

Conditional Probabilities

$$P(A | B) = \frac{P(A \cap B)}{P(B)}$$

$$\mathbf{P(A \cap B)} = P(A|B)P(B)$$

$$\mathbf{P(A \cap B)} = P(B|A)P(A)$$

Bayes and Naïve Bayes

$$\mathbf{P(S/1^{st})} = \frac{\begin{matrix} = P(1^{st} \& S) \\ P(1^{st}|S)P(S) \end{matrix}}{P(1^{st})}$$

$$\mathbf{P(\sim S/1^{st})} = \frac{\begin{matrix} = p(1s \& \sim s) \\ P(1^{st}|\sim S)P(\sim S) \end{matrix}}{P(1^{st})}$$

See the excel file

Bayes and Naïve Bayes

$$\mathbf{P(S/1^{st} \& Female)} = \frac{P(1^{st} \& Female|S)P(S)}{P(1^{st} \& Female)}$$

$$\mathbf{P(\sim S/1^{st} \& Female)} = \frac{P(1^{st} \& Female|\sim S)P(\sim S)}{P(1^{st} \& Female)}$$

See the excel file

Naïve Bayes

$$\mathbf{P(S/1st\&Female)} = P(1st\&Female|S)P(S) =$$

$$\overset{\text{Naive}}{P(1st/S) * p(Female|S)P(S)}$$

$$\mathbf{P(\sim S/1s\&Female)} = P\left(\frac{1st\&Female}{\sim S}\right)P(\sim S) =$$

$$\overset{\text{Naive}}{P(1st|\sim S) * P(Female/\sim S)P(\sim S)}$$

Bayes and Naïve Bayes

Max of $P(\theta_1|S)P(\theta_2|S)P(S)$, **Over all possible s**