

CS261 Data Structures

Heap Implementation



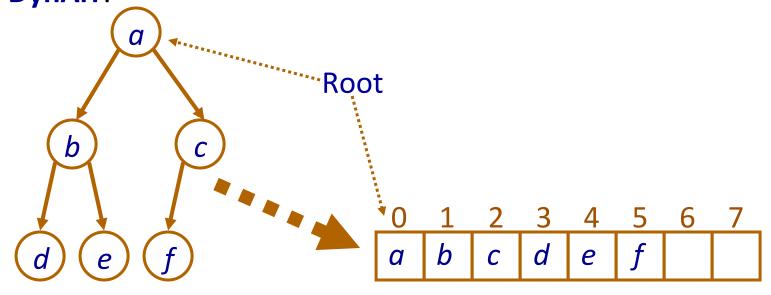
Goals

- Heap Representation
- Heap Priority Queue ADT Implementation



Dynamic Array Representation

Complete binary tree has structure that is efficiently implemented with a **DynArr**:

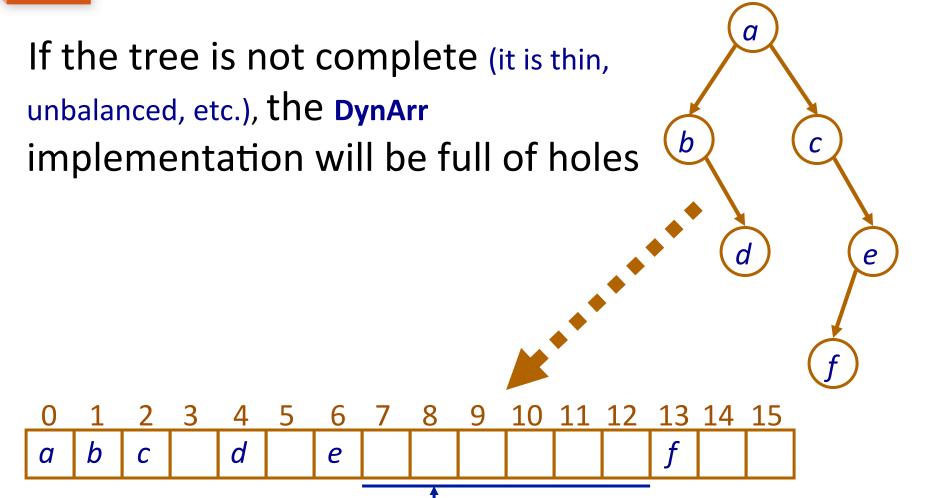


- Children of node i are stored at 2i + 1 and 2i + 2
- Parent of node i is at floor((i 1) / 2)

Why is this a bad idea if tree is not complete?



Dynamic Array Implementation (cont.)



Big gaps where the level is not filled!

Heap Implementation: add

```
void addHeap(struct DynArr *heap, TYPE val) {
        int parent;
        int pos = sizeDynArr(heap);
        addDynArr(heap, val); /*sets capacity if necessary */
       while(pos != 0){
         parent = (pos-1)/2;
         if(compare(getDynArr(heap, pos), getDynArr(heap, parent)) == -1){
             swapDynArr(heap, parent, pos);
             pos = parent;
percolate up
           else return;
                                                  Parent position
                                                                                Next open spot
      Example: add 4 to the heap
                                                      (parent)
                                                                                      (pos)
         Prior to addition, size = 11
                                                                                  10
                                                              6
                                                                  14
```

Heap Implementation: add (cont.)

```
void addHeap(struct DynArr *heap, TYPE val) {
  int parent;
  int pos = sizeDynArr(heap);
  addDynArr(heap, val); /*sets capacity if necessary */
  while(pos != 0){
    parent = (pos-1)/2;
    if(compare(getDynArr(heap, pos), getDynArr(heap, parent)) == -1){
       swapDynArr(heap, parent, pos);
       pos = parent;
    } else return;
                      After first iteration: "swapped" new value (4) with parent (7)
                                                                    New parent value: 5
                                     parent
                                                    pos
                                                           6
                                               10
```

Heap Implementation: add (cont.)

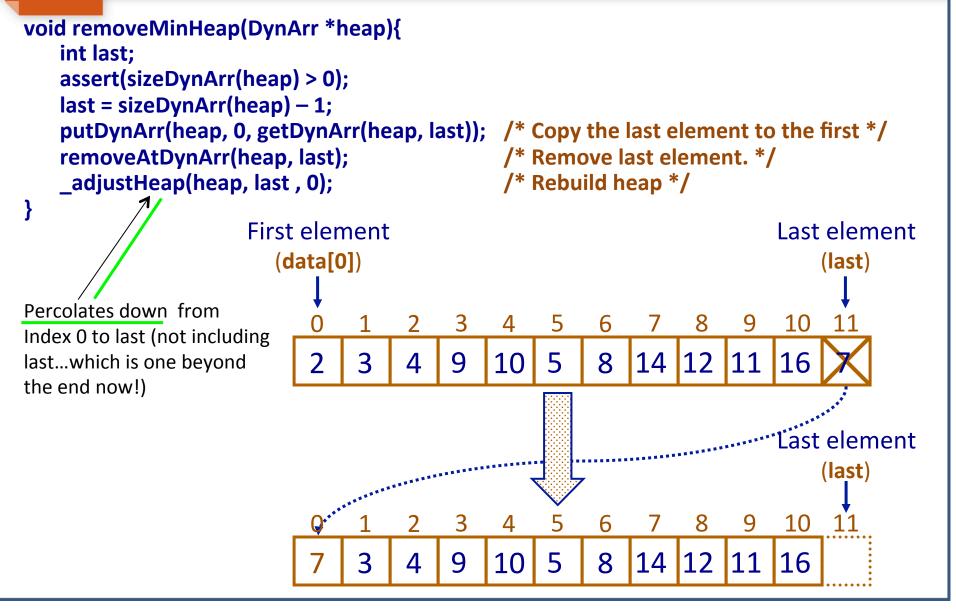
```
void addHeap(struct DynArr *heap, TYPE val) {
  int parent;
  int pos = sizeDynArr(heap);
  addDynArr(heap, val); /*sets capacity if necessary */
  while(pos != 0){
    parent = (pos-1)/2;
    if(compare(getDynArr(heap, pos), getDynArr(heap, parent)) == -1){
       swapDynArr(heap, parent, pos);
       pos = parent;
    } else return;
                     After second iteration: "swapped" new value (4) with parent (5)
                                                                      New parent value: 2
                         parent
                                   pos
                                              10
```

Heap Implementation: add (cont.)

```
void addHeap(struct DynArr *heap, TYPE val) {
  int parent;
  int pos = sizeDynArr(heap);
  addDynArr(heap, val); /*sets capacity if necessary */
  while(pos != 0){
    parent = (pos-1)/2;
    if(compare(getDynArr(heap, pos), getDynArr(heap, parent)) == -1){
       swapDynArr(heap, parent, pos);
        pos = parent;
    } else return;
                      If test fails: returns from iteration
                           parent
                                     pos
                                                                                10
                                                           6
                                                           8
                                                               14
                                                                               16
```

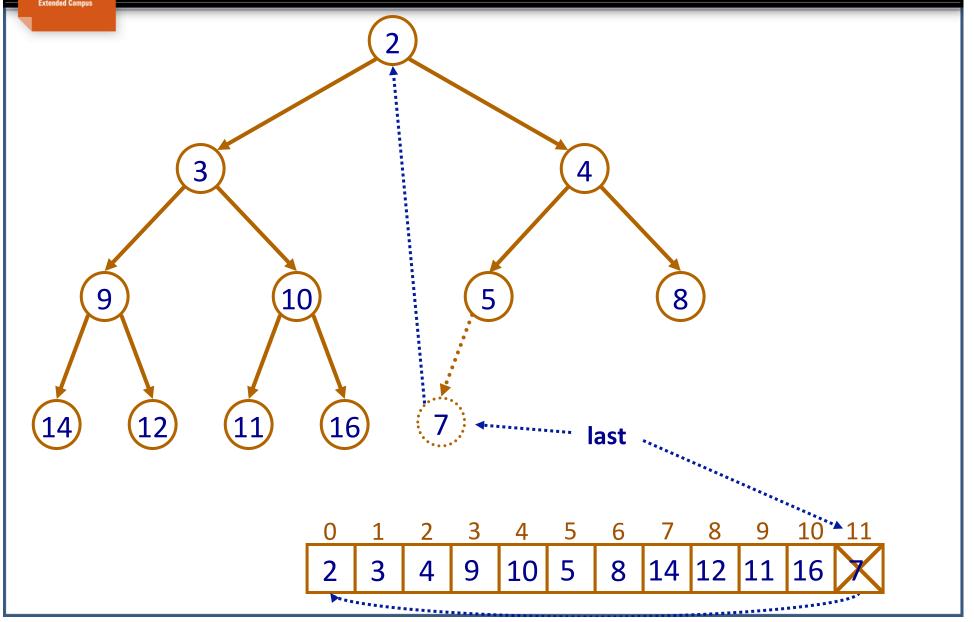


Heap Implementation: removeMin



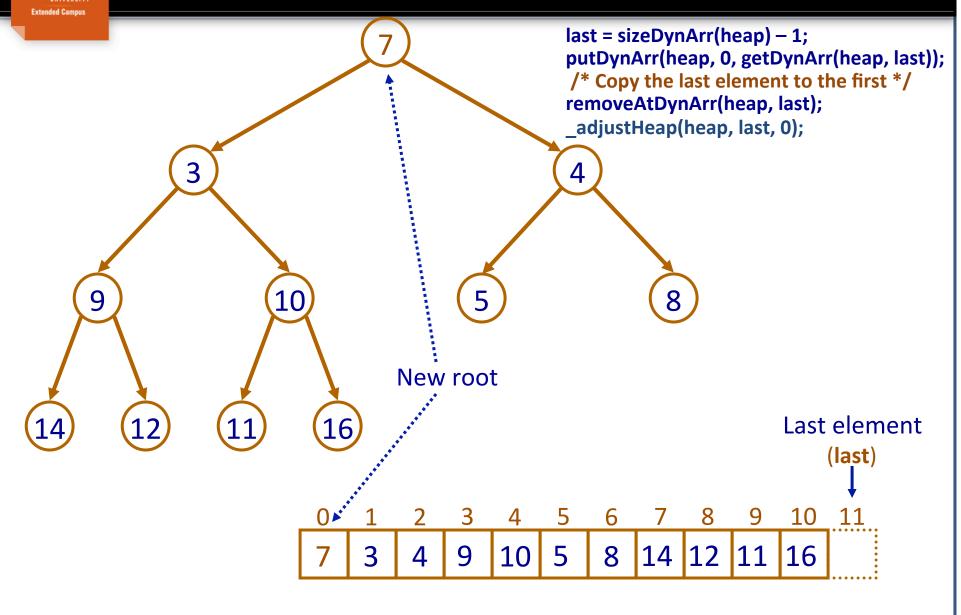


Heap Implementation: removeMin



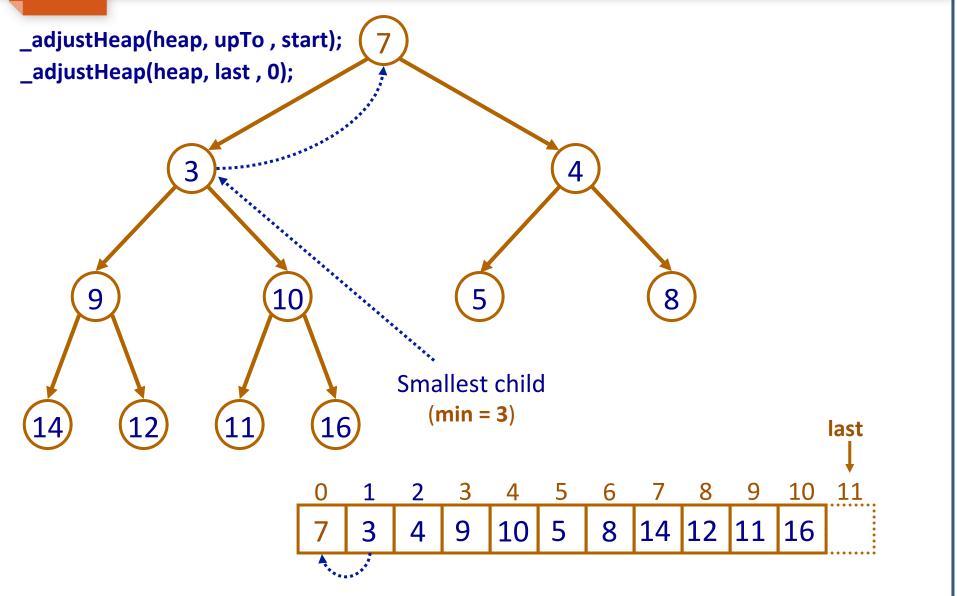


Heap Implementation: removeMin (cont.)



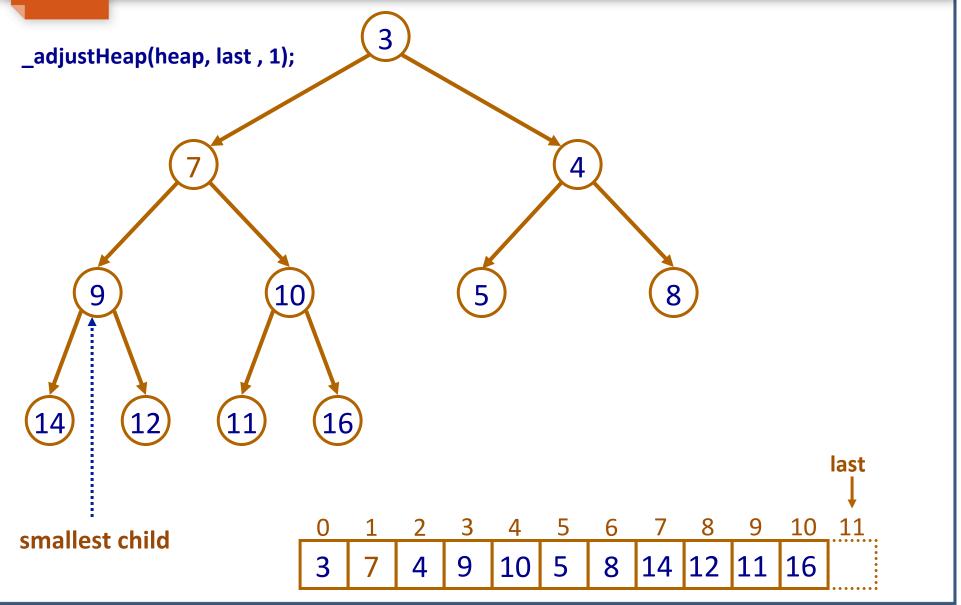


Heap Implementation: _adjustHeap



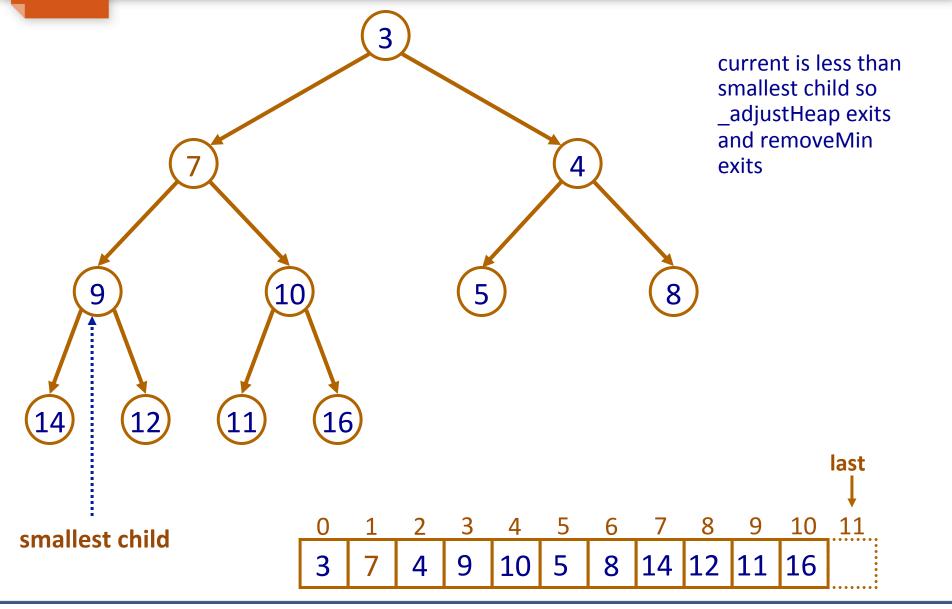


Heap Implementation: _adjustHeap





Heap Implementation: _adjustHeap



Recursive _adjustHeap

```
void _adjustHeap(struct DynArr *heap, int max, int pos) {
 int leftIdx = pos *2 + 1;
 int rghtldx = pos * 2 + 2;
 if (rghtIdx < max) {</pre>
  /* Have two children? */
  /* Get index of smallest child (_minldx). */
  /* Compare smallest child to pos. */
   /* If necessary, swap and call _adjustHeap(max, minIdx). */
 else if (leftIdx < max) {
  /* Have only one child. */
   /* Compare child to parent. */
   /* If necessary, swap and call _adjustHeap(max, leftIdx). */
   /* Else no children, we are at bottom \rightarrow done. */
```

Useful Routines

```
void swap(struct DynArr *arr, int i, int j) {
 /* Swap elements at indices i and j. */
 TYPE tmp = arr->data[i];
 arr->data[i] = arr->data[j];
 arr->data[j] = tmp;
int minIdx(struct DynArr *arr, int i, int j) {
 /* Return index of smallest element value. */
 if (compare(arr->data[i], arr->data[j]) == -1)
  return i;
 return j;
```



Priority Queues: Performance Evaluation

	SortedVector	SortedList	Heap
add	O(n) Binary search Slide data up	O(n) Linear search	O(log <i>n</i>) Percolate up
getMin	O(1) get(0)	O(1) Returns firstLink val	O(1) Get root node
removeMin	O(n) Slide data down O(1): Reverse Order	O(1) removeFront()	O(log <i>n</i>) <u>Percolate down</u>

So, which is the best implementation of a priority queue?



Priority Queues: Performance Evaluation

- Recall that a priority queue's main purpose is rapidly accessing and removing the smallest element!
- Consider a case where you will insert (and ultimately remove) n elements:
 - –ReverseSortedVector and SortedList:

Insertions: $n * n = n^2$

Removals: n * 1 = n

Total time: $n^2 + n = O(n^2)$

-Heap:

Insertions: n * log n

Removals: n * log n

Total time: $n * \log n + n * \log n = 2n \log n = O(n \log n)$



Your Turn

Complete Worksheet #33