

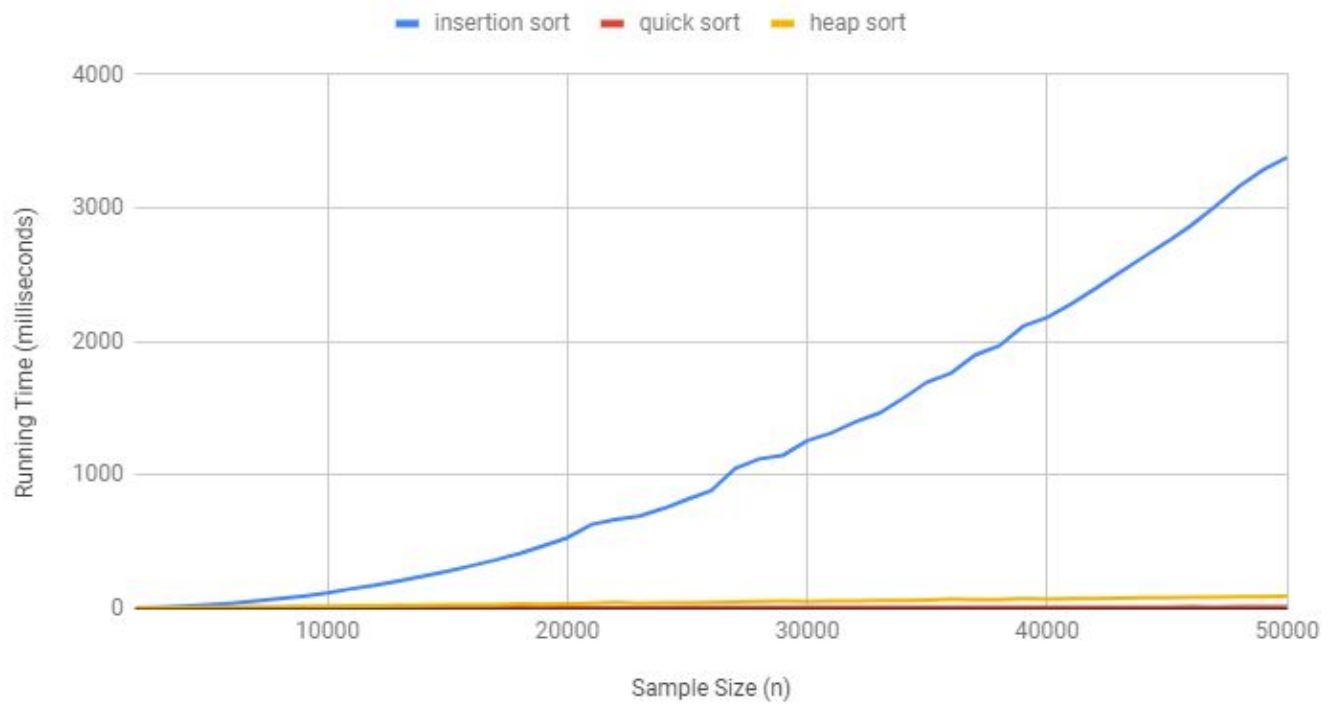
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 COT4400 Programming Assignment

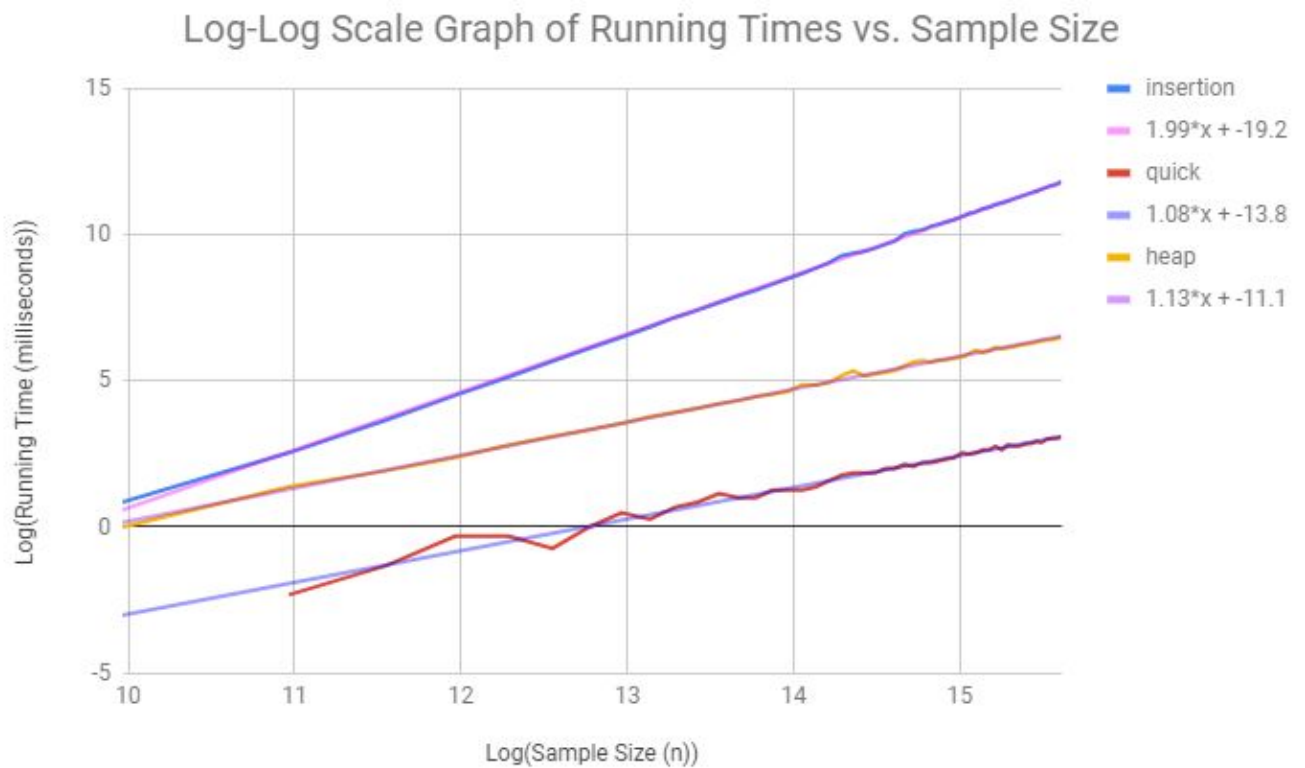
| SAMPLE SIZE DATA | RUNNING TIME (Milliseconds) |            |           | CONSTANT (RUNNING TIME / THEORETICAL TIME) |                      |                 |
|------------------|-----------------------------|------------|-----------|--|----------------------|-----------------|
| n                | insertion sort              | quick sort | heap sort | insertion                                  | quick                | heap            |
| 1000             | 1.8                         | 0          | 1         | 0.0000018                                  | 0                    | 0.0001003433319 |
| 2000             | 5.8                         | 0.2        | 2.6       | 0.00000145                                 | 0.00000005           | 0.0001185505721 |
| 3000             | 12.6                        | 0.4        | 3.8       | 0.0000014                                  | 0.0000000444444444   | 0.0001096610193 |
| 4000             | 22.6                        | 0.8        | 5.2       | 0.0000014125                               | 0.00000005           | 0.0001086431085 |
| 5000             | 35.2                        | 0.8        | 7         | 0.000001408                                | 0.000000032          | 0.0001139349585 |
| 6000             | 51                          | 0.6        | 8.6       | 0.000001416666667                          | 0.00000001666666667  | 0.0001142030317 |
| 7000             | 69.4                        | 1          | 10        | 0.000001416326531                          | 0.00000002040816327  | 0.0001118418429 |
| 8000             | 90                          | 1.4        | 11.6      | 0.00000140625                              | 0.000000021875       | 0.000111832803  |
| 9000             | 114.6                       | 1.2        | 13.6      | 0.000001414814815                          | 0.00000001481481481  | 0.00011503841   |
| 10000            | 144.2                       | 1.6        | 15.2      | 0.000001442                                | 0.000000016          | 0.0001143913984 |
| 11000            | 171.2                       | 1.8        | 16.8      | 0.000001414876033                          | 0.00000001487603306  | 0.0001137615021 |
| 12000            | 204.4                       | 2.2        | 18.6      | 0.000001419444444                          | 0.00000001527777778  | 0.0001143848398 |
| 13000            | 240.6                       | 2          | 20        | 0.000001423668639                          | 0.00000001183431953  | 0.0001125740027 |
| 14000            | 275.8                       | 2          | 22        | 0.000001407142857                          | 0.00000001020408163  | 0.0001140937115 |
| 15000            | 316.6                       | 2.4        | 23.4      | 0.000001407111111                          | 0.00000001066666667  | 0.0001124512766 |
| 16000            | 360.2                       | 2.4        | 25        | 0.00000140703125                           | 0.000000009375       | 0.0001118805767 |
| 17000            | 409.6                       | 2.4        | 29.4      | 0.000001417301038                          | 0.00000000830449827  | 0.0001230613643 |
| 18000            | 466.4                       | 2.6        | 29        | 0.000001439506173                          | 0.000000008024691358 | 0.0001139745504 |
| 19000            | 527.4                       | 3          | 30.8      | 0.000001460941828                          | 0.000000008310249307 | 0.0001140485086 |
| 20000            | 626                         | 3.4        | 36.2      | 0.000001565                                | 0.0000000085         | 0.0001266822814 |
| 21000            | 662.8                       | 3.6        | 40.4      | 0.000001502947846                          | 0.000000008163265306 | 0.0001339877348 |
| 22000            | 688.6                       | 3.6        | 36        | 0.000001422727273                          | 0.000000007438016529 | 0.0001134377223 |
| 23000            | 745.2                       | 3.6        | 37.6      | 0.000001408695652                          | 0.000000006805293006 | 0.0001128265266 |
| 24000            | 815                         | 4          | 39.4      | 0.000001414930556                          | 0.000000006944444444 | 0.0001128235335 |
| 25000            | 881.2                       | 4          | 41.2      | 0.00000140992                              | 0.0000000064         | 0.0001128022283 |

|       |        |     |      |                   |                      |                 |
|-------|--------|-----|------|-------------------|----------------------|-----------------|
| 26000 | 1048   | 4.4 | 45.6 | 0.000001550295858 | 0.00000000650887574  | 0.0001195840288 |
| 27000 | 1118.6 | 4.2 | 50.2 | 0.000001534430727 | 0.000000005761316872 | 0.0001263026094 |
| 28000 | 1146.2 | 4.6 | 51.6 | 0.000001461989796 | 0.000000005867346939 | 0.0001247437743 |
| 29000 | 1255.2 | 4.6 | 49.8 | 0.000001492508918 | 0.000000005469678954 | 0.0001158438053 |
| 30000 | 1312   | 4.8 | 52.4 | 0.000001457777778 | 0.000000005333333333 | 0.0001174413265 |
| 31000 | 1394.4 | 5   | 53   | 0.000001450988554 | 0.000000005202913632 | 0.0001145897884 |
| 32000 | 1461   | 5.2 | 54.8 | 0.000001426757813 | 0.000000005078125    | 0.0001144276817 |
| 33000 | 1573.4 | 5.8 | 56.8 | 0.000001444811754 | 0.000000005325987144 | 0.0001146696645 |
| 34000 | 1695   | 5.6 | 60.6 | 0.000001466262976 | 0.000000004844290657 | 0.0001184032207 |
| 35000 | 1761.8 | 5.8 | 65.8 | 0.000001438204082 | 0.000000004734693878 | 0.0001245439959 |
| 36000 | 1897.2 | 6.2 | 62.6 | 0.000001463888889 | 0.000000004783950617 | 0.0001148865148 |
| 37000 | 1966   | 6.2 | 65   | 0.000001436084733 | 0.000000004528853178 | 0.0001157646949 |
| 38000 | 2114.2 | 6.8 | 71   | 0.000001464127424 | 0.000000004709141274 | 0.0001228116503 |
| 39000 | 2178.6 | 6.2 | 68.4 | 0.00000143234714  | 0.000000004076265615 | 0.000114997358  |
| 40000 | 2280.8 | 7   | 70.2 | 0.0000014255      | 0.000000004375       | 0.0001147980781 |
| 41000 | 2395.8 | 6.8 | 72   | 0.000001425223081 | 0.000000004045211184 | 0.0001146028207 |
| 42000 | 2512   | 6.8 | 75   | 0.000001424036281 | 0.000000003854875283 | 0.0001162718101 |
| 43000 | 2630.4 | 7.2 | 76.2 | 0.000001422606814 | 0.000000003893996755 | 0.0001151304169 |
| 44000 | 2745.8 | 7.2 | 77.8 | 0.000001418285124 | 0.000000003719008264 | 0.0001146293076 |
| 45000 | 2869.4 | 7.6 | 80   | 0.000001416987654 | 0.00000000375308642  | 0.0001150096702 |
| 46000 | 3009.8 | 7.4 | 83   | 0.000001422400756 | 0.000000003497164461 | 0.0001164896051 |
| 47000 | 3161.4 | 8   | 83.8 | 0.000001431145315 | 0.000000003621548212 | 0.0001148798877 |
| 48000 | 3286.6 | 8.2 | 85.6 | 0.000001426475694 | 0.000000003559027778 | 0.0001146783082 |
| 49000 | 3380.2 | 8.2 | 86.8 | 0.000001407830071 | 0.000000003415243648 | 0.0001136952754 |
| 50000 | 3598.4 | 8.4 | 91.2 | 0.00000143936     | 0.00000000336        | 0.0001168508655 |

|                         |            |                 |
|-------------------------|------------|-----------------|
|                         |            |                 |
| MAX VALUES FOR CONSTANT |            |                 |
| insertion               | quick      | heap            |
| 0.0000018               | 0.00000005 | 0.0001339877348 |

## Running Time vs. Sample Size





The graph above has linear regression lines to estimate the complexity. Insertion-sort behaves as  $t(n) = n^2$ , while quick-sort and heap-sort behave as something between  $n$  and  $n^2$ , so likely  $n \log(n)$ . We do know, however, that the  $O(n)$  of quick-sort  $\neq n^2$ , but its average complexity is  $n \log(n)$ .