

長庚大學期中、期末考試答案用紙

學年度 第 _____ 學期 _____ 考 試 系 姓名 楊千峰 學號 130729021

[1] a. 虛無假設 $\mu \geq 70$

$$\text{樣本定點估計量 } Z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}} = \frac{73 - 70}{8/\sqrt{5}} = \frac{15}{8} = 1.875$$

拒絕區 (臨界值) $R = \{Z > 1.645\}$ $\because 1.875 > 1.645, \therefore$ 拒絕 H_0 b. 虛無假設 $\mu \geq 70$

$$\text{樣本定點估計量 } Z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}} = \frac{73 - 70}{9/\sqrt{5}} = \frac{15}{9} = 1.6667$$

拒絕區 (臨界值) $R = \{Z > 1.645\}$ $\because 1.6667 > 1.645, \therefore$ 拒絕 H_0 [2] a. $E(\hat{p}) = E\left(\frac{X}{n}\right) = \frac{1}{n} E(X) = \frac{1}{n} n \cdot p = p$

$$b. \text{Var}(\hat{p}) = \text{Var}\left(\frac{X}{n}\right) = \frac{1}{n^2} \text{Var}(X) = \frac{1}{n^2} \cdot n \cdot p \cdot q = \frac{1}{n} p \cdot q = \frac{p \cdot q}{100} = \frac{p(1-p)}{100}$$

$$\text{std}(\hat{p}) = \sqrt{\frac{p \cdot q}{100}}$$

c. $\hat{p} = 0.6$

$$0.6 - 1.96 \cdot \sqrt{\frac{0.6 \times 0.4}{100}} = 0.6 - 1.96 \times \frac{2\sqrt{6}}{100} = 0.6 - 1.96 \times \frac{4.89}{100} = 0.504$$

$$0.6 + 1.96 \cdot \sqrt{\frac{0.6 \times 0.4}{100}} = 0.6 + 0.09584 = 0.69584$$

信心區間為 $[0.504, 0.69584]$ d. 信心區間為 $[0.051942, 0.68058]$ [3] a. $P(X=66) = \frac{0.6}{0.66} = \frac{60}{66} = 0.9091$

$$b. P(X \geq 66) = 1 - \text{norm.cdf}(0.66, 0, 1) = 0.25462$$

c.

d. 不拒絕 H_0

(請翻面繼續作答)