Q1: Suppose we roll a red die and a green die

(i) What is the sample space for this experiment?

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{1,1} {1,2} {1,3} {1,4} {1,5} {1,6} {2,1} {2,2} {2,3} {2,4} {2,5} {2,6} {3,1} {3,2} {3,3} {3,4} {3,5} {3,6} {4,1} {4,2} {4,3} {4,4} {4,5} {4,6} {5,1} {5,2} {5,3} {5,4} {5,5} {5,6} {6,1} {6,2} {6,3} {6,4} {6,5} {6,6}
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(ii) What is the probability that the number on the green die is larger than the number on the red die?

5/12

(iii)Define what it means for two events E and F to be independent.

Two events E and F are independent if the order in which they occur doesn't matter. Alternatively, if observing one doesn't affect the other.

$$P(E \cap F) = P(E)P(F)$$

(iv) Let event E be that the sum of the dice equals 2 or 3 and event F be that the sum equals 3. Are E and F independent? Explain with reference to the definition given above

No, E and F are not independent. Observing E affects the outcome of F. Using the mathematical definition $P(E \cap F) = P(E)P(F)$:

$$P(E \cap F) = 1/36$$
, $P(E)P(F) = 1/12 * 1/18 = 1/216$
Thus, E and F are dependent as $P(E \cap F) != P(E)P(F)$

Q2:

(i) State Bayes Rule

$$P(E|F) = (P(F|E)P(E))/P(F)$$

(ii) Suppose 1% of computers are infected with a virus. There is an imperfect test for detecting the virus. When applied to a computer with the virus the test gives a positive result 90% of the time.

When applied to a computer which does not have the virus, the test gives a negative result 99% of the time. Suppose that the test is positive for a computer. What is the probability that the computer has the virus?

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E = actually has virus, F = test positive for virus P(F|E) = 0.9, P(E)=0.01, P(F) = (0.9*0.01 + 0.01*(1-0.01)) = 0.0189 P(E|F) = (0.9*0.01)/0.0189 = 0.4761904761904762
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