

Assignment 6:

Constraint Satisfaction Problem (CSP)

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4-Queens problem by Constraint Satisfaction

Variables:

$$X_i \rightarrow X_1, X_2, X_3, X_4$$

Domains:

$$D_i = \{1, 2, 3, 4\}, \text{ values can take each } X_i$$

Constraints:

$$C_i = (x_i \neq x_j \text{ and } |x_i - x_j| \neq |i - j|),$$

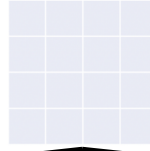
such that there are non attacking queens in the board

Initial State (S):

	X_1	X_2	X_3	X_4
1				
2				
3				
4				

START

Depth = 0



Depth = 1



$X_1 = 1$



$X_1 = 2$



$X_1 = 3$



$X_1 = 4$

Depth = 2



$X_2 = 3$



$X_2 = 4$

No solution for X_3 from $X_2 = 3$, so we continue expanding $X_2 = 4$

Depth = 3



$X_3 = 2$

Depth = 4

START



Depth = 0

Depth = 1



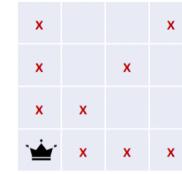
$X_1 = 1$



$X_1 = 2$



$X_1 = 3$



$X_1 = 4$

Depth = 2



$X_2 = 3$



$X_2 = 4$

Depth = 3



$X_3 = 2$

No solution for X_4 from $X_3 = 2$ and there is not other possible solution from $X_2 = 4$, so we have to backtrack

Depth = 4

START

Depth = 0



Depth = 1



$X_1 = 1$



$X_1 = 2$



$X_1 = 3$



$X_1 = 4$

Depth = 2



$X_2 = 3$



$X_2 = 4$

No other unexplored solution for X_2 from $X_1 = 1$, so backtrack again

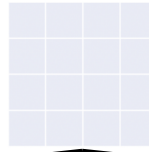
Depth = 3



$X_3 = 2$

Depth = 4

START



Depth = 0

Depth = 1



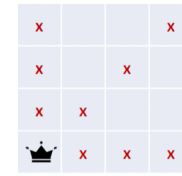
$X_1 = 1$



$X_1 = 2$



$X_1 = 3$



$X_1 = 4$

Depth = 2



$X_2 = 3$



$X_2 = 4$



$X_2 = 4$

Depth = 3



$X_3 = 2$



$X_3 = 1$

Depth = 4

One solution found:

$x_1 \leftarrow 2$

$x_2 \leftarrow 4$

$x_3 \leftarrow 1$

$x_4 \leftarrow 3$



$X_4 = 3$

10 nodes constructed

4 bytes x node = 40 bytes total

1 sec x node = 10 secs