

Painting the Fence

diff: 表示当最后两块颜色不同的方案数

same: 表示当最后两块颜色相同的方案数

total ways = diff + same

1. $n = 1$, diff = k , same = 0, total = k

2. $n = 2$, diff = $k * (k - 1)$, same = k , total = $k + k * (k - 1)$

3. $n = 3$, diff = $[k + k * (k - 1)] * (k - 1)$, same = $k * (k - 1)$

又因为 $total[i] = same[i] + diff[i]$

综上得到

$same[i] = diff[i - 1]$

$diff[i] = (diff[i-1] + diff[i-2]) * (k-1) = total[i - 1] * (k - 1)$

```
#include <bits/stdc++.h>

#define MOD 1000000007
#define MAX 100001
using namespace std;

// dp[i] 表示用k种颜色涂i个方块的方案
vector<long long int> dp(MAX);
void paintingFence(int k) {
    dp[1] = k;
    int same = 0, diff = k;
    for (int i = 2; i < dp.size(); ++i) {
        same = diff;
        diff = (dp[i - 1] * (k - 1)) % MOD;
        dp[i] = (same + diff) % MOD;
    }
}

int main() {
    int T;
    scanf("%d", &T);
    while (T--) {
        int n, k;
        scanf("%d %d", &n, &k);
        paintingFence(k);
        printf("%lld\n", dp[n]);
    }
}
```

