

# **Intel® MKL Data Fitting component. Overview**

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# Agenda

- 1D interpolation problem statement
- Functional decomposition of the problem
- Application areas
- Data Fitting in Intel® MKL
- Data Fitting API and usage models
- Data Fitting performance

# 1D interpolation problem statement

For given table function  $\{x(i), y(i)\}$ ,  $i=1, \dots, n$  where  
 $x(i)$  - breakpoints in ascending order,  $y(i)$  - values

- Approximate function  $f(x)$ :  $f(x(i))=y(i)$
- Evaluate value  $f(t(j))$  and derivative  $f'(t(j))$ 
  - Site  $t(j)$  is any real value  $[x(1), x(n)]$ ,  $j=1, \dots, m$
- Evaluate integral of  $f(x)$  over interval  $[a(j), b(j))$ 
  - Integration limits  $a(j)$  and  $b(j)$  belong to or are outside of interpolation interval  $[x(1), x(n)]$ ,  $j=1, \dots, m$

# 1D interpolation problem statement

- **Splines – methodology for solution of interpolation problem**

- Can be preferable vs polynomial interpolation
  - Runge's phenomenon
    - Interpolation error for  $g(x)=1/(1+25x^2)$  increases with order of the polynomial

- **Spline – piece-wise polynomial function**

- $g(x) := P_j(x)$ ,  $x$  belongs to  $[x(j), x(j+1))$ 
  - $P_j(x)$  -polynomial of degree  $k$  on the interval  $[x(j), x(j+1))$
- Spline - smooth up to order  $q$  at  $x(j)$  if values of derivatives up to order  $q$  for  $P(j-1)$  and  $P_j$  at  $x(j)$  exist and equal

# Functional decomposition of the problem

Construct spline of given order  
for  $n$  break points  $x(i)$



Compute value of spline and/or its derivative  
at  $M$  interpolation sites  $t(j)$ ,  $m \gg n$

Find interval  $[x(i), x(i+1))$  containing  $t(j)$

Compute value of  $P_i$  polynomial at  $t(j)$

**Integration has similar computational flow**  
**Search – key building block**

# Application areas

- **Data analysis and analytics**

- Approximation of statistical estimates like histogram

- **Manufacturing**

- Geometrical modeling
- *"B-spline recurrence relations ... were used at Boeing, ..., five hundred million times a day"* Carl de Boor, On Wings of Splines Newsletter of Institute for Mathematical Sciences, ISSUE 5 2004

- **Energy**

- Surface approximation

- **ISV**

- Software libraries

# Data Fitting in Intel® MKL

- **Intel® MKL Data Fitting – SW solution for**
  - Spline construction
  - Spline based interpolation and computation of derivatives
  - Spline based integration
  - Cell Search

# Data Fitting in Intel® MKL

## • Components of Intel® MKL Data Fitting Spline construction

Spline	Spline type	Boundary conditions	Internal conditions
Linear		Not-a-knot	1 <sup>st</sup> derivative
Quadratic	Default, Subbotin	Free-end	2 <sup>nd</sup> derivative
Cubic	Default, Natural, Hermite, Bessel, Akima	1 <sup>st</sup> derivative at the left/right endpoint	Knot array
Look-up		2 <sup>nd</sup> derivative at the left/right endpoint	
Stepwise constant	Continuous-right, Continuous-left	Periodic	
User-defined		Function value at mid point of first cell	

**Rich collection of splines that support different boundary or/and internal conditions**



# Data Fitting in Intel® MKL

## • Components of Intel® MKL Data Fitting Interpolation/extrapolation/integration

Feature	Comment
Computation of value, derivative of arbitrary order	<ul style="list-style-type: none"><li>• Support of a-priori information about structure of partition, and/or interpolation sites</li><li>• In addition to default spline based interpolation library supports user-defined functions to<ul style="list-style-type: none"><li>• re-define default spline based computations on interpolation or/and extrapolation intervals</li><li>• re-define cell search functions</li></ul></li><li>• Option to get results of cell search simultaneously with interpolation</li><li>• User defined threading-friendly API</li></ul>
Computation of integrals	<ul style="list-style-type: none"><li>• Support of a-priori info about structure of partition, and/or integration limits</li><li>• In addition to default spline based interpolation library supports user-defined functions to<ul style="list-style-type: none"><li>• re-define default integration on interpolation or/and extrapolation intervals</li><li>• re-define cell search functions</li></ul></li><li>• User defined threading-friendly API</li></ul>

**Flexibility in support of various usage models for spline based computations**

# Data Fitting in Intel® MKL

## • Components of Intel® MKL Data Fitting

### Search

Feature	Comment
Computation of cell indices containing given sites	<ul style="list-style-type: none"><li>• Support of a-priori information about structure of partition, and/or interpolation sites</li><li>• In addition to default cell search computation library supports user-defined function to<ul style="list-style-type: none"><li>• re-define cell search functions</li></ul></li><li>• User defined threading-friendly API</li></ul>

**Flexibility in support of various usage models for cell search**

# Data Fitting API and usage models

Step	Code example	Comment
Create a task	<pre>status = dfdNewTask1D( &amp;task, nx, x, xhint, ny, y, yhint );</pre>	You can call the Data Fitting function several times to create multiple tasks
Modify the task parameters.	<pre>status = dfdEditPPSpline1D( task, s_order, c_type, bc_type, bc, ic_type, ic, scoeff, scoeffhint );</pre>	
Perform Data Fitting spline-based computations	<pre>status = dfdInterpolate1D(task, estimate, method, nsite, site, sitehint, ndorder, dorder, datahint, r, rhint, cell );</pre>	You may reiterate steps 2-3 as needed
Destroy the task or tasks	<pre>status = dfDeleteTask( &amp;task );</pre>	

API and usage model similar to that in Vector Statistical component, Fourier Transforms in Intel® MKL

# Data Fitting API and usage models

## Cubic Spline-Based Interpolation

```
#include "mkl.h"

int main(){
    /* Initialize the partition and set their values */
    nx = N;
    xhint = DF_NON_UNIFORM_PARTITION /* The partition is non-uniform. */
    /* Initialize the function and set their values */
    ny = 1; /* The function is scalar. */
    yhint = DF_NO_HINT; /* No additional information about the function is provided. */
    /* Create a Data Fitting task */
    status = dfdNewTask1D( &task, nx, x, xhint, ny, y, yhint );

    /* Initialize spline parameters */
    s_order = DF_PP_CUBIC; /* Spline is of the fourth order (cubic spline). */
    s_type = DF_PP_BESSEL; /* Spline is of the Bessel cubic type. */

    ic_type = DF_NO_IC; ic = NULL; /* Define internal conditions for cubic spline construction (none in this example) */
    bc_type = DF_BC_NOT_A_KNOT; bc = NULL; /* Use not-a-knot boundary conditions */
    scoeffhint = DF_NO_HINT; /* No additional information about the spline. */

    /* Set spline parameters in the Data Fitting task */
    status = dfdEditPPSpline1D( task, s_order, s_type, bc_type, bc, ic_type, ic, scoeff, scoeffhint );
    /* Construct a cubic Bessel spline:  $P_i(x) = c_{1,i} + c_{2,i}(x - x_i) + c_{3,i}(x - x_i)^2 + c_{4,i}(x - x_i)^3$ ; the library packs spline
       coefficients to scoeff:  $scoeff[4*i+0] = c_{1,i}$ ,  $scoeff[4*i+1] = c_{2,i}$ ,  $scoeff[4*i+2] = c_{3,i}$ ,  $scoeff[4*i+3] = c_{4,i}$  */
    status = dfdConstruct1D( task, DF_PP_SPLINE, DF_METHOD_STD );

    /* Initialize interpolation parameters and set site values */
    nsite = NSITE;
    sitehint = DF_NON_UNIFORM_PARTITION; /* Partition of sites is non-uniform */
    ndorder = 1; dorder = 1; /* Request to compute spline values */
    datahint = DF_NO_APRIORI_INFO; /* No additional information about breakpoints or sites is provided. */
    rhint = DF_MATRIX_STORAGE_ROWS; /* The library packs interpolation results in row-major format. */
    cell = NULL; /* Cell indices are not required. */
    /* Compute the spline values at the points site(i), i=0,..., nsite-1 and place the results to array r */
    status = dfdInterpolate1D(task, DF_INTERP, DF_METHOD_STD, nsite, site, sitehint, ndorder, &dorder, datahint, r, rhint, cell );

    /* De-allocate Data Fitting task resources */
    status = dfDeleteTask( &task );
    return 0;
}
```

# Data Fitting API and usage models

## Cell Search

```
#include "mkl.h"

int main(){

    /* Initialize a uniform partition */
    nx = N;
    /* Set values of partition x: for uniform partition, provide end-points of the interpolation interval [-1.0,1.0] */
    x[0] = -1.0f; x[1] = 1.0f;
    xhint = DF_UNIFORM_PARTITION; /* Partition is uniform */

    /* Initialize function parameters; in cell search, function values are not necessary and are set to zero/NULL values
    */
    ny = 0;
    y = NULL;
    yhint = DF_NO_HINT;

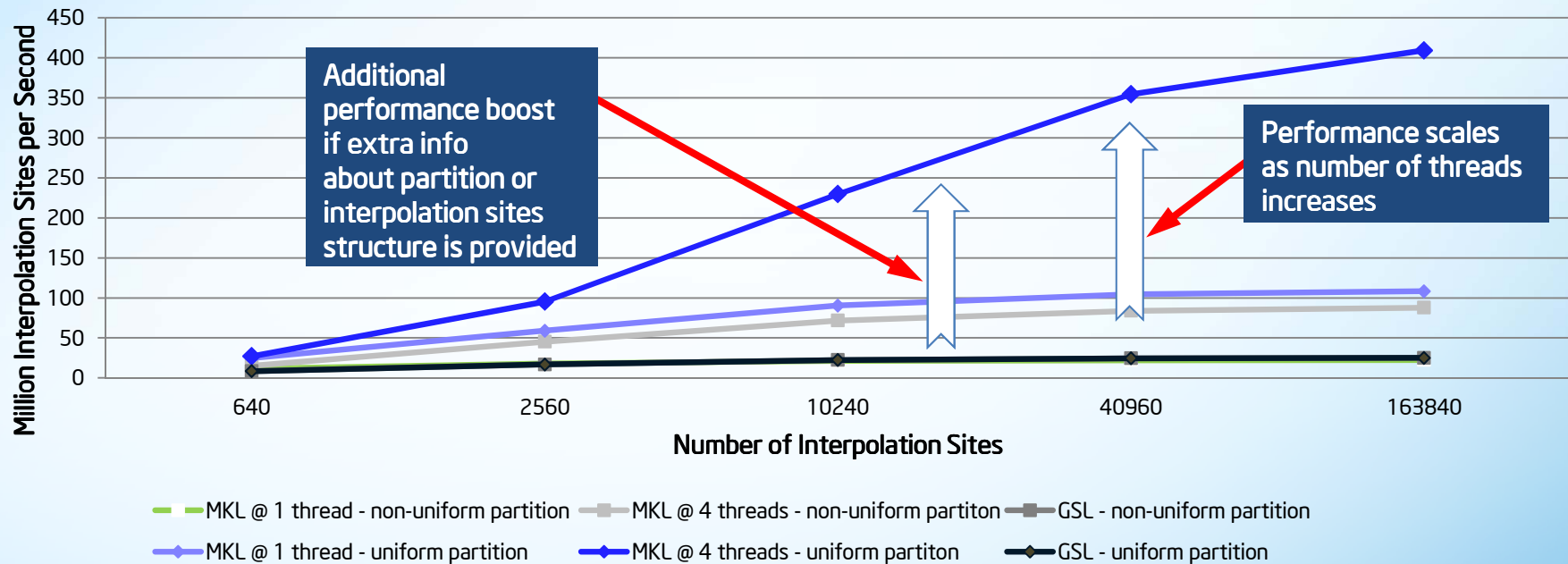
    /* Create a Data Fitting task */
    status = dfdNewTask1D( &task, nx, x, xhint, ny, y, yhint );
    ...
    /* Initialize interpolation (cell search) parameters */
    nsite = NSITE;
    /* Set sites in the ascending order */
    ...
    sitehint = DF_SORTED_DATA; /* Sites are provided in the ascending order. */
    datahint = DF_NO_APRIORI_INFO; /* No additional information about breakpoints/sites is provided.*/

    /* Compute indices of the cells that contain interpolation sites. The library places the index of the cell containing
       site(i) to the cell(i), i=0,...,nsite-1 */
    status = dfSearchCell1D( task, DF_METHOD_STD, nsite, site, sitehint, datahint, cell );

    /* Process cell indices */
    status = dfDeleteTask( &task );
    return 0;
}
```

# Data Fitting performance

## Data Fitting Performance Improvements using Intel® Math Kernel Library versus GSL\* Spline Construction and Interpolation



Construction of natural cubic spline with free end boundary conditions for function defined on uniform and non-uniform partitions. Partition size is 1280. Spline-based values and first derivatives are computed.

Configuration Info - Versions: Intel® Math Kernel Library (Intel® MKL) 10.3.8 GSL 1.15; Hardware: Intel® Core® i7-2600 Processor, 3.40Ghz, 8 MB L2 cache, 4 GB Memory; Operating System: Fedora 14 x86\_64; Benchmark Source: Intel Corporation.

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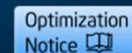
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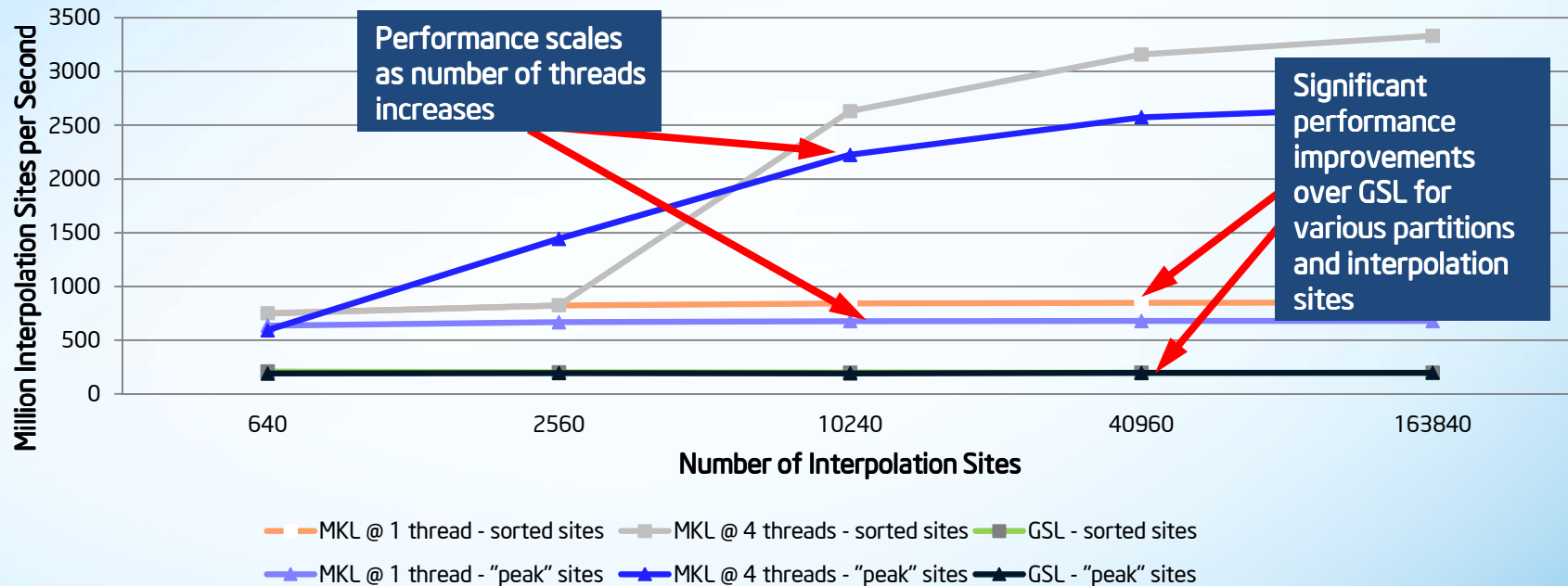


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# Data Fitting performance

## Data Fitting Performance Improvements using Intel® Math Kernel Library versus GSL\* Cell Search



Performing cells search on non-uniform partition. Partition size is 1280.

Sorted sites - interpolation sites are sorted; "peak" sites - distribution of interpolation sites has a clear peak.

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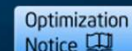
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