

遞迴01

範例程序01

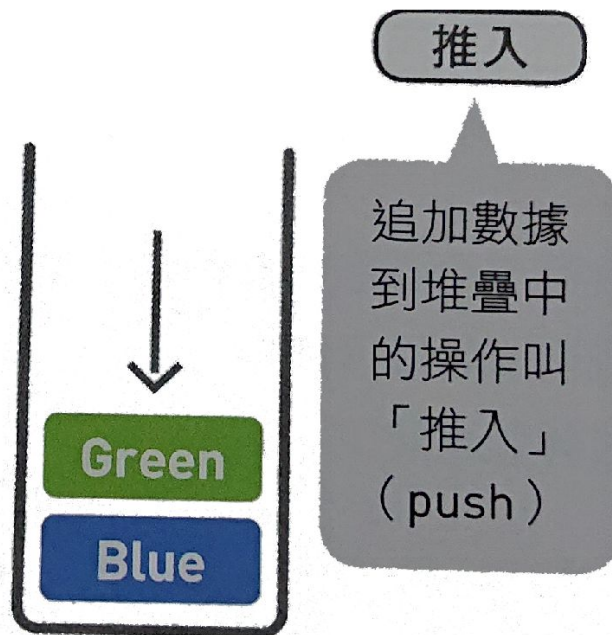
```
void setup(){  
  size(800,600,P3D);  
  rectMode(CENTER);  
}  
void draw() {  
  background(255);  
  camera(0, 0, 600, 0, 0, 0, 0, 1, 0);  
  strokeWeight(2);  
  stroke(200, 0, 0);  
  line(0, -height, 0, 0, height, 0);  
  stroke(0, 100, 0);  
  line(-width, 0, 0, width, 0, 0);
```

```
  noStroke();  
  fill(150);  
  pushMatrix();  
  translate(300,-200);  
  pushMatrix();  
  rotate(radians(frameCount));  
  rect(0, 0, 200, 60);  
  popMatrix();  
  rect(0, 0, 200, 60);  
  popMatrix();  
  rect(0, 0, 100, 60);  
}
```

堆疊(stack)

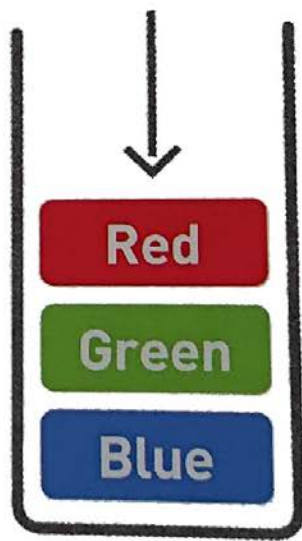


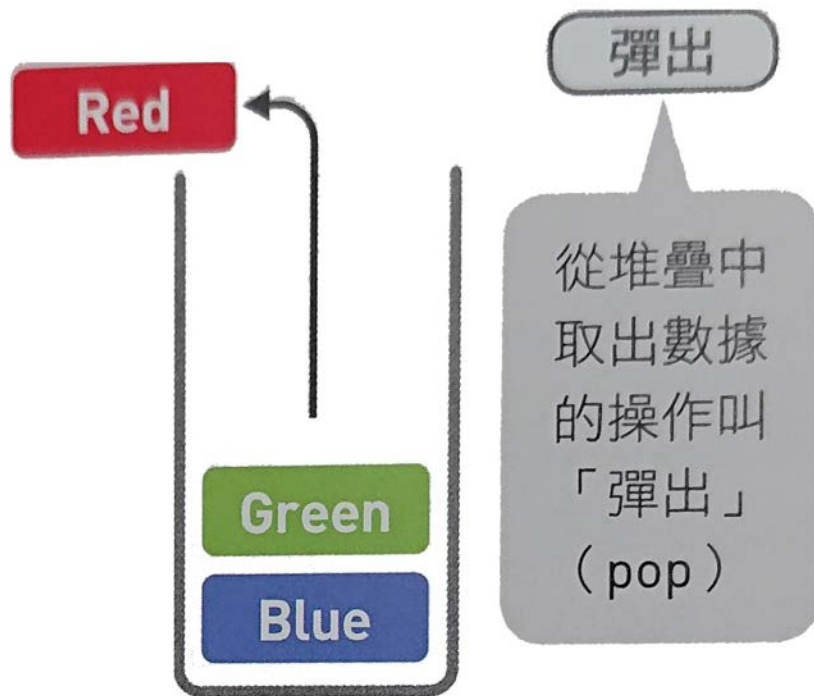
追加數據到堆疊中時，
數據加在最上面



推入

Push





Green

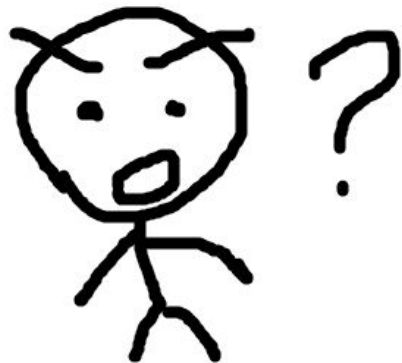


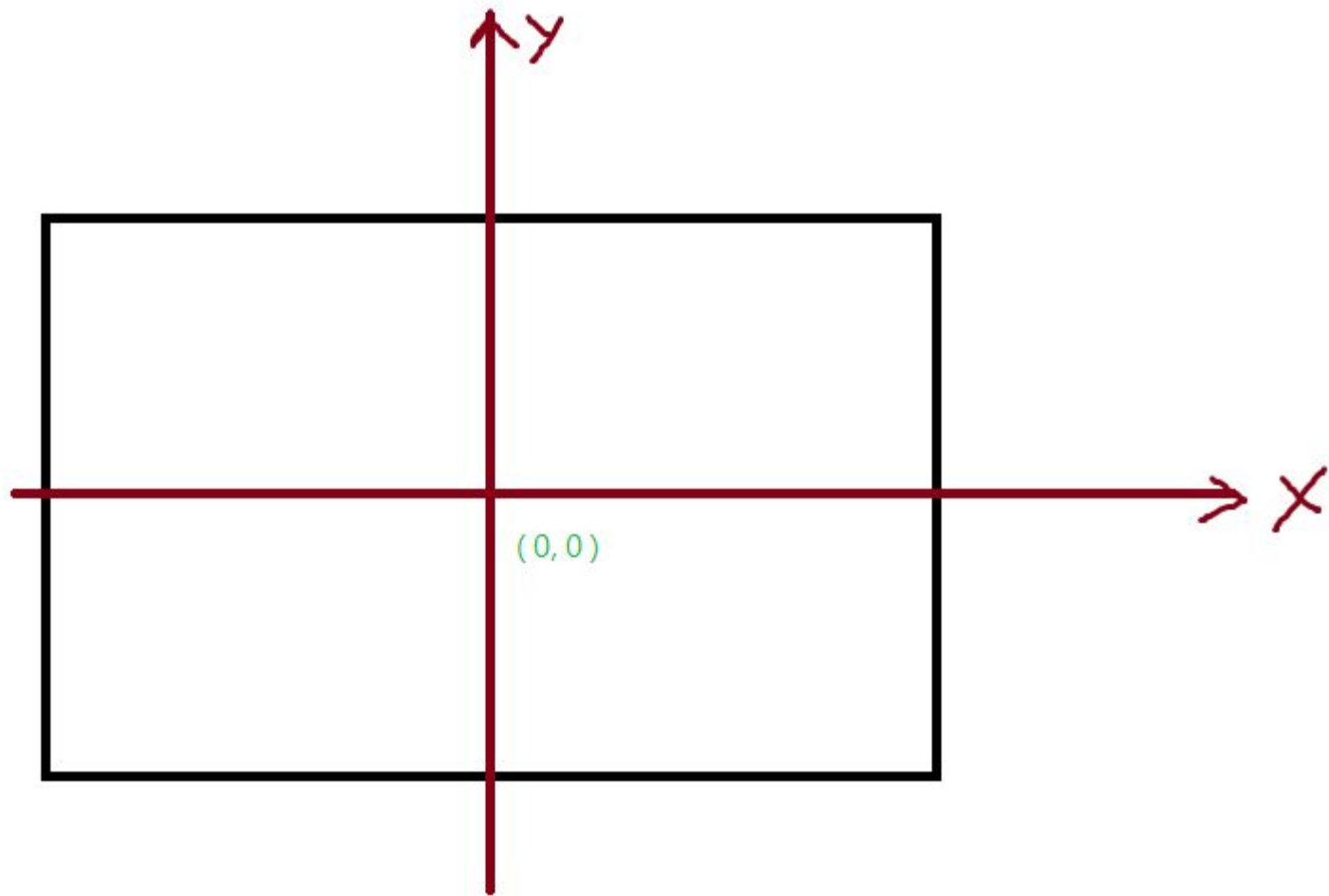
Blue

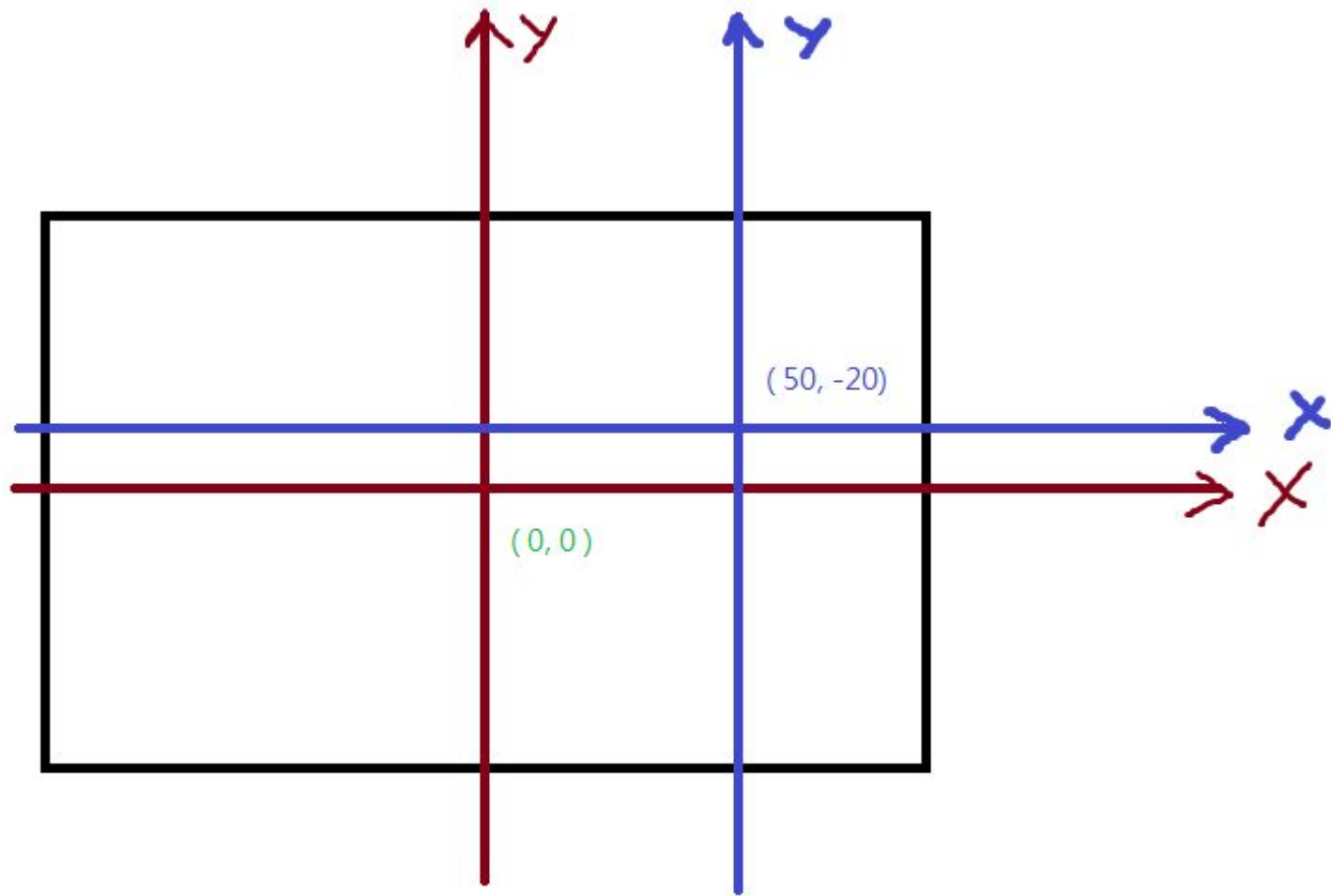
彈出

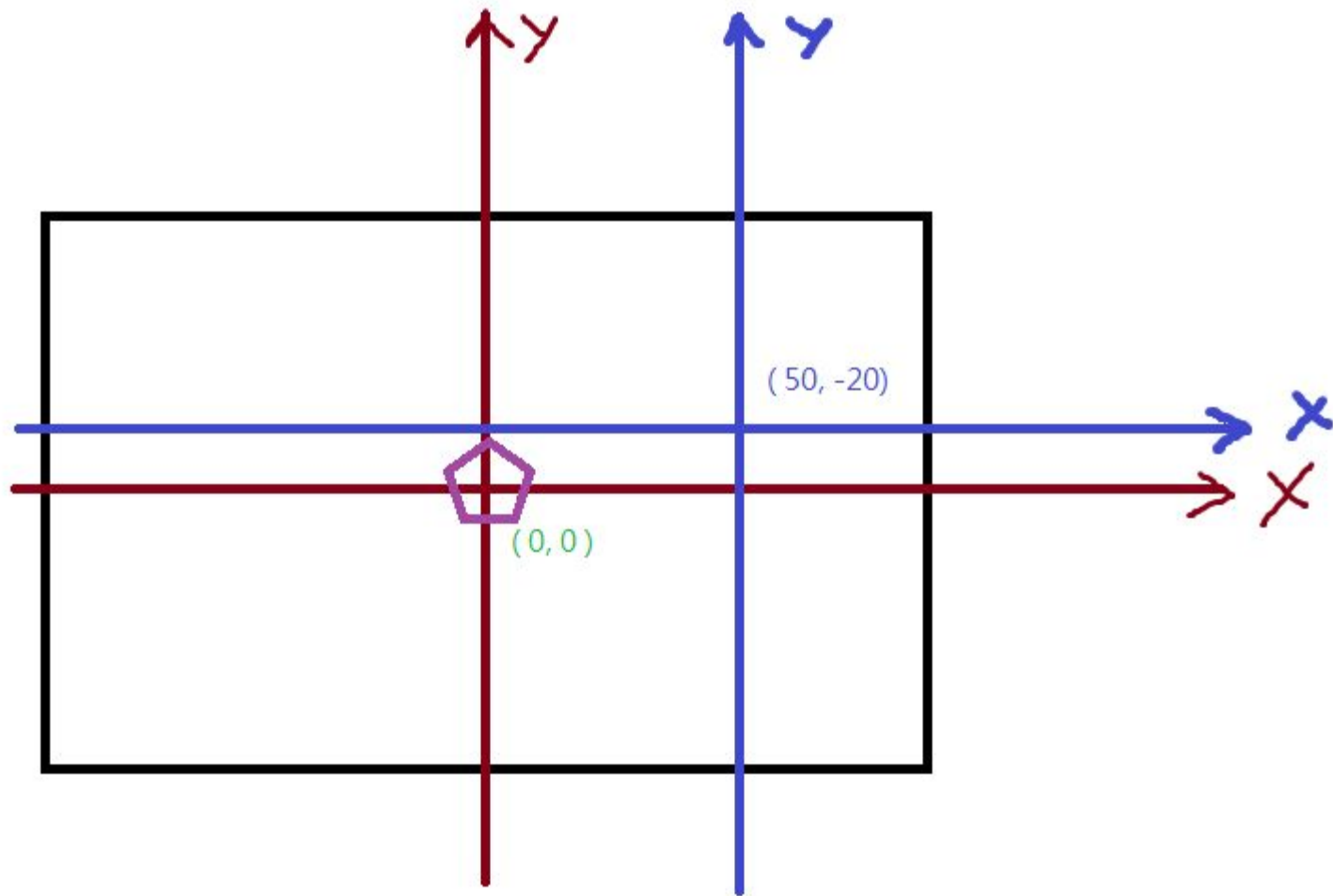
Pop !

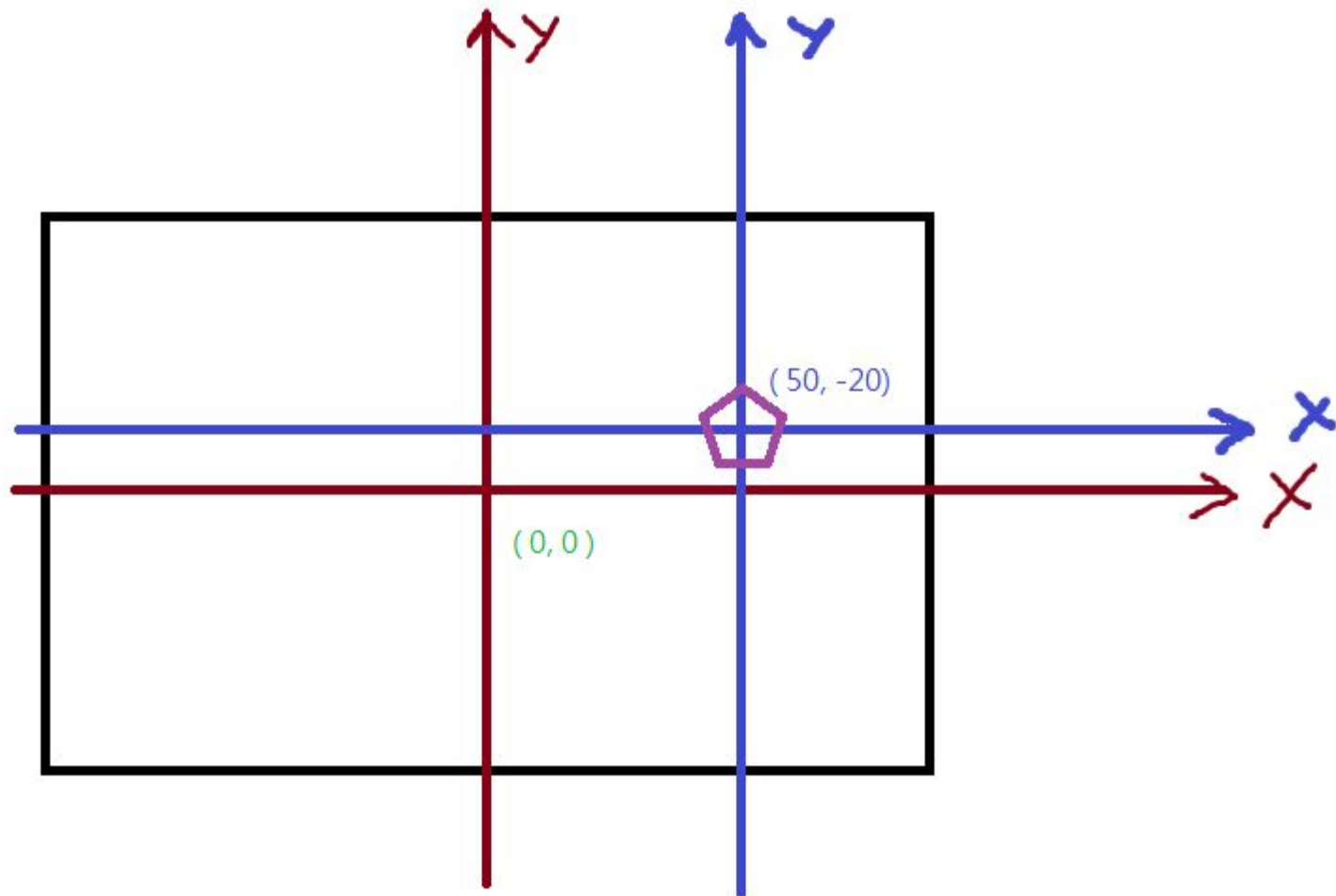
Push/Pop ???

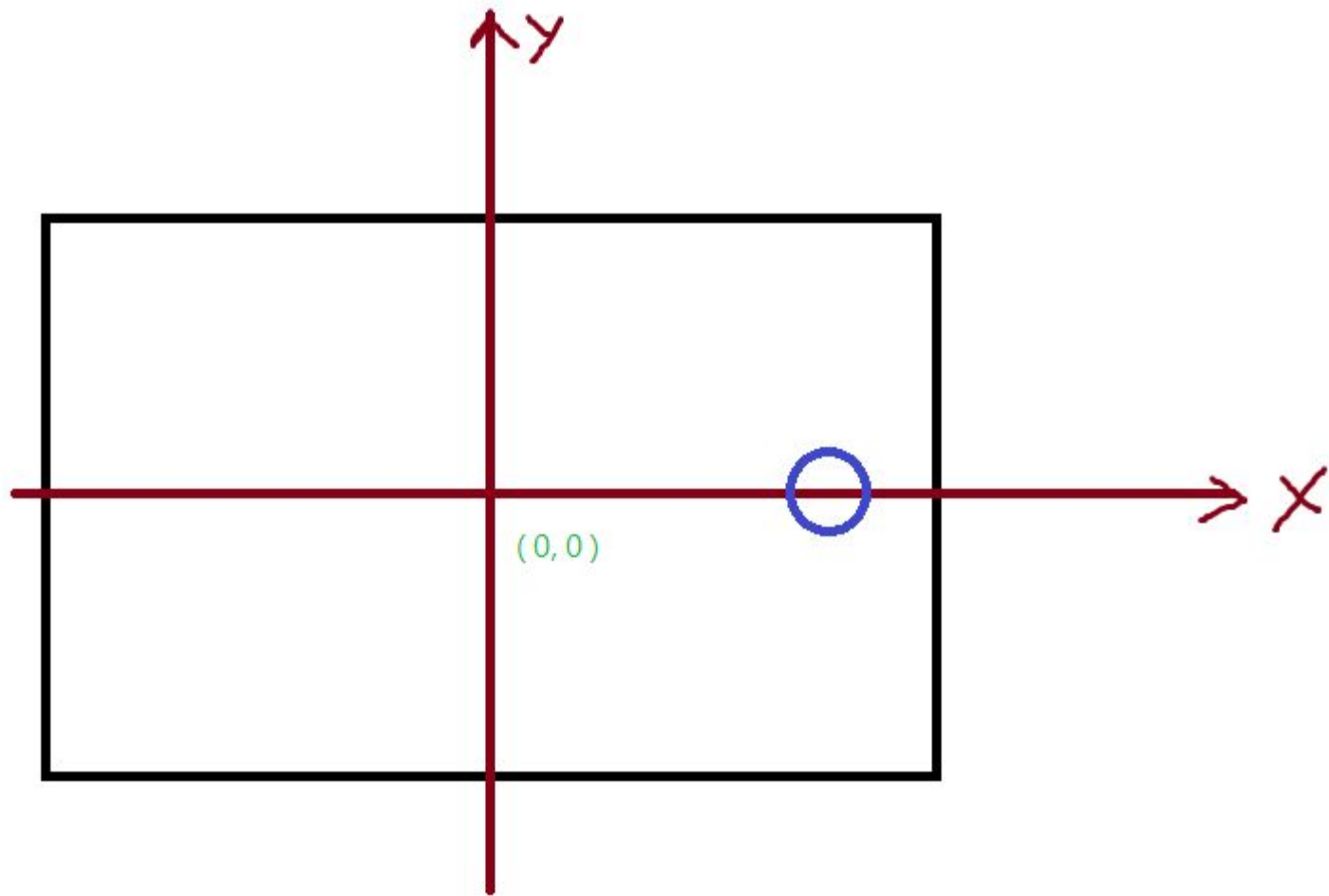


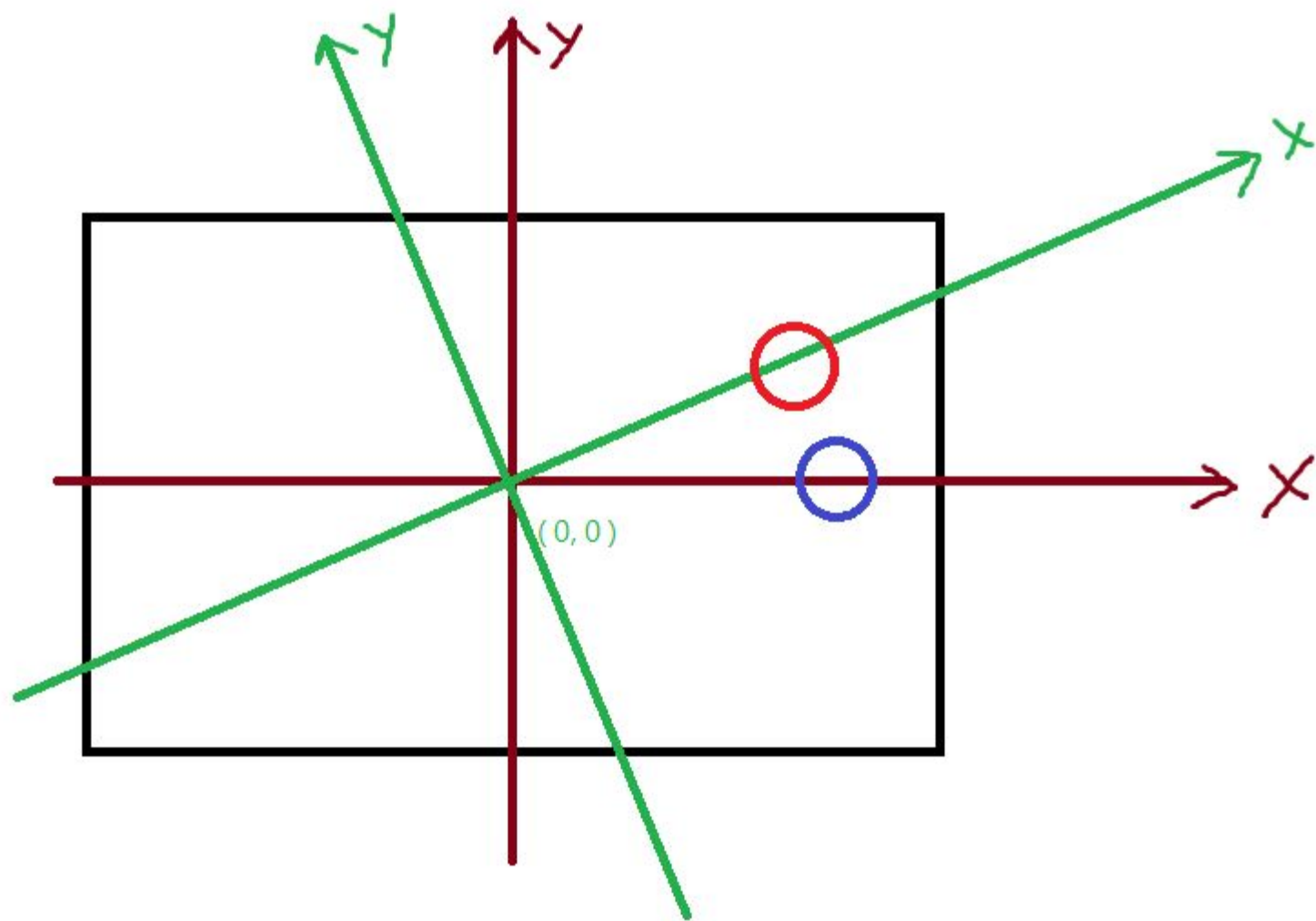


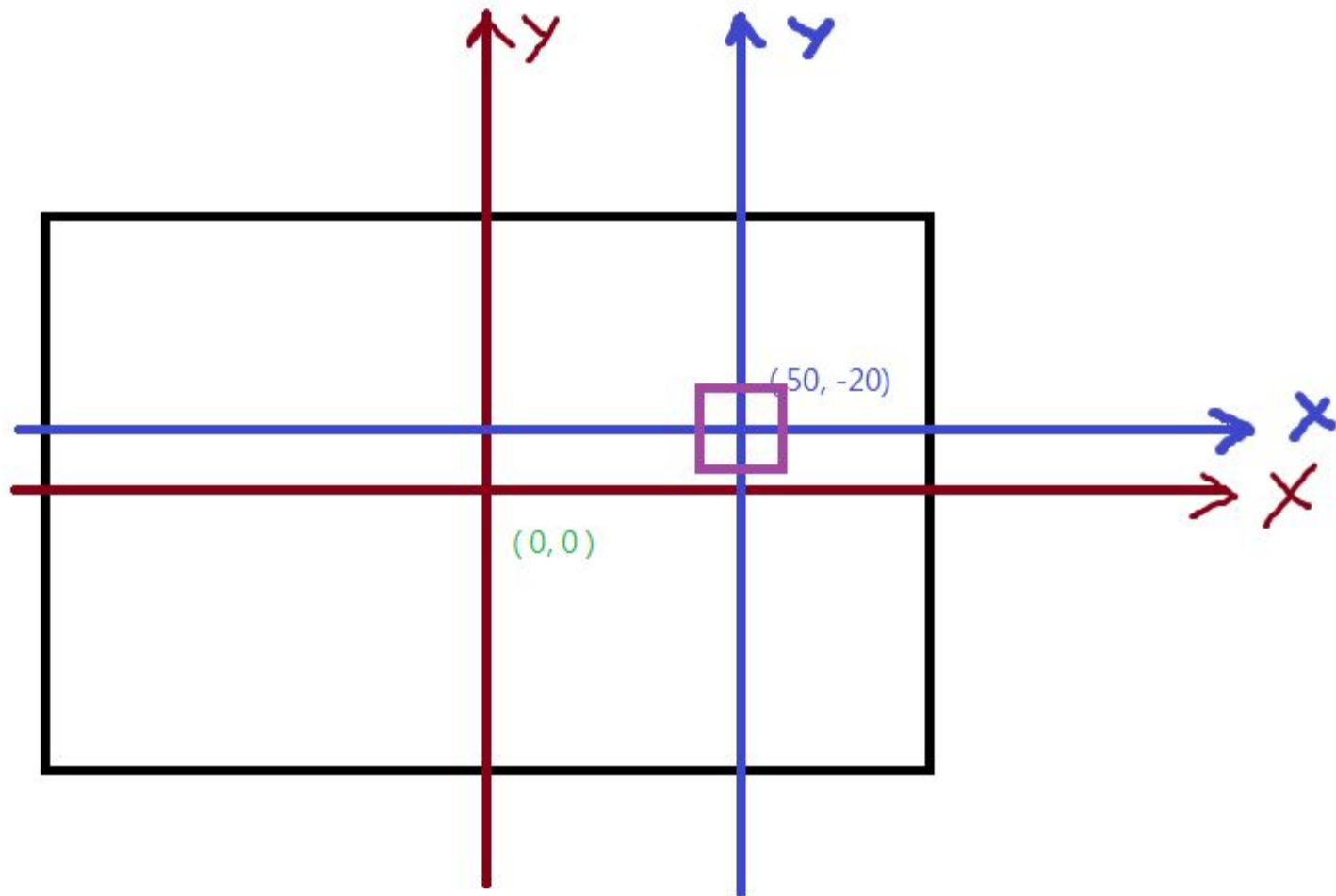


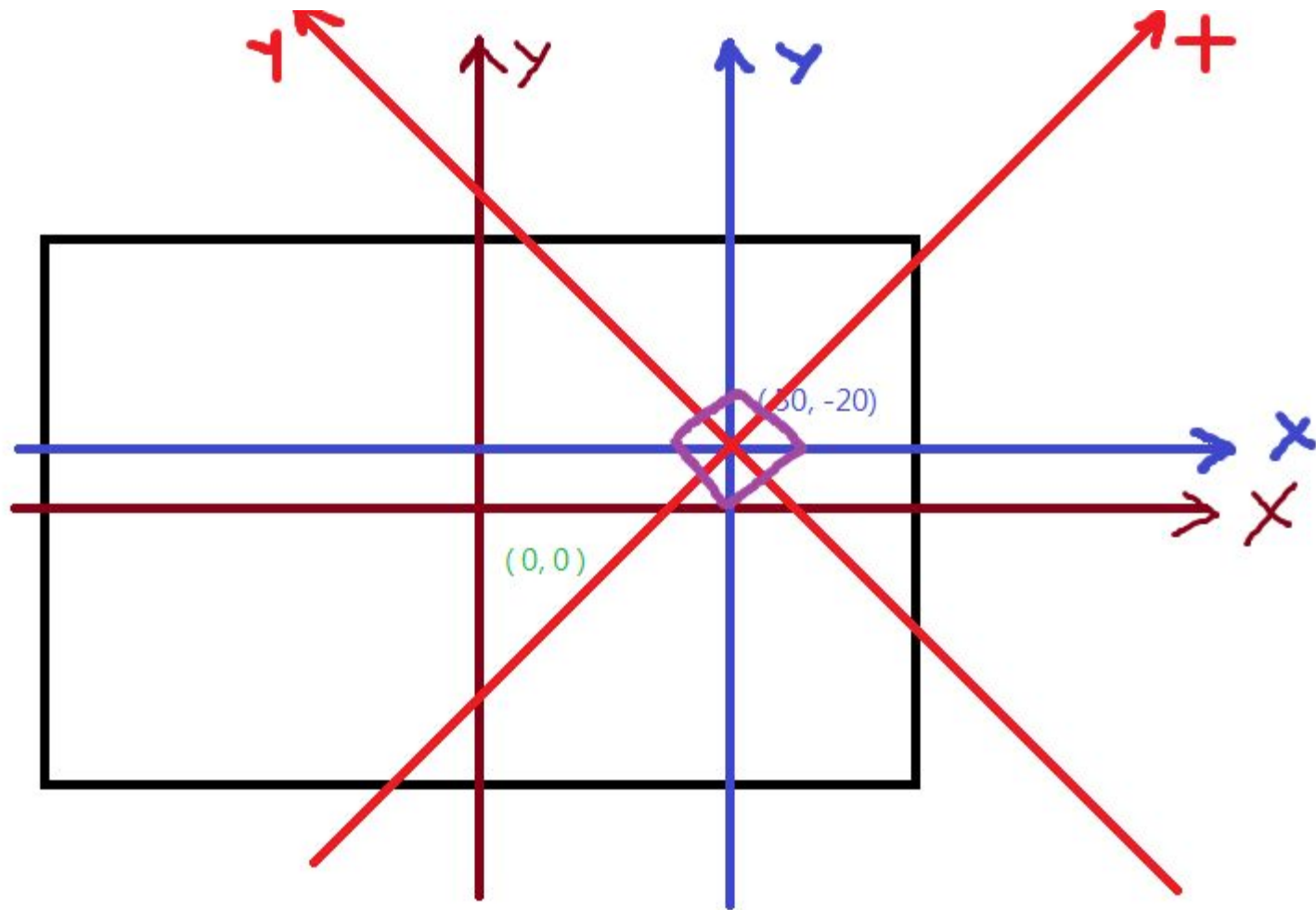


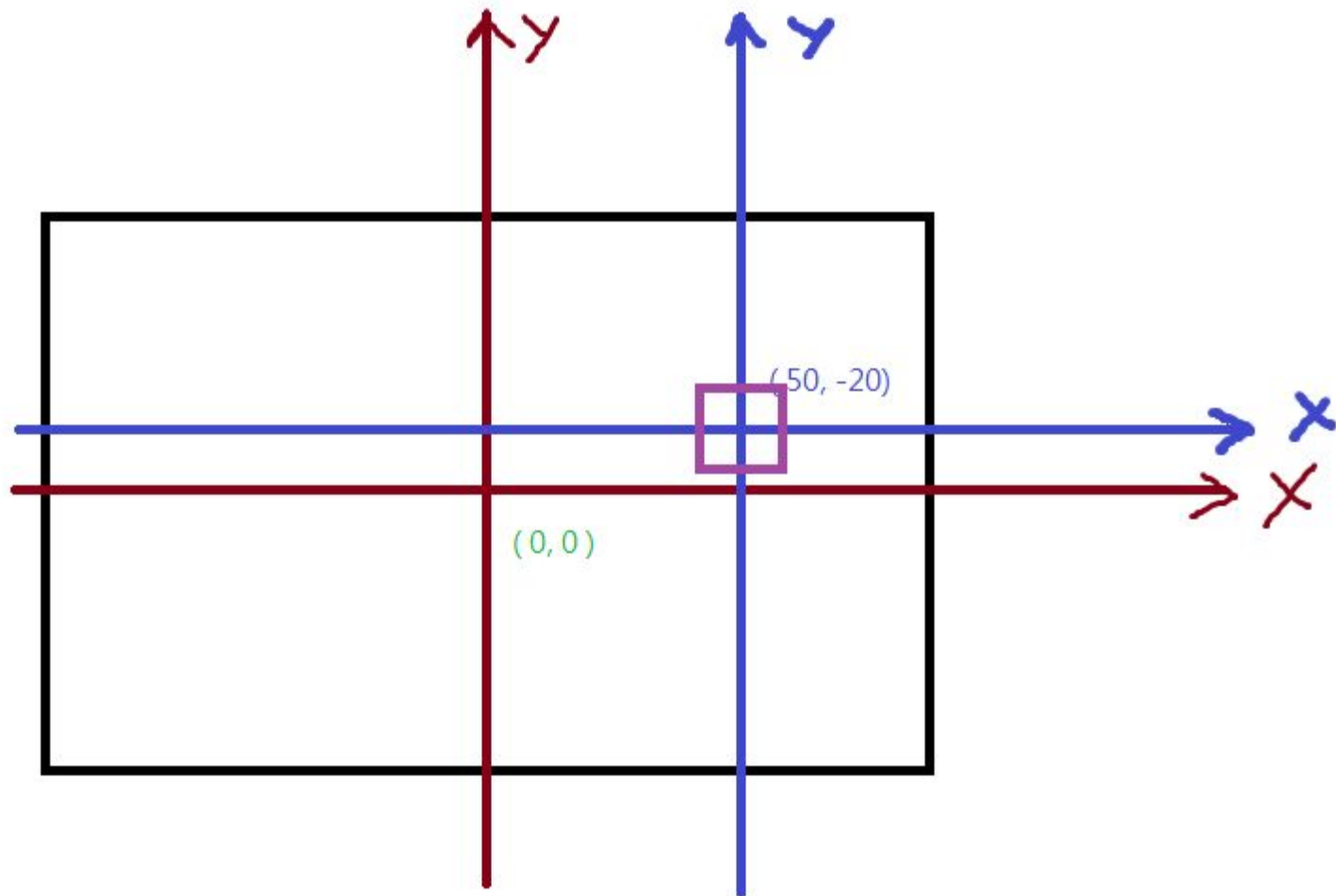




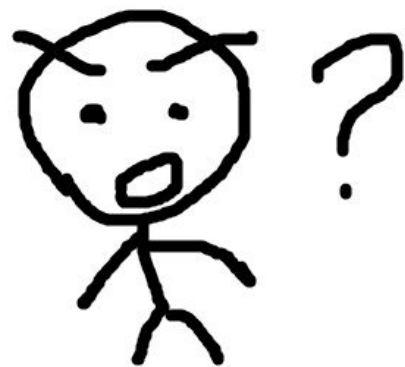








先旋轉再平移？



佇列

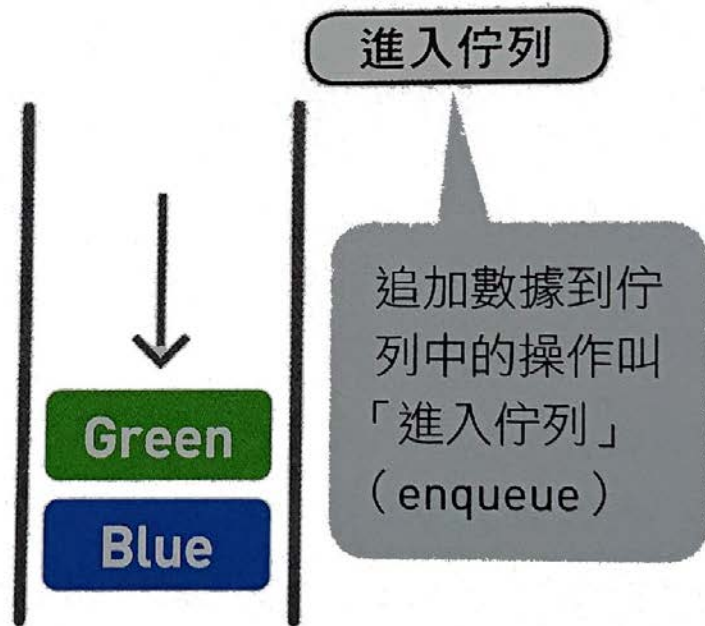
Queue



A diagram illustrating a stack data structure. It consists of two vertical black lines representing the boundaries of the stack. Between these lines, at the bottom, is a blue rounded rectangle containing the word "Blue". To the right of the stack, there is a grey speech bubble pointing towards the stack.

Blue

追加數據到佇列中時，
數據加在最上面



進入佇列

enqueue!



Red

Green

Blue

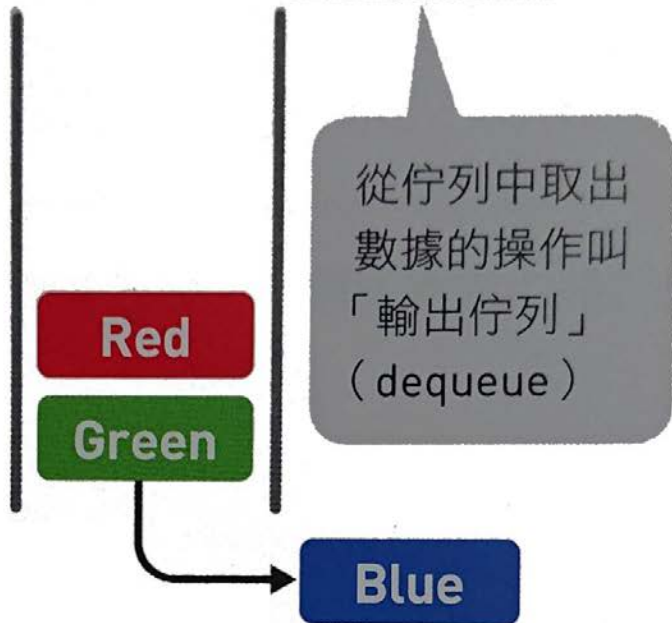
輸出佇列

從佇列中取出
數據的操作叫
「輸出佇列」
(dequeue)

Red

Green

Blue





遞迴

recursion

DEMO
CODE

```
void setup() {  
  size(800, 600, P3D);  
  rectMode(CENTER);  
}
```

```
void draw() {  
  background(255);  
  drawSquare(width/2, height/2, 100);  
}
```

```
void drawSquare(float x, float y, float R) {  
  rect(x, y, R, R);  
}
```

自己呼叫自己


DEMO 1

CODE

```
void setup() {  
  size(800, 600, P3D);  
  rectMode(CENTER);  
}  
void draw() {  
  background(255);  
  drawSquare(width/2, height/2, 100);  
}  
void drawSquare(float x, float y, float R) {  
  rect(x, y, R, R);  
  drawSquare(x, y-R, R/2);  
}
```

stack overflow

堆疊溢位



☺ 呼叫太多次堆疊導致程式的記憶體爆掉

☺ 程式設計的問答網站

遞迴？ 堆疊？

Recursion/ Stack





?

遞迴? 堆疊?

Recursion/ Stack

如何才能不會stack overflow?



?

遞迴？ 堆疊？

Recursion/ Stack

如何才能不會stack overflow?



設定遞迴的停止條件

DEMO3

CODE

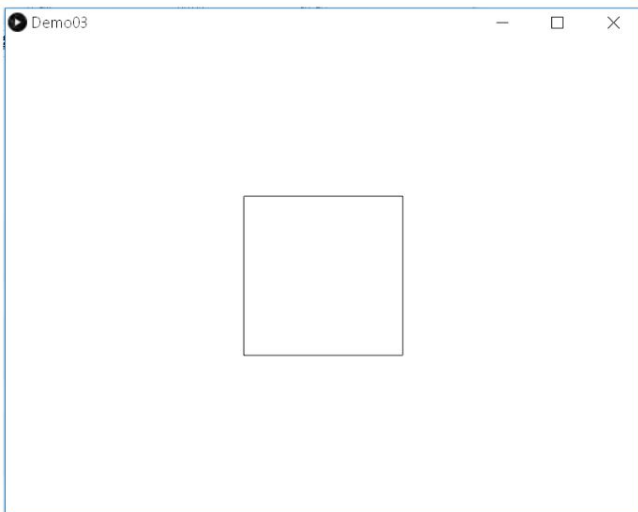
```
void setup() {  
  size(800, 600, P3D);  
  rectMode(CENTER);  
}  
void draw() {  
  background(255);  
  drawSquare(width/2, height/2, 200, 5);  
}  
void drawSquare(float x, float y, float R, int i) {  
  if (i > 0) {  
    rect(x, y, R, R);  
    drawSquare(x, y-R/2, R/2, i-1);  
  }  
}
```

```
drawSquare(width/2, height/2, 200, 4);
```



```
void drawSquare(float x, float y, float R, int i) {  
  if (i > 0) {  
    rect(x, y, R, R);  
    drawSquare(x, y-R/2, R/2, i-1);  
  }  
}
```

$x = 400, y = 300, R = 200, i = 4$




```
drawSquare(width/2, height/2, 200, 4);
```



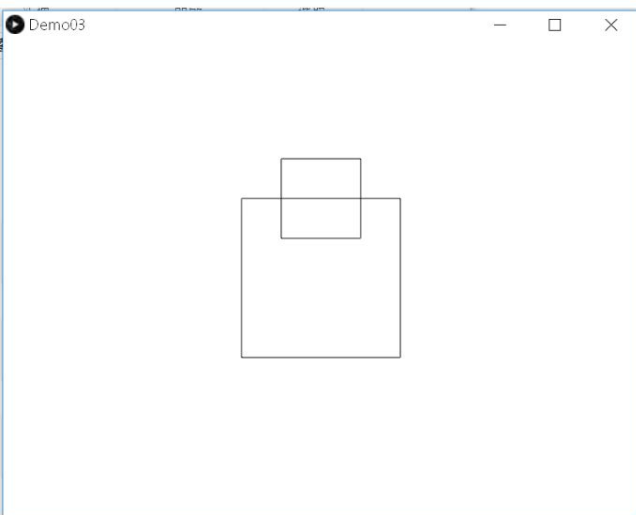
```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=300, R=200, i=4



```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=200, R=100, i=3




```
drawSquare(width/2, height/2, 200, 4);
```



```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

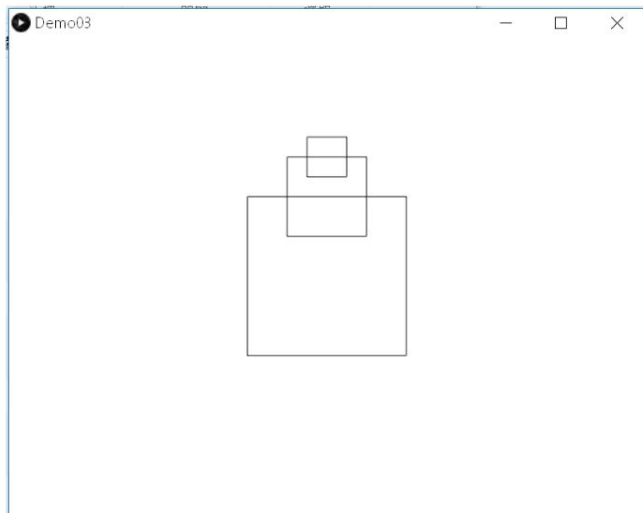
x=400, y=300, R=200, i=4

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=200, R=100, i=3

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=150, R=50, i=2




```
drawSquare(width/2, height/2, 200, 4);
```




```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=300, R=200, i=4




```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=200, R=100, i=3



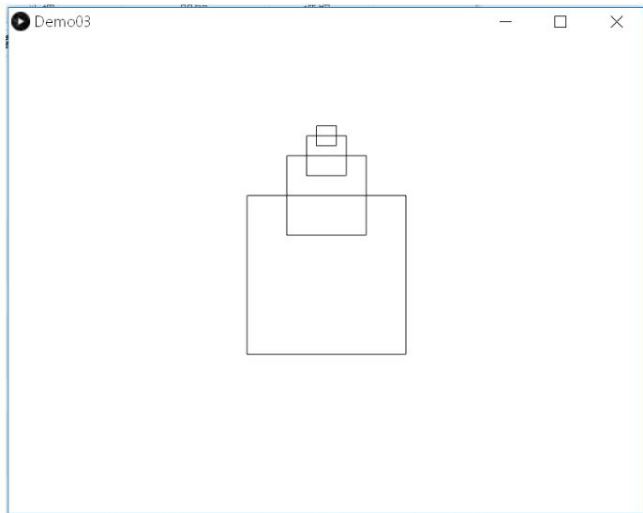
```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=150, R=50, i=2



```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=125, R=25, i=1



```
drawSquare(width/2, height/2, 200, 4);
```



```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=300, R=200, i=4

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=200, R=100, i=3

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

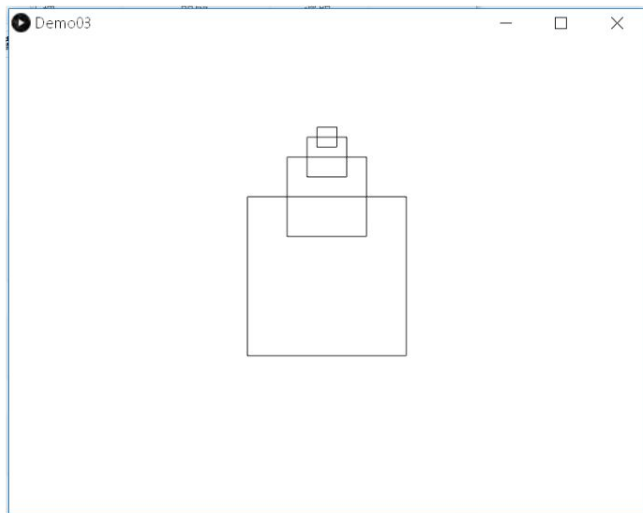
x=400, y=150, R=50, i=2

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=125, R=25, i=1

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=112.5, R=12.5, i=0



```
drawSquare(width/2, height/2, 200, 4);
```



```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=300, R=200, i=4

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=200, R=100, i=3

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

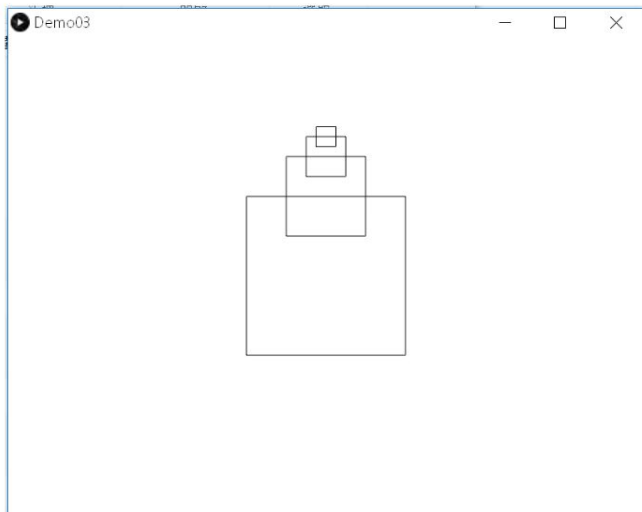
x=400, y=150, R=50, i=2

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=125, R=25, i=1

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=112.5, R=12.5, i=0



```
drawSquare(width/2, height/2, 200, 4);
```



```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=300, R=200, i=4

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

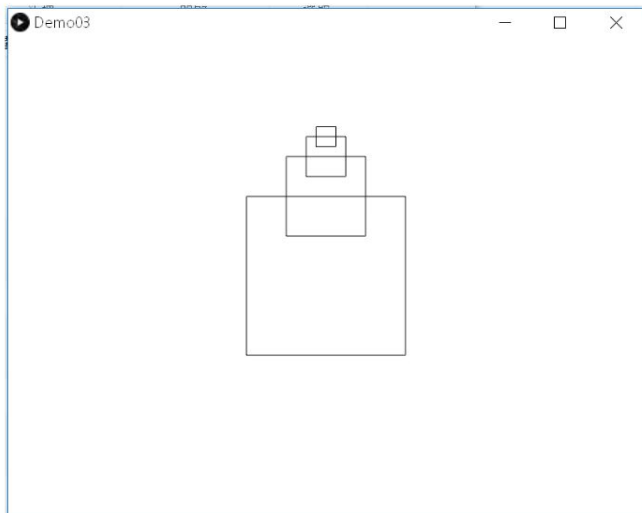
x=400, y=200, R=100, i=3

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=150, R=50, i=2

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=125, R=25, i=1



```
drawSquare(width/2, height/2, 200, 4);
```



```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

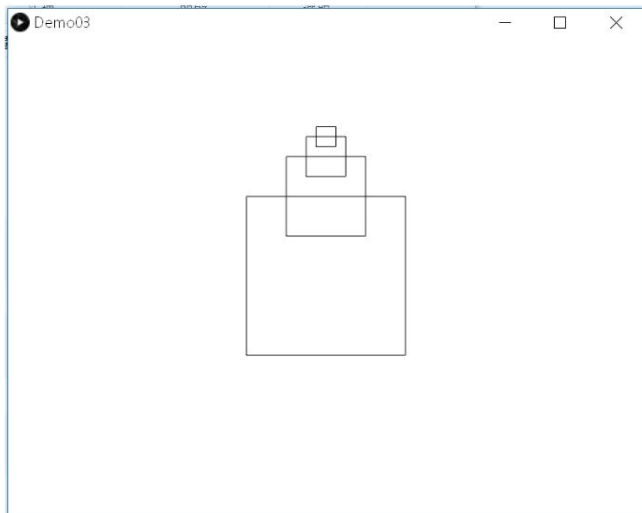
x=400, y=300, R=200, i=4

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=200, R=100, i=3

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=150, R=50, i=2



```
drawSquare(width/2, height/2, 200, 4);
```

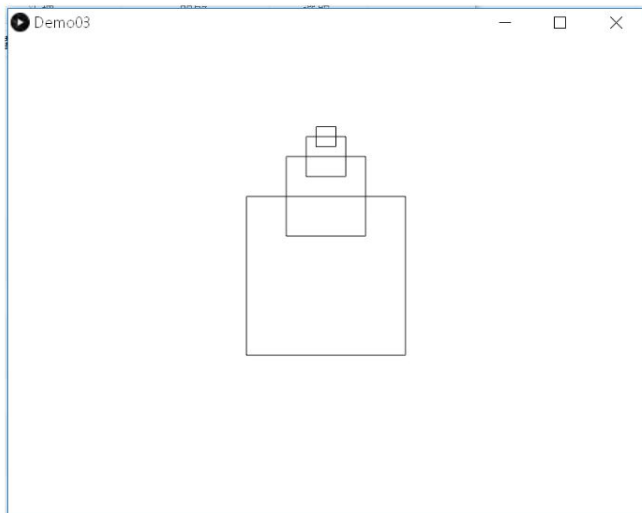


```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=300, R=200, i=4

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R);  
        drawSquare(x, y-R/2, R/2, i-1);  
    }  
}
```

x=400, y=200, R=100, i=3

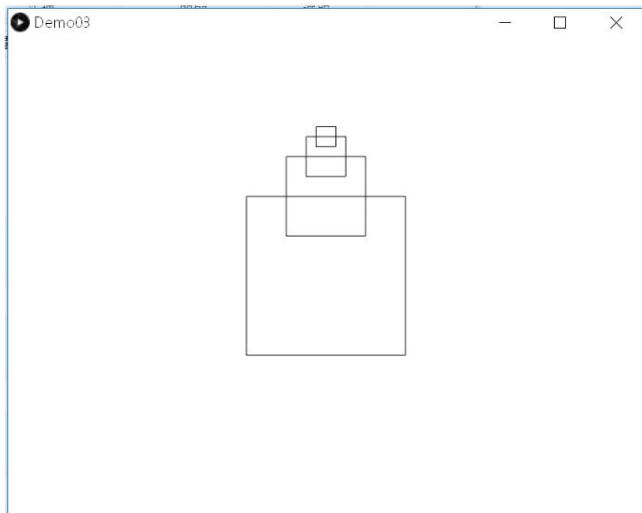


```
drawSquare(width/2, height/2, 200, 4);
```

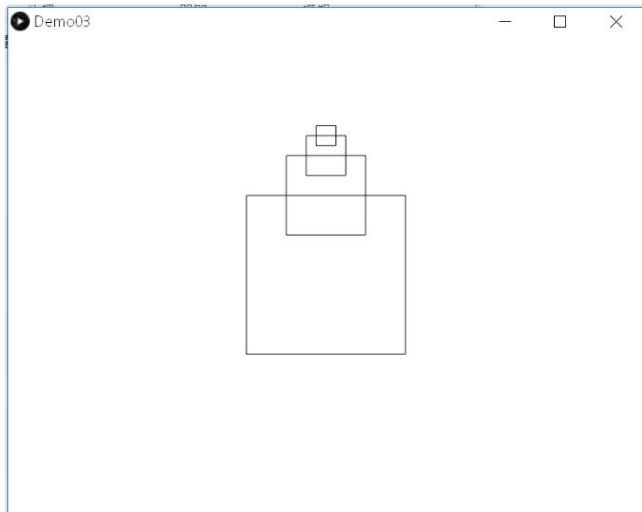


```
void drawSquare(float x, float y, float R, int i) {  
  if (i > 0) {  
    rect(x, y, R, R);  
    drawSquare(x, y-R/2, R/2, i-1);  
  }  
}
```

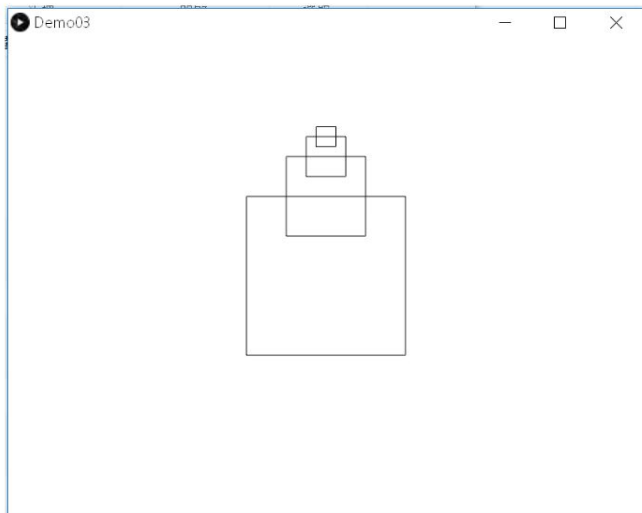
$x=400, y=300, R=200, i=4$




```
drawSquare(width/2, height/2, 200, 4);
```



```
drawSquare(width/2, height/2, 200, 4);
```



```
drawSquare(float x, float y, float R, int i)
```

```
x=400, y=125, R=25, i=1
```

```
drawSquare(float x, float y, float R, int i)
```

```
x=400, y=150, R=50, i=2
```

```
drawSquare(float x, float y, float R, int i)
```

```
x=400, y=200, R=100, i=3
```

```
drawSquare(float x, float y, float R, int i)
```

```
x=400, y=300, R=200, i=4
```

Stack

$n!$

$$n! = n \times (n-1) \times (n-2) \times \dots \times 2 \times 1$$

DEMO 4

CODE

```
void setup() {  
  size(800, 600, P3D);  
  println(factorial(5));  
}
```

```
void draw() {  
  background(255);  
}
```

```
int factorial(int n) {  
  if (n <= 0) {  
    return 1;  
  } else {  
    return n*factorial(n-1);  
  }  
}
```

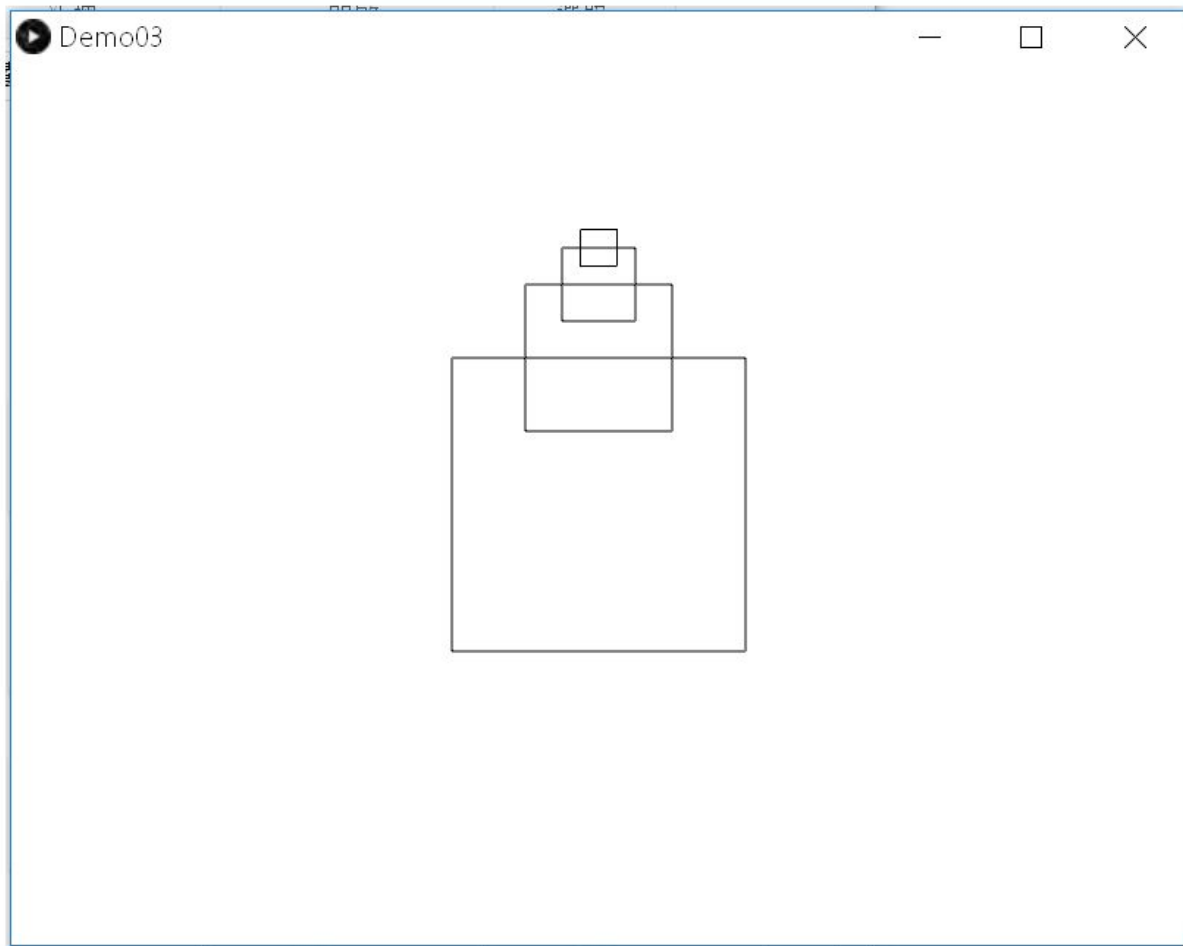
DEMO 5

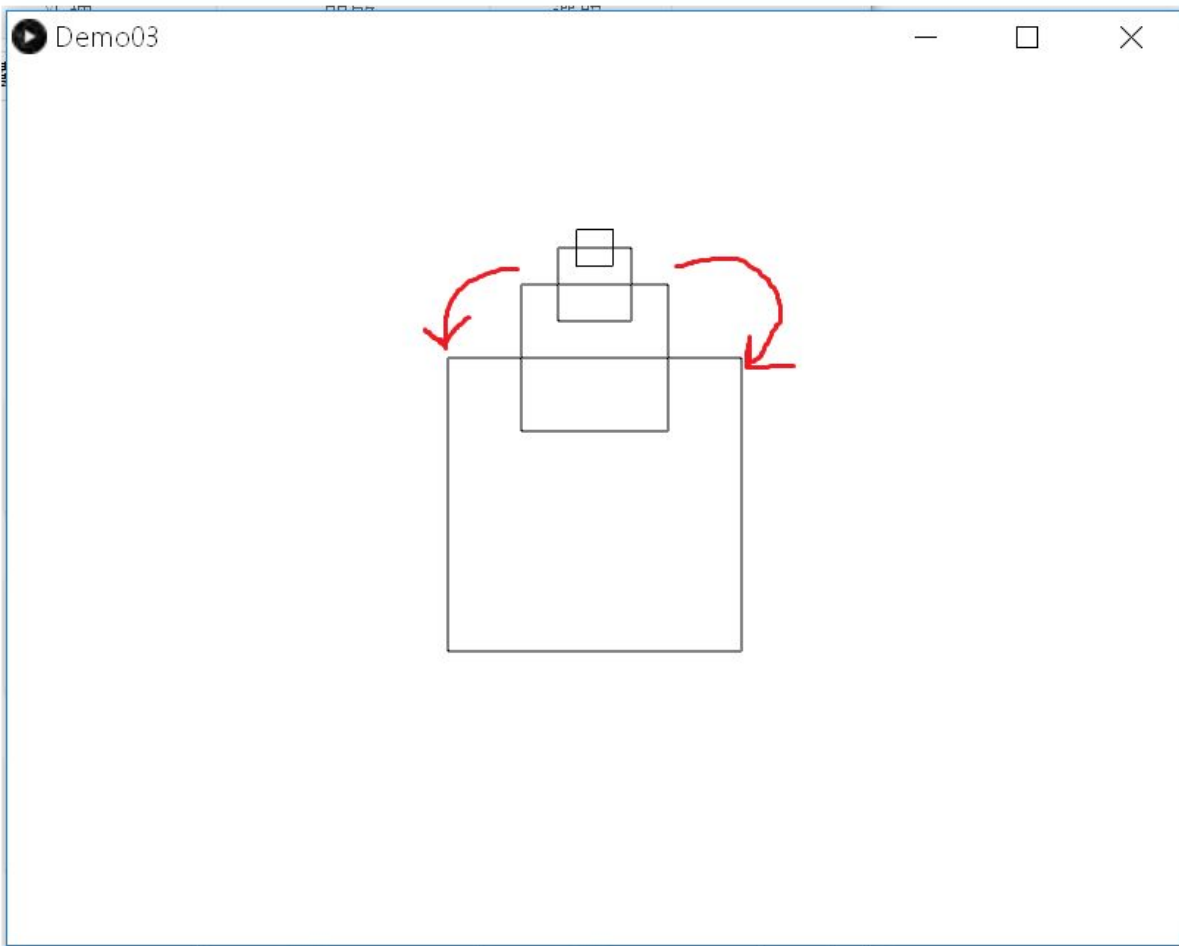
CODE (非遞迴)

```
void setup() {  
  size(800, 600, P3D);  
  println(factorial(5));  
}
```

```
void draw() {  
  background(255);  
}
```

```
int factorial(int n) {  
  int sum = 1;  
  for (int i = n; i >= 1; i--) {  
    sum = sum*i;  
  }  
  return sum;  
}
```



DEMO 6

CODE

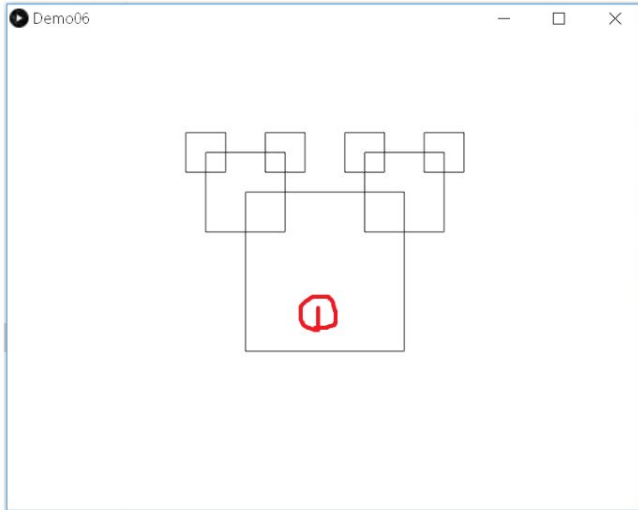
```
void setup() {  
  size(800, 600, P3D);  
  rectMode(CENTER);  
}  
  
void draw() {  
  background(255);  
  drawSquare(width/2, height/2, 200, 3);  
}
```

```
void drawSquare(float x, float y, float R, int i) {  
  if (i > 0) {  
    rect(x, y, R, R);  
    //drawSquare(x, y-R/2, R/2, i-1);  
    drawSquare(x-R/2, y-R/2, R/2, i-1);  
    drawSquare(x+R/2, y-R/2, R/2, i-1);  
  }  
}
```

```
drawSquare(width/2, height/2, 200, 3);
```



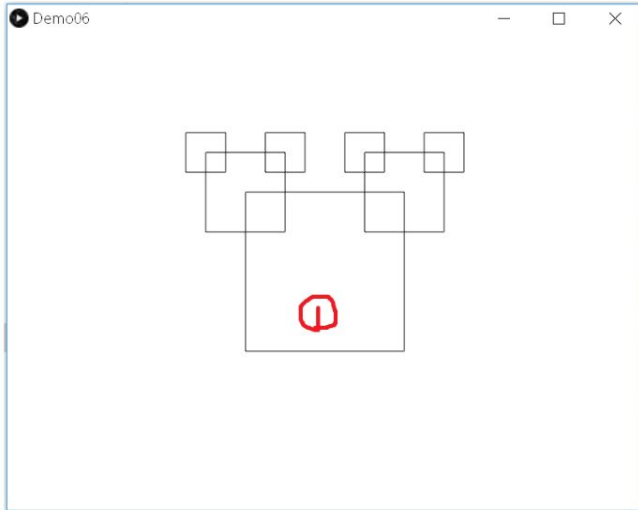
```
void drawSquare(float x, float y, float R, int i) {  
  if (i > 0) {  
    ① rect(x, y, R, R);  
    //drawSquare(x, y-R/2, R/2, i-1);  
    drawSquare(x-R/2, y-R/2, R/2, i-1);  
    drawSquare(x+R/2, y-R/2, R/2, i-1);  
  }  
}
```



```
drawSquare(width/2, height/2, 200, 3);
```



```
void drawSquare(float x, float y, float R, int i) {  
  if (i > 0) {  
    ① rect(x, y, R, R);  
    //drawSquare(x, y-R/2, R/2, i-1);  
    drawSquare(x-R/2, y-R/2, R/2, i-1);  
    drawSquare(x+R/2, y-R/2, R/2, i-1);  
  }  
}
```

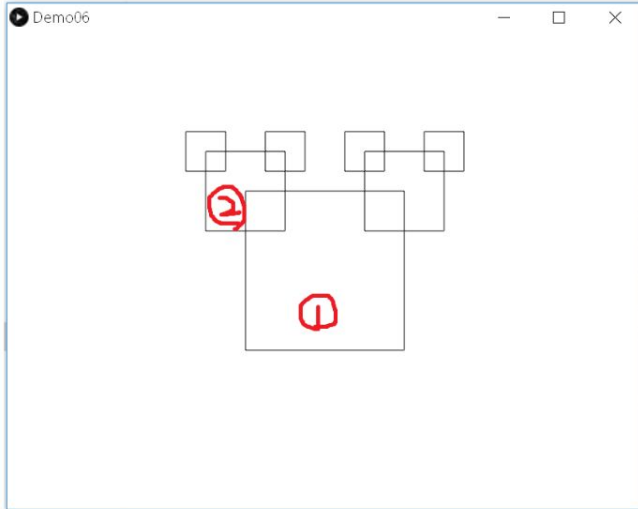


```
drawSquare(width/2, height/2, 200, 3);
```



```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        ① rect(x, y, R, R);  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1);  
        drawSquare(x+R/2, y-R/2, R/2, i-1);  
    }  
}
```

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R); ②  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1);  
        drawSquare(x+R/2, y-R/2, R/2, i-1);  
    }  
}
```

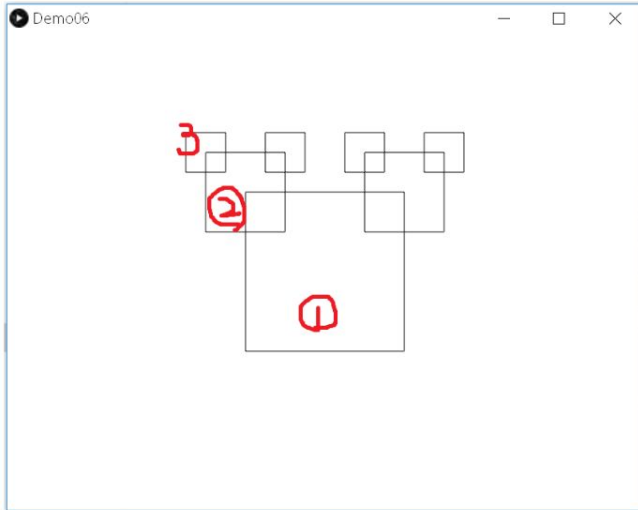


```
drawSquare(width/2, height/2, 200, 3);
```



```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        ① rect(x, y, R, R);  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1);  
        drawSquare(x+R/2, y-R/2, R/2, i-1);  
    }  
}
```

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R); ①  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1); 3  
        drawSquare(x+R/2, y-R/2, R/2, i-1);  
    }  
}
```

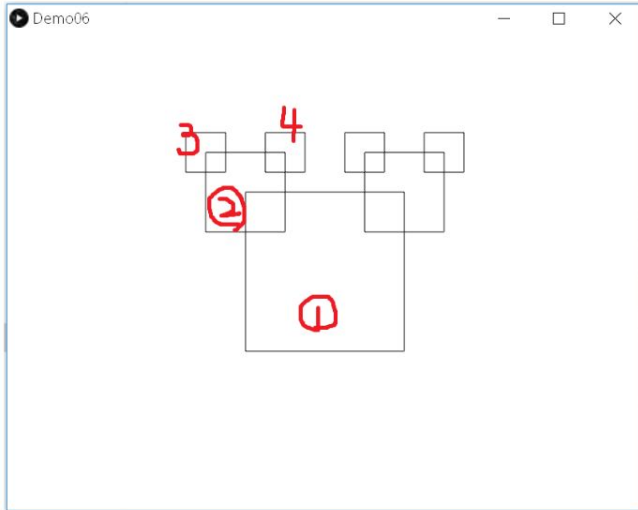



```
drawSquare(width/2, height/2, 200, 3);
```



```
void drawSquare(float x, float y, float R, int i) {  
  if (i > 0) {  
    ① rect(x, y, R, R);  
    //drawSquare(x, y-R/2, R/2, i-1);  
    drawSquare(x-R/2, y-R/2, R/2, i-1);  
    drawSquare(x+R/2, y-R/2, R/2, i-1);  
  }  
}
```

```
void drawSquare(float x, float y, float R, int i) {  
  if (i > 0) {  
    rect(x, y, R, R); ①  
    //drawSquare(x, y-R/2, R/2, i-1);  
    drawSquare(x-R/2, y-R/2, R/2, i-1); 3  
    drawSquare(x+R/2, y-R/2, R/2, i-1); 4  
  }  
}
```



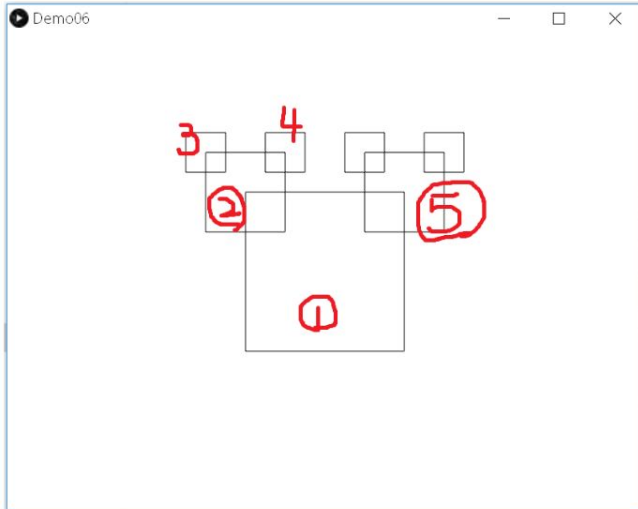
```
drawSquare(width/2, height/2, 200, 3);
```



```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        ① rect(x, y, R, R);  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1);  
        drawSquare(x+R/2, y-R/2, R/2, i-1);  
    }  
}
```

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R); ①  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1); 3  
        drawSquare(x+R/2, y-R/2, R/2, i-1); 4  
    }  
}
```

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R); ⑤  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1);  
        drawSquare(x+R/2, y-R/2, R/2, i-1);  
    }  
}
```



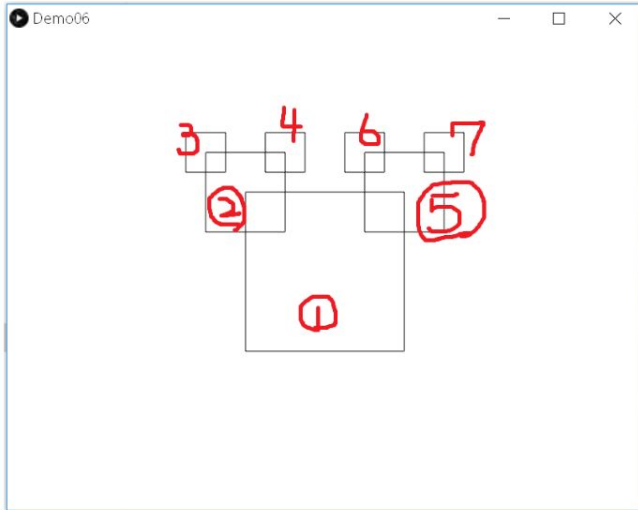
```
drawSquare(width/2, height/2, 200, 3);
```



```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        ① rect(x, y, R, R);  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1);  
        drawSquare(x+R/2, y-R/2, R/2, i-1);  
    }  
}
```

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R); ①  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1); 3  
        drawSquare(x+R/2, y-R/2, R/2, i-1); 4  
    }  
}
```

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R); ⑤  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1); 6  
        drawSquare(x+R/2, y-R/2, R/2, i-1); 7  
    }  
}
```



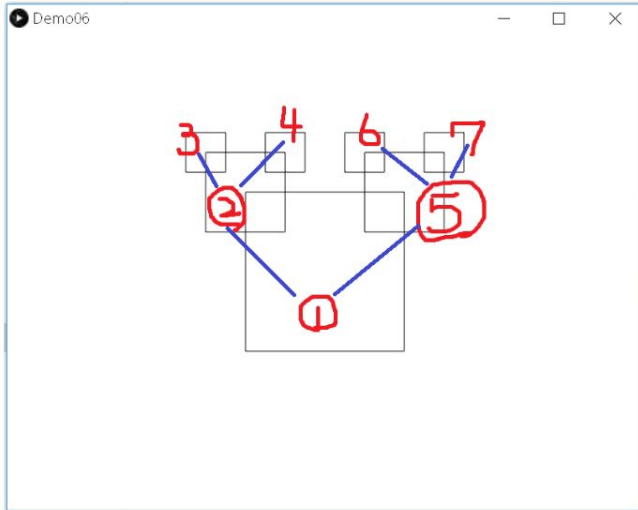
```
drawSquare(width/2, height/2, 200, 3);
```



```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        ① rect(x, y, R, R);  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1);  
        drawSquare(x+R/2, y-R/2, R/2, i-1);  
    }  
}
```

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R); ①  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1); 3  
        drawSquare(x+R/2, y-R/2, R/2, i-1); 4  
    }  
}
```

```
void drawSquare(float x, float y, float R, int i) {  
    if (i > 0) {  
        rect(x, y, R, R); ⑤  
        //drawSquare(x, y-R/2, R/2, i-1);  
        drawSquare(x-R/2, y-R/2, R/2, i-1); 6  
        drawSquare(x+R/2, y-R/2, R/2, i-1); 7  
    }  
}
```



Example->Topics -> Fractals and L-Systems -> Tree