

# Shape Matching and Object Recognition using Low Distortion Correspondences

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## Abstract

*We approach recognition in the framework of deformable shape matching, relying on a new algorithm for finding correspondences between feature points. This algorithm sets up correspondence as an integer quadratic programming problem, where the cost function has terms based on similarity of corresponding geometric blur point descriptors as well as the geometric distortion between pairs of corresponding feature points. The algorithm handles outliers, and thus enables matching of exemplars to query images in the presence of occlusion and clutter. Given the correspondences, we estimate an aligning transform, typically a regularized thin plate spline, resulting in a dense correspondence between the two shapes. Object recognition is then handled in a nearest neighbor framework where the distance between exemplar and query is the matching cost between corresponding points. We show results on two datasets. One is the Caltech 101 dataset (Fei-Fei, Fergus and Perona), an extremely challenging dataset with large intraclass variation. Our approach yields a 48% correct classification rate, compared to Fei-Fei et al's 16%. We also show results for localizing frontal and profile faces that are comparable to special purpose approaches tuned to faces.*

## 1. Introduction

Our thesis is that recognizing object categories, be they fish or bicycles, is fundamentally a problem of deformable shape matching. Back in the 1970s, at least three different research groups working in different communities initiated such an approach: in computer vision, Fischler and Elschlager [10], in statistical image analysis, Grenander ([12] and earlier), and in neural networks, von der Malsburg ([15] and earlier). The core idea that related but not identical shapes can be deformed into alignment using simple coordinate transformations dates even further back, to D'Arcy Thompson, in the 1910's with, *On Growth and Form* [30].

The basic subroutine in deformable matching takes as

input an image with an unknown object (shape) and compares it to a model by: solving the *correspondence problem* between the model and the object, using the correspondences to estimate and perform an *aligning transformation* and computing a *similarity* based on both the aligning transform and the residual difference after applying the aligning transformation. This subroutine can be used for object recognition by using stored exemplars for different object categories as models, possibly with multiple exemplars for different 2D aspects of a 3D object.

Practically speaking, the most difficult step is the *correspondence problem*: how do we algorithmically determine which points on two shapes correspond? The correspondence problem in this setting is more difficult than in the setting of binocular stereopsis, for a number of reasons:

1. Intra-category variation: the aligning transform between instances of a category is not a simple parameterized transform. It is reasonable to assume that the mapping is a smooth, but it may be difficult to characterize by a small number of parameters as in a rigid or affine transform.
2. Occlusion and clutter: while we may assume that the stored prototype shapes are present in a clean, isolated version, the shape that we have to recognize in an image is in the context of multiple other objects, possibly occluding each other.
3. 3D pose changes: since the stored exemplars represent multiple 2D views of a 3D object, we could have variation in image appearance which is purely pose-related, the 3D shapes could be identical

The principal contribution of this paper is a novel algorithm for solving the correspondence problem for shape matching.

We represent shape by a set of points sampled from contours on the shape. Typically 50-100 pixel locations sampled from the output of an edge detector are used; as we use more samples we get better approximations. Note that there is nothing special about these points – they are *not* required to be keypoints such as those found using a Harris/Forstner

type of operator or scale-space extrema of a Laplacian of Gaussian operator, such as used by Lowe [18].

We exploit three kinds of constraints to solve the correspondence problem between shapes:

1. Corresponding points on the two shapes should have similar local descriptors. There are several choices here: SIFT [18], Shape contexts [3], and Geometric blur[4]. We use geometric blur.
2. Minimizing geometric distortion: If  $i$  and  $j$  are points on the model corresponding to  $i'$  and  $j'$  respectively, then the vector from  $i$  to  $j$ ,  $\vec{r}_{ij}$  should be consistent with the vector from  $i'$  to  $j'$ ,  $\vec{r}_{i'j'}$ . If the transformation from one shape to another is a translation accompanied by pure scaling, then these vectors must be scalar multiples. If the transformation is a pure Euclidean motion, then the lengths must be preserved. Etc.
3. Smoothness of the transformation from one shape to the other. This enables us to interpolate the transformation to the entire shape, given just the knowledge of the correspondences for a subset of the sample points. We use regularized thin plate splines to characterize the transformations.

The similarity of point descriptors and the geometric distortion is encoded in a cost function defined over the space of correspondences. We purposely construct this to be an integer quadratic programming problem (cf. Maciel and Costeira [19]) and solve it using fast-approximate techniques.<sup>1</sup>

We address two object recognition problems, multiclass recognition and face detection. In the multiple object class recognition problem, given an image of an object we must identify the class of the object and find a correspondence with an exemplar. We use the Caltech 101 object class dataset consisting of images from 101 classes of objects: from accordion to kangaroo to yin-yang, available at [1]. This dataset includes significant intra class variation, a wide variety of classes, and clutter. On average we achieve **48%** accuracy on object classification with quite good localization on the correctly classified objects. This compares favorably with the state of the art of 16% from [8].

We also consider face detection for large faces, suitable for face recognition experiments. Here the task is to detect and localize a number of faces in an image. The face dataset we use is sampled from the very large dataset used in [5] consisting of news photographs collected from yahoo.com. With only 20 exemplar faces our generic system provides a ROC curve with slightly better generalization, and slightly worse false detection rate than the quite effective specialized face detector of Mikolajczyk [21] used in [5].

<sup>1</sup>It is worth noting that this formulation is amenable to various probabilistic models, maximum likelihood estimation for a product of Gaussians among others, but we do not address this further in this paper.

## 2. Related Work

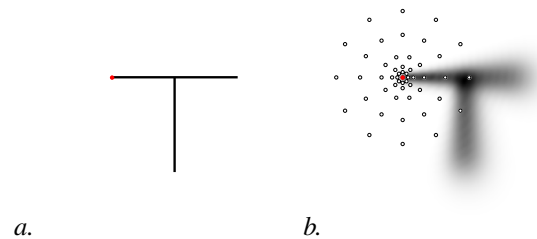
There have been several approaches to shape recognition based on spatial configurations of a small number of keypoints or landmarks. In geometric hashing [16], these configurations are used to vote for a model without explicitly solving for correspondences. Amit et al. [2] train decision trees for recognition by learning discriminative spatial configurations of keypoints. Leung et al. [17], Schmid and Mohr [27], and Lowe [18] additionally use gray level information at the keypoints to provide greater discriminative power. Lowe's SIFT descriptor has been shown in various studies e.g. [22] to perform very well particularly at tasks where one is looking for identical point features. Recent work extends this approach to category recognition [9, 7, 8], and to three-dimensional objects[26].

It should be noted that not all objects have distinguished key points (think of a circle for instance), and using key points alone sacrifices the shape information available in smooth portions of object contours. Approaches based on extracting edge points are, in our opinion, more universally applicable. Huttenlocher et al. developed methods based on the Hausdorff distance [14]. A drawback for our purposes is that the method does not return correspondences. Methods based on Distance Transforms, such as [11], are similar in spirit and behavior in practice. Work based on shape contexts is indeed aimed at first finding correspondences [3, 23] and is close to the spirit of this work. Another approach is the non-rigid point matching of [6] based on thin plate splines and "softassign".

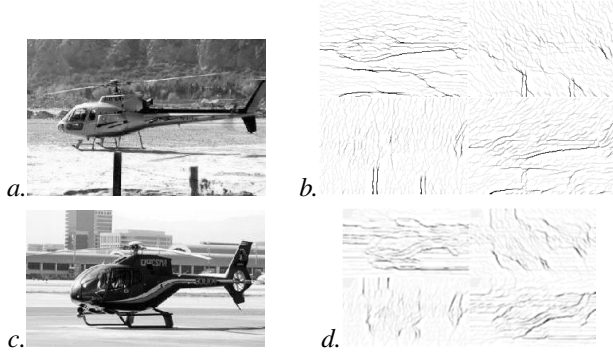
One can do without extracting either keypoints or edge points: Ullman et al propose using intermediate complexity features, a collection of image patches,[32].

For faces and cars the class specific detectors of [33, 29, 28] have been very successful. These techniques use simple local features, roughly based on image gradients, and a cascade of classifiers for efficiency. Recent work on sharing features [31] has extended this to multiclass problems.

## 3. Geometric Blur Descriptor



**Figure 1.** A sparse signal  $S$  (a.) and the geometric blur of  $S$  around the feature point marked in red (b.) We only sample the geometric blur of a signal at small number of locations  $\{s_i\}$ , indicated in (b.)



**Figure 2.** Two images (a. and c.) and four oriented edge channels derived from the images using the boundary detector of [20] (b. and d. respectively). A feature point descriptor is the concatenation of the subsampled geometric blur descriptor at the feature point for each of the channels.

We use features based on a subsampled version of the geometric blur descriptor of [4]. This descriptor is a smoothed version of the signal around a feature point, blurred by a spatially varying kernel. The objective is to provide discriminative information by using an extended patch of signal, while providing robustness to geometric distortion. There are two design choices when using geometric blur descriptors: the signal, and the blur. The signal should be sparse and indicate the presence of some interesting feature such as an edge in the image. The blur is determined by the nature of geometric distortion expected.

The experiments in this paper use one of two types of sparse channels from which to compute geometric blur descriptors: the oriented boundary detector output of [20] or oriented edge energy computed using quadrature pairs, following [24]. See Figure 2 for an example of the former. In each case the edge detector is used to produce four channels of oriented edge responses.

Throughout we use a spatially varying Gaussian kernel to compute geometric blur. Given one of the oriented channels discussed above as the signal,  $S$ , we compute blurred versions,  $S_d = S * G_d$ , by convolving with a Gaussian of standard deviation  $d$ . The geometric blur descriptor around location  $x_0$  is then

$$B_{x_0}(x) = S_{\alpha|x|+\beta}(x_0 - x) \quad (1)$$

Where  $\alpha$  and  $\beta$  are constants that determine the amount of blur. The intuition is that under an affine transform that fixes a feature point, the distance a piece of the signal moves is linearly proportional to the distance that piece was from the feature point.

In practice the geometric blur of a signal is usually rather smooth far from a feature point, we take advantage of this by subsampling the geometric blur, as shown in figure 1. We sample  $B_{x_0}(x)$  at a sparse set of points  $x = s_i$  as shown in figure 1, so we need only compute  $S_d$  for a few distinct val-

ues of  $d = \alpha|s_i| + \beta$ . Since the Gaussian is a separable kernel and we can subsample the signal for larger standard deviations, extracting geometric blur descriptors is quite fast, taking less than a second per image in our experiments.

The feature descriptor at a point is the concatenation of the subsampled geometric blur descriptor computed at that point in each of the channels. We compare geometric blur descriptors using ( $L_2$ ) normalized correlation.

## 4. Geometric Distortion Costs

We consider correspondences between feature points  $\{p_i\}$  in model image  $P$  and  $\{q_j\}$  in image  $Q$ . A correspondence is a mapping  $\sigma$  indicating that  $p_i$  corresponds to  $q_{\sigma(i)}$ . To reduce notational clutter we will sometimes abbreviate  $\sigma(i)$  as  $i'$ , so  $\sigma$  maps  $p_i$  to  $q_{i'}$ .

The quality of a correspondence is measured in two ways: how similar feature points are to their corresponding feature points, and how much the spatial arrangement of the feature points is changed. We refer to the former as the match quality, and the latter as the distortion of a correspondence.

We express the problem of finding a good correspondence as minimization of a cost function defined over correspondences. This cost function has a term for the match quality and for the geometric distortion of a correspondence:  $\text{cost}(\sigma) = \omega_m C_{\text{match}}(\sigma) + \omega_d C_{\text{distortion}}(\sigma)$

Where constants  $\omega_m$  and  $\omega_d$  weigh the two terms. The match cost for a correspondence is:

$$C_{\text{match}}(\sigma) = \sum_i c(i, i') \quad (2)$$

Where  $c(i, j)$  is the cost of matching  $i$  to  $j$  in a correspondence. We use the negative of the correlation between the feature descriptors at  $i$  and  $j$  as  $c(i, j)$ .

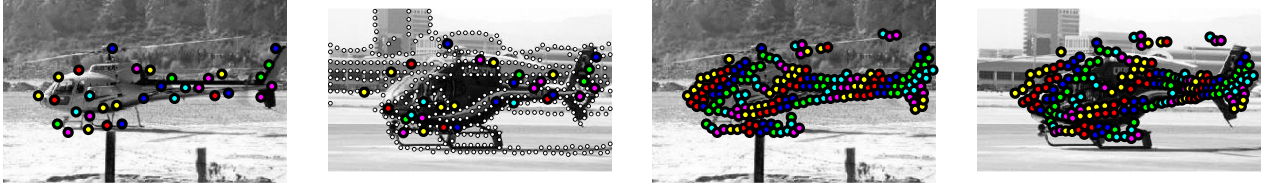
We use a distortion measure computed over pairs of model points in an image. This will allow the cost minimization to be expressed as an integer quadratic programming problem.

$$C_{\text{distortion}}(\sigma) = \sum_{ij} H(i, i', j, j') \quad (3)$$

Where  $H(i, j, k, l)$  is the distortion cost of mapping model points  $i$  and  $j$  to  $k$  and  $l$  respectively. While there are a wide variety of possible distortion measures, including the possibility of using point descriptors and other features, in addition to location, we concentrate on geometric distortion and restrict ourselves to measures based on the two offset vectors  $r_{ij} = p_j - p_i$  and  $s_{i'j'} = q_{j'} - q_{i'}$ .

$$C_{\text{distortion}}(\sigma) = \sum_{ij} \text{distortion}(r_{ij}, s_{i'j'})$$

Our distortion cost is made up of two components:



**Figure 3.** An exemplar with a subset of feature points marked (left), the novel “probe” image with all feature points in white, and the feature points found to correspond with the exemplar feature points marked in corresponding colors (left center), the exemplar with all its feature points marked in color, coded by location in the image (right center), and the probe with the exemplar feature points mapped by a thin plate spline transform based on the correspondences, again colored by position in the exemplar (far right). See Figure 7 for more examples

$$C_{\text{distortion}}(\sigma) = \sum_{ij} \gamma d_a(\sigma) + (1 - \gamma) d_l(\sigma) \quad (4)$$

$$d_a(\sigma) = \left( \frac{\alpha_d}{|r_{ij}|} + \beta_d \right) \left| \arcsin \left( \frac{s_{i'j'} \times r_{ij}}{|s_{i'j'}| |r_{ij}|} \right) \right| \quad (5)$$

$$d_l(\sigma) = \frac{|s_{i'j'}| - |r_{ij}|}{(|r_{ij}| + \mu_d)} \quad (6)$$

where  $d_a$  penalizes the change in direction, and  $d_l$  penalizes change in length. A correspondence  $\sigma$  resulting from pure scale and translation will result in  $d_a(\sigma) = 0$ , while  $\sigma$  resulting from pure translation and rotation will result in  $d_l(\sigma) = 0$ . The constants  $\alpha_d, \beta_d, \mu_d$ , are all terms allowing slightly more flexibility for nearby points in order to deal with local “noise” factors such as sampling, localization, etc. They should be set relative to the scale of these local phenomena. The constant  $\gamma$  weighs the angle distortion term against the length distortion term.

**Outliers** Each point  $p_i$ , in  $P$ , is mapped to a  $q_{\sigma(i)}$ , in  $Q$ . This mapping automatically allows outliers in  $Q$  as it is not necessarily surjective – points  $q_j$  may not be the image any point  $p_i$  under  $\sigma$ . We introduce an additional point  $q_{\text{null}}$  and use  $\sigma(i) = \text{null}$  to allow a point  $p_i$  to be an outlier. We limit the number of points  $p_i$  which can be assigned to  $q_{\text{null}}$ , thus allowing for outliers in both  $P$  and  $Q$ .

## 5. Correspondence Algorithm

Finding an assignment to minimize a cost function described by the terms in Equations 3 and 2 above can be written as an Integer Quadratic Programming (IQP) problem.

$$\text{cost}(x) = \sum_{a,b} H(a,b) x_a x_b + \sum_a c(a) x_a \quad (7)$$

Where the binary indicator variable  $x$  has entries  $x_a$ , that if 1, indicate  $\sigma(a_i) = a_j$ . We then have  $H(a,b) = H(a_i, a_j, b_i, b_j)$ , and  $c(a) = c(a_i, a_j)$  from Equations 3 and 2.

We constrain  $x$  to represent an assignment. Write  $x_{ij}$  in place of  $x_{a_i a_j}$ . We require  $\sum_j x_{ij} = 1$  for each  $i$ . Furthermore if we allow outliers as discussed in Section 4, then we

require  $\sum_i x_{i\text{null}} \leq k$ , where  $k$  is the maximum number of outliers allowed. Using outliers does not increase the cost in our problems, so this is equivalent to  $\sum_i x_{i\text{null}} = k$ . Each of these linear constraints are encoded in one row of  $A$  and an entry of  $b$ . Replacing  $H$  with a matrix having entries  $H_{ab} = H(a,b)$  and  $c$  with a vector having entries  $c_a = c(a)$ . We can now write the IQP in matrix form:

$$\begin{aligned} \min \text{cost}(x) &= x' H x + c' x \quad \text{subject to,} \\ A x &= b, \quad x \in \{0, 1\}^n \end{aligned} \quad (8)$$

### 5.1. Approximation

Integer Quadratic Programming is NP-Complete, however specific instances may be easy to solve. We follow a two step process that results in good solutions to our problem. We first find the minimum of a linear bounding problem, an approximation to the quadratic problem, then follow local gradient descent to find a locally minimal assignment. Although we do not necessarily find global minima of the cost function in practice the results are quite good.

We define a linear objective function over assignments that is a lower bound for our cost function in two steps. First compute  $q_a = \min_b \sum_b H_{ab} x_b$ . Note that from here on we will omit writing the constraints  $Ax = b$  and  $x \in \{0, 1\}^n$  for brevity.

If  $x_a$  represents  $\sigma(i) = j$  then  $q_a$  is a lower bound for the cost contributed to any assignment by using  $\sigma(i) = j$ . Now we have  $L(x) = \sum_a (q_a + c_a) x_a$  as a lower bound for  $\text{cost}(x)$  from Equation 8. This construction follows [19], and is a standard bound for a quadratic program. Of note is the operational similarity to geometric hashing.

The equations for  $q_a$  and  $L$  are both integer linear programming problems, but since the vertices of the constraint polytopes lie only on integer coordinates, they can be relaxed to linear programming problems without changing the optima, and solved easily. In fact due to the structure of the problems in our setup they can be solved explicitly by construction. If  $n$  is the length of  $x$ , each problem takes  $O(n)$  operations with a very small constant. Computing  $q_a$  for  $a = 1 \dots n$  requires  $O(n^2)$  time.

We then perform gradient descent changing up to two elements of the assignment at each step. This takes  $O(n^2)$  operations per step, and usually requires a very small number of steps (we put an upper bound on the number of steps). In practice we can solve problems with  $m = 50$  and  $n = 2550$ , 50 possible matches for each of 50 model points with outliers, in less than 5 seconds.

## 6. Correspondence results

Given a model image  $P$  of an object, and a target image  $Q$ , possibly containing an instance of a similar object we find a correspondence between the images as follows:

1. Extract sparse oriented edge maps from each image.
2. Compute features based on geometric blur descriptors at locations with high edge energy.
3. Allow each of  $m$  feature points from  $P$  to potentially match any of the  $k$  most similar points in  $Q$  based on feature similarity and or proximity.
4. Construct cost matrices  $H$  and  $c$  as in Section 4.
5. Approximate the resulting Binary Quadratic Optimization to obtain a correspondence. Store the cost of the correspondence as well.
6. Extend the correspondence on  $m$  points to a smooth map using a regularized thin plate spline [25].

See Figures 3 and 7 for a number of examples. In the left-most column of the figures is the image,  $P$ , shown with  $m$  points marked in color. In the middle left column is the target image  $Q$  with the corresponding points found using our algorithm. A regularized thin plate spline is fit to this correspondence to map the full set of feature points on the object in  $P$ , shown in the middle right column, to the target, as shown on the far right column. Corresponding points are colored the same and points are colored based on their position (or corresponding position) in  $P$  – in  $P$  colors are assigned in uniform diagonal stripes, the distortion of these striped in the far right column of the figure gives some idea of the distortion in the correspondence.

## 7. Recognition Experiments

Our recognition framework is based on nearest neighbors.

*Preprocessing:* For each object class we store a number of exemplars, possibly replicated at multiple scales, and compute features for all of the exemplars.

*Indexing:* Extract features from a query image. For each feature point in an exemplar, find the best matching feature point in the query based on normalized correlation of the geometric blur descriptors. The mean of these best correlations is the similarity of the exemplar to the query. We

form a shortlist of the exemplars with highest similarity to the query image.

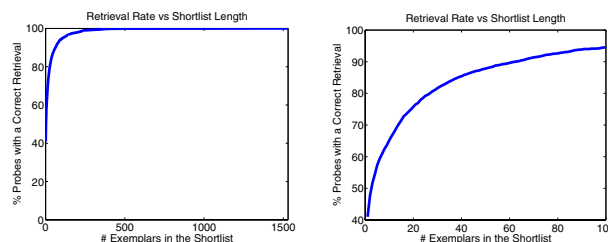
*Correspondence:* Find a correspondence from each exemplar in the shortlist to the query as described above. Pick the exemplar with the least cost.

We apply our technique to two different data sets, the Caltech set of 101 object categories (available here [1]) and a collection of news photographs containing faces gathered from yahoo.com (provided by the authors of [5]). In the experiments that follow, we utilize the same parameters for both datasets except for those specifically mentioned.

For all images edges are extracted at four orientations and a fixed scale. For the Caltech dataset where significant texture and clutter are present, we use the boundary detector of [20] at a scale of 2% of the image diagonal. With the face dataset, a quadrature pair of even and odd symmetric gaussian derivatives suffices. We use a scale of  $\sigma = 2$  pixels and elongate the filter by a factor of 4 in the direction of the putative edge orientation.

Geometric blur features are computed at 400 points sampled randomly on the image with the blur pattern shown in Figure 1. We use a maximum radius of 50 pixels (40 for faces), and blur parameters  $\alpha = 0.5$  and  $\beta = 1$ .

For correspondence we use 50 (40 for faces) points, sampled randomly on edge points, in the correspondence problem. Each point is allowed to match to any of the most similar 40 points on the query image based on feature similarity. In addition for the caltech 101 dataset we use  $\gamma = 0.9$  allowing correspondences with significant variation in scale, while for the faces dataset we handle scale variation partly by repeating exemplars at multiple scales and use  $\gamma = 0.5$ .



**Figure 4.** For a probe or query image exemplars are ranked according to feature similarity. We plot the percentage of probes for which an exemplar of the correct class was found in the shortlist. Here the first exemplar is correct 41% of the time. **Left** Full curve. **Right** Curve up to shortlist length 100 for detail.

## 8. Caltech 101 Results

**Basic Setup:** Fifteen exemplars were chosen randomly from each of the 101 object classes and the background class, yielding a total 1530 exemplars. For each class, we select up to 50 testing images, or “probes” excluding those used as exemplars. Results for each class are weighted evenly so there is no bias toward classes with more images.



The spatial support of the objects in exemplars is acquired from human labeling. The top entry in the shortlist is correct 41% of the time. One of the top 20 entries is correct 75% of the time. (Figure 4).<sup>2</sup>

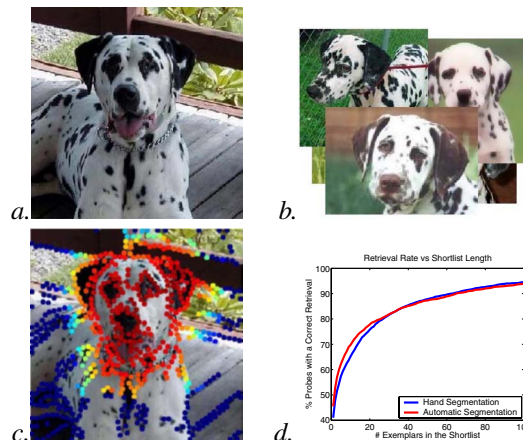
**Recognition and localization:** Using each of the top ten exemplars from the shortlist we find a good correspondence in the probe image. We do this by first sampling 50 locations on the exemplar object and allowing each to be matched to its 50 best matching possibilities in the probe with up to 15% outliers. This results in a quadratic programming problem of dimension 2550. We use a distortion cost based mainly on the change in angle of edges between vertices ( $\gamma = 0.9$ ). This allows matches with relatively different scales (Figure 7 line 3). The exemplar with the lowest distortion correspondence gives **48%** correct classification, at the same time providing localization. A baseline experiment comparing grayscale images using SSD and 1-nearest neighbor classification gives 16%. At press, results from the Caltech group are 27% using discriminative methods [13].

**Multiscale:** We compute exemplar edge responses and features at a second scale for each exemplar resulting in twice as many exemplars. This improves shortlist performance by 1% or less, and does not change recognition performance. This illustrates the lack of scale variation in Caltech 101. The face dataset exhibits a large range of scale variation.

## 9. Face Detection Results

We apply the same technique to detecting medium to large scale faces for possible use in face recognition experiments. The face dataset is sampled from the very large dataset in [5] consisting of A.P. news photographs. A set of 20 exemplar faces split between front, left, and right facing, was chosen from the database by hand, but without care. The test set was selected randomly from the remaining images on which the face detector of [21] found at least one  $86 \times 86$  pixels or larger face. We use the generic object recognition framework described above, but after finding the lowest cost correspondence we continue to look for others. A comparison of the ROC curves for our detector and that of [21] is found in Figure 6. Our detector has an advantage in generalization, while producing more false positives. While not up to the level of specialized face detectors, these are remarkably good results for a face detector using 20 exemplars and a generative model for classification, without any negative training examples.

<sup>2</sup>We note that these results are on the Caltech 101 dataset as presented in 8, which contains some duplicates. Using the currently available dataset [1] which has no duplicates the performance drops by approximately 3% across all experiments, in this case to 38% and 72% respectively. For the recognition results using correspondence performance drops from 48% with duplicates to 45% without duplicates.



**Figure 5.** Illustrating automatic model segmentation: One training image (a.) the remaining 14 training images (b.) colors indicate how well on average feature points match after aligning transforms to each of the other training images (c.) At lower right, the percentage of probes for which an exemplar of the correct class was found in the shortlist. The blue curve shows performance with hand segmented exemplars, the red curve shows performance with automatically segmented exemplars. For hand segmented exemplars the first exemplar is correct 41% of the time, for automatically segmented exemplars 45%. (d.)

## 10. Automatic Model Building

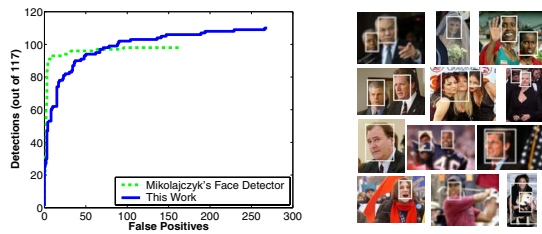
In the recognition experiments above, exemplar objects were hand segmented from their backgrounds. We now show how this can be automated by finding the repetitive aspects of objects in the example images. Ideally this would be computed for all images simultaneously. We show that in many cases it is sufficient to find the similar parts in pairs of images independently.

Starting with a set of example images  $\{I_i\}$  from an object class find the support of the object in an image  $I_{i_0}$  as follows. **1)** For each image  $I_j$  where  $j \neq i_0$ : **1)** find a correspondence from  $I_{i_0}$  to  $I_j$ .<sup>3</sup> **2)** Use a regularized thin plate spline to map all of the feature points in  $I_{i_0}$  to  $I_j$ . **3)** For each mapped feature from  $I_{i_0}$ , the quality of the match is the similarity to the best matching nearby feature in  $I_j$ . The median quality of match for a feature is the measure of how common that feature is in the training images.

Feature points with median quality within 90% of the best for that image are considered part of the object. Repeating the recognition experiments in Section 8, the shortlist accuracy improves by 1-4% (Fig. 5). While the estimated support is usually not perfect, recognition performance is similar to that using hand segmented images, 48%.

The learned models of support reflect a region of the image that is consistent across training images, as opposed to

<sup>3</sup>Here we allow 40% outliers instead of 15% as used in the recognition experiments.



**Figure 6.** Left ROC curves for our face detector using 20 exemplar images of faces (split between frontal and profile) and the detector of Mikolajczyk [21] (similar to [29]) evaluated on a dataset of ap news photos. Mikolajczyk's detector has proven to be effective on this dataset [5]. Our detector works by simply finding sets of feature points in an image that have a good correspondence, based on distortion cost, to an exemplar. Good correspondences allow detection and localization of faces using a simple generative model, no negative examples were used. Right Detections from our face detector marked with rectangles.

individual discriminative features. For instance the cheek on a face is not by itself discriminative for faces, but when considering faces transformed into alignment the cheek is usually consistent. More at [www.cs.berkeley.edu/~aberg](http://www.cs.berkeley.edu/~aberg)

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**Figure 7.** Each row shows a correspondence found using our technique described in section 5. Leftmost is an exemplar with some feature points marked. Left center is a probe image with the correspondences found indicated by matching colors (all possible feature matches are shown with white dots). All of the feature points on the exemplar are shown center right, and their image using a thin plate spline warp based on the correspondence are shown in the right most image of the probe. Note the ability to deal with clutter (1,6), scale variation(3), intraclass variation all, also the whimsical shape matching (2), and the semiotic difficulty of matching a bank note to the image of a bank note painted on another object (5).