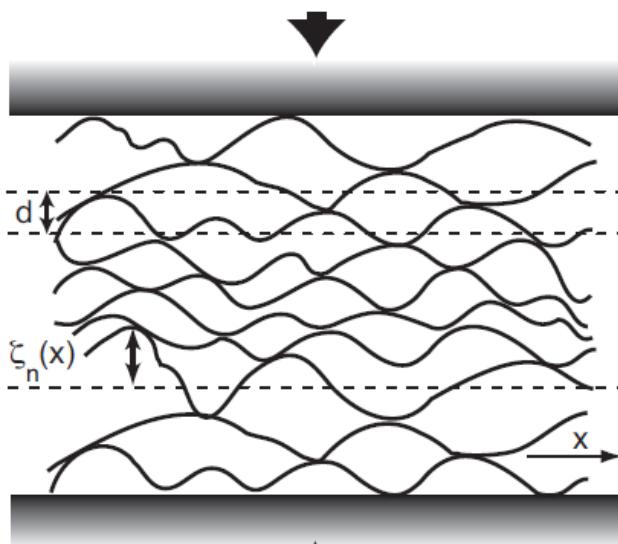
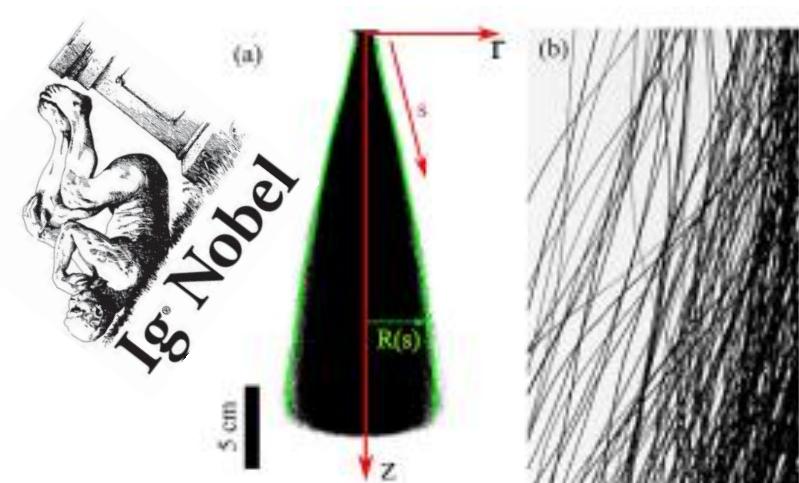


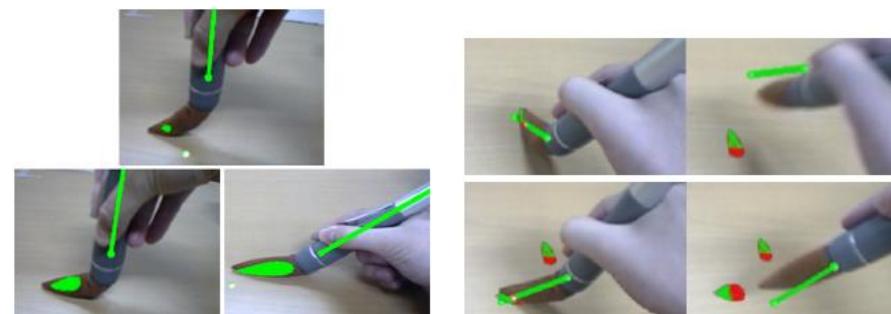
Sano, 2019



Beckrich,  
2003



Goldstein, 2012



(a) Changing the shape.

(b) Rotating.

Otsuki, 2010



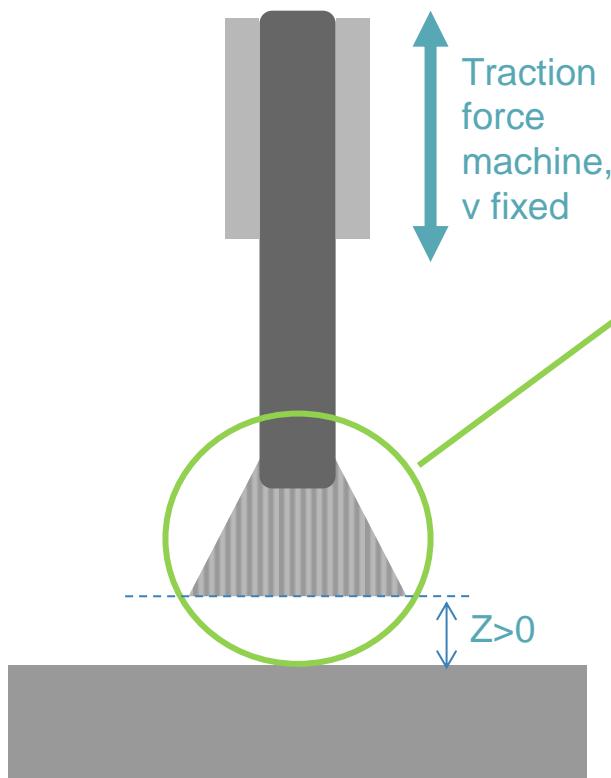
David, 2011

# Compressing a fiber bundle against a rigid surface

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Raphaelle Taub – 2nd year PhD Student  
Supervisors : Frédéric Restagno, Christophe Poulard  
LPS Orsay

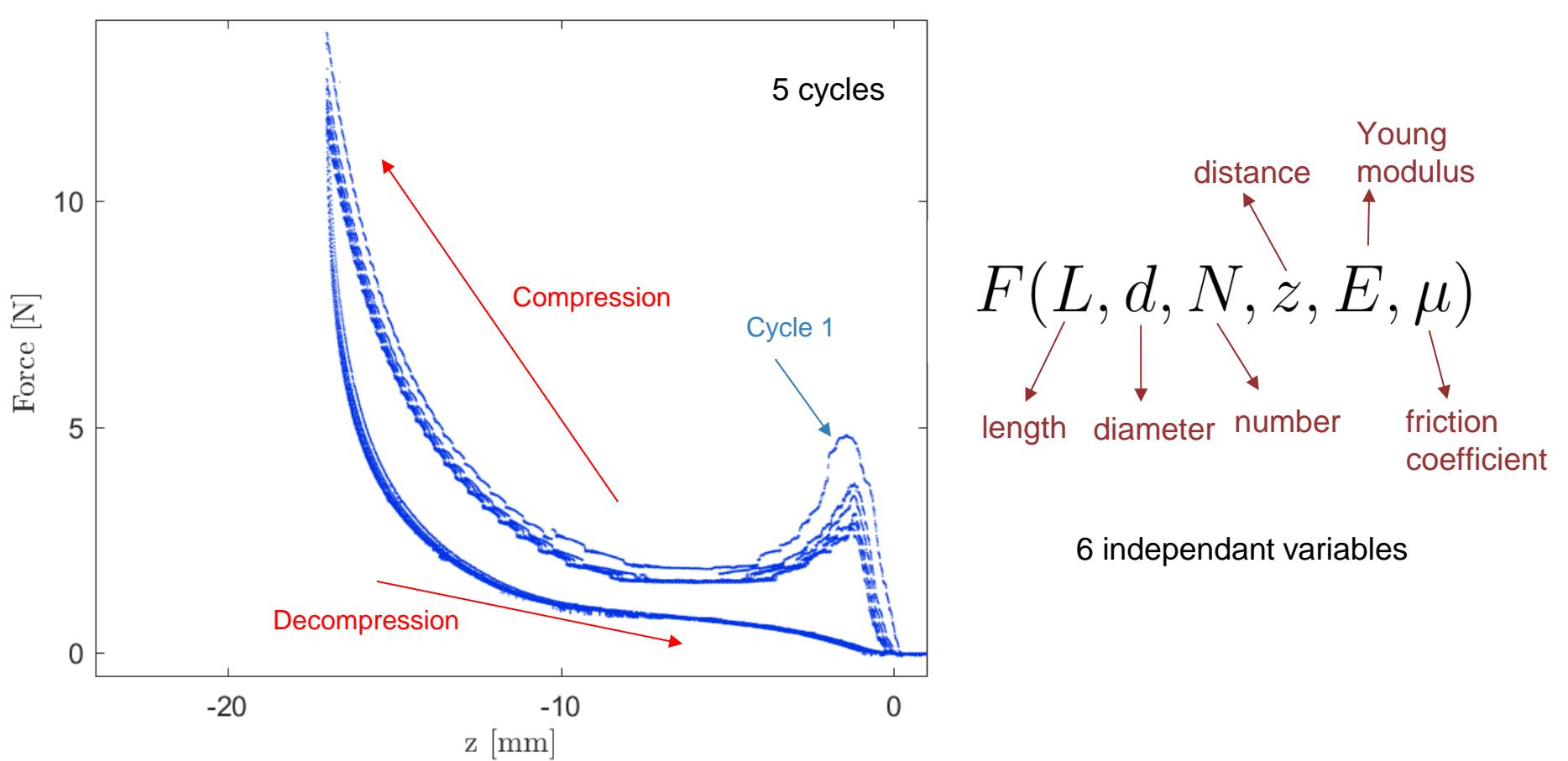
# Setup



$v = 1 \text{ cm/mn}$   
N hairs (around 27000)

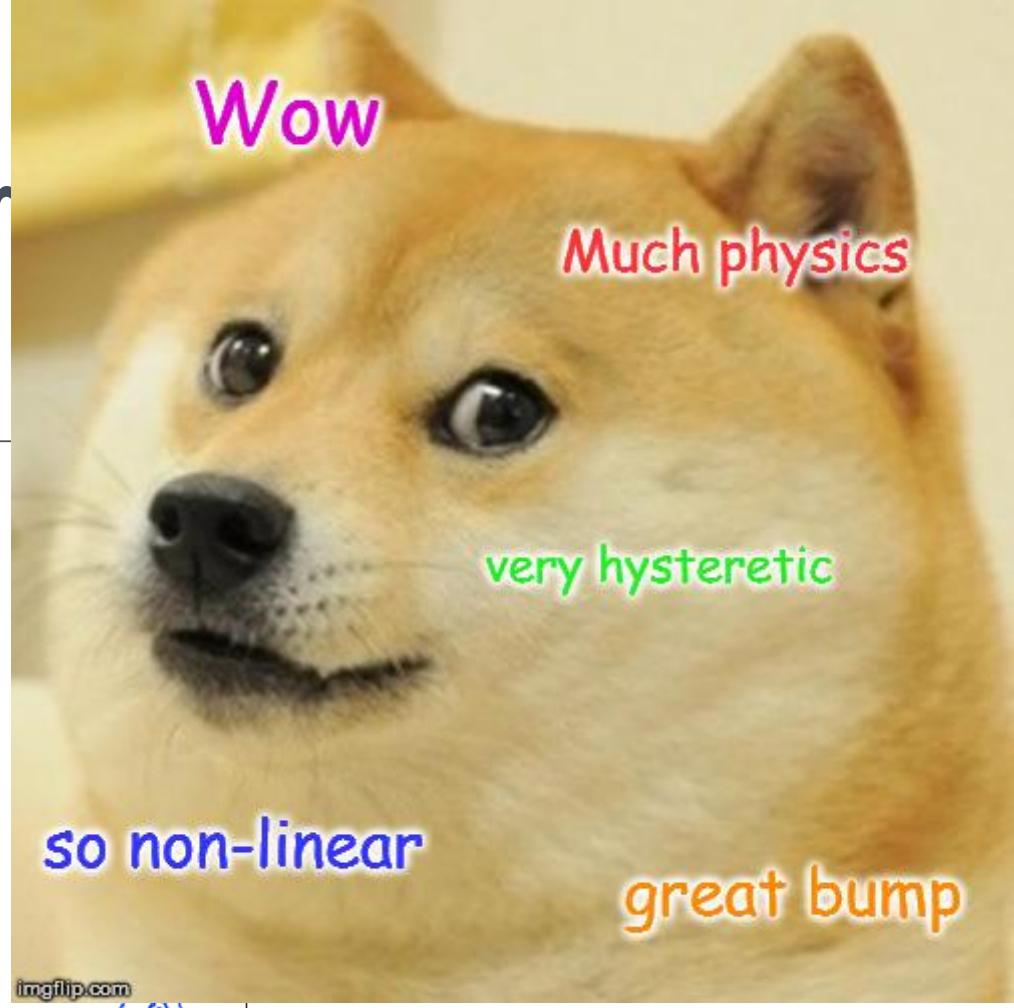
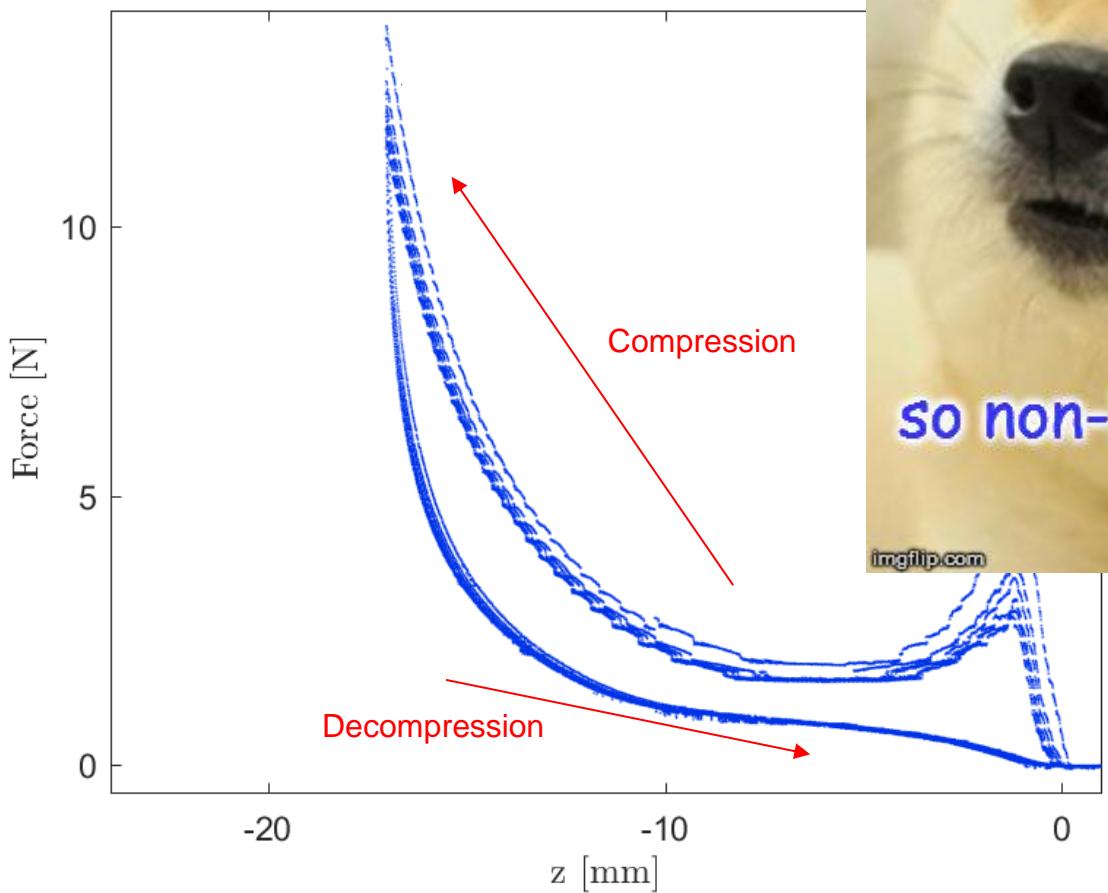
1 hair:  
d (diameter) : 80-60 microns  
L (length) : 3-5 centimeters  
E (young modulus) : 3-5 GPa

# Variation of the force in the height z



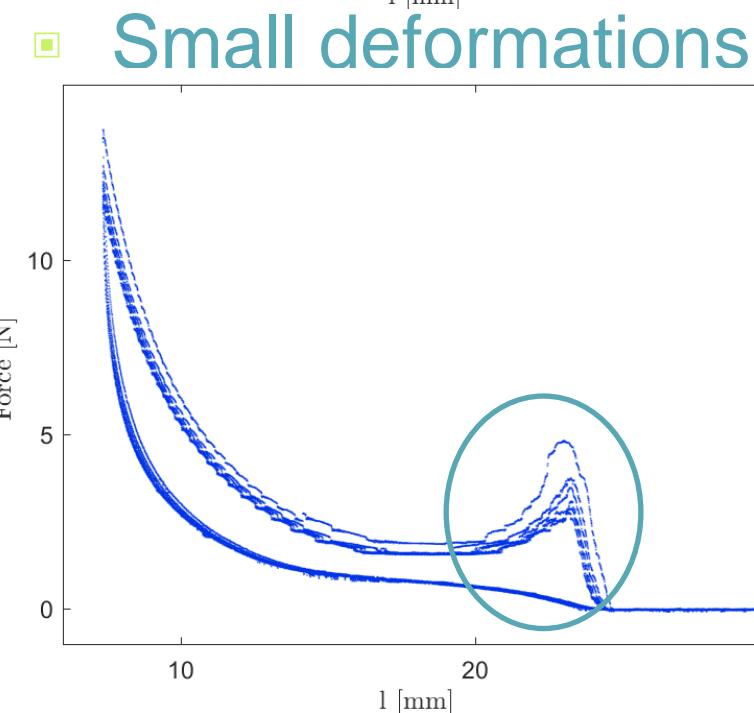
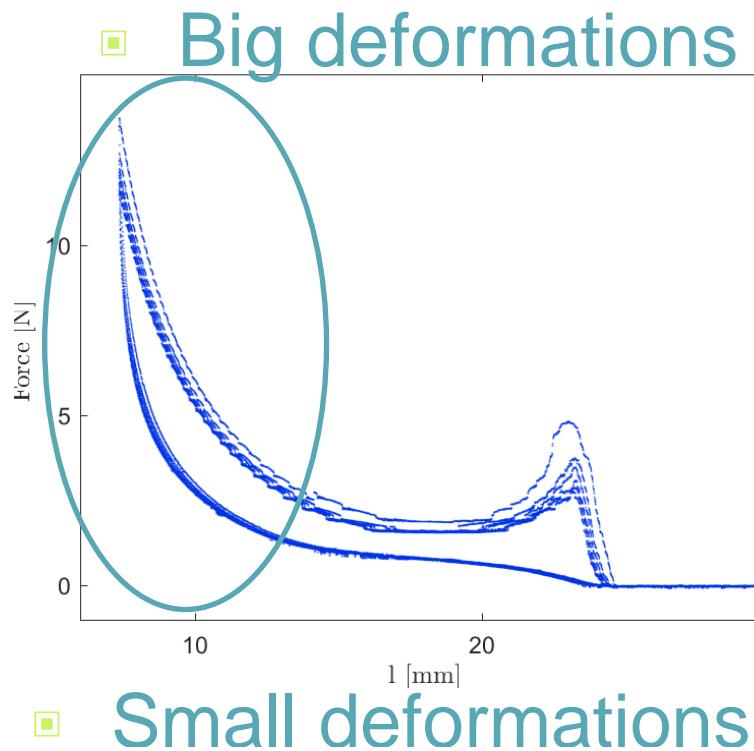
# Variation of the force

Forces measured by a force sensor

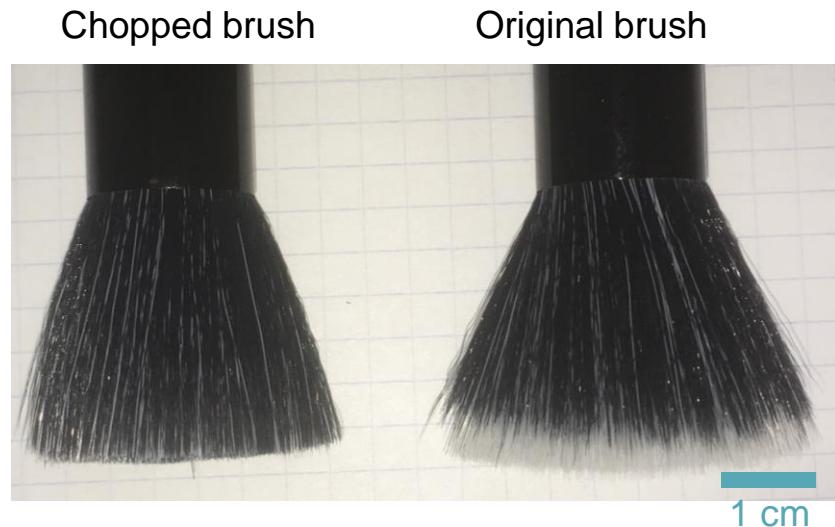
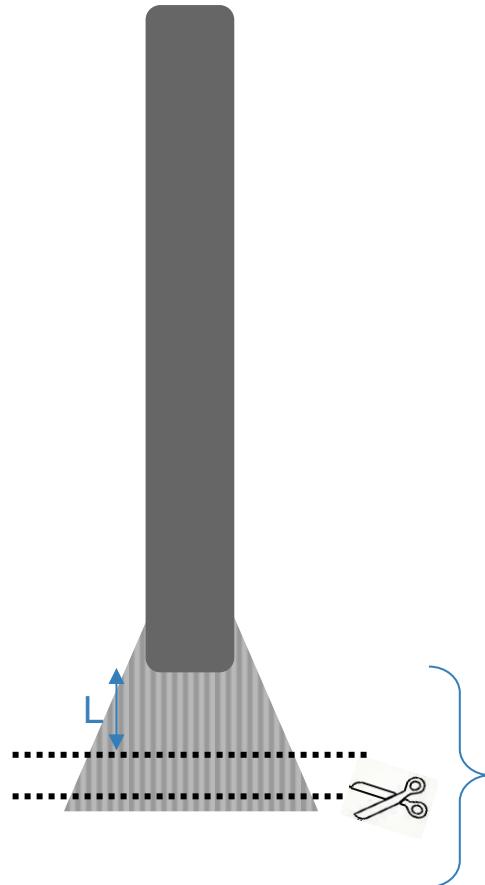




imgflip.com



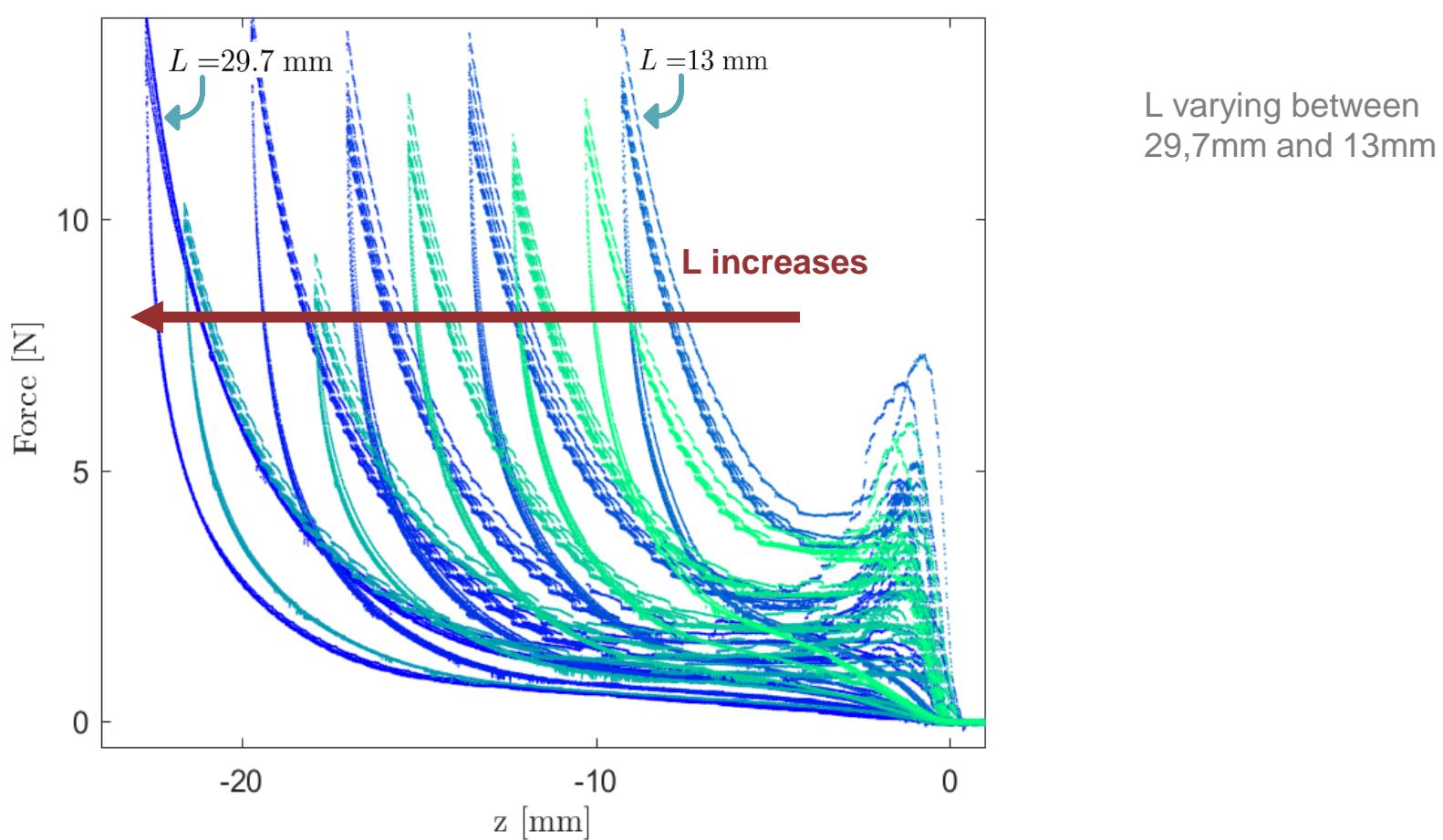
# Compressing brushes and varying the fibers' length



11 cutting planes  
2 brushes

L varying between  
29,7mm and 13mm

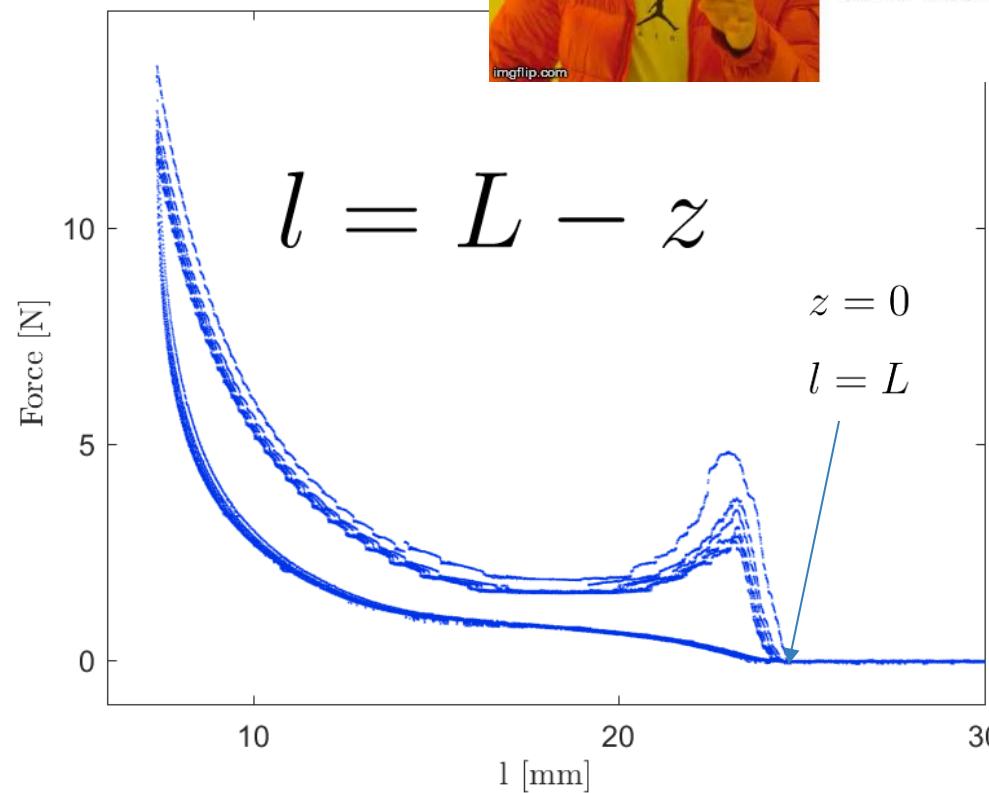
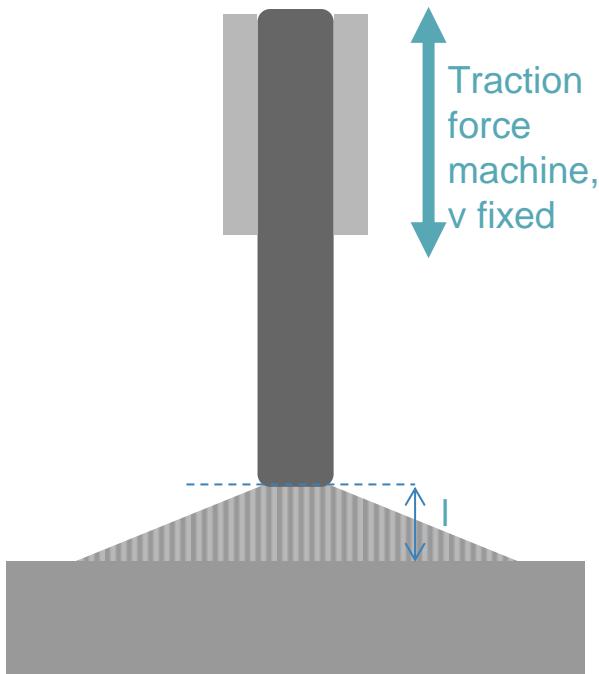
# Compressing brushes and varying the fibers' length



# New unit: crushing distance $l$

One notation for one coordinate

- F only depends on  $l$



Two notations  
for one  
coordinate so no  
one understands

# Scaling law model for the force

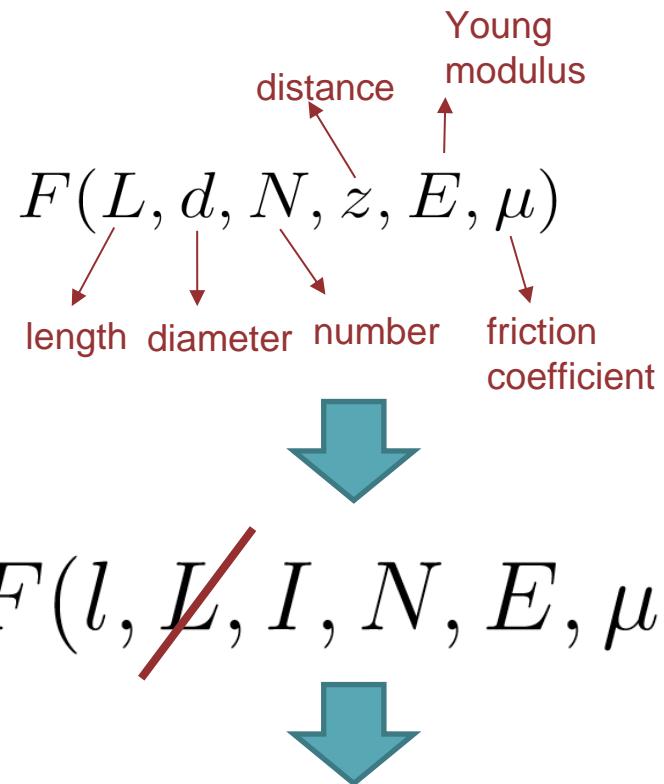
With :  $E = 3 - 5 \text{ GPa}$

$$I = 2.9 \cdot 10^{-18} \text{ m}^4$$

$$I = \frac{\pi d^4}{64}$$

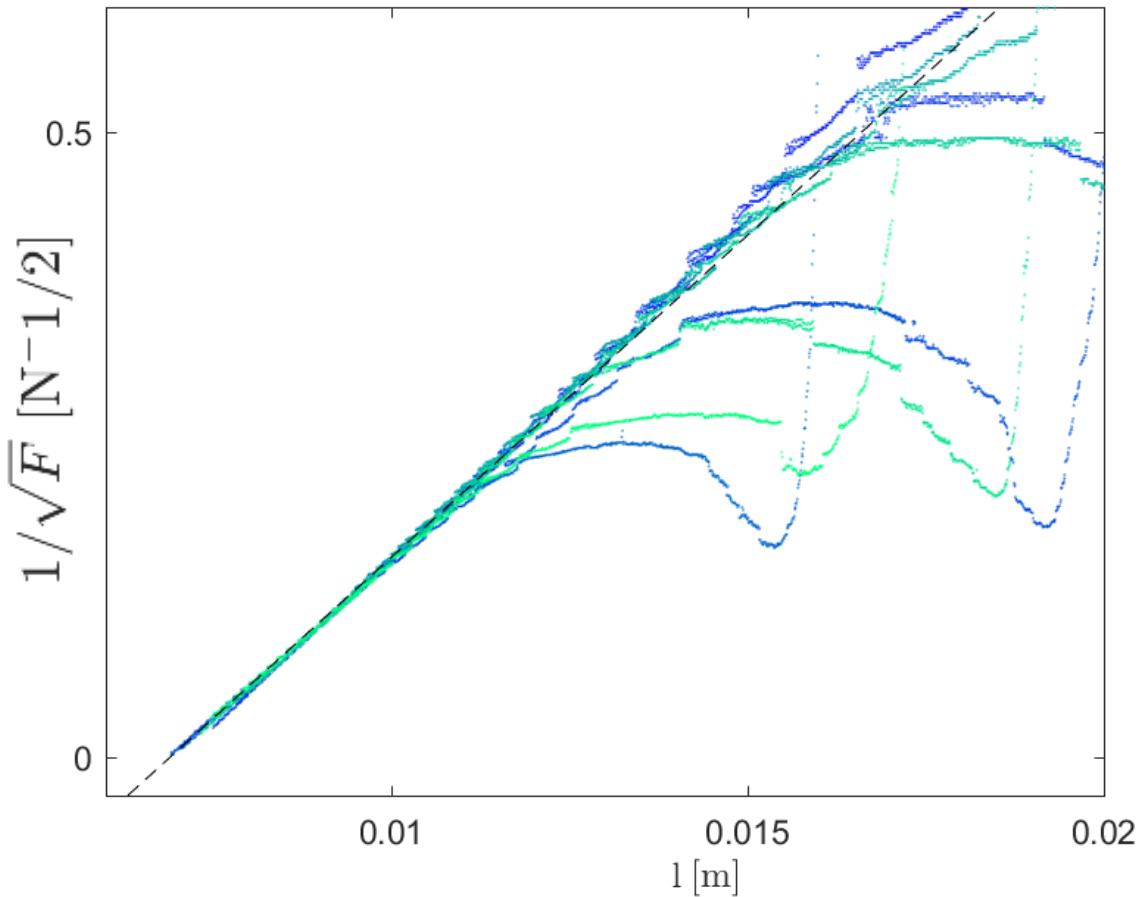
$$l = L - z$$

Scaling law for F



$$F \propto \frac{EI}{l^2}$$

# Compressing brushes and varying the fibers' length



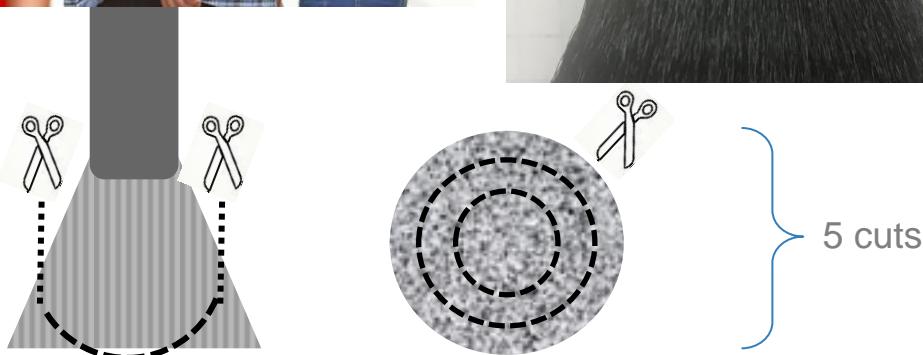
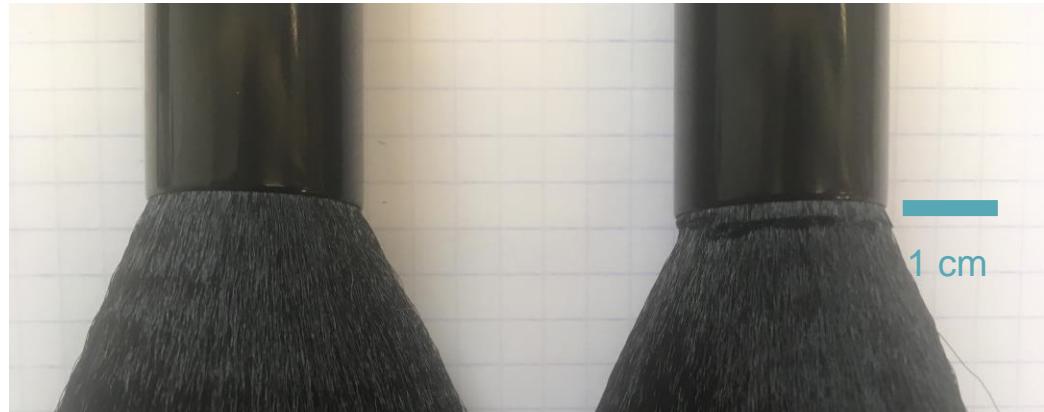
■ Mastercurve for every fibers' length

$$F \propto \frac{EI}{l^2}$$

# Compressing brushes and varying the number of fibers



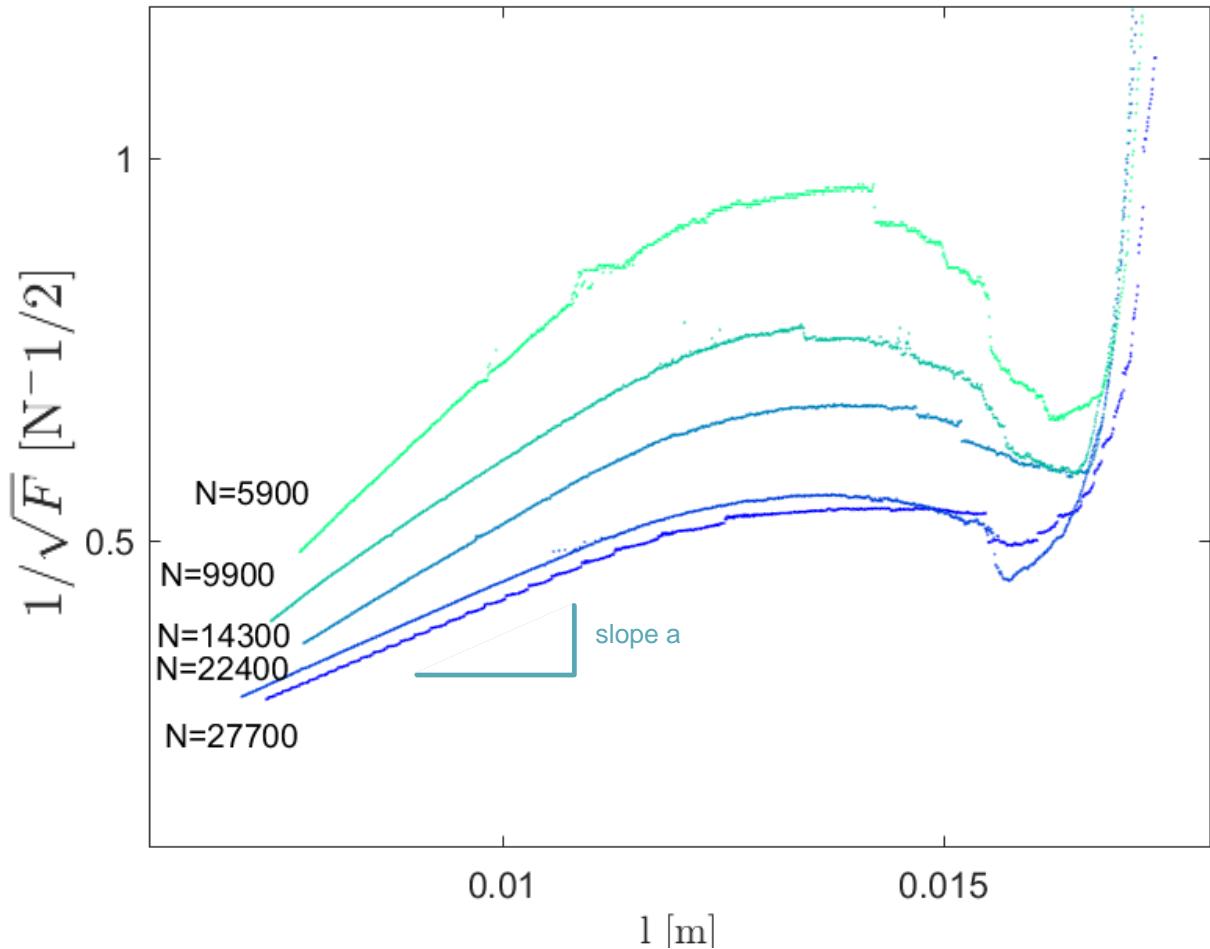
$$F(l, I, \textcircled{N}, E, \mu)$$



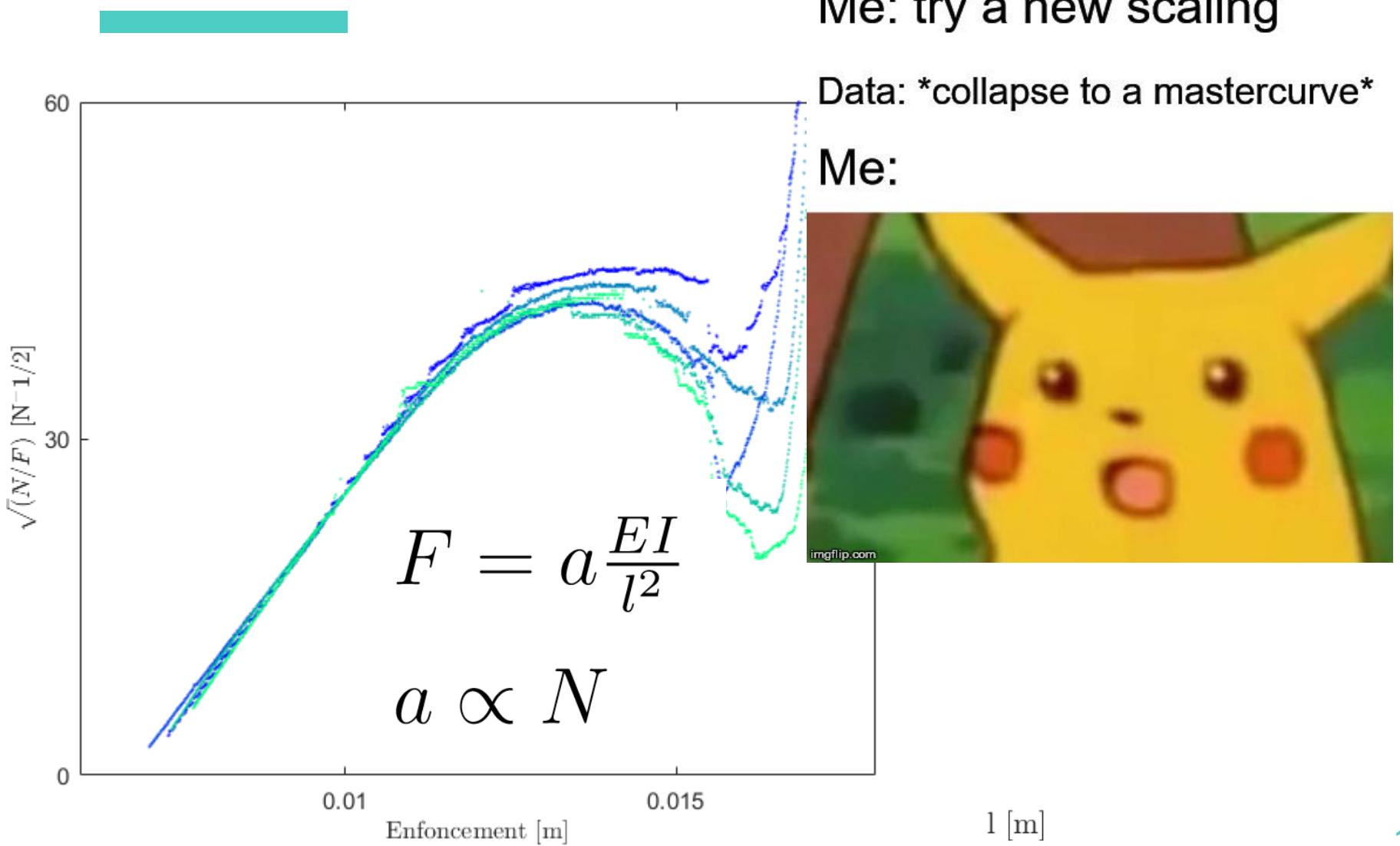
N varying between  
27 700 and 5800 fibers

# Compressing brushes and varying the number of fibers

$$F = a \frac{EI}{l^2}$$



# Compressing brushes and varying the number of fibers



# Types of brushes



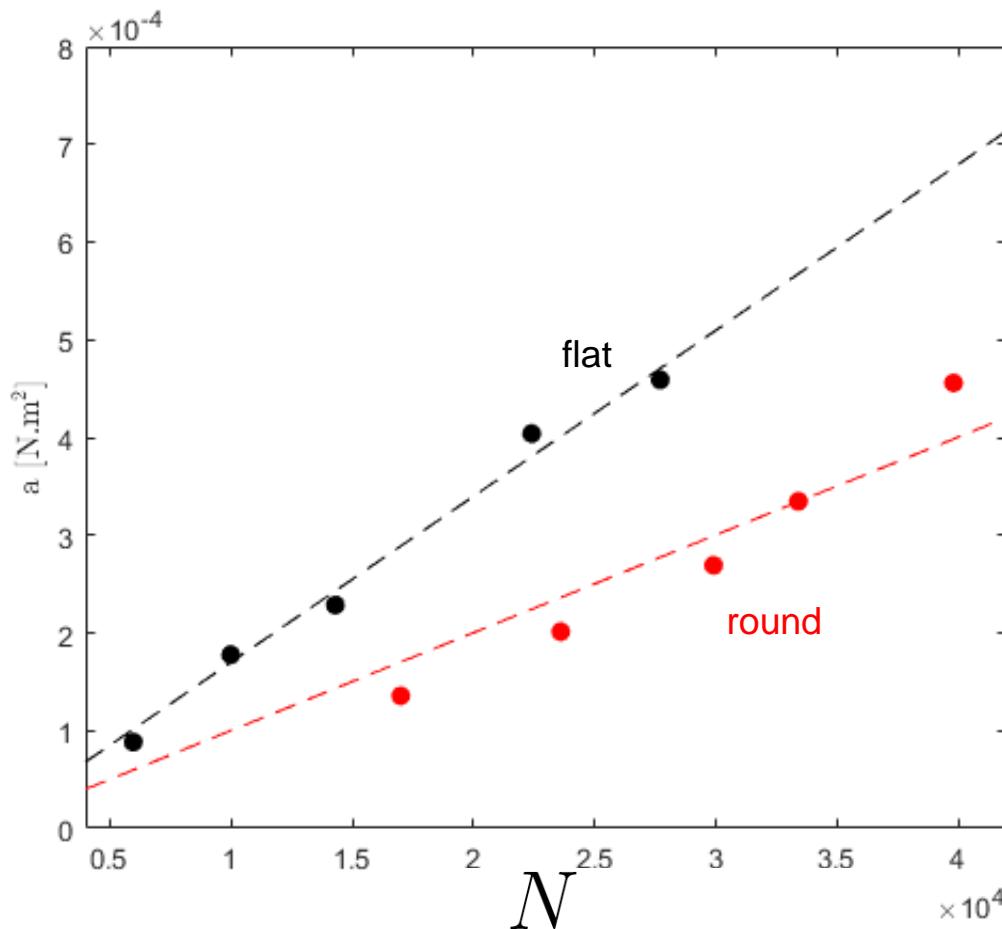
using  
one brush



using  
two brushes



# Slope for different number of fibers – round brush



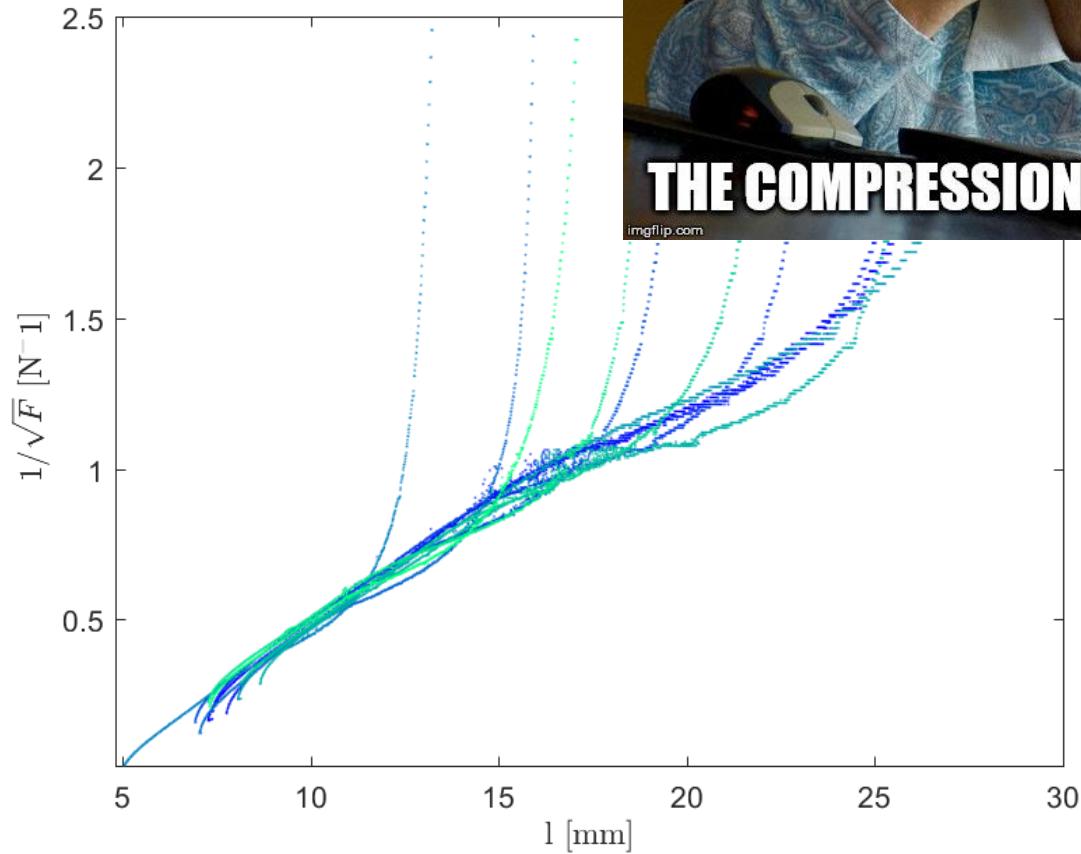
$$a \propto N$$

It works for both of our brushes, with different coefficients

IS THAT

# Return - decompression

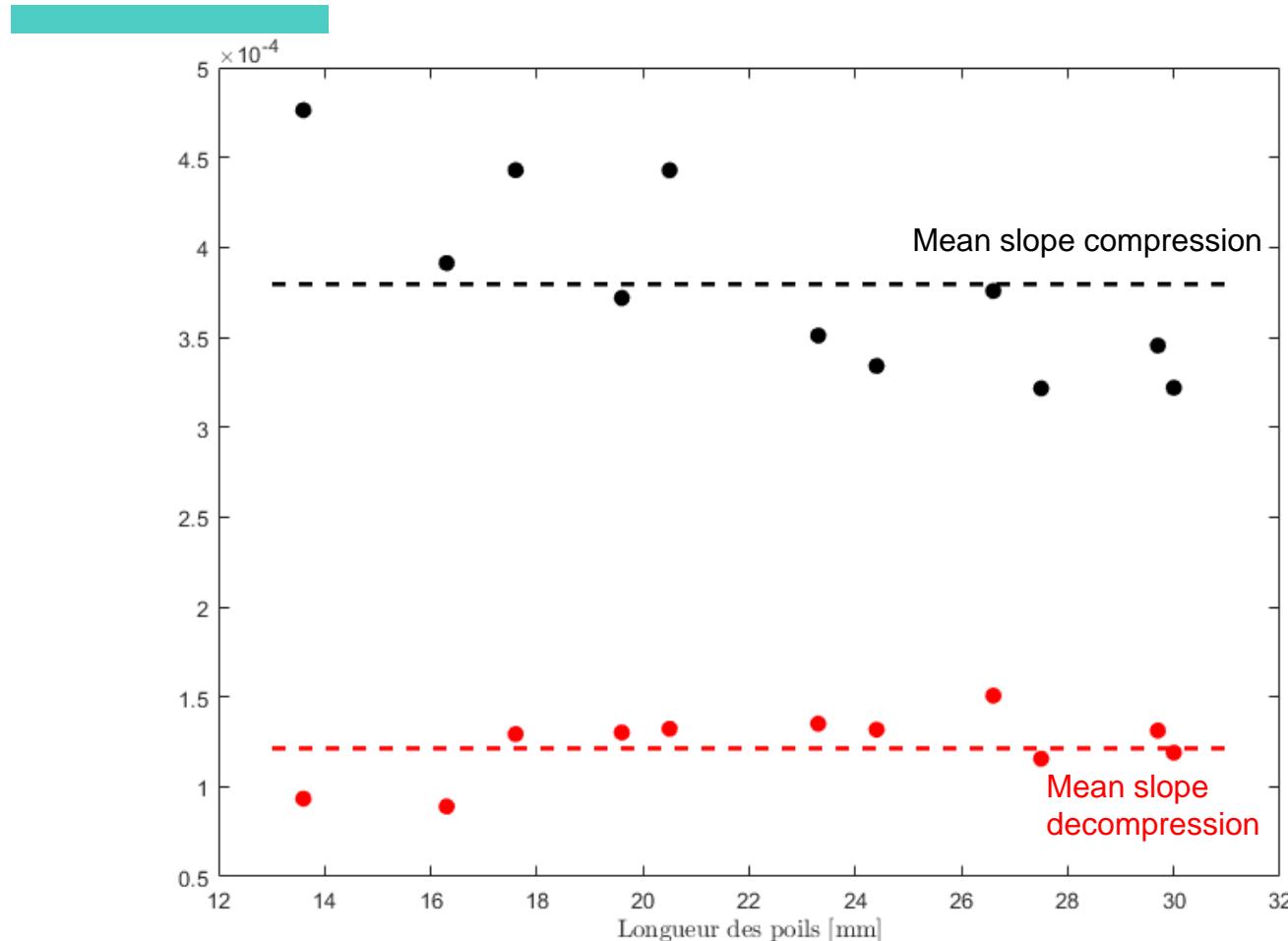
return compression



- Mastercurve for every fibers' length



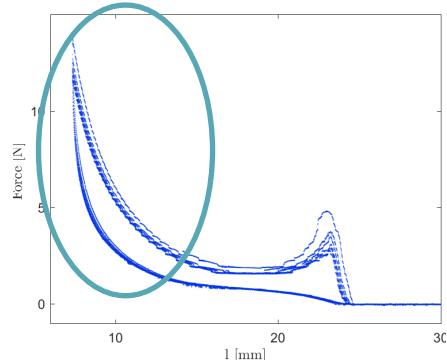
# Comparison compression and decompression



- Different prefactor for traction and compression

# Conclusion

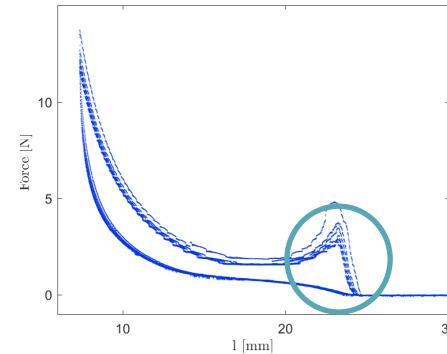
## □ Big deformations



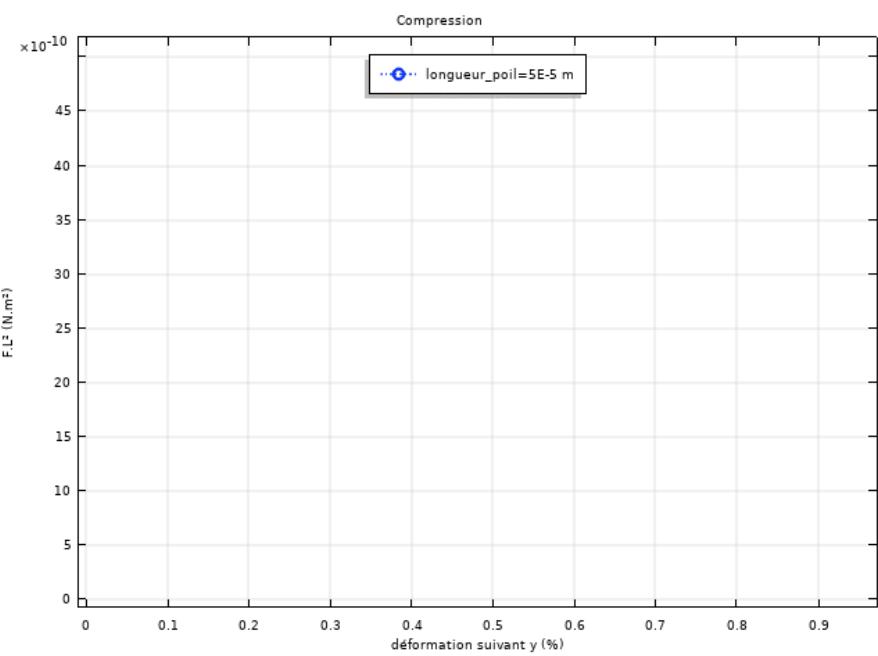
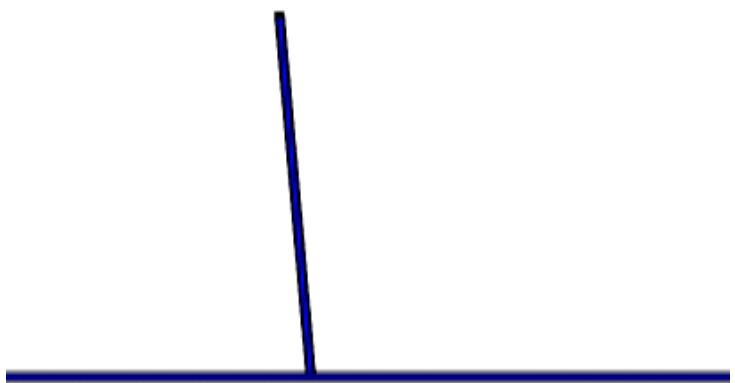
$$F = kN \frac{EI}{l^2}$$

- $k$  is different for compression and decompression
- $k$  does not depend on  $L$

## □ Small deformations



- Bump at constant  $\epsilon$
- But different from single hair experiments

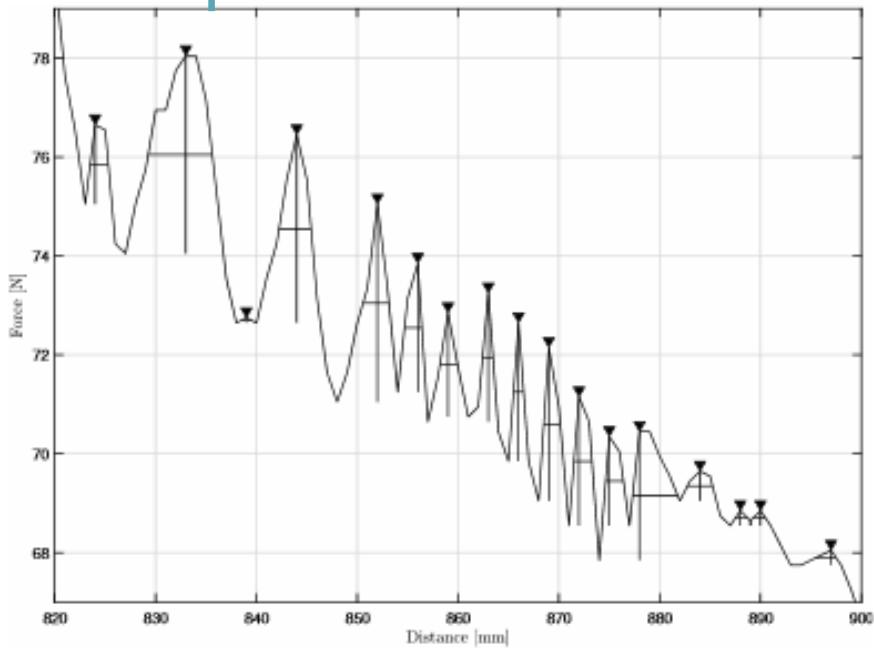


# Perspectives

- Interleaving two brushes



- Statistics of the force-displacement curves



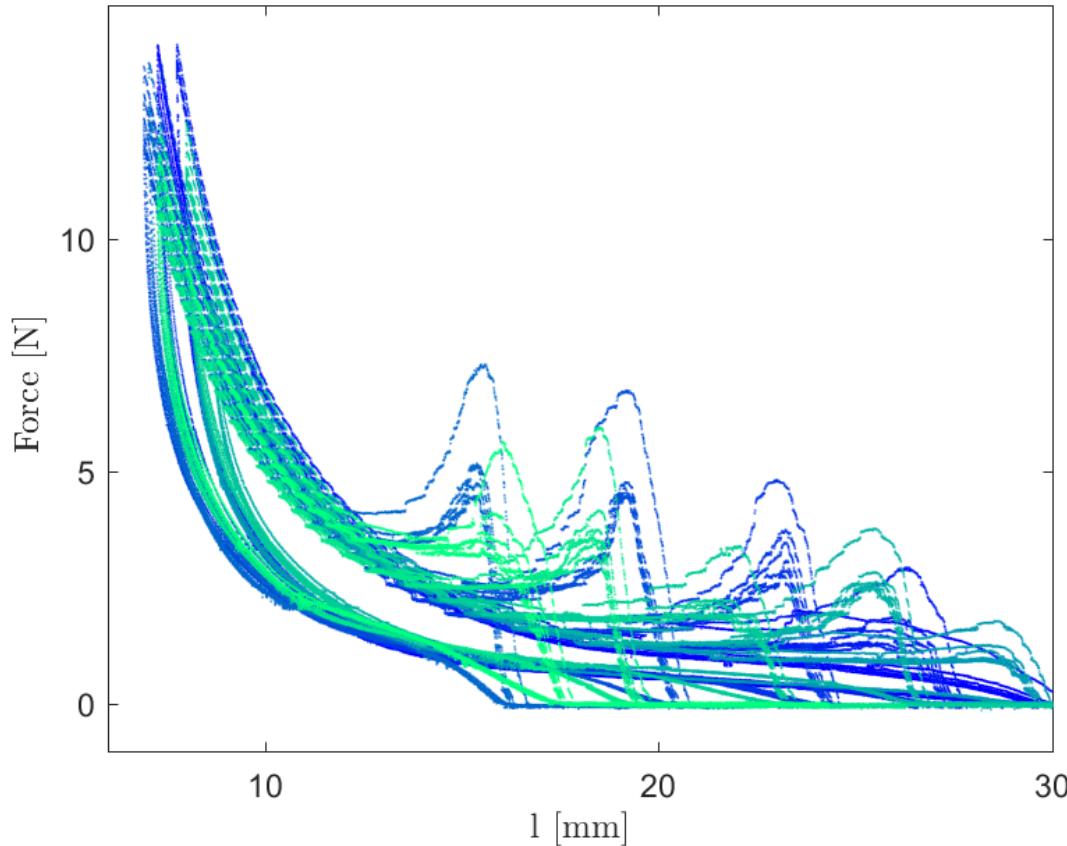
# Thanks!

## Any questions?

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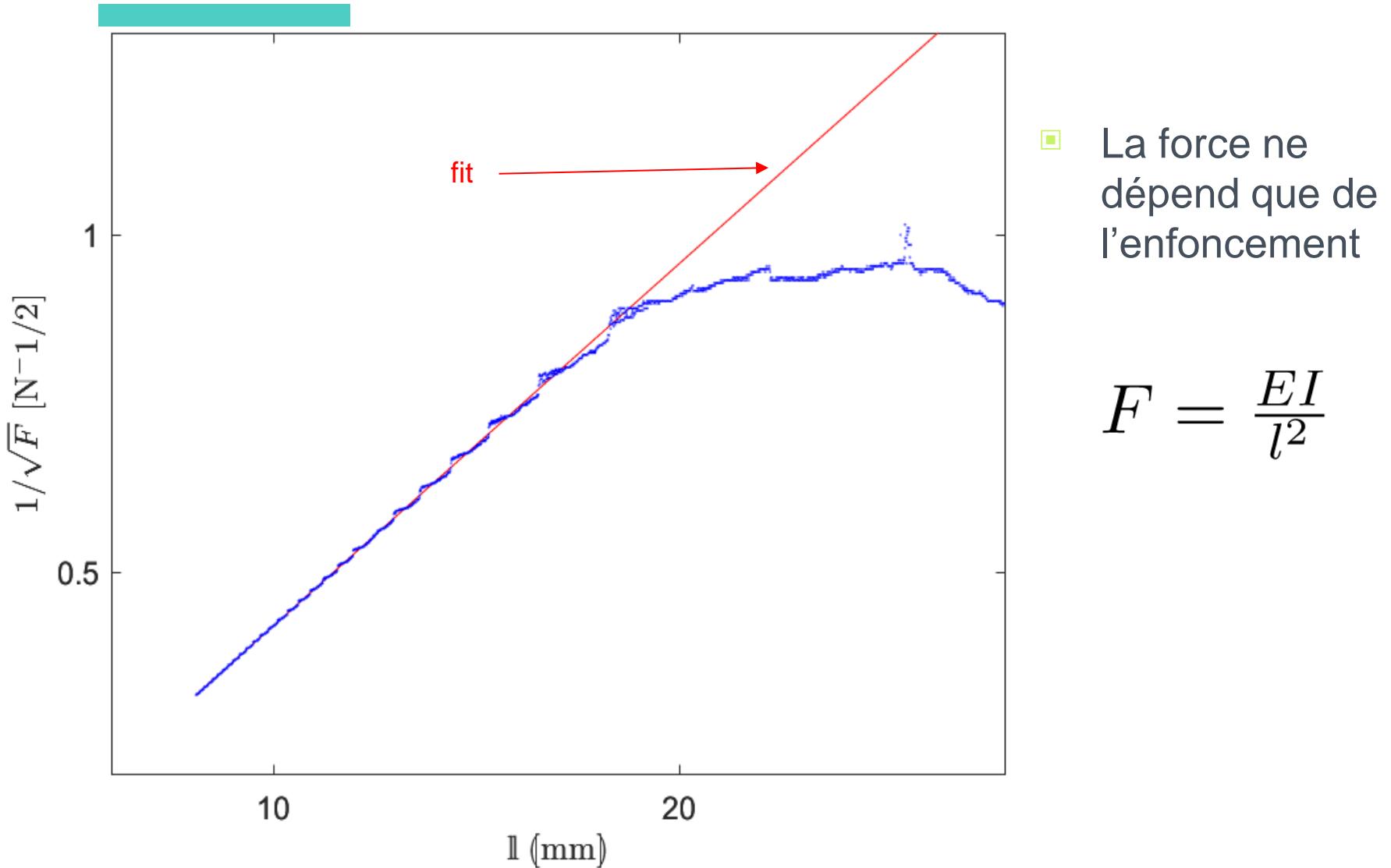
Raphaelle Taub  
PhD Student – Université Paris Sud  
[raphaelle.taub@u-psud.fr](mailto:raphaelle.taub@u-psud.fr)

# Compressing brushes and varying the fibers' length

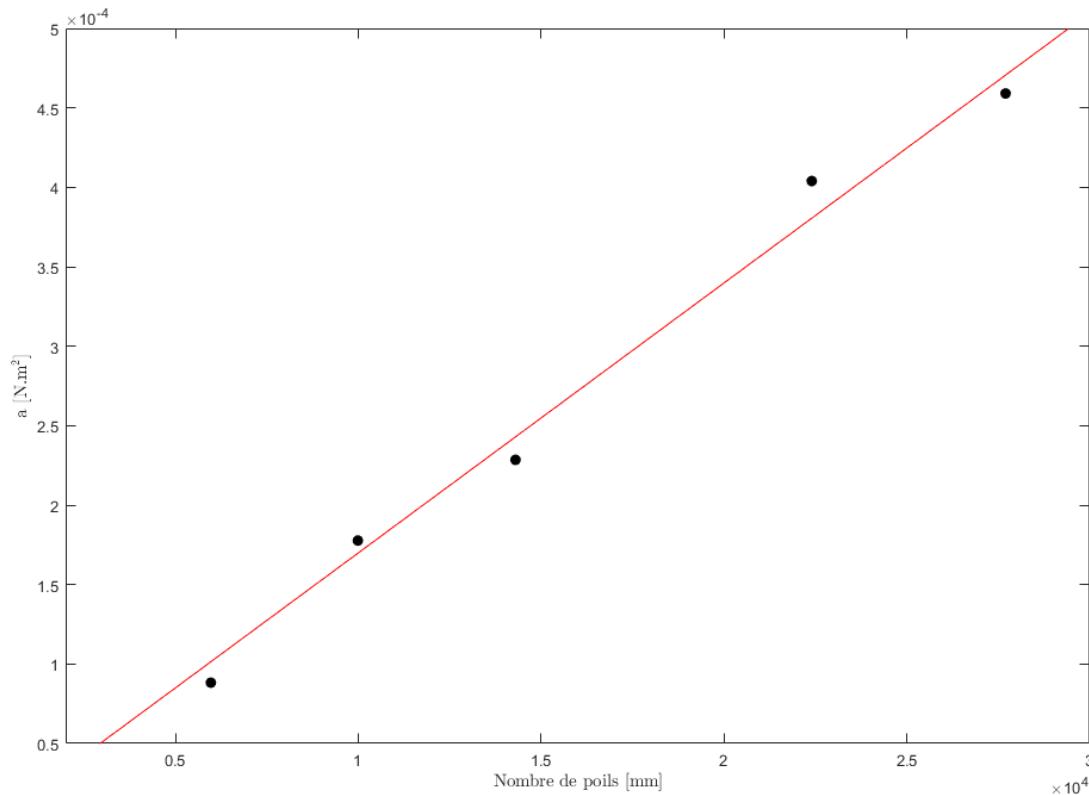


- ▢ No dependency in the fibers' lengths

# Compression du pinceau – fit



# Slope for different number of fibers – flat brush



$$a \propto N$$

# Figure récapitulative sur les pentes et préfacteurs

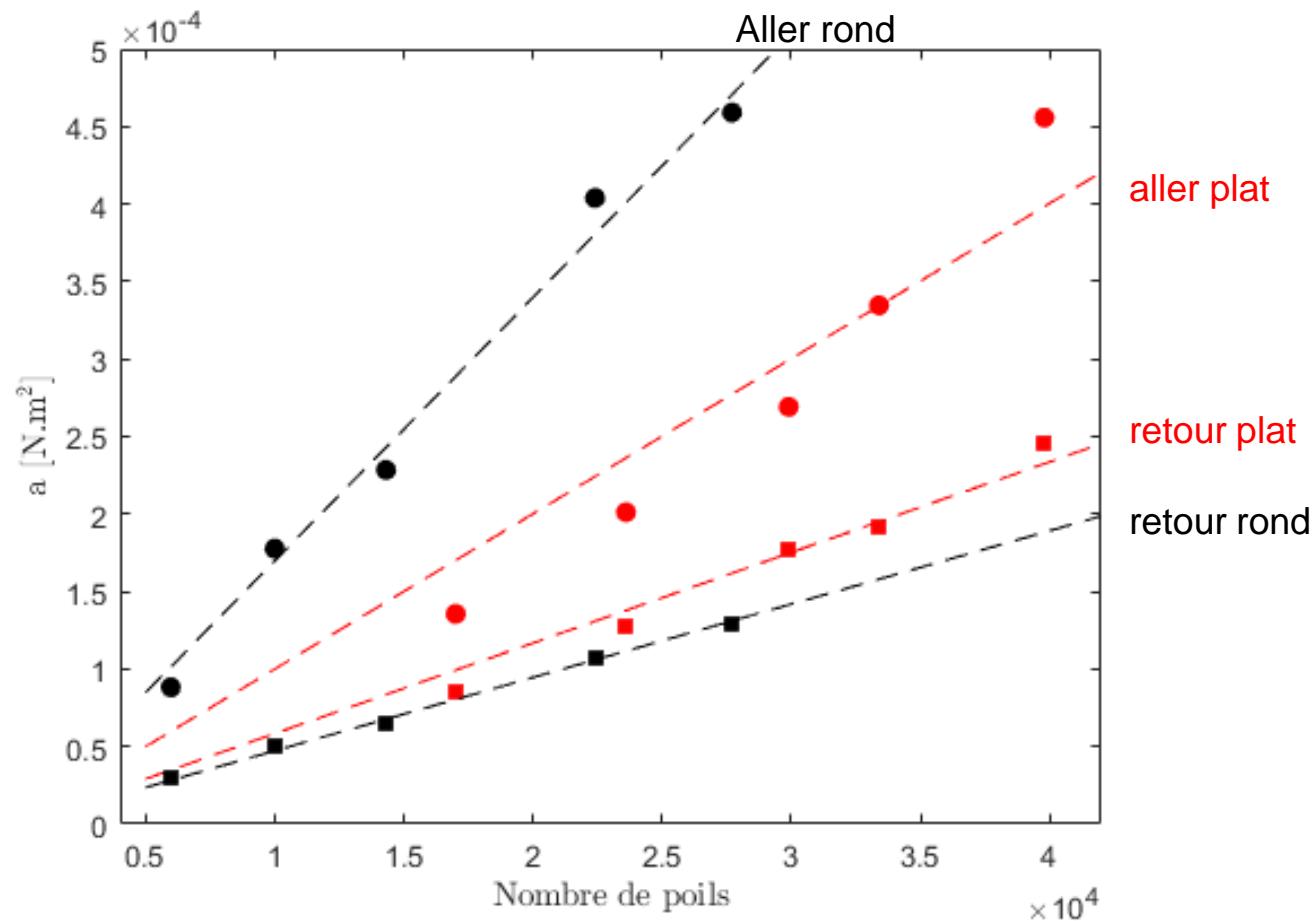
$$F = kN \frac{EI}{l^2}$$

$$a = kNEI$$

Aller rond :  $kEI = 1.001 \cdot 10^{-8}$   
Retour rond :  $kEI = 5.841 \cdot 10^{-9}$   
Aller plat :  $kEI = 1.699 \cdot 10^{-8}$   
Retour plat :  $kEI = 4.73 \cdot 10^{-9}$

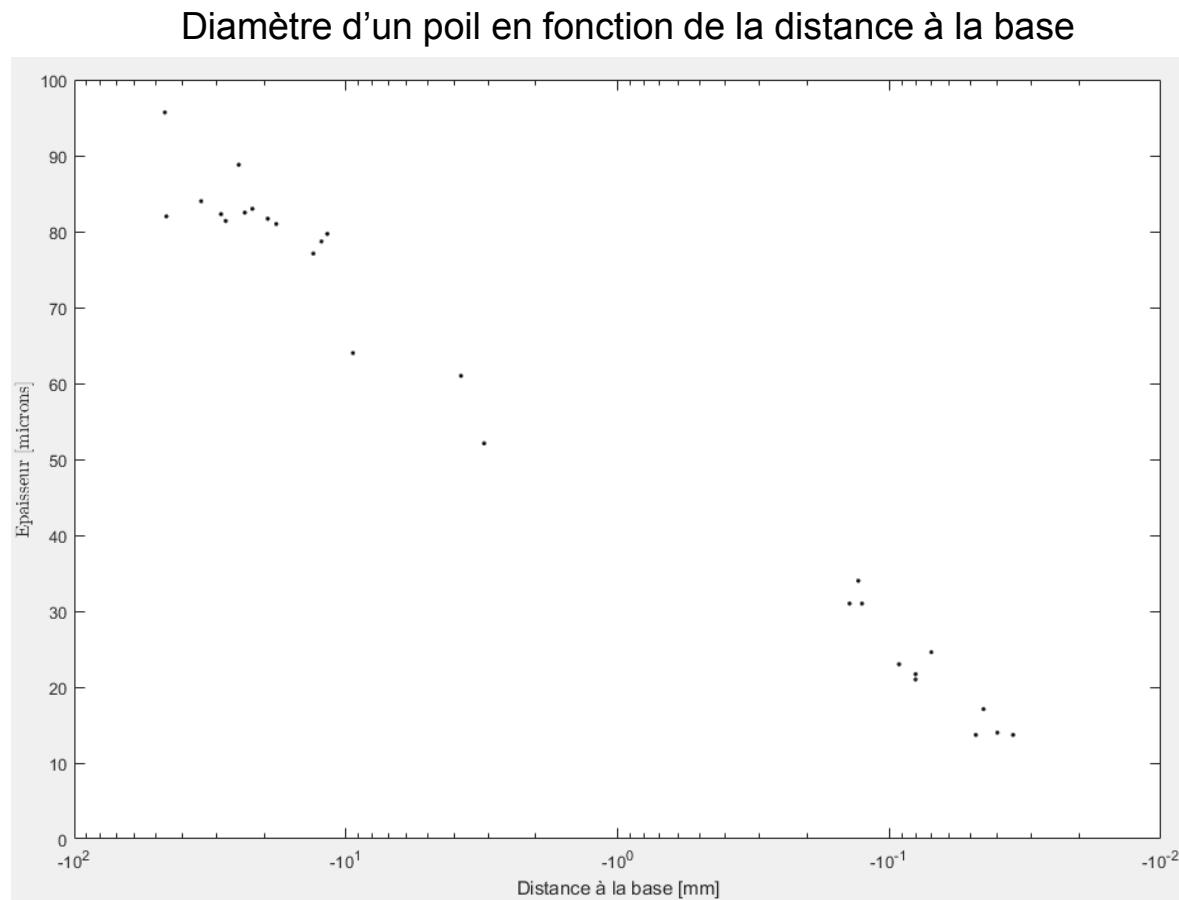
Pinceau rond  
 $I = 2.9 \cdot 10^{-18} \text{ m}^4$

Pinceau plat  
 $I = 2.44 \cdot 10^{-18} \text{ m}^4$



# Caractéristiques des poils

- Diamètre varie le long du poil,
- Module d'Young : 3 à 5 GPa pour des poils en polyamide,
- Longueur : 2 à 5 cm
- Nombre de poils :  
27700 (mesure pesée)  
à 37600 (mesure géométrique)



# Questions en suspens

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$$F = kN \frac{EI}{l^2}$$

- Pourquoi le préfacteur  $k$  est différent à l'aller et au retour ? Est-ce qu'il est possible d'avoir une prédition théorique pour  $k$  (il est proche de 1 à l'aller) ?
- Est-ce qu'il est possible d'avoir un modèle qui fitte mieux les données des très grandes déformations, et qui explique donc l'hystérésis ?
- D'où vient le décalage sur le snap entre les expériences à poil unique et les expériences avec les pinceaux ?