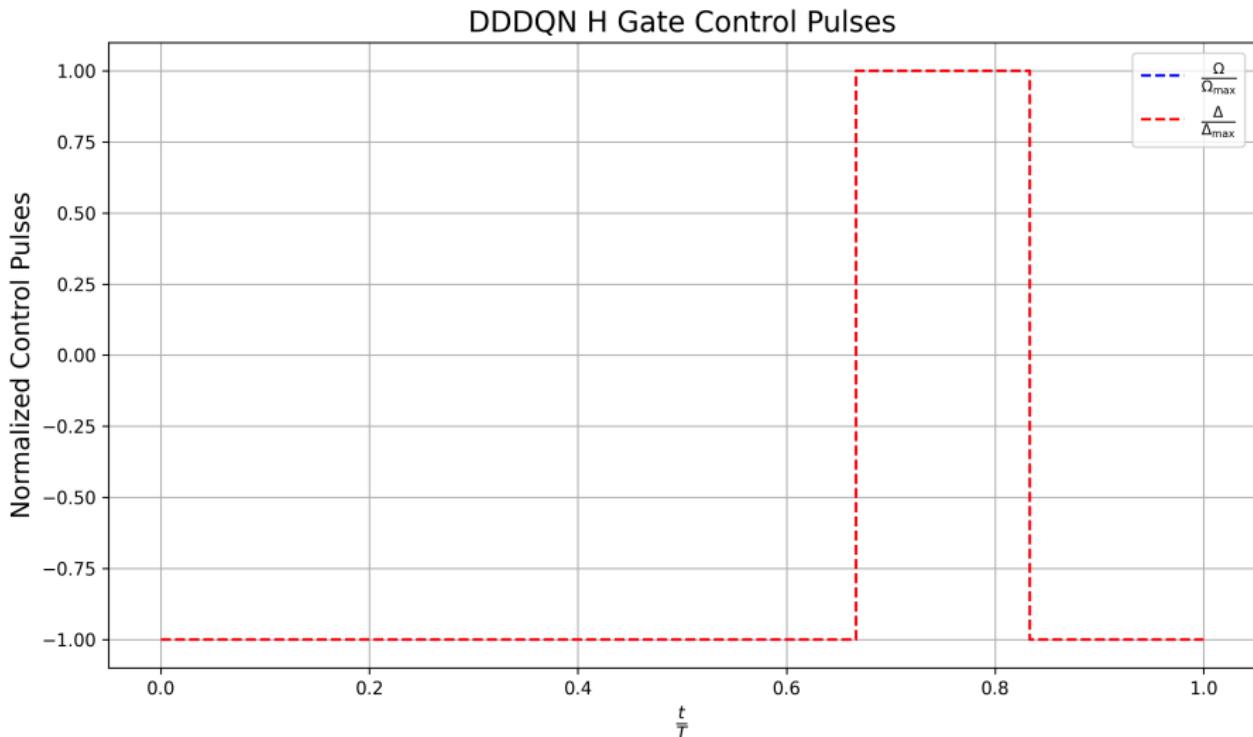
# H Gate Performance Metrics

	Agent	Max Fidelity	Max Log Infidelity	Avg Fidelity	Time Steps
5	TD3	0.999990	5.005089	0.999993	10
1	DPPO	1.000000	6.516003	1.000000	5
3	DGRPO	1.000000	6.516003	1.000000	5
0	DDDQN	1.000000	6.516003	1.000000	7
2	CPPO	1.000000	7.395267	1.000000	5
4	CGRPO	1.000000	7.650909	1.000000	5

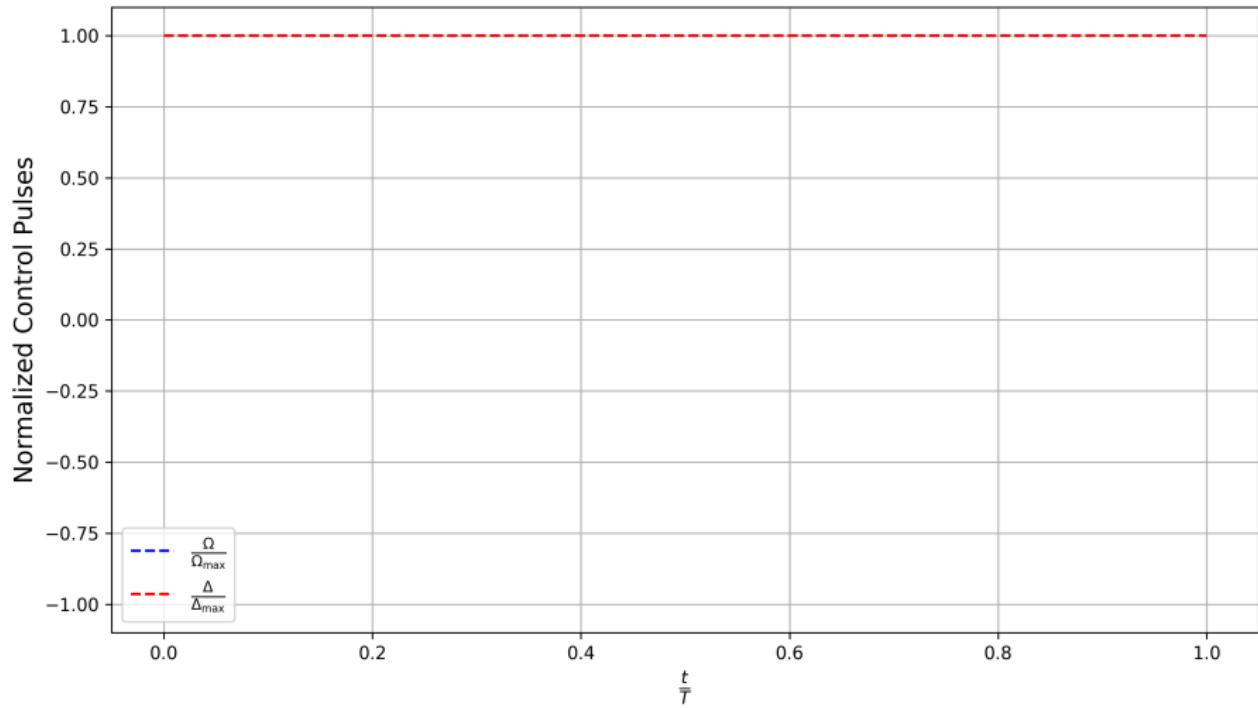
H-Gate Maximum Fidelity Trajectory Log Infidelity per episode



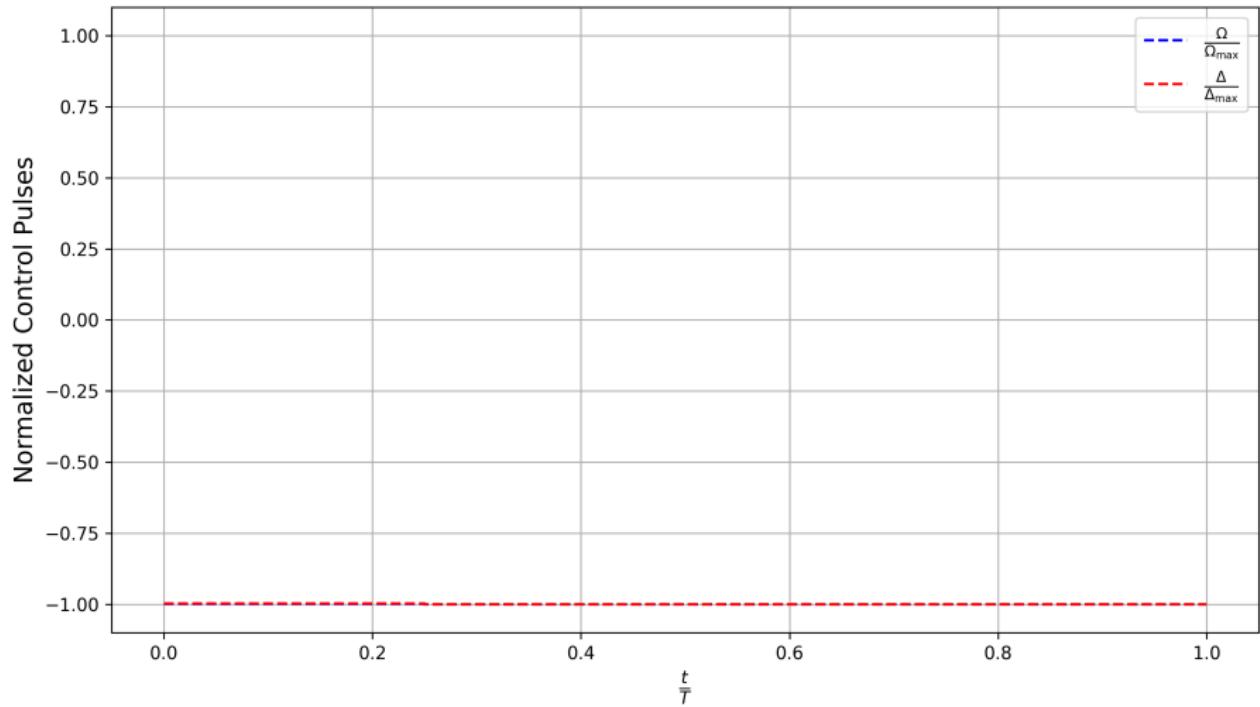
# H Gate Control Pulses



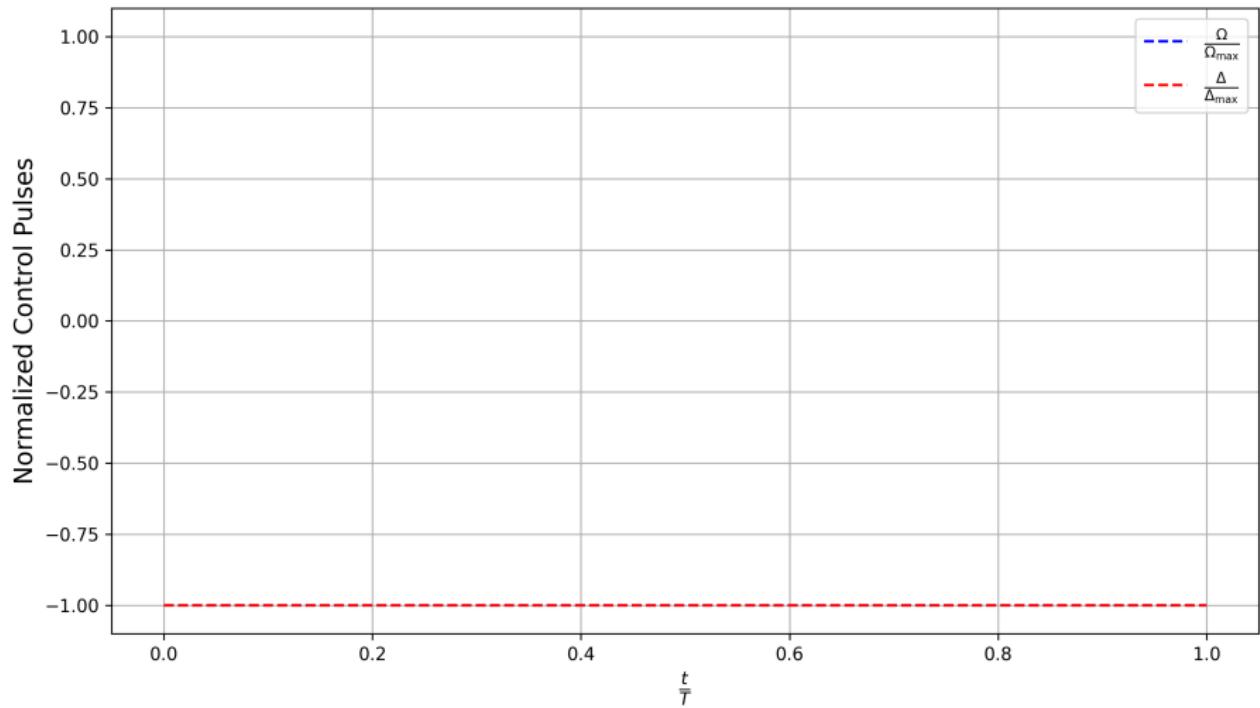
## DPPO H Gate Control Pulses



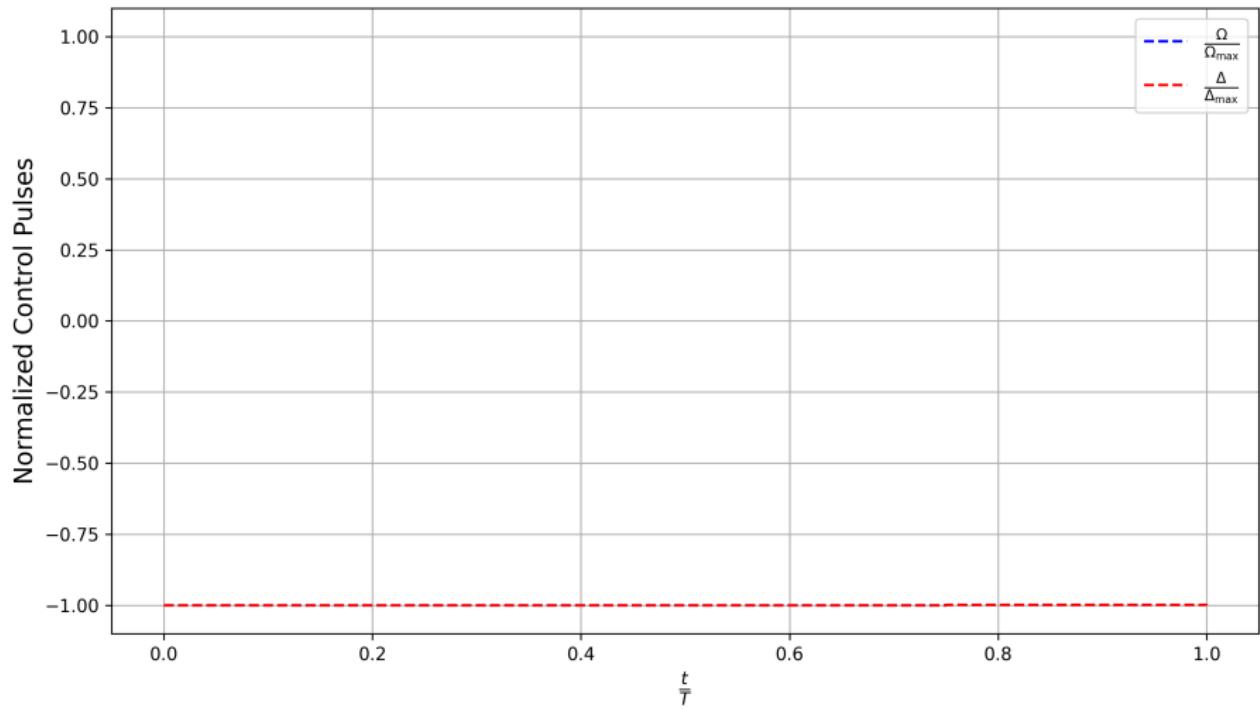
## CPPO H Gate Control Pulses



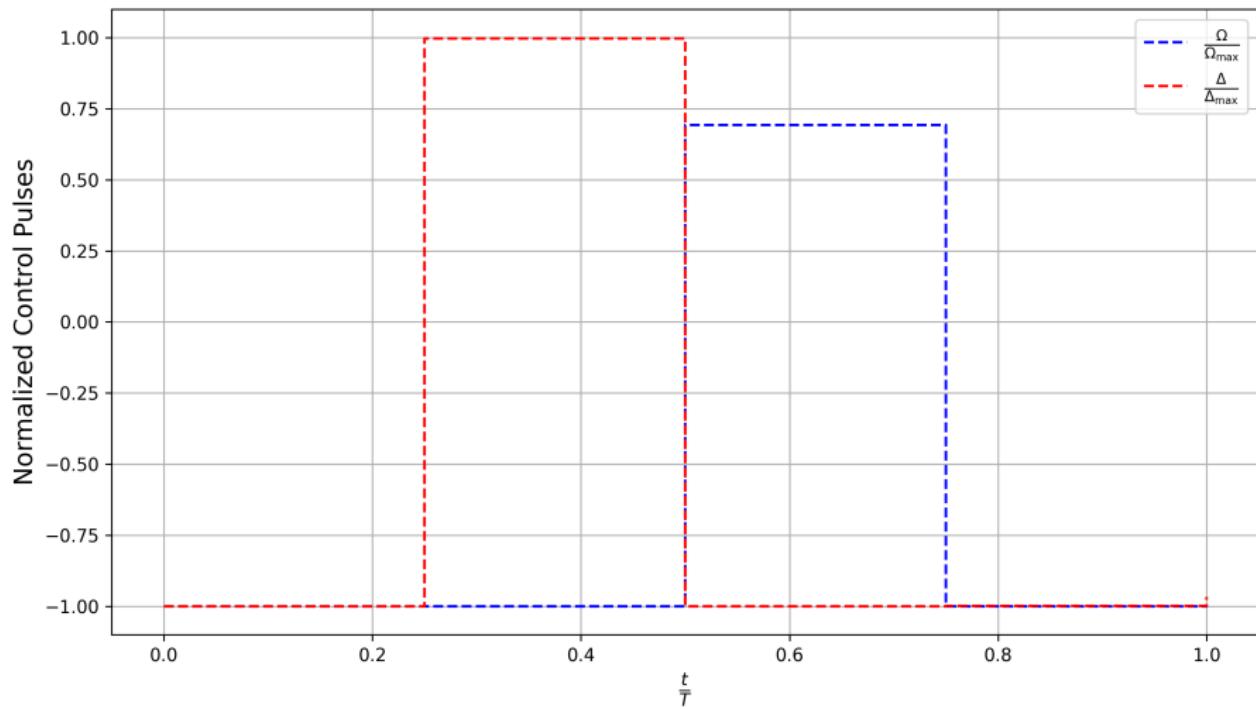
## DGRPO H Gate Control Pulses



## CGRPO H Gate Control Pulses

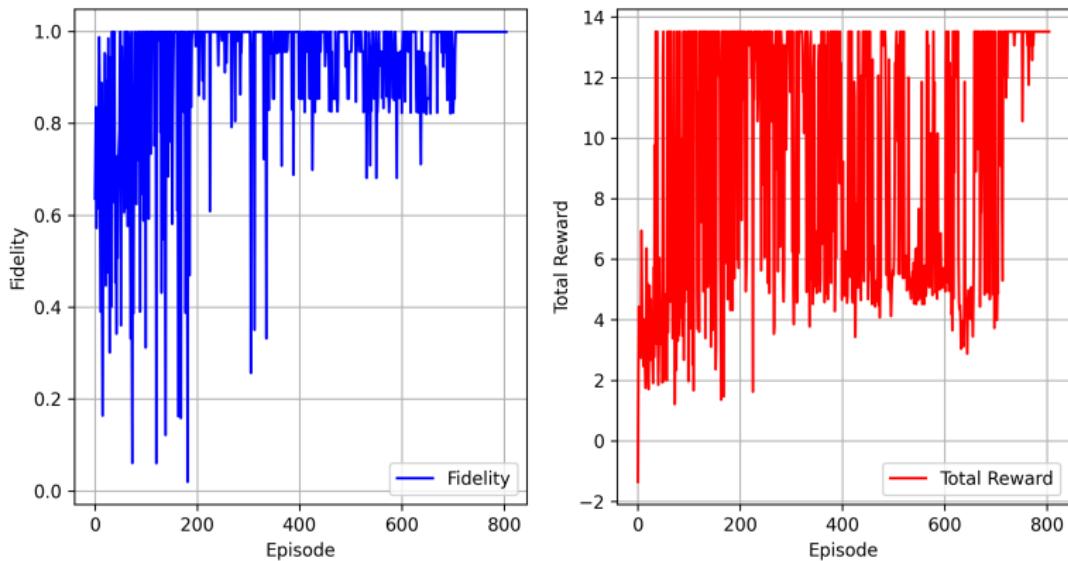


## TD3 H Gate Control Pulses

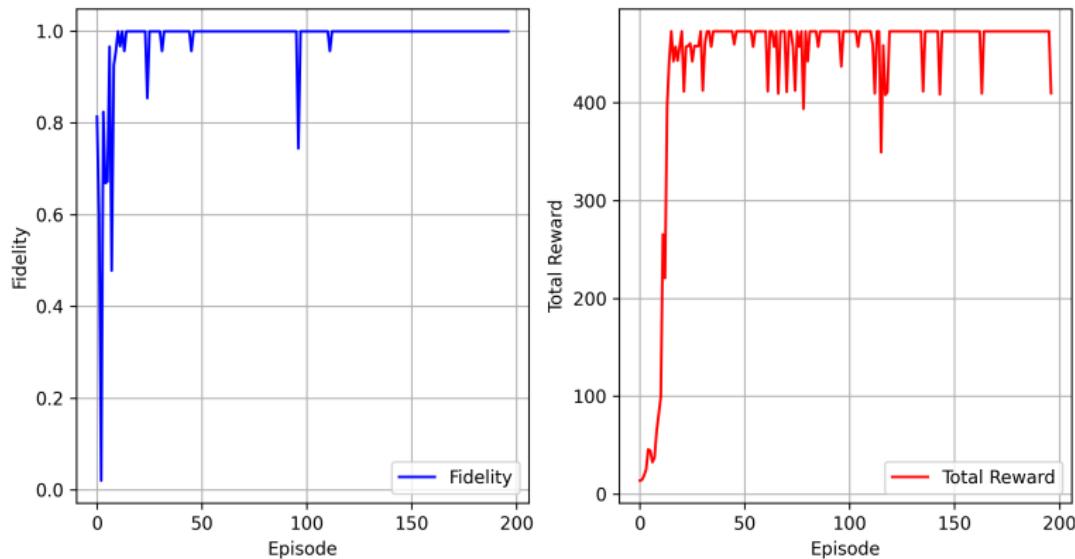


# T Gate Training

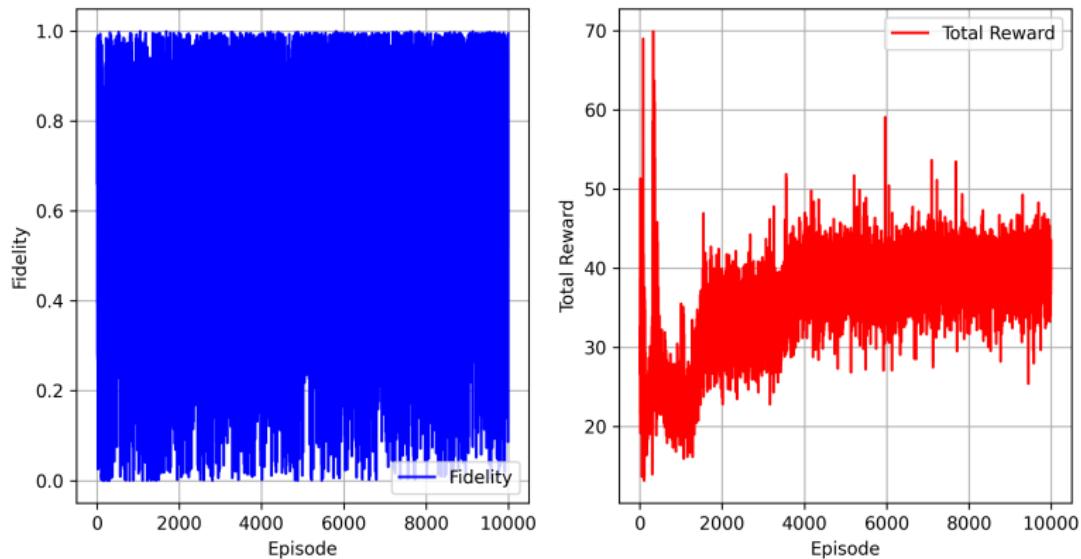
DDQN T-Gate Training



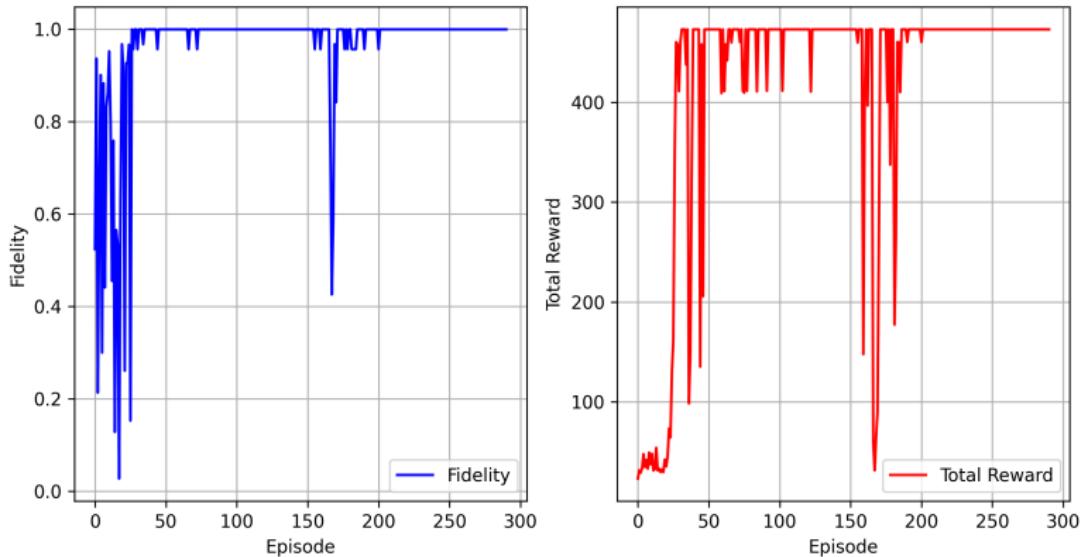
### DPPO T-Gate Training



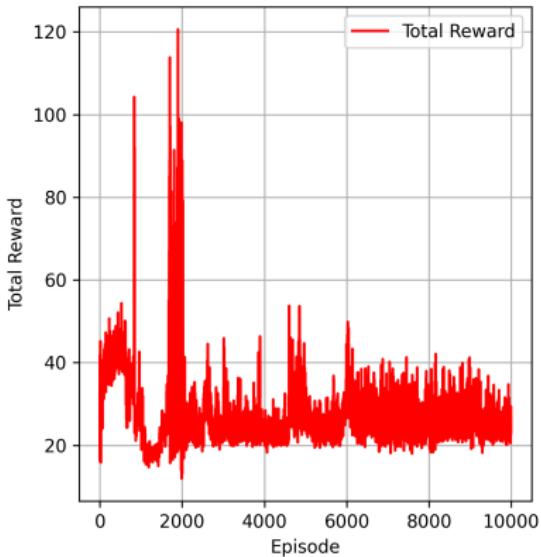
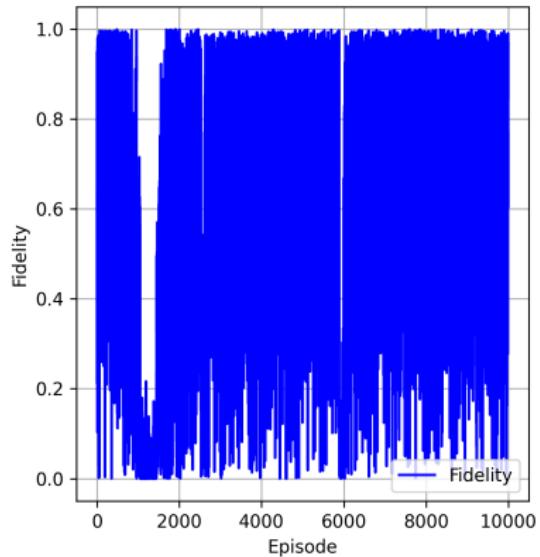
### CPPO T-Gate Training



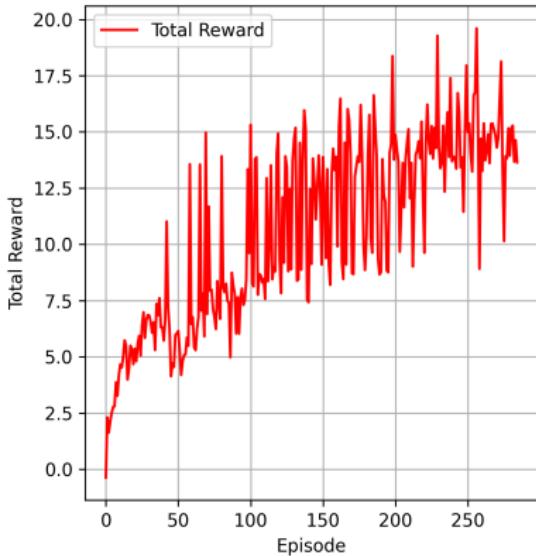
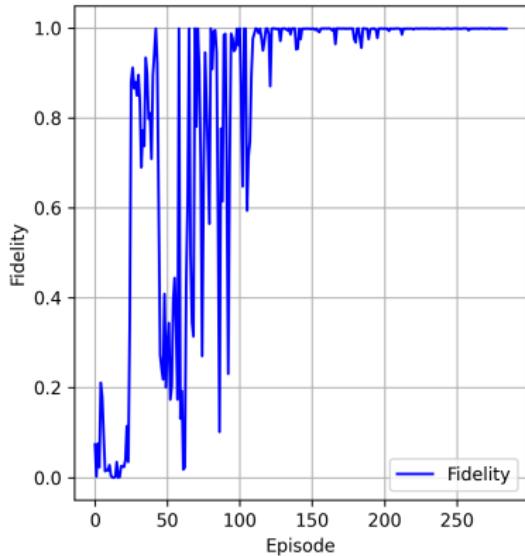
### DGRPO T-Gate Training



### CGRPO T-Gate Training



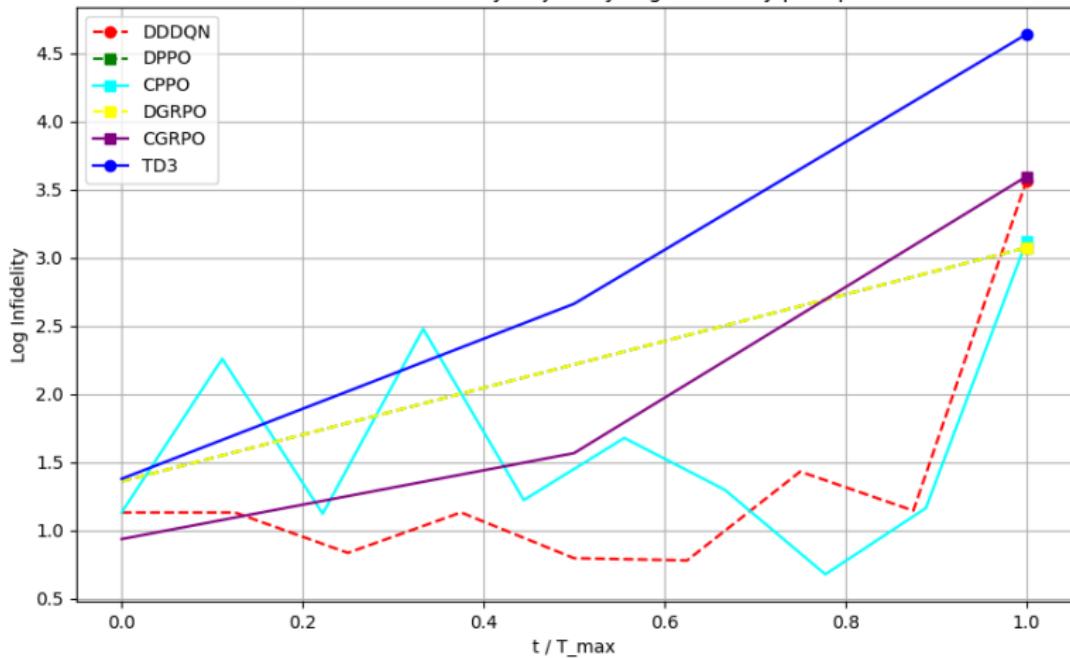
### TD3 T-Gate Training



# T Gate Performance Metrics

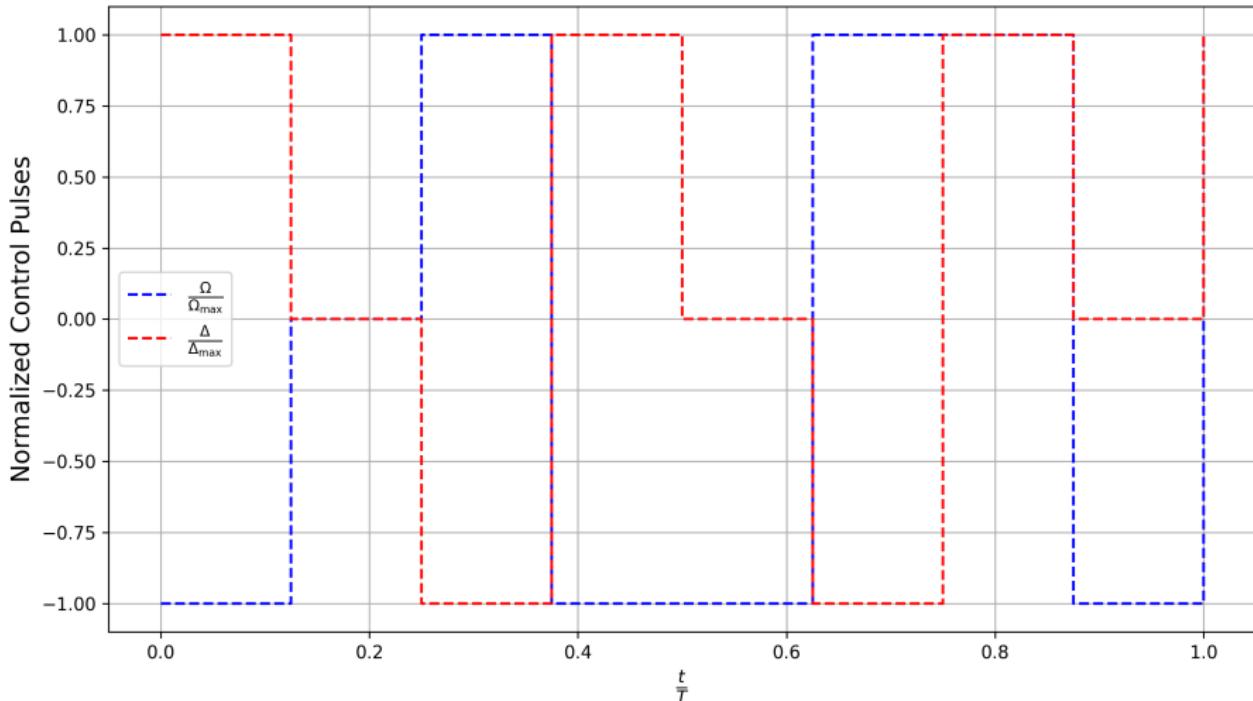
	Agent	Max Fidelity	Max Log Infidelity	Avg Fidelity	Time Steps
1	PPO-D	0.999156	3.073450	0.999437	2
3	GRPO-D	0.999156	3.073450	0.999437	2
2	PPO-C	0.999240	3.119451	0.999494	10
0	DDDQN	0.999726	3.562547	0.999817	9
4	GRPO-C	0.999746	3.594970	0.999831	3
5	TD3	0.999977	4.638075	0.999985	3

T-Gate Maximum Fidelity Trajectory Log Infidelity per episode

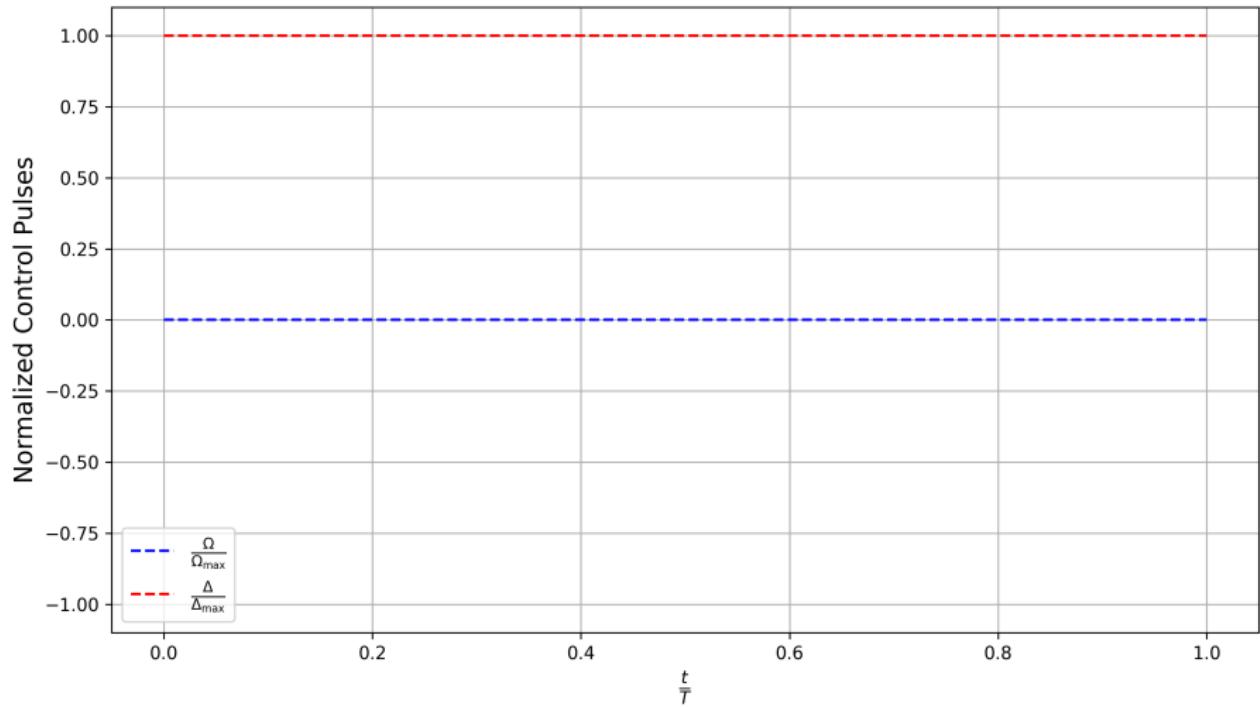


# T Gate Control Pulses

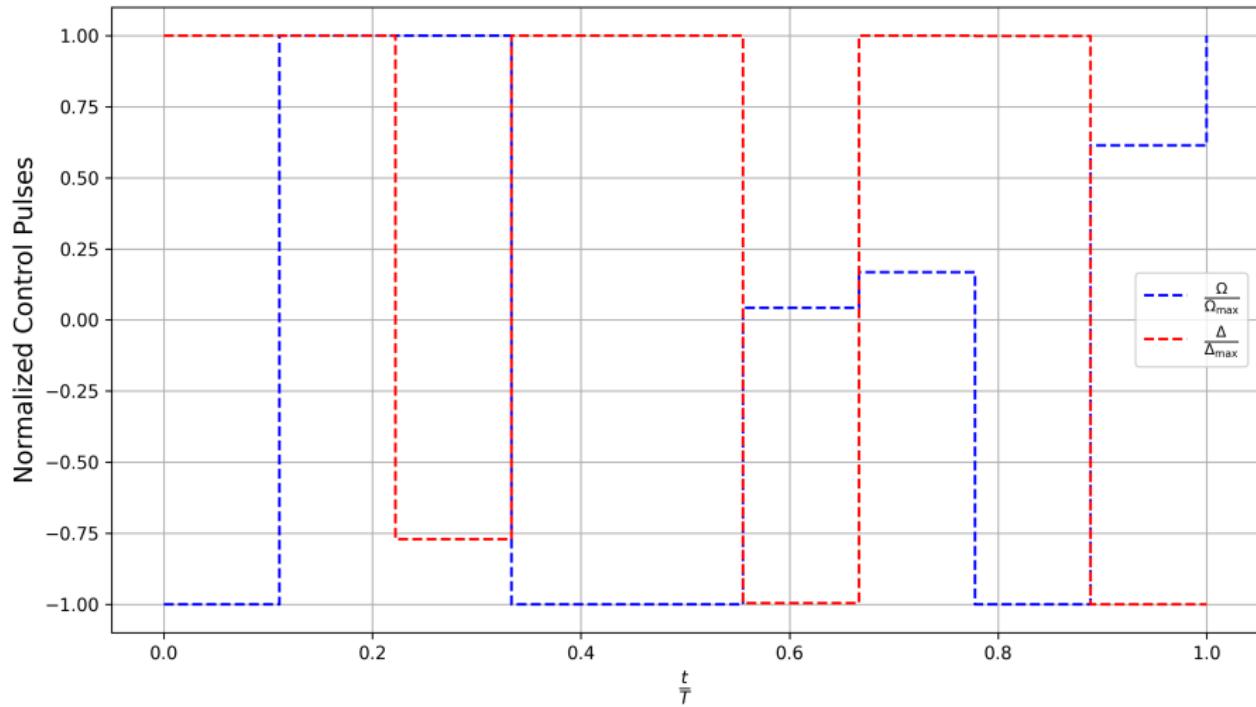
DDDQN T Gate Control Pulses



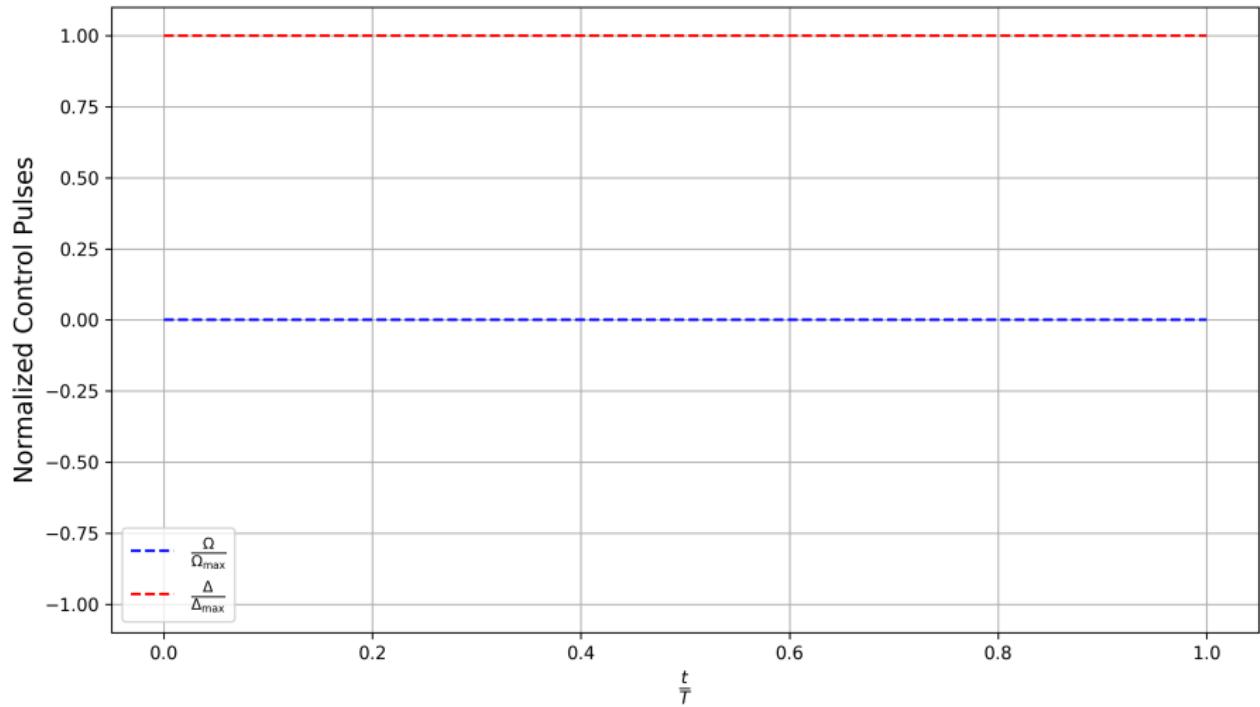
## DPPO T Gate Control Pulses



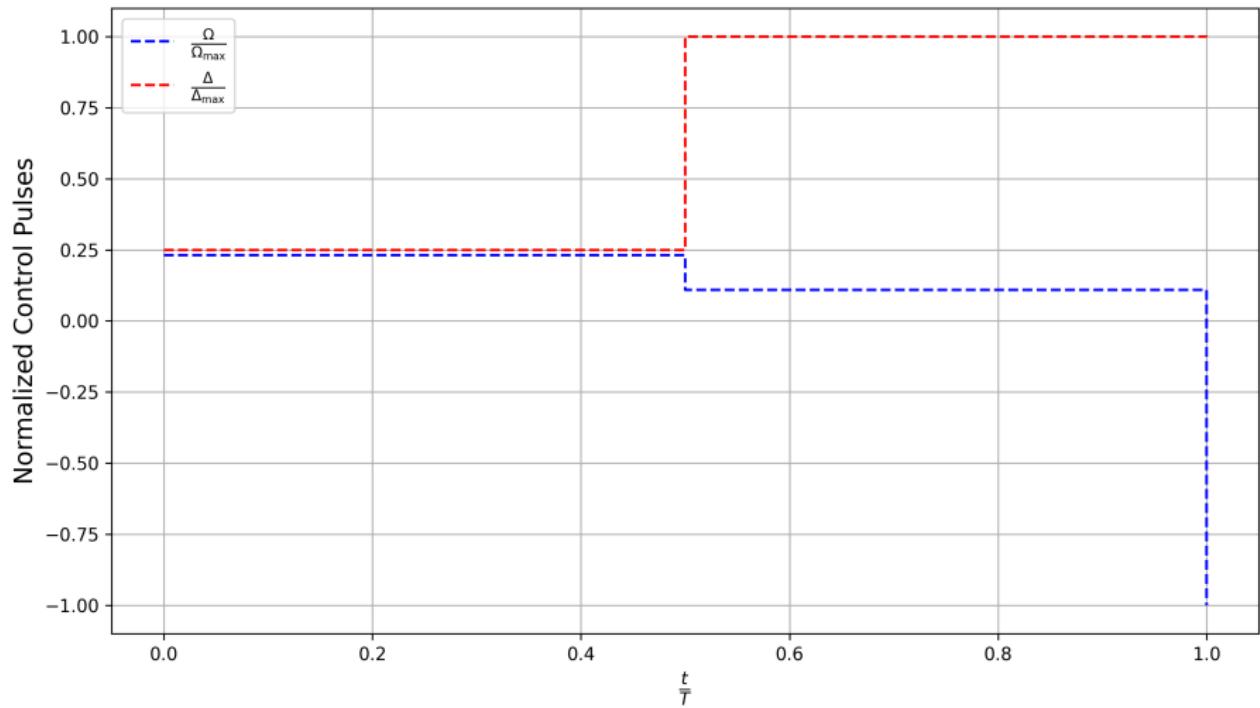
## CPPO T Gate Control Pulses



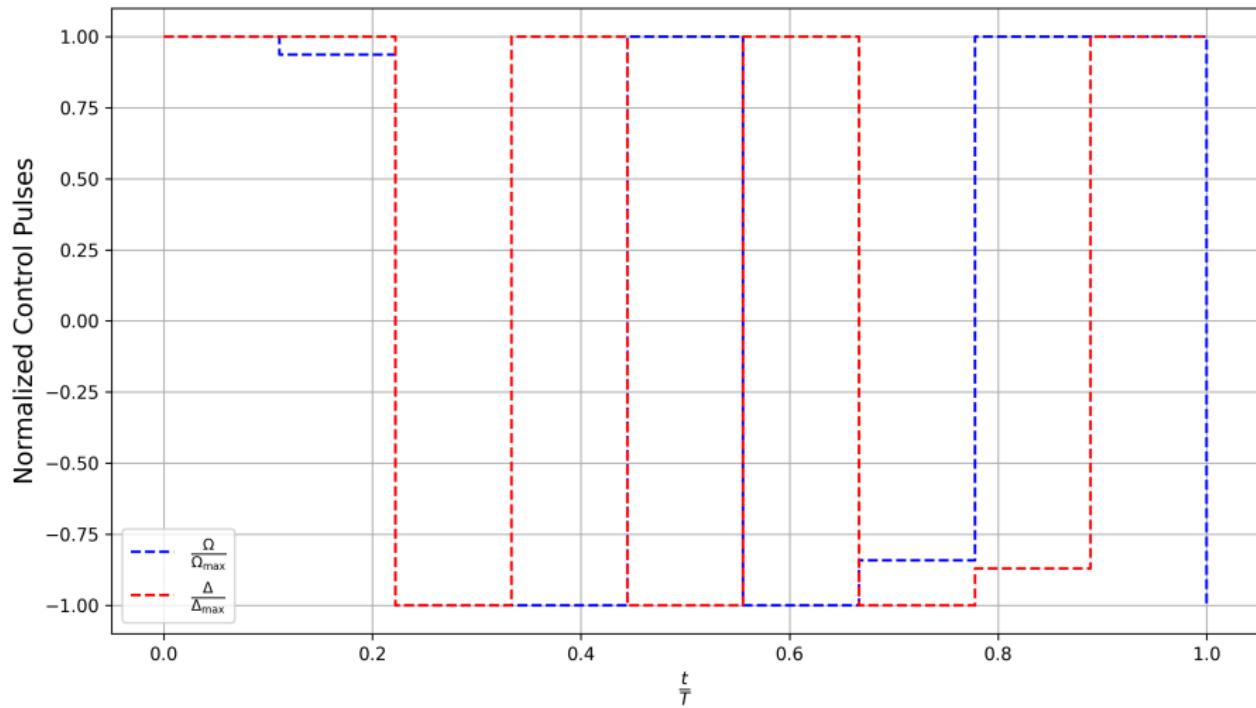
## DGRPO T Gate Control Pulses



## CGRPO T Gate Control Pulses

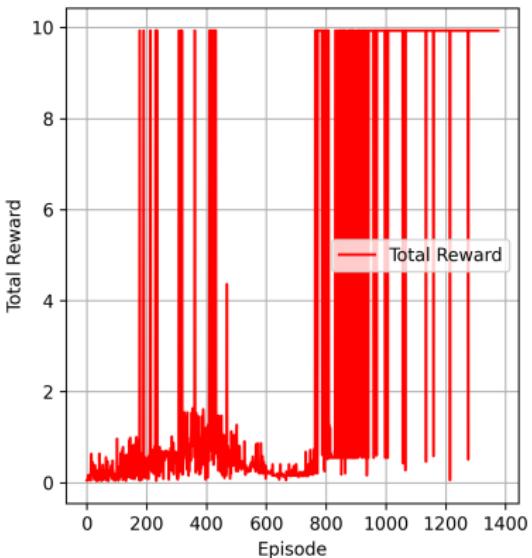
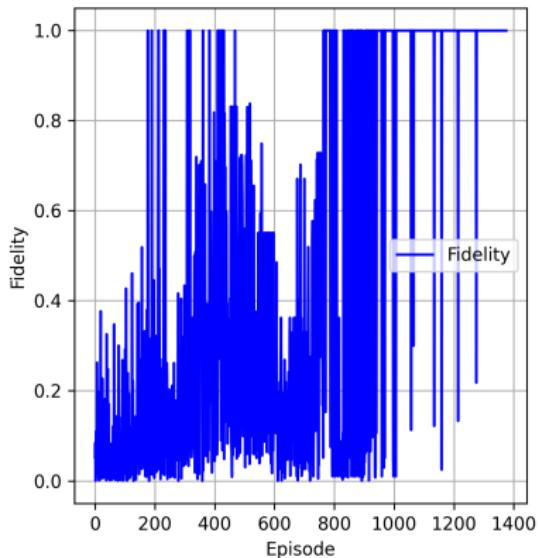


## TD3 T Gate Control Pulses

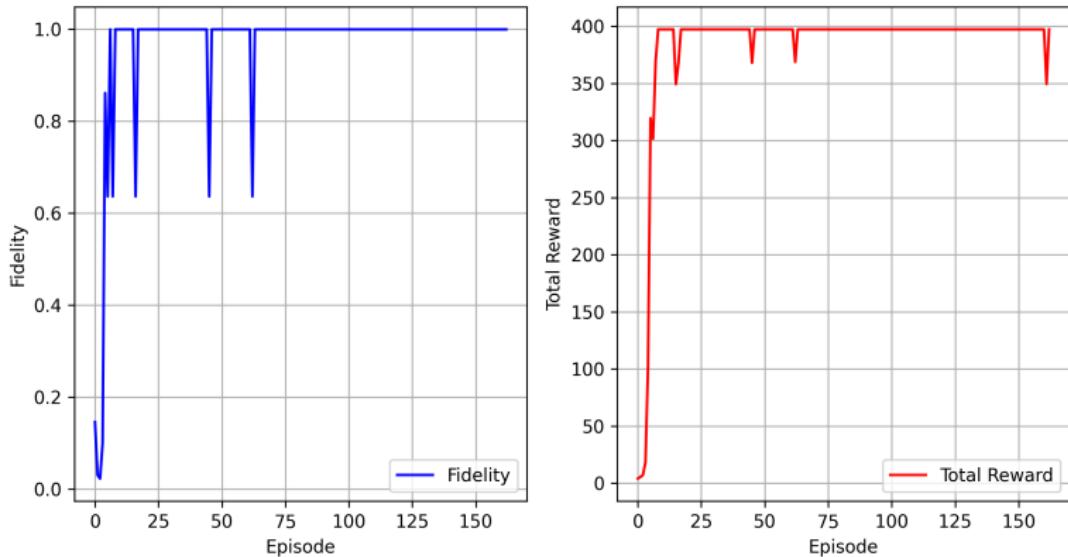


# CNOT Gate Training

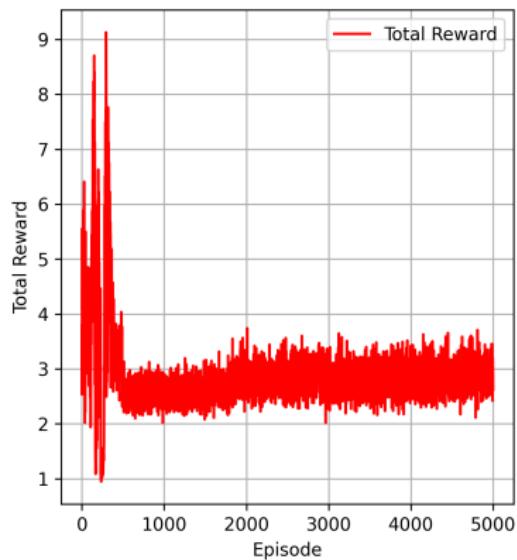
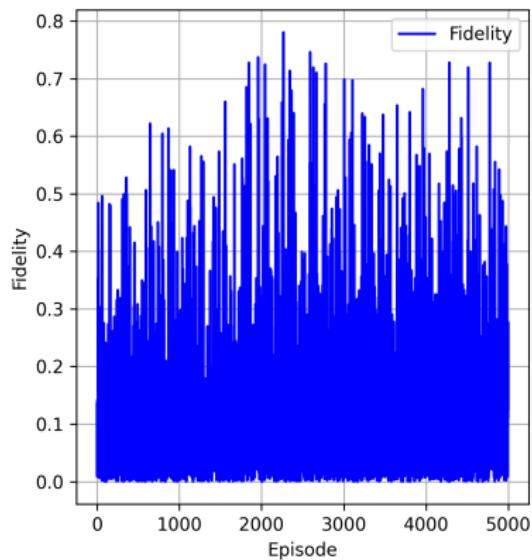
DDDQN CNOT-Gate Training



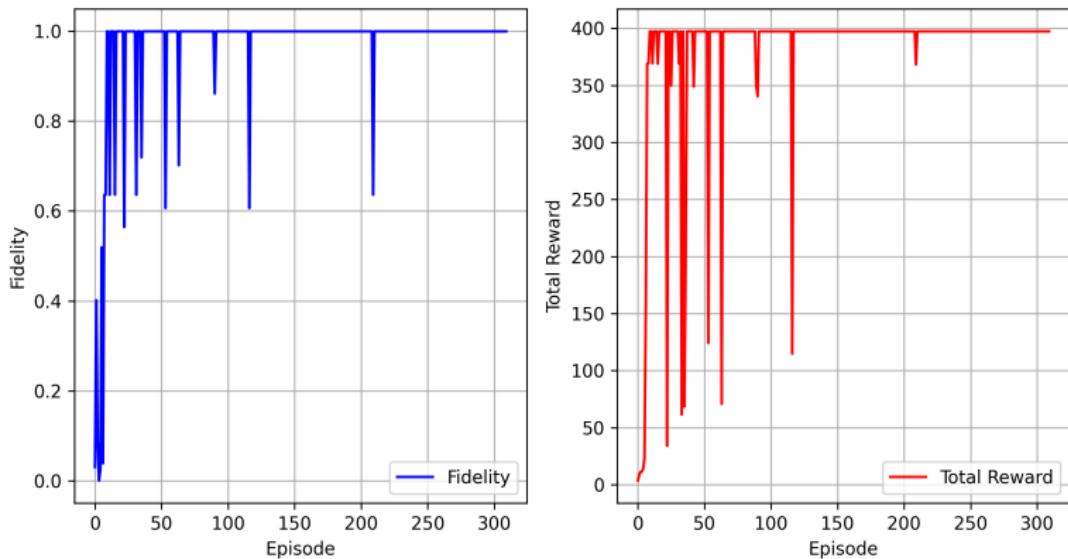
### DPPO CNOT-Gate Training



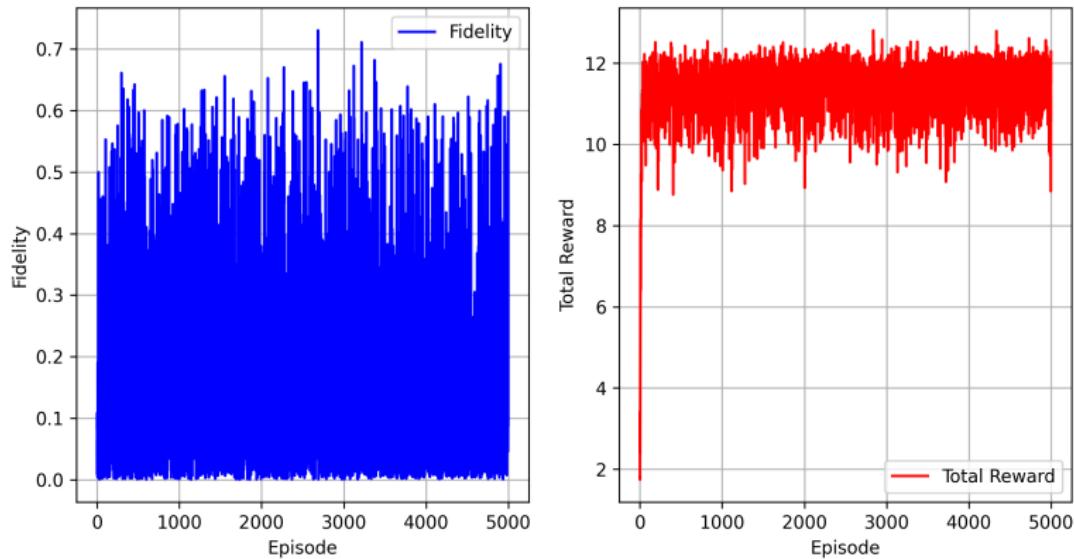
### CPPO CNOT-Gate Training



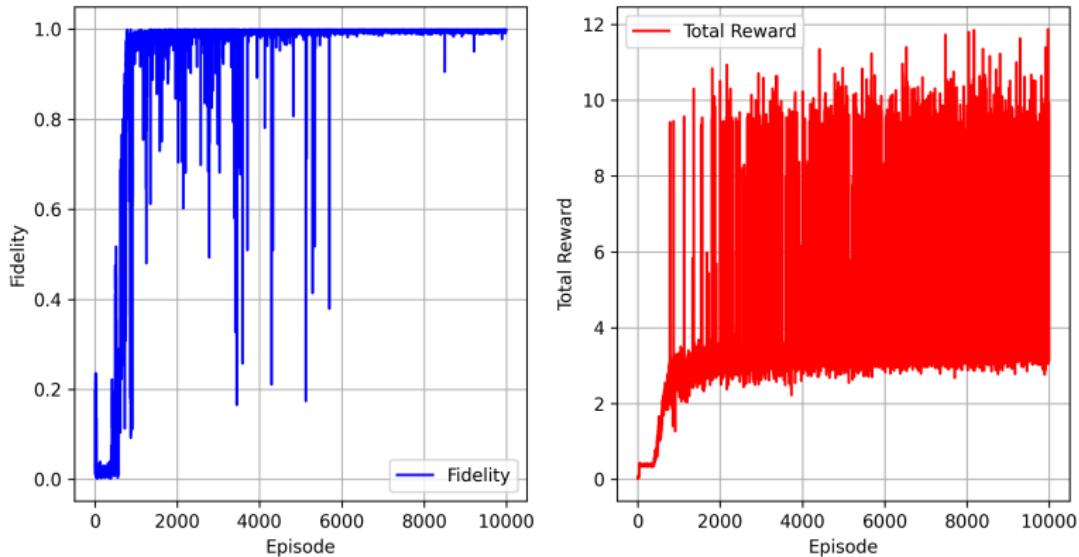
### DGRPO CNOT-Gate Training



### CGRPO CNOT-Gate Training



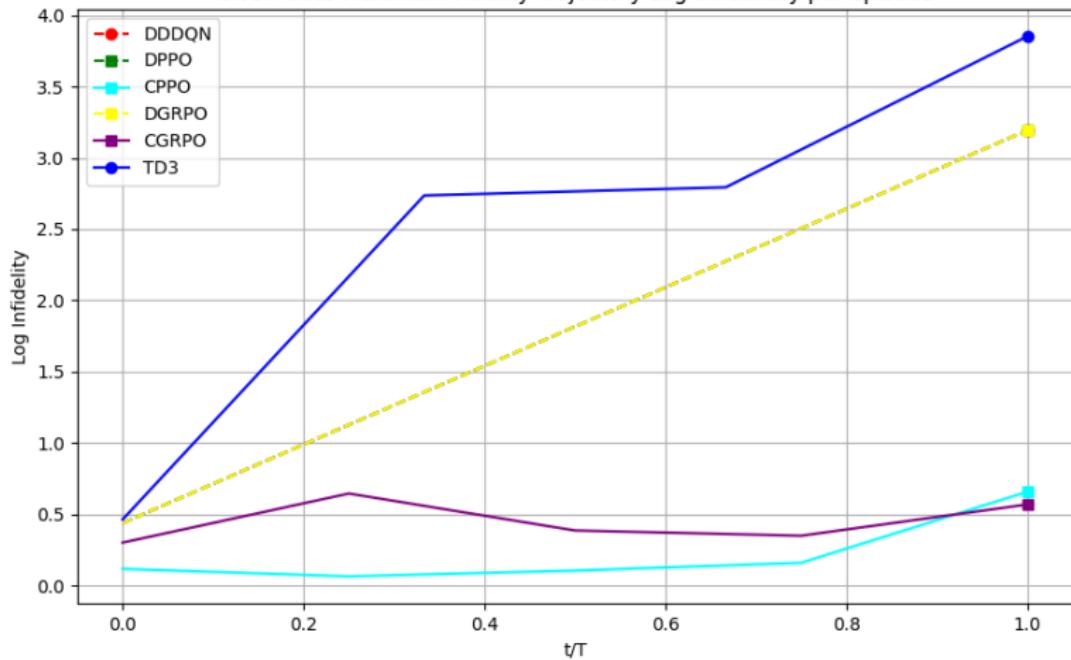
### TD3 CNOT-Gate Training



# CNOT Gate Performance Metrics

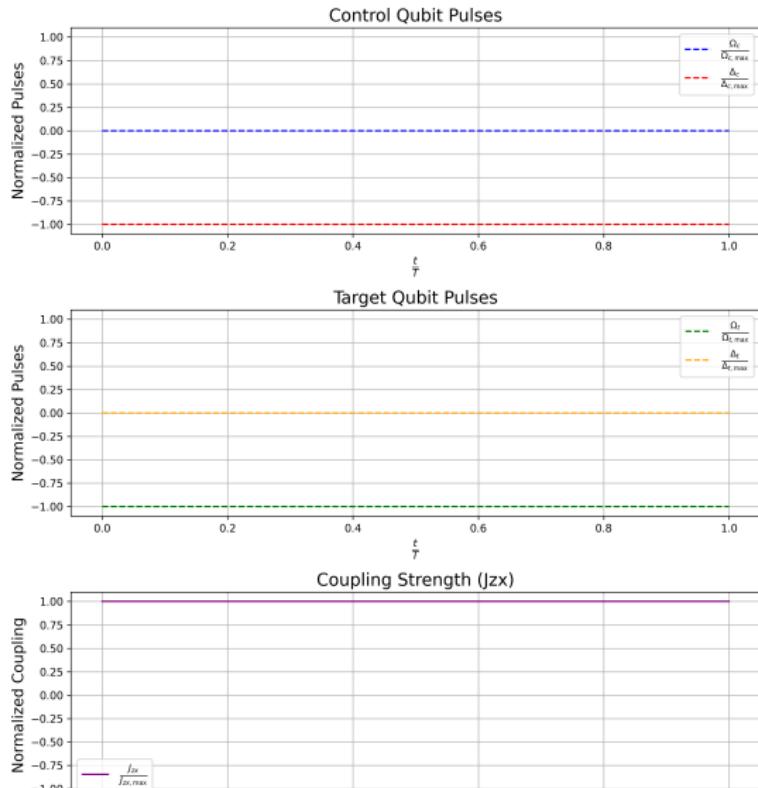
Agent	Max Fidelity	Max Log Infidelity	Avg Fidelity	Time Steps
GRPO-C	0.730429	0.569327	0.784343	5
PPO-C	0.780537	0.658638	0.824429	5
DDDQN	0.999361	3.194187	0.999488	2
PPO-D	0.999361	3.194187	0.999488	2
GRPO-D	0.999361	3.194187	0.999488	2
TD3	0.999860	3.852707	0.999888	4

### CNOT-Gate Maximum Fidelity Trajectory Log Infidelity per episode

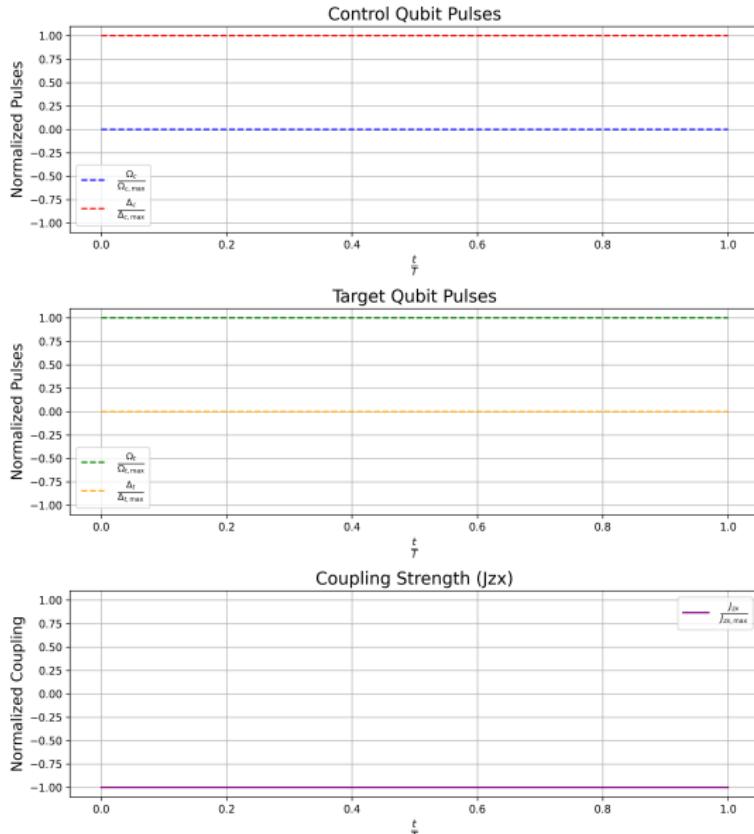


# H Gate Control Pulses

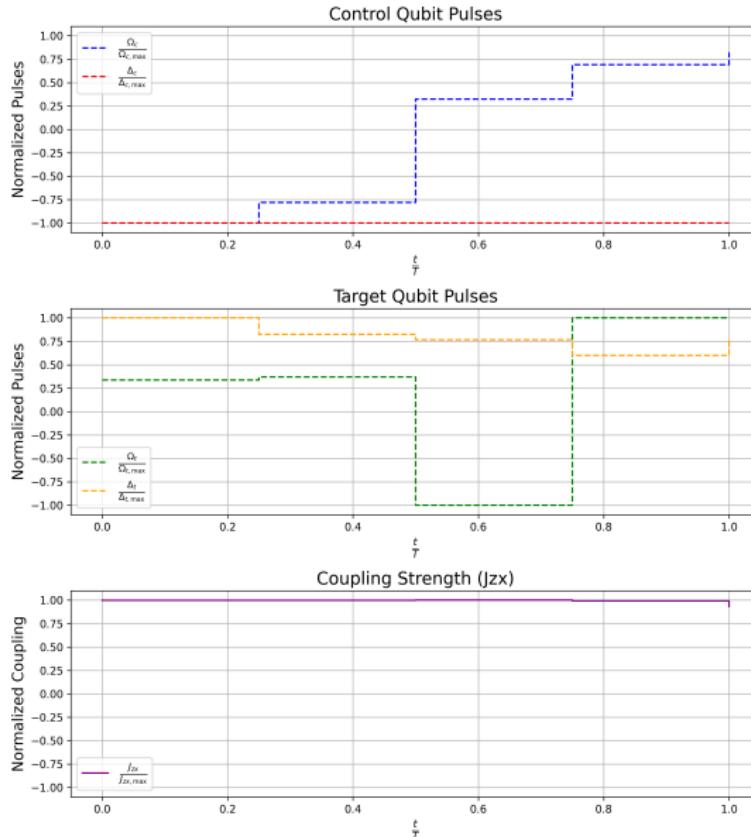
DDDQN CNOT Gate Control Pulses



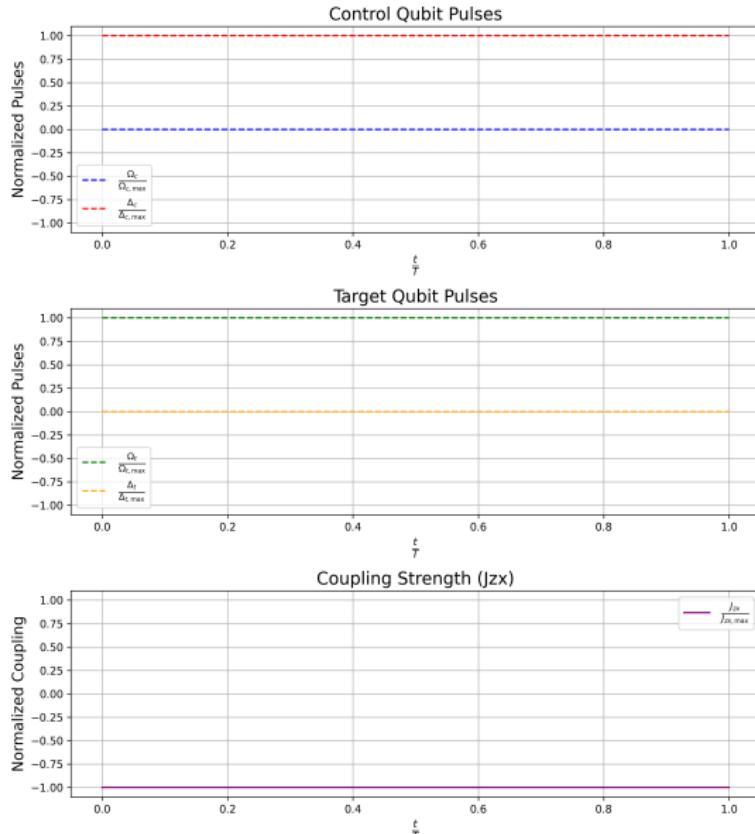
## DPPO CNOT Gate Control Pulses



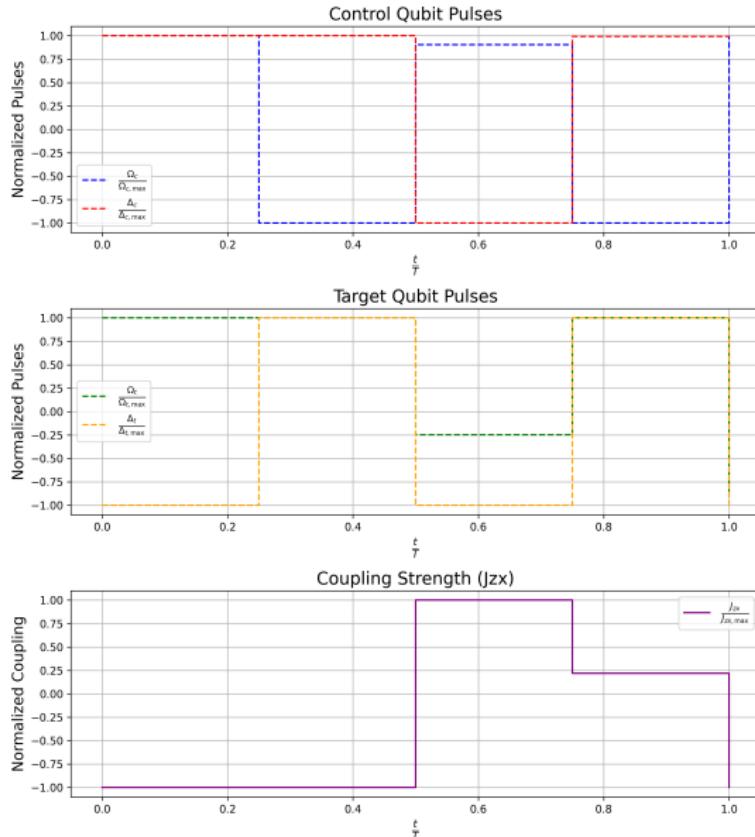
## CPPO CNOT Gate Control Pulses



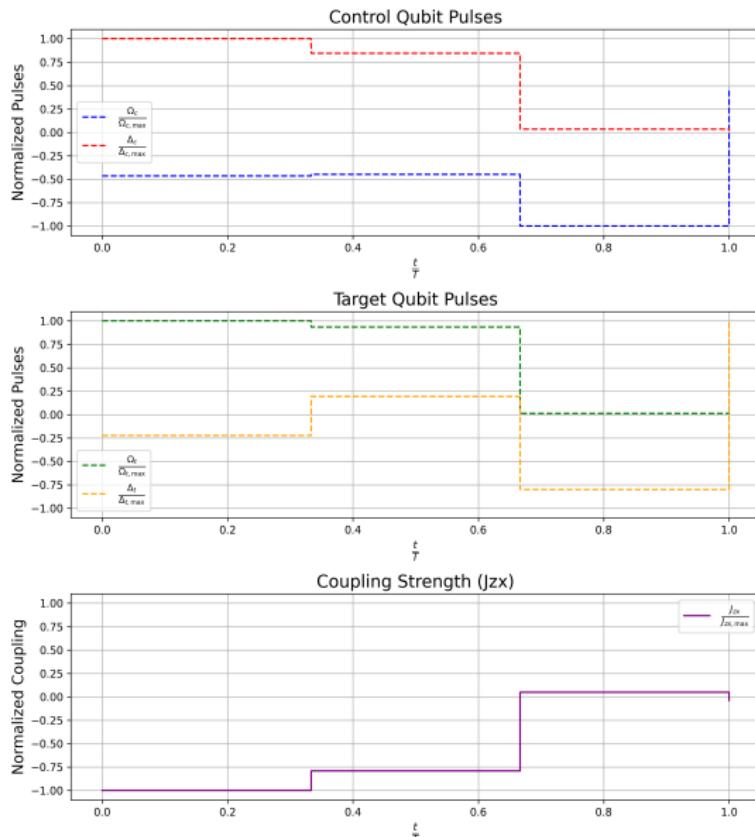
## DGRPO CNOT Gate Control Pulses



# CGRPO CNOT Gate Control Pulses



## TD3 CNOT Gate Control Pulses



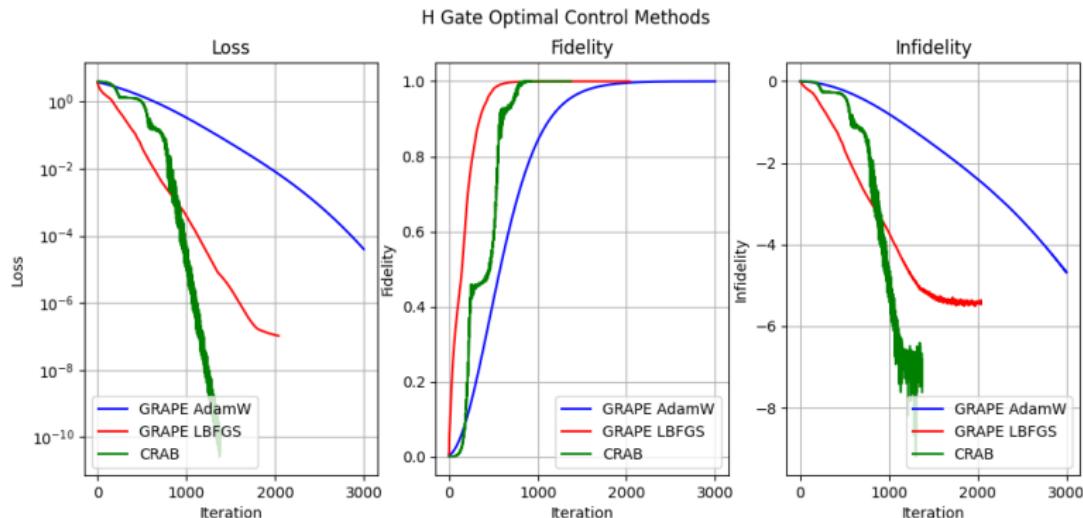
# Summary

DDDQN, DPPO and DGRPO required the least number of episodes to achieve high fidelities. TD3 converged in the second place. CPPO and CGRPO as they struggle to achieve stable learning curves, they required more time than deterministic or discrete approaches.

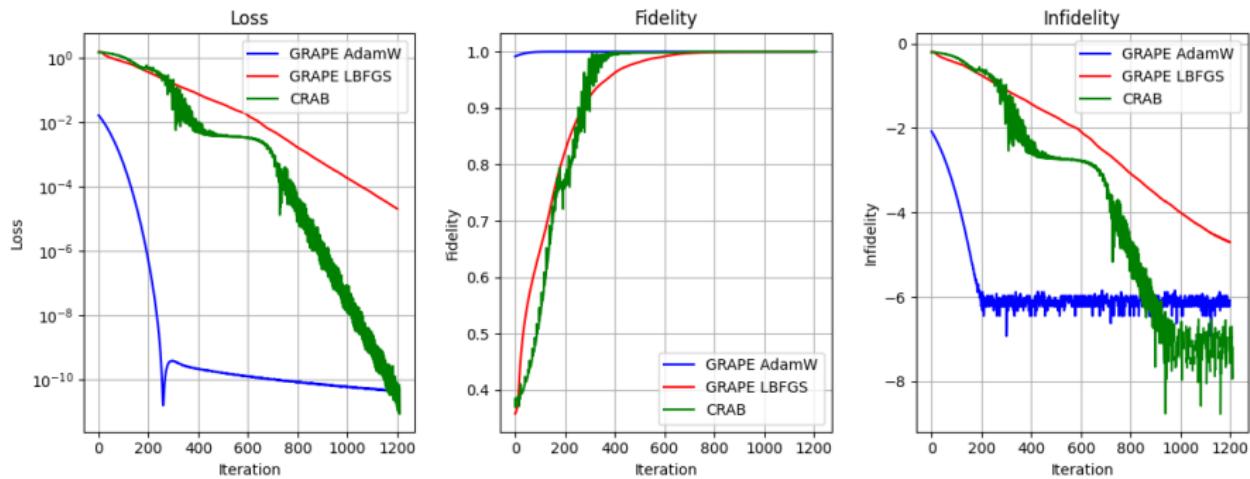
TD3 exhibited minor fluctuations due to the approximation errors of the function. DDDQN, DPPO and DGRPO showed the most stable learning due to their deterministic way of solving the problem. CPPO and CGRPO struggle due to General Advance Estimation (GAE) and stochasticity. DGRPO and GRPO were in line with the deterministic albeit stochastic due to categorical sampling in a finite and small discrete set.

To ensure the accuracy of the RL-based quantum control, the results were compared with GRAPE and CRAB.

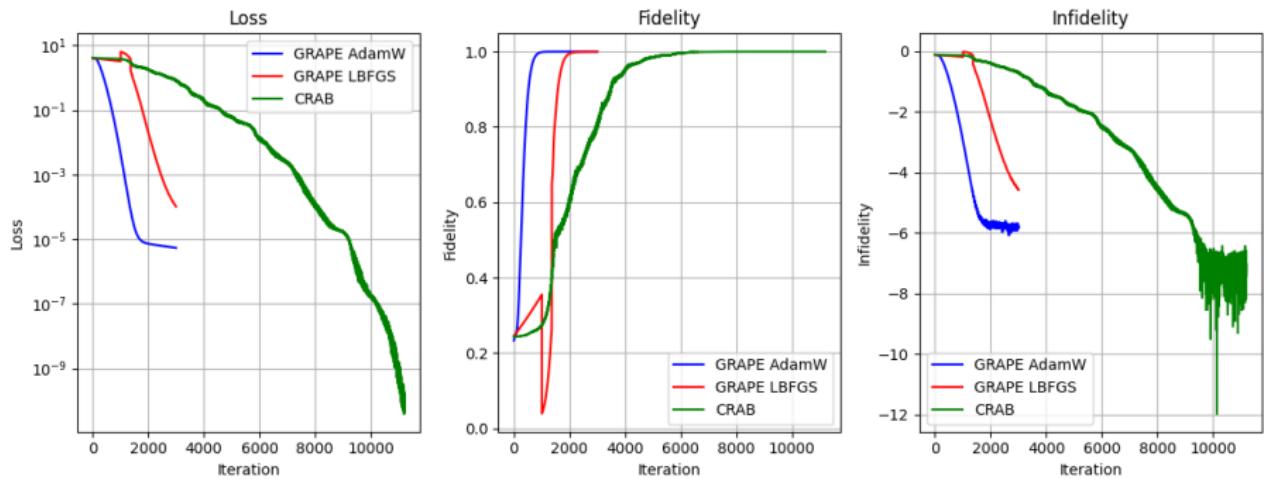
# Optimal Quantum Control



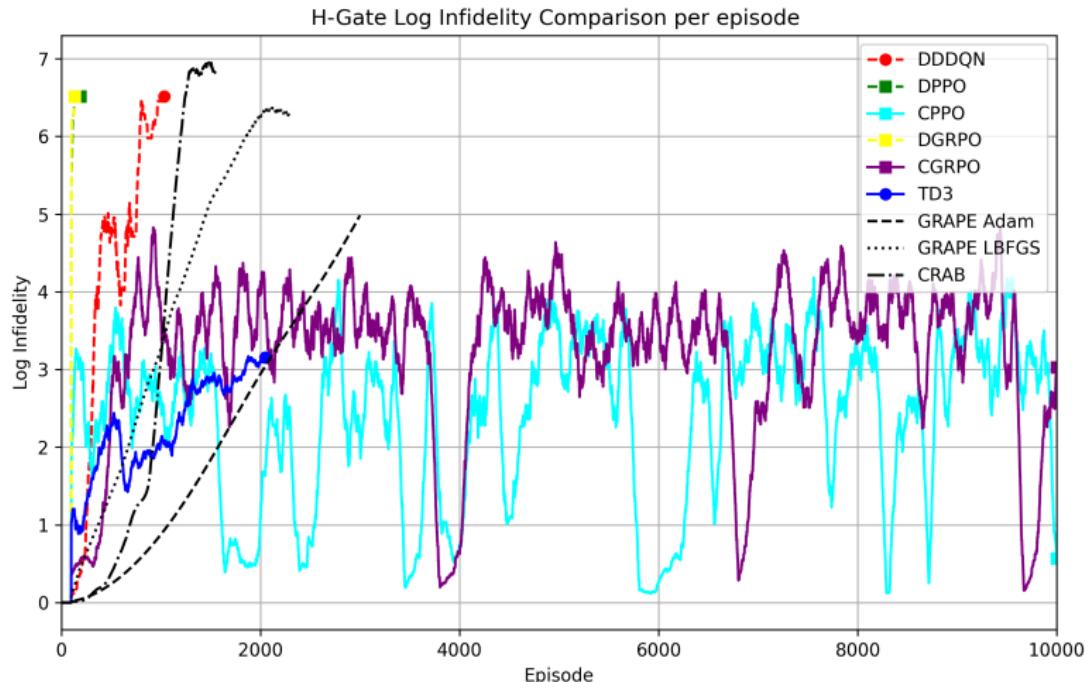
### T-Gate Optimal Control Methods



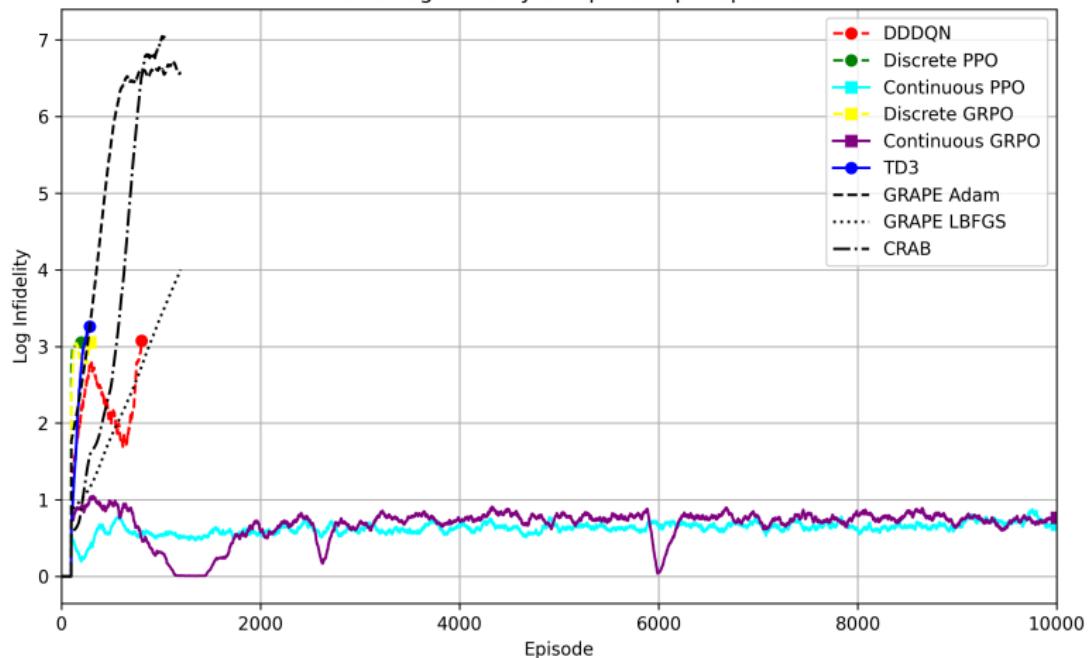
### CNOT-Gate Optimal Control Methods



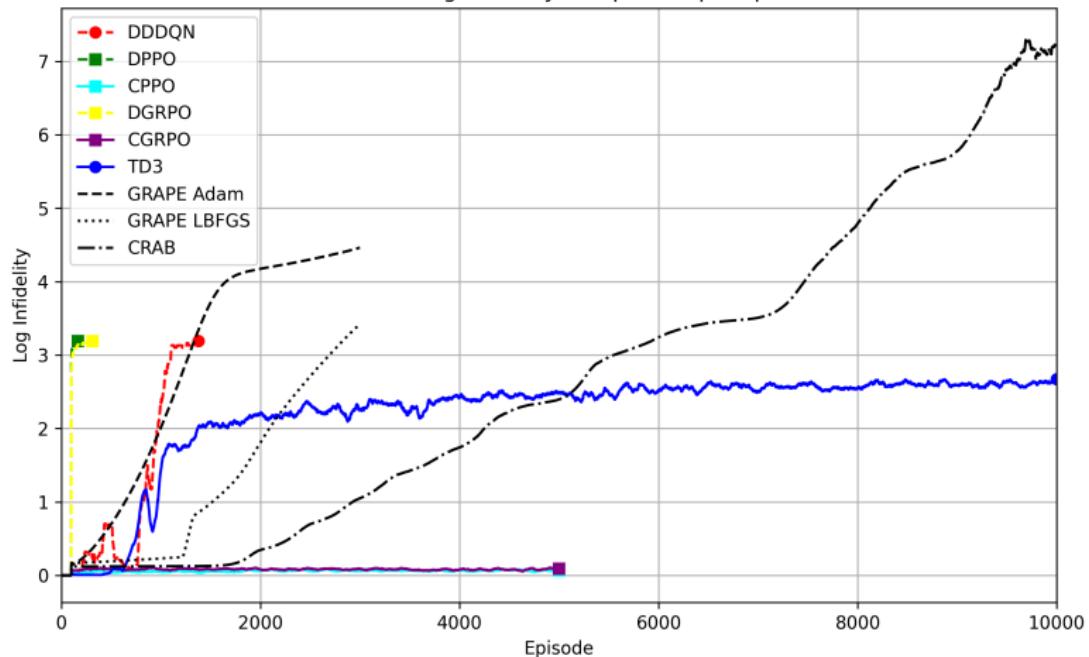
# Comparisons



T-Gate Log Infidelity Comparison per episode



CNOT-Gate Log Infidelity Comparison per episode



# Conclusions

# Applications

## ① Algorithms:

Quantum Fourier Transform  
Grover's Search  
VQA

## ② Scalability:

HRL  
MARL  
Large Circuit Compilation

## ③ Error Correction/Mitigation:

FTQC  
QEC  
Logical Gate Optimization and Compilation

# Future Work

- ① Implementation of RL-optimized quantum gates on real quantum hardware.
- ② Hybrid quantum-classical RL methods. An approach is quantum reinforcement learning (QRL).
- ③ Multi-agent reinforcement learning or hierarchical reinforcement learning exploration.
- ④ RL-driven error mitigation techniques that enable RL agents to dynamically adjust gate parameters to compensate for decoherence.
- ⑤ RL policies to adapt control sequences in real time based on measured noise fluctuations in quantum hardware.
- ⑥ Improve fault-tolerant operations by optimizing quantum error correction strategies via RL.

# Acknowledgments



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# Thanks for your attention

## Questions?



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