Exam 1 Notes Name: Cooper Morris

## C1S1:

**Population:** the entire set of all potential measurement

Sample: any subset of a population

Simple Random Sample: A sample of size n taken in such a way that any group of size n has the same chance of being selected

Sampling Variability: different samples from the same population can lead to differences

Stratified Random Sampling: the population is broken into groups based off a characteristic. Then a SRS is taken from each group

Cluster Sampling: target population has many groups, groups are selected by SRS of the groups. All elements of each group are selected

Systematic Sample: A listing is generated over time, every  $k^{\text{th}}$  member is included in the sample.

**Tangible Population:** A population composed of members/individuals that exist.

Conceptual Population: A population composed of all values that can potentially be observed. They do not necessarily exist at any point in time. Observations: The measurement, or set of measurements recorded from any individual in a sample.

Variables: The characteristics being observed from individuals.

Quanitative Variables: Possible values that represent quantiles of something. Numbers of things. Ratio Variables: Inherent zero value and ratios between values make sense.

Interval Variables: No meaningful ratios and arbitrary zero

Qualitative: A variable that takes a category of possible values.

**Nominal:** Ordering of categories makes sense.

Ordinal: No inherent ranking in categories.

**Observational Study:** Observe a sample from a population with minimal interaction.

**Experimental Study:** A study performed where

the environment of subjects is strictly controlled.

Response Variable(s): The variable(s) of interest in a study.

**Explanatory Variable:** Variables to explain changes in the response variable.

Confounding Variable(s): Variables unaccounted for i a study that may explain changes in the response variable.

## C1S2:

Measures of Central Tendency: Values that represent where the "center" of a dataset is located. Measures of Variability: Values that indicate how spread out the data are.

Mode: The measurement that occurs most often. Median: The middle value in an ordered set.

**Mean:** The sum of all measurements divided by the total number of measurements.

p% Trimmed Mean: The p% lowest values and p% of the highest values are removed from data, mean is taken.

**p**<sup>th</sup> **percentile:** Value such that p% of observations are at or below and (100-p)% are above.

Range: difference between largest and smallest data points.

More <u>relative</u> variation is higher CV, less <u>relative</u> variation is lower CV.

## C1S3:

**Histogram:** Number of classes should be smallest whole number K that makes  $2^K \ge \text{number of measurements}$ . For large data sets either  $\log_2(n)$  or  $2n^{1/3}$ 

Unimodal: One major peak Bimodal: Two major peaks Symmetric: Symmetric

**Right Skewed:** Long right tail, short left tail **Boxplots:** Outliers are outside  $1.5 \times IQR$ . Box goes from  $Q_1$  to  $Q_3$ , horizontal line at median, whiskers to largest data point inside  $1.5 \times IQR$ , X's for outliers

## C2S1:

**Probability:** the chance that something happens. Experiment: A process with an uncertain outcome

Sample Space (S): The set of all possible outcomes in an experiment.

Outcome: Each individual and non-reducible element of a sample space

**Event:** A set of 1 or more outcomes

**Union:** For events A and B the union is all outcomes in A, B, or Both.  $A \cup B$ 

**Intersection:** The set of outcomes that are in both A and B.  $A \cap B$ 

**Complement:** The set of outcomes in the sample space not in A.  $A^C$ 

Mutually Exclusive Events: Events that share no outcomes in common.

C2S2:

Sample Mean:  $\bar{y} = \frac{\sum_{i=1}^{n} y_i}{n}$ First Quartile:  $Q_1 = y_{25\%}$ Second Quartile:  $Q_2 = \text{median}$ Third Quartile:  $Q_3 = y_{75\%}$ 

Interquartile Range:  $IQR = Q_3 - Q_1$ 

Sample Variance:  $s^2 = \frac{\sum_{i=1}^n (y_i - \bar{y})^2}{n-1}$ Sample Variance:  $s^2 = \frac{\sum_{i=1}^n y_i - \frac{(\sum y_i)^2}{n}}{n-1}$ 

Sample Standard Deviation:  $s = \sqrt{s^2}$ 

Coefficient of Variation:  $CV = \frac{\sigma}{|u|}$ 

Histogram Classes:  $2^K >$  Measurements Histogram Large Set Classes:  $\log_2(n)$  or  $2n^{1/3}$ 

Histogram Class Length:  $\frac{Max - Min}{K}$ 

P(S) = 10 < P(A) < 1

If A & B are mutually exclusive:

 $P(A \cup B) = P(A) + P(B)$ 

 $P(A^{C}) = 1 - P(A)$ 

 $P(A \cup B) = P(A) + P(B) - P(A \cap B)$ 

For k operations with  $n_i$  ways the sequence of k operations:

$$\prod_{i=1}^{k} n_i$$

Permutation of n objects: n!

Permutation of k objects from n objects:  $\frac{n!}{(n-k)!}$ Combinations of k objects from n objects:  $\frac{n!}{k!(n-k)!}$ Combinations of groups with n objects, r groups, and group sizes  $k_i$ :  $\frac{n!}{k_1! \cdot k_2! \cdot k_3! \dots k_r!}$  N total outcomes and  $n_a$  outcomes for event A has

probability:  $P(A) = \frac{n_a}{N}$